



DECEMBER 2021: END SEMESTER ASSESSMENT (ESA) B TECH II SEMESTER

UE18/19MA151 – ENGINEERING MATHEMATICS- II

Time: 3 Hrs

Answer All Questions

Max Marks: 100

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| 1 | a) | A particle moves along the curve $x = t^3 + 1$, $y = t^2$, $z = t + 5$ where t is time. Find the components of its velocity and acceleration at time $t = 1$ in the direction of the vector $\hat{i} + 3\hat{j} + 2\hat{k}$. | 6 |
| | b) | Evaluate $\int_S (4x\hat{i} - 2y^2\hat{j} + z^2\hat{k}) \cdot \hat{n} dS$ where S is the surface taken over the region bounded by $x^2 + y^2 = 4$, $z = 0$ and $z = 3$ using Gauss Divergence theorem. | 7 |
| | c) | Evaluate $\int \int_S \nabla \times \vec{F} \cdot \hat{n} dS$ where $\vec{F} = (y^2 + z^2 - x^2)\hat{i} - (z^2 + x^2 - y^2)\hat{j} + (x^2 + y^2 - z^2)\hat{k}$ and S is the surface $x^2 + y^2 - 2ax + az = 0$ above the plane $z = 0$. | 7 |
| 2 | a) | Prove that $\int_0^1 \frac{dx}{(1-x^n)^{\frac{1}{n}}} = \frac{\pi}{n \sin(\frac{\pi}{n})}$ | 6 |
| | b) | Show that $J_0^2 + 2J_1^2 + 2J_2^2 + 2J_3^2 + \dots = 1$ | 7 |
| | c) | If n is a positive integer then show that $J_n(x) = \frac{1}{n} \int_0^\pi \cos(n\theta - x \sin\theta) d\theta$. | 7 |
| 3 | a) | Find the Laplace transform of the square wave function $F(t) = \begin{cases} E & \text{for } 0 \leq t \leq \frac{T}{2} \\ -E & \text{for } \frac{T}{2} \leq t \leq T \end{cases} \text{ and } F(t+T) = F(t)$ | 6 |
| | b) | Use Laplace transforms to evaluate $\int_0^\infty \left[\frac{\cos 6t - \cos 4t}{t} \right] dt$ | 7 |
| | c) | Represent $F(t)$ in terms of Unit-Step function and hence find the Laplace Transform of $F(t) = \begin{cases} 0, & \text{for } t < 1 \\ t^2, & \text{for } t \geq 1 \end{cases}$ | 7 |
| 4 | a) | Find $L^{-1} \left[\frac{(3s+7)}{s^2-2s-3} \right]$ | 6 |
| | b) | Find inverse Laplace transform of $\frac{s}{(s^2+4)^2}$ using convolution theorem. | 7 |
| | c) | A particle is moving along the x-axis according to the law $\frac{d^2x}{dt^2} + 6\frac{dx}{dt} + 25x = 0$ If the particle started at $x = 0$ with an initial velocity of 12 feet per second, determine x in terms of t , using Laplace transformation method. | 7 |

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| 5 | a) | Find the Complex form of the Fourier series for the function $f(x) = \sin x$ in $0 < x < \pi$, $f(x + \pi) = f(x)$. | 6 |
| | b) | Find the Fourier Series of the function $f(x) = \frac{\pi-x}{2}$ in $0 < x < 2\pi$. Hence deduce that $\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$ | 7 |
| | c) | If $f(x) = \begin{cases} x & \text{for } 0 < x < \frac{\pi}{2} \\ \pi - x & \text{for } \frac{\pi}{2} < x < \pi \end{cases}$ then show that $f(x) = \frac{4}{\pi} \left[\sin x - \frac{1}{3^2} \sin 3x + \frac{1}{5^2} \sin 5x - \dots \right]$ | 7 |