

# Assignment No. 2

2) print element of an array forward & backward.

Example:

Input: arr = [1, 2, 3, 4]

Output (forward): 1 2 3 4

Output (backward): 4 3 2 1

→ int [] arr = {1, 2, 3, 4};

int for (int i=0; i<5; i++) {  
 print (i);

Output: 1, 2, 3, 4

backward

for (int i=4; i>0; i--) {

print (i);

}

Output: 4, 3, 2, 1

3) find sum of all digits of a Number

Example:

Input N: 1234

Output: 10

Explanation: 1+2+3+4 = 10

Parameterized way

main() { int sum = 0;

int sum = f(n);

print (sum);

Here n is 4

int f (int n) {

if (n == 0) {

return 0;

}

Return n + f(n-1);

\* 3 \*

int f (int n) {

if (n == 0) {

return 0;

}

Return n + f(n-1);

\* 3

\* 3 - 1

\* 2 \*

int f (int n) {

if (n == 0) {

return 0; } }

Return n + f(n-1);

\* 2 - 1 = 1

int f (int n) {

if (n == 0) {

return 0; } }

Return n + f(n-1); } } } }

\* 0 \*

int f (int n) {

if (n == 0) {

return 0; } }

Q.2) find sum all digits of a Number

Example:

Input: N: 1234  
Output 10: 10

functional way

$$N = 1234$$

Main () {

    int sum = f(n);  
    point(sum);

}

int f (int n) {

    if (n == 0) {  
        return 0;

}

    return n + f(n-1);

}

2

int f (int n) {

    if (n == 0) {  
        return 0;

}

    return n + f(n-1);

$$\cancel{2+0=2}$$

0

int f (int n)

    if (n == 0) {

$$0 = 0$$

        return 0;

3

int f (int n);  
    if (n == 0) {

        return 0;

    Return n + f(n-1);

$$\frac{3-1}{3-1} = 2$$

$$3+2 = 5$$

1 0

int f (int n) {

    if (n == 0) {  
        return 0;

}

    return n + f(n-1);

$$\frac{1-1}{1-1} = 0$$

$$1+0 = 1$$

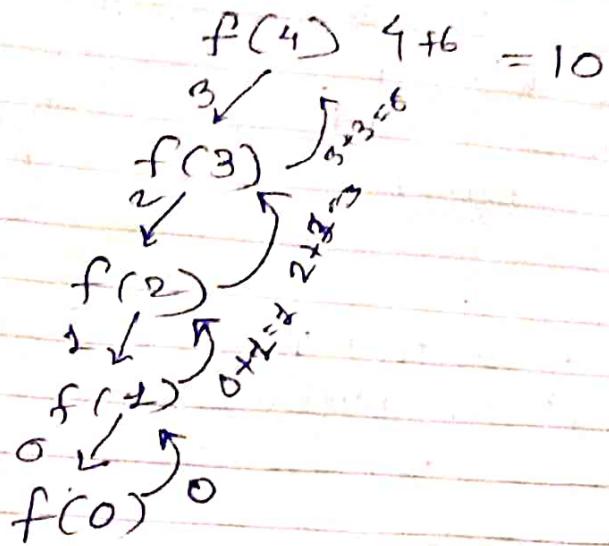
f(0)

f(1)

f(2)

f(3)

f(n)



Parameterized way

Here  $n = 4$

Main () {

    int sum = 0;

    f (sum, n);

}

Void f (sum, n) {

    If (n <= 1) { (n <= 1)

        Print(sum); return;      false

}

    sum = sum + n;      0+4 = 4

    f (sum, n-1);

    }

    Void f (sum, n-1) {

        If (n <= 2) { (n <= 2)

            Print(sum); return;      false

}

    sum = sum + n      4+3 = 7

    f (sum, n-1);

}

```

    ↗ 2
Void f (sum, n-1) {
    ↗ 2
    If (n <= 1) { (2 <= 2)
        print(sum); return; false
    }
}

```

$\text{sum} = \text{sum} + n$        $7 + 2 = 9$   
 $f (\text{sum}, n-1);$   
 ↗

```

    ↗ 1
Void f (sum, n-1) {
    ↗ 1
    If (n <= 1) { (1 <= 1)
        print (sum); false
        return;
    }
}

```

$\text{sum} = \text{sum} + n$        $9 + 1 = 10$   
 $f (\text{sum}, n-1);$   
 ↗

```

    ↗ 0
Void f (sum, n-1) {
    ↗ 0
    If (n <= 1) {
        print (sum);
        return;
    }
}

```

per output: 10

$f(0, 4)$

$n^3$  ✓

$f(4, 3)$

$n^2$  ✓

$f(7, 2)$

$n$  ✓

$f(9, 1)$

$n^0$  ✓

$f(10, 0)$
$f(9, 1)$
$f(7, 2)$
$f(5, 3)$
$f(0, 4)$

3) find the product of digits of Number using recursion

Example 1:

Input:  $N = 231$

Output: 6

Explanation:  $2 \times 3 \times 1 = 6$

Parameterized way

Here  $N = 232$

Main C {  
    f (int n) {  
        if (n == 0) {  
            Return 1;  
        }

}

return ( $n \% 10$ )

prod = ( $n \% 10$ );

~~232~~ % 10 = 2

Return prod \* f( $n / 10$ );

=

23

f (int n) {  
    if (n == 0) {  
        Return 1;      false  
    }

}

prod = ( $n \% 10$ ) = 23 % 10 = 3

Return prod \* f( $n / 10$ );

3 \* 2 = 6

f (int n) {  
    if (n == 0) {  
        Return 1;      false  
    }

}

prod = ( $n \% 10$ ) = 2 % 10 = 2

Return prod \* f( $n / 10$ );

Date \_\_\_\_\_

```
f(int n) {
    if (n == 0) {
        Return 1;
    }
}
```

$0 == 0$   
true  
return 1

4. Count Number of digits of Number

Example 2:

Input N: 98765

Output: 5

```
main () {
    f(int n) 98765
    int count; // count
}
```

```
int f (int n) {
    If (n == 0) 98765 == 0
    return 0;
}
```

$$98765 / 10 = 9876$$

~~count = return 1 + f(n/10);~~

~~print (count);~~

count = return 1 + f(n/10);

print (count); ↑

$$1+4=5$$

$$9876$$

```
int f (int n) {
    If (n == 0) 9876 == 0
    return 0;
}
```

$$9876 == 0$$

false

$$9876 / 10 = 987$$

return 1 + f(n/10);

$$\text{count} = 1' \quad 1+3=4$$

$\text{int f (int n) } \{$

$\text{if (n == 0) } \{$

$\text{return 0; }$

$\} \quad \text{else}$

$\text{return } 1 + \text{f}(n/10);$

$\}$

$\text{int f (int n) } \{$

$\text{if (n == 0) } \{$

$\text{return 0; }$

$\} \quad \text{else}$

$\text{return } 1 + \text{f}(n/10);$

$\}$

$\text{int f (int n) } \{$

$\text{if (n == 0) } \{$

$\text{return 0; }$

$\} \quad \text{else}$

$\text{return } 1 + \text{f}(n/10);$

$\}$

$\text{int f (int n) } \{$

$\text{if (n == 0) } \{$

$\text{return 0; }$

$0 == 0$

& true

$\}$

5) Find the maximum element in an array

→ Example :

Input : arr [2, 5, 9, 1, 6]

Output : 9

Main () {

int [] arr = [2, 5, 9, 1, 6]

int m = Max (arr, arr.length);  
}      s.o.p ("maximum element is " + m)

void max (int [] arr, int n) {

. if (n == 1) {      s == 1  
    return arr[0];      false  
}.

int max (int arr, n);

int return

3

int a = max (arr, n - 1);

return Math.max (arr[n - 1],

9, 6

max = 6

Void max (arr, n) {

. if (n == 1) {      4 == 1  
    return arr[0];      false  
}.

3

4 - 1 = 3

int a = max (arr, n - 1);

return Math.max (arr[n - 1], a);

9, 1

```

void MaxCarry(n) {
    if (n == 1) {
        return arr[0];
    }
    int a = MaxCarry(n-1);
    Return math.max(arr[n-1], a);
}

Void max (arr, n) {
    if (n == 1) {
        return arr[0];
    }
    int a = MaxCarry(n-1);
    Return math.max(arr[n-1], a);
}

Void max (arr, n) {
    if (n == 1) {
        return arr[0];
    }
}

```

(2) true

(3) false

(4) 5

(5) true

6) check of an array is sorted (strictly increasing)

- Example 1:

Input : arr = [1, 2, 3, 4]

Output: true

Example 2:

Input: arr = [2, 2, 2, 3]

false

Input: arr = [1, 2, 2, 3]

Output:

Main () {

int [] arr = [1, 2, 3, 4];

S. O. P ("array is strictly  
increasing") + f (arr, arr);

}

\* boolean f (int [] arr, int n) {

if (n == 0) {  
    return true; } false

}

if (arr[n - 2] >= arr[n - 1])

    return false; } true

    return f (arr, n - 1);

}

3

boolean f (int [] arr, n) {

if (n == 1) {

    3 == 0

    return true; } false

3

if (arr[n - 2] >= arr[n - 1])

    return false; } 2 >= 3

3

true

    return f (arr, n - 1);

boolean f (arr, n- $\frac{1}{2}$ ) {  
    if ( $n = 1$ ) {  
        return true;  
    }  
    if ( $arr[n-2] > arr[n-1]$ ) {  
        return false;  
    }  
    return f (arr, n-1);  
}

if ( $arr[n-2] >= arr[n-1]$ ) {  
    return false;  
}  
    return true;

boolean f (arr, n- $\frac{1}{2}$ ) {  
    if ( $n = 1$ ) {  
        return true;  
    }

7. check if a Number is prime

Example 1:

Input N = 2

Output: true

Example 2:-

Input N = 10

Output: false

Main () {

    int n = 10;

    prime();

bott

```
main () {  
    int num = 10;
```

```
    if (n <= 1) {  
        is_prime =  
        return false;
```

{

```
    for (int i = 2; i < num; i++) {
```

```
        if (n % i == 0) {
```

```
            return false;  
            break;
```

{

{

```
    if (return false) {
```

```
        S.O.P ("n + " is a prime");
```

not

{ else {

```
        S.O.P ("n + " is a not prime);
```

{

{

## 8 Reverse a number using recursion.

Example 2:

Input N = 1234

Output = 4321

```
Main () {
```

```
    int num = 1234;
```

```
    int reversed = reverse (N, 0);
```

```
    S.O.P ("Reversed number: " + reversed);
```

{

1234

0

```
int reverse (int n, int rev) {
```

```

if (n == 0) {
    return rev;
}
return reverse(n/10, rev*(10 + n%10));

```

1234 == 0      false

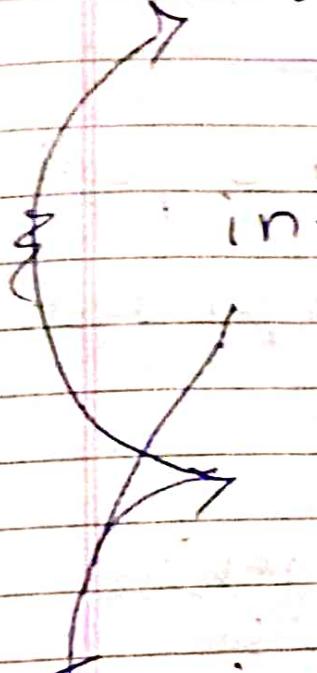
  

```

int reverse (int n, int rev) {
    if (n == 0) {
        return rev;
    }
    return reverse (n/10, rev*(10 + n%10));
}

```

123 == 0      false

```

int reverse (int n, int rev) {
    if (n == 0) {
        return rev;
    }
    return reverse (n/10, rev*(10 + n%10));
}

```

12 == 0      false

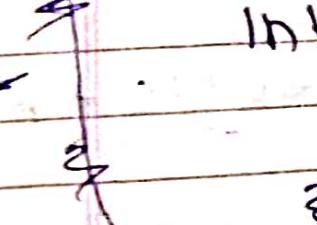
  

```

int reverse (int n, int rev) {
    if (n == 0) {
        return rev;
    }
    return reverse (n/10, rev*(10 + n%10));
}

```

1 == 0      false

```

int reverse (int n, int rev) {
    if (n == 0) {
        return rev;
    }
    return reverse (n/10, rev*(10 + n%10));
}

```

0 == 0      true

9.

check if a number is palindrome

Example :-

Input  $N = 121$

Output : true

Input  $N = 123$

Output : false

Main() {

    int num = 121;

    int reversed = reverse(num, 0);

    if (num == reversed) {

        S.O.P ("Number is palindrome");

    } else {

        S.O.P ("Number is not palindrome");

}

}

int ~~void~~ reverse (int n, int rev) {

    if (n == 0) return rev;      121 == 0

}

    return reverse (n / 10, rev \* 10 + n % 10);

}

121 / 10

0 \* 10 + 12 % 10

12

12

~~Void~~ int reverse (int n, int rev) {

    if (n == 0) return rev;      12 == 12

}

false

    return reverse (n / 10, rev \* 10 + n % 10);

12 / 10 = 1

1 \* 10 + 2 =

```
int reverse (int n, int rev) {  
    if (n == 0) return rev;  12 == 0  
    else  
        return reverse (n/10, rev*10 + n%10);
```

$\frac{12}{10} = 1$ ,  $12 + 10 + 2 \% 10$   
 $12$

```
int reverse (int n, int rev) {  
    if (n == 0) return rev;  0 == 0  
    else
```

~~12~~ Number is palindrome.

me"); 10) Find GCD (HCF) of two Numbers using recursion.

Example :-

Input : A = 24, B = 36

Output : 12

Main () {

int a = 24;

int b = 36;

int result = f (A, B);  
S.O.P ("GCD is " + result);

3 int f (int a, int b) {

if (b == 0) {

return a;

$36 = 0$   
return false

3

return f (b, a % b);

$36 \quad 24 \% 36 \quad 24$

3

int f (int a, int b) {

if (b == 0) {

return a;

$24 = 0$   
false

return f(b, a%b);  
~~24~~      ~~36%24 = 12~~

3

int f (int a, int b) {  
    if (b == 0) {  
        return a;  
    }

~~42~~ == 0      ~~12 == 0~~  
false

return f (~~24~~ b, a%b);  
~~12~~      ~~24%12 = 0~~

3

int f (int a, int b) {  
    if (b == 0) {  
        return a;  
    }

output GCD is 12

1) print all Numbers from 2 to N  
divisible by 3

Example 2.

Input N=10

Output: 3.6.9

Main () {

    int n=20;  
    f (int 2, n);

3

for Void f (int temp, int n) {  
    if (temp > n) {  
        return;  
    } else {  
        cout << temp << endl;

7

$2 \% 3 \neq 0$

```
if (temp%3 == 0) {
    s.o.p (temp);
```

```
}  
- f (temp+1, n);  
f (temp+2, n);
```

```
}  
void f (int temp, int n) {
    if (temp > n) {  
        return; }  
    else false
```

```
}  
if (temp%3 == 0) {
    s.o.p (temp);  
}  
f (temp+1, n);
```

```
}  
void f (int temp, int n) {
    if (temp > n) {
        return; }  
    else 3 > n false
```

```
}  
if (temp % 3 == 0) {
    s.o.p (temp); }  
else
```

```
f (temp+1, n);
```

```
}  
Now it iterate till temp is Reach  
to 22 so
```

(2)

Find power of a number using recursion

Example :-

Input : A = 2, B = 4

Output : 16

Explanation :  $2^4 = 2 \times 2 \times 2 \times 2 = 16$

Main() {

    int A = 2;

    int B = 4;

    int result = ~~Power(A, B)~~; power(A, B);  
    S.O. p ("the result is" + result);

}

\* int power (int A, int B) {

    if (B == 0) {      2 == 0  
        return 1;              false

}

    return A \* power (A, B - 1);

    2 \* 2 = 16

8

int power (int A, int B) {

    if (B == 0) {      3 == 0  
        return 1;              false

}

    return A \* power (A, B - 1);

    2 \* 2 = 8

    2, 2

3

int power (int A, int B) {

    if (B == 0) {      2 == 0  
        return 1;              false

2

    return A \* power (A, B - 1);

    2 \* 2 = 4

    2, 1

1

1  
int Power (int A, int B) {  
    if (B == 0) {  
        return 1; }  
    else {  
        return A \* Power (A, B - 1); }  
}

2  
int Power (int A, int B) {  
    if (B == 0) {  
        return 1; }  
    else {  
        return A \* Power (A, B - 1); }  
}

The Result is 10

(3) count how many times a digit appear in a Number

Example 1:

Input: N = 727237, D = 7  
Output: 3

Main () {

    int N = 727237;

    int D = 7;

    int result = f (N, D);  
    S. O. P (result);

}

void f (int N, int D) {

    if (N == 0) {  
        return 0; }  
    else {

}

    int last = N % 10;      717237 % 10 = 7

    if (last == D) {  
        return 1 + f (N / 10, D); }  
    else {

}

}

717237 / 10 = 7

else %  
return f (n/10, D);

```
71723    7  
void f (int N, intD) {  
    if (N == 0) {  
        return 0;  
    }  
    71723    7
```

```

int last = n % 10;    // 71723 % 10 = 3
If C last == D) {
    return 2 + f (N / 10, D);    false
} else {
    return f (N / 10, D);
}

```

```
71723 7  
void f ( int N, int D ) {  
    if ( N == 0 ) {  
        return 0;  
    } else {  
        return N % D + f( N / D, D );  
    }  
}
```

```

int last = n % 10;    7172 % 10 = 2
if (last == D) {      false
    return 1 + f(N/10, D);
} else {
    return f(N/10, D);
}

```

```
void f(int N, int D) {  
    if (N == 0) {  
        return 0;  
    } else {  
        return f(N-1, D) + D;  
    }  
}
```

find the first index of an element  
in an array

Example 1:

Input : arr = [4, 2, 7, 7, 9], key = 7

Output : 2

main () {

int [] arr = { 4, 2, 7, 7, 9 };

int key = 7;

int result = f (arr, 0, key);

S. O. P ("First index of " + key +  
" is " + result);

}

int f (int [] arr, int index, int key);

{ if (index == arr.length) {  
return -1; } false

5

if (arr [index] == key) {  
4 == 7  
return index; } false

3

return f (arr, index + 1, key);

2

int f ( ) {

{ if (index == arr.length) {  
return -1; } false

3

if (arr [index] == key) {  
1 == 7  
return index; } false

3

```
    return f (arr, index+1, key);
```

```
} int f (
```

```
    if (index == arr.length) { 7 == 7  
        return -1; } false
```

```
    if (arr[index] == key) { 7 == 7  
        return index; }
```

first index of 7 is 2

Q.15) find the last index of an element in an array

Example 2:

Input : arr = [4, 2, 7, 7, 9]

key = 7

Output : 3;

Main C) {

```
int arr[] = {4, 2, 7, 7, 9};
```

int key = 7;

```
int result = f (arr, 0, key);
```

```
s.o.p ("Last index of " + key + " is "  
      + result);
```

)

```
}
```

```
* int f (int [] arr, int index, int key);  
if (index == arr.length) { 4 == 7  
    return -1; } false
```

```
}
```

```
int a = f (arr, index+1, key);
```

```
if (a != -1) ;  
    return a;
```

}

```
if (arr [index] == key) {  
    return index;
```

}

```
return -1;
```

}

```
f (arr, index, key);
```

```
if (index == arr.length) { -1 == 9  
    return -1; false
```

}

```
int a = f (arr, index+1, key);
```