

# Dask IO for sequentially splitting, merging and resplitting multidimensional arrays

1<sup>st</sup> Timothée Guédon

Department of Computer Science and Software Engineering  
Concordia University  
Montreal, Quebec, Canada  
t\_guedon@encs.concordia.ca

2<sup>nd</sup> Tristan Glatard

Department of Computer Science and Software Engineering  
Concordia University  
Montreal, Quebec, Canada  
tristan.glatard@concordia.ca

3<sup>rd</sup> Valérie Hayot-Sasson

Department of Computer Science and Software Engineering  
Concordia University  
Montreal, Quebec, Canada  
valerie.hayot-sasson@concordia.ca

**Abstract**—In this paper, we define a new algorithm to resplit a multidimensional array stored into a set of files, and we show that it can also be used to split and merge data with the same behavior than the “multiple” strategy. We also give an implementation of this algorithm into a Python library called “Dask IO”, available as an optimization package for the Python big data library Dask.

**Index Terms**—multidimensional, array, split, merge, resplit, IO, processing, Dask, Python

## INTRODUCTION

### A. Context

With the improvement of acquisition methods in several scientific domains like health sciences, geology and astrophysics, new big data challenges have emerged. It includes processing a big amount of data, as well as processing very big files like ultra high resolution images. An example of a ultra high resolution image in the neuroscience field is Big Brain, a model of the brain providing microscopic data (20 micrometers) for modeling and simulation. Most image processing pipelines process only specific ROI (Region Of Interest) or process data by block. At the end of such pipelines, merging back those blocks into one reconstructed image may be required as well. The problem is that naive algorithms perform poorly due to the amount of seeks occurring on disk [1]. Previous work in [1] introduced two types of sequential algorithms to split and merge multidimensional arrays: the “clustered” and “multiple” strategies. To the best of our knowledge however, no algorithm has been proposed for the resplit task. Moreover, the split and merge tasks are special cases of the resplit task, which gives an opportunity to solve the three problems at once. It is easy to see that the “clustered” and “multiple” strategies are non optimal for the resplit task, that is why we searched for another strategy.

### B. Problem definition

Consider a multidimensional array of shape  $R = (R_i, R_j, R_k)$ , stored in some input files with a

given shape  $I = (I_i, I_j, I_k)$ , all input files having the same shape. Our goal is to optimize the process of sequentially resplitting the input files into output files with a different shape  $O = (O_i, O_j, O_k)$ , all output files having the same shape, too.

The resplit process has two particular cases:

- It becomes a split process if there is one input file and several output files,
- It becomes a merge process if there are several input files and one output file.

For this I/O process to be fast, one needs to minimize the number of seeks that occur on disk while reading and writing. We consider that a seek occurs either when opening a file or seeking into a file.

Let us consider a basic sequential resplit algorithm: One can repeatedly read the maximum amount of data possible from the input files into a buffer stored in main memory, and then write this buffer down into the output files requiring this data, until all output files have been completely written. This resplit algorithm is described in Algorithm 1.

The algorithm described in Algorithm 1 takes a list of input and output files *inFiles* and *outFiles* as parameters, as well as the amount of memory  $m$  available in RAM for the buffer and the list of the buffers’ coordinates. We call  $m'$  the amount of memory available in the buffer at a given time during the execution of the algorithm ( $m' = m$  at initialization). The list of buffers’ coordinates contains the coordinates of each buffer to be loaded in the referential of the reconstructed image.

The algorithm successively loads as much data as it can from the input files into the buffer and write it down to the output files that are supposed to contain this data. Although we could use a naive shape for the buffer, we

can use the input and output files shapes to elaborate more efficient strategies as we will see in the next sections. The algorithm ends when all buffers have been read. Therefore, the buffers must cover the whole reconstructed image such that when the algorithm end all the output files have been completely written. For the latter statement to be true, we also need to ensure that all data read from input files are either stored in RAM or directly written, such that all the output files are completely written at the end of the algorithm.

Given Algorithm 1, the optimization problem that we want to solve can be stated as follows: Given the amount of main memory available  $m$ , as well as the shapes of the input and output files  $I$  and  $O$ , how to select the best buffer shape  $B$  which will minimize the number of seeks that take place during reading and writing?

We add two restrictions on the buffers: We shall use only non-overlapping buffers, all buffers having the same size, and each buffer has to be written only once.

---

**Algorithm 1** Basic resplit algorithm

---

**Inputs:** inFiles, outFiles,  $m$ , buffersList  
**for** buffer in buffersList **do**  
    read(inFiles, buffer)  
    write(outFiles, buffer)  
**end for**

---

### C. Consistency with previous works

For the sake of consistency with previous works [1], we call the original array of shape  $R$  stored in the input files the “reconstructed image” (see Figure 1). Of course, the input files’ positions in the reconstructed image have to be stored in some way. Also with a view to be consistent with previous works, we assume the files to be written in column-order. In column ordering (also called “F” ordering) the fastest moving dimension is the last dimension of the array and the slowest moving dimension is the first dimension. For example a 3D array with dimensions  $i, j$  and  $k$  would be written on disk by writing the complete columns in the  $k$  dimension first (see Figure 2).

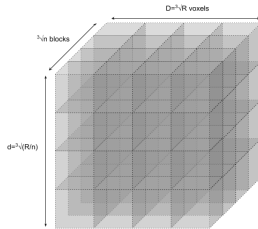


Fig. 1. Illustration of the reconstructed image divided into input files at the initialization of the resplit algorithm.

### D. Naive algorithm

As a base case for our problem, let us define a naive algorithm which loads one input file at a time and write it down into the different output files that requires the data. The buffers have the same shape as the input files ( $B = I$ ) and the order is the same order than the storage order i.e. the column order in this study ( $[k, j, i]$  order).

### E. A particular case

If the input shape is a multiple of the output shape such that one input file covers several output files entirely without falls, then the problem is easily solved: one must read as much input files as one, i.e. the buffer shape  $B$  is a multiple of the input shape  $I$ . The algorithm will produce one seek per input file and one seek to write each output file, which is the minimum number of seeks possible for a resplit.

If there is a mismatch between the shapes in any dimension however, one needs a strategy to manage with this overlap while minimizing the number of seeks. We will introduce a strategy to keep falls temporarily into memory in the next section, this strategy’s efficiency is completely dependent on the amount of main memory available.

Also, the resplit process requires multiple buffers to be read. If there is no overlap between input and output files, then the order in which we load buffers is not important. In case of an overlap however, the order may have an important impact on the number of seeks produced.

### THE “KEEP” ALGORITHM

The algorithm presented in this paper is called the “keep” algorithm, as it relies on a so-called “keep strategy” that is presented below.

### F. The “keep” strategy

At initialization, we assign a shape  $B = (0, 0, \dots, 0)$  for the buffer. We will then stretch the buffer in each dimension until all the available memory  $m$  has been used while keeping the number of seeks as small as possible.

Let us consider the first dimension  $f$  that we increase: Ideally, one wants the buffer to cover both the input file and the output file,  $I_f$  and  $O_f$ , such that we read and write in one seek each. If there is a mismatch between  $O_f$  and  $I_f$  (meaning one is not a multiple of the other) we want to read a multiple of  $O_f$  or  $I_f$  such that we either read partially or write partially but not both at the same time. We must therefore choose between reading a multiple of  $O_f$  or  $I_f$ . Reading a multiple of  $I_f$  in the case of a shape mismatch is equivalent to  $B_f = nI_f = mO_f + xO_f$  with  $0 < x < 1$ ,  $n$  and  $m$  are integers. We call “extra data” the data contained in the overlap areas/volumes between input and output shapes (Figure 3). In this example the extra data is  $xO_f$ . An output file that is involved in an overlap is called an “incomplete

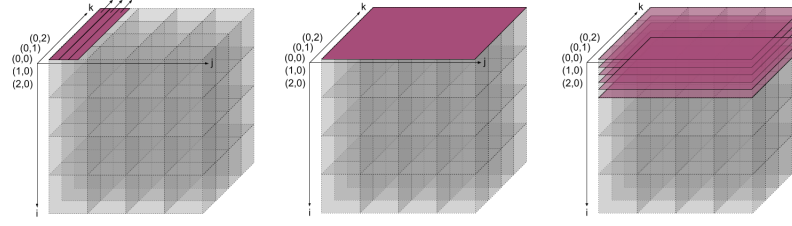


Fig. 2. Illustration of the column-order storage of voxels in a file.

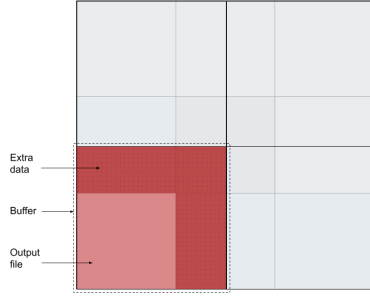


Fig. 3. Illustration of the concept of extra data with a 2D case. In this example the black bordered rectangles represent the input files and the gray bordered rectangles represent the output files. After having read the red buffer we can see that the output file covered by the light red area can be written directly. After having written the data from the light red area however, we are left with the dark red, dotted area which represents some extra data we would like to keep in memory until we read the rest of the incomplete output files in order to read the incomplete output files with one seek.

output file”.

One can try to keep the extra data in memory instead of writing it directly into the output file: this is what we call the “keep strategy” (Figure 4). The idea is to read “more than necessary” from the input files, ideally reading each input file in one seek, and to keep as much extra data in memory as possible. The goal of this strategy is to read input files in one seek, and write as much output files as possible in one seek as well. If we were to read a multiple of  $O_f$  however, we would read an input file partially and there is nothing that one can do about it. It may be that we can only keep some of the overlaps in memory as it could take too much buffers until we can write an incomplete output file in one seek without running out of memory. Extra data that cannot be kept in memory is written directly in the output file(s). By doing so we ensure that when the algorithm ends all the data has successfully been written.

### G. Input aggregates

We call “input aggregate”,  $\Lambda$ , the aggregate of the minimum number of input files that covers one output file entirely in all dimensions (see Figure 6, Figure 5). The input aggregate is the minimal buffer shape we would like to have to be capable of minimizing the number of seeks as it allows to read the input files in one seek and to use the keep strategy. The mismatch between the input and output shapes and the

limited memory available for the buffer may prevent it to be possible.

### H. Stretching the buffer in the storage order

The first step of the algorithm is therefore to make the dimensions of the buffer match the dimensions of the input aggregate as much as possible (we want  $B = \Lambda$ ). If more memory is available after that, we may want to increase the buffer’s dimension even further (it is discussed in subsection “Stretching beyond the input aggregate shape” below). The question of which dimension should be increased first remains. One should increase the buffer’s dimensions in the order of the fastest moving dimensions. For example if one is processing a 3D image stored in files following the column-order, one should increase the buffer in the  $k$  dimension first, then the  $j$  dimension and finally the  $i$  dimension.

Let us first consider the 2D case in which the input and output files overlap in one dimension only. An overlap occurring in the  $k$  dimension would incur  $B_k$  seeks as opposed to 1 seek only (see Figure 7) in the case of an overlap in the  $j$  dimension (see Figure 8). Note that the keep strategy is not useful if we cannot store the extra data in one direction completely (see Figure 8).

Let us define 3 overlapping areas, represented in Figure 9. The  $a$  area is the overlap in the  $k$  axis. The  $b$  area is the upper right overlap which combines the overlaps in both axis. One can see the  $b$  area as the continuity of the  $a$  area. The  $c$  area is the overlap in the  $j$  axis only. The  $a$  area becomes the  $A$  volume in 3D, the  $B$  volume corresponds to the  $b$  area, etc.

In terms of the number of seeks,

$$\Omega_j > (\Lambda_j - \Omega_j) > 1 \Rightarrow \text{seeksIn}(a) > \text{seeksIn}(b) > \text{seeksIn}(c)$$

in 2D, and this stays true when increasing the number of dimensions. We must therefore use the memory available for stretching the buffer to store  $a$  first, then  $b$ , and finally  $c$ . The same way that it is not useful to save part of the  $c$  area as opposed to storing the whole  $c$  area, it is not useful to increase  $B_j$  if  $B_k < \Lambda_k$ . Indeed, the number of seeks will

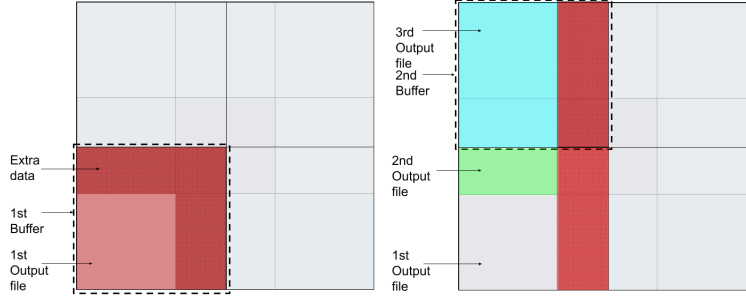


Fig. 4. Illustration of the keep strategy with a 2D case. In this example the black bordered rectangles represent the input files and the gray bordered rectangles represent the output files. As shown on the left figure, the keep strategy consists in reading more than one output file (light red area) into the first buffer. Then the first output file is written and the dark red area is kept in memory. On the left figure the second buffer has been loaded. It allows to free part of the overlap in the  $k$  direction (the green area) as the second file data is complete in main memory. The third output file has been read completely and can therefore be written. This lets the overlap in the  $j$  direction (dark red area) in main memory for the next buffer.

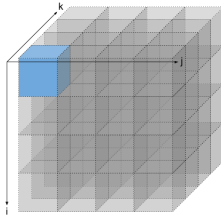


Fig. 5. First buffer in the column-order storage.

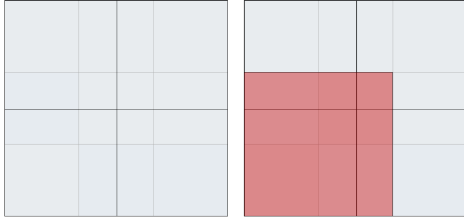


Fig. 6. Illustration of an input aggregate in two dimensions. On the left schema, consider the surface containing all rectangles as being the reconstructed image, with the small rectangles (with black borders) being the input files and the big rectangles (with gray borders) being the output files. On the right side an input aggregate is illustrated by the red area: it is the smallest number of input files such that the surface of at least one output file is completely covered. In this example, four input files are required to cover the first output file.

be the same than without using the keep strategy. As the  $b$  area is the continuity of the  $a$  area in the  $j$  direction, if the available buffer memory  $m'$  allows to store the  $b$  area but not the  $b$  and  $c$  areas together it seems that increasing  $B_j$  from  $\Omega_j$  to  $\Lambda_j$  while storing only the  $b$  area could save a lot of seeks.

As a conclusion, we should increase the fastest moving dimension first to allow the reduction of the number of seeks in the  $a$  and  $b$  areas in the  $k$  direction. Then we should increase  $B_j$  as much as possible, while saving only  $a$  and then  $b$ , even if we cannot cover it entirely. Finally, if we can store the whole  $c$  area, we should do it before increasing the  $i$  dimension to prevent the 1 seek to be multiplied by  $B_i$ .

### I. Stretching beyond the input aggregate shape

Using small input and output file shapes, it is probable for the buffer to have been stretched to the input aggregate, which means that a good amount of RAM is still available. One have no reason to stop increasing the shape of the buffer from that point. The first idea which comes to mind is to stretch the buffer such that the buffer length becomes a multiple of the output file length in a given dimension  $x$ :  $B_x = nO_x$ . Again, this would create an overlap in the input files however, which would prevent the keep strategy to be applied and create a maximum number of seeks. Therefore, one can only stretch the buffer by adding one input file length to a given dimension of the buffer shape (see Figure 10). A good idea seems to be to extend the buffer shape in the dimension of the biggest overlap area/volume such that we accumulate extra data from the smallest overlap volumes only. Again, if we can stretch the buffer such that  $B_x = R_x$  in the dimension  $x$  of the biggest overlap area/volume, we then increase in the dimension of the second biggest overlap size, etc.

### J. Pseudo-code of the algorithm

The algorithm is described in Algorithm 2.

Details:

- line 15: sort the axes in decreasing order of overlap cuboid size
- line 16: for each dimension in this order, try to increase the buffer size
- lines 17, 18: keep adding the length of an input aggregate in that dimension while there is memory left.

Nomenclature:

- $A_i$ : Area of the  $i^{th}$  component
- $m$ : Amount of main memory available for the buffer at initialization
- $m'$ : Amount of main memory available for the buffer during the algorithm execution
- $iterable[i]$ : Access the  $i^{th}$  element of an iterable

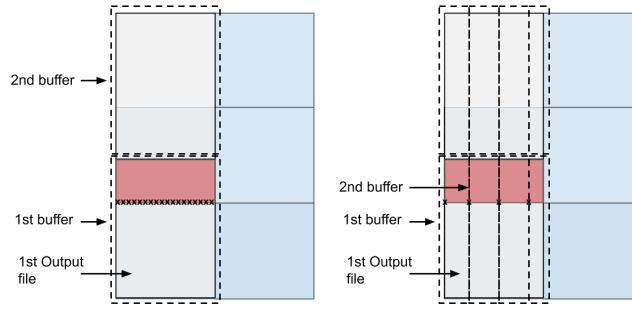


Fig. 7. Left figure: without keep strategy. Right: with keep strategy. Keeping extra data in memory reduces the number of seeks caused by writing but increases the number of buffers needed to write an output file. The crosses represent the number of seeks that happen in both cases.

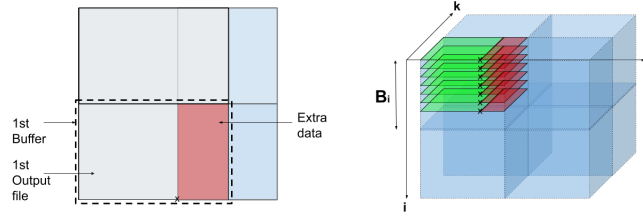


Fig. 8. Illustration of an overlap in the  $j$  dimension. The black crosses represents one seek each. In the 2D case on the left we can see that writing down the data into the next output file on the right would take only one seek. In the 3D case however (right side), writing the data down into the next output file would take  $B_i$  seeks.

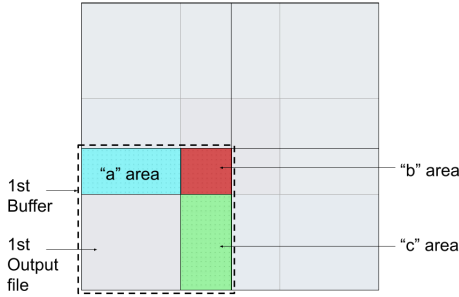


Fig. 9. Illustration of the different overlapping areas in 2D. The blue area is called the  $a$  area, the red area is called the  $b$  area and we call  $c$  area the green one.

- $B = (B_i, B_j, B_k)$ : Shape of the buffer
- $(B_i B_j B_k)$ : Size of the buffer in voxels
- $R_i, R_j, R_k$ : Length of the reconstructed image in the  $i^{th}$  dimension
- $I_i, I_j, I_k$ : Length of an input file in the  $i^{th}$  dimension
- $O_i, O_j, O_k$ : Length of an output file in the  $i^{th}$  dimension
- $C_i(x), C_j(x), C_k(x)$ : Overlap size in voxels in the  $i^{th}$  dimension, when loading the  $t^{th}$  buffer.
- $\Lambda_i, \Lambda_j, \Lambda_k$ : Length of an input aggregate in the  $i^{th}$  dimension
- $b_i, b_j, b_k = \frac{R_i}{B_i}$ : The number of buffers in the  $i^{th}$  dimension in the reconstructed image
- $f_1, f_2, f_3$ : Names of the overlap areas in 2D
- $F_1, F_2, F_3, F_4$ : Names of the overlap volumes in 3D
- $N_s$ : Number of buffers in a slice

- $n_s$ : Number of buffers read so far from the current slice.

---

#### Algorithm 2 getBufferShape in ND

---

```

1: Inputs:  $m, \Lambda, B$ 
2:  $m' \leftarrow m$ 
3: for  $d$  in  $dims$  do
4:   if  $m' \geq \text{maxMemoryCost}(B.add(\Lambda_{dim}), dim)$  then
5:      $B.append(\Lambda_{dim})$ 
6:   end if
7:   if  $\text{maxMemoryCost}(\dots B, 1) \leq m' < \text{maxMemoryCost}(B.add(\Lambda_{dim}, dim))$  then
8:      $maxnbcols = \frac{m'}{\text{cost}}$ 
9:      $bufferShape.append(maxnbcols)$ 
10:  end if
11:  if  $m' < \text{maxMemoryCost}(B.add(1, dim))$  then
12:    nb dims so far = (dim - 1)
13:    nb dims left = nb dims - nb dims so far
14:     $bufferShape = bufferShape + \text{ones}(nbDimsLeft)$ 
15:  end if
16: end for
17:  $maxIndexes = \text{sortIndexofMaximumFall}(B)$ 
18: for  $maxIndex$  in  $maxIndexes$  do
19:   while  $m' > \text{maxMemoryCost}(B.add(\Lambda_{maxIndex}), maxIndex)$  do
20:      $B[maxIndex] += \Lambda_{maxIndex}$ 
21:   end while
22: end for

```

---

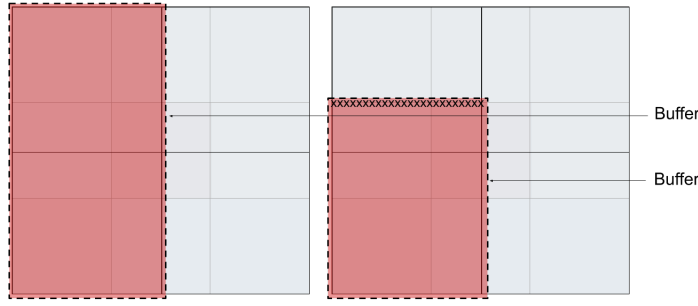


Fig. 10. Left side: Extending the buffer to the next input length. Right side: Extending the buffer to the next output length. The crosses indicates the number of seeks. As we can see, extending the buffer to the next output shape incurs a lot of seeks in the next input file when loading the buffer. As the input file is incomplete, there is no extra data, therefore the keep strategy cannot be used.

### K. Special case of non optimality

When the amount of memory available is too small, a special case arise where the algorithm is not optimal. Consider the 2D case where there is an overlap in the  $k$  dimension only (see Figure 7). Let us say that the buffer size is such that  $B_k = \Lambda_k$ , but is too small to extend  $B_j$  to  $\Lambda_j$ . Keeping the extra data from the overlap in the  $k$  dimension in memory allows us to write contiguously in the output files but it implies using more buffers in the  $j^{th}$  axis. In the worst case,  $B_j = 1$  which incurs  $\Lambda_j$  seeks. As soon as  $B_j > 1$  however (keeping  $B_k = \Lambda_k$ ), we divide the number of seeks produced by writing in the incomplete output file per the number of buffers. This observation is true for the other dimensions as well: as soon as  $B_x = \Lambda_x$  in a given dimension  $x$ , the more we can read in the next dimension  $x + 1$ , the better. This proves that we should not increase a dimension if  $B_x < \Lambda_x$  in the preceeding dimensions.

### L. Impact of the buffer order on performance

Using the keep strategy in case of overlaps, one may order the buffer loadings to further reduce the number of seeks. By optimizing the buffer ordering one can reduce the maximum quantity used to store the extra data in memory. For example, if an overlap occurs only in the  $k$  axis, loading the next buffers in this direction will enable recycling the extra data kept in memory, resulting in a smallest memory consumption over time. The memory saved thanks to a smart ordering could enable the storage of more overlaps in memory using the “keep strategy”, further reducing the overall number of seeks.

As we will see, the buffer ordering problem is complex and does not seem easily solvable. Thankfully, the impact of the buffer ordering on performance can be mitigated. Indeed, the impact of the buffer ordering depends on the size of the falls, i.e. the overlaps between the buffer and the incomplete output files’ shapes. One can reduce the falls’ sizes by using smallest chunks: Even if the overlap between the input and output files is big with respect to their size, the area/volume of the falls will be kept small. In particular, we remark that the falls tends to be smaller when the buffer shape is bigger than the output

file shape, as the overlaps are smallest and concentrated on the borders (see Figure 11). We can stimulate this property by using small chunks such that we use buffer bigger input aggregates (see Stretching beyond the input aggregate shape), while keeping the overlaps small at the borders.

### A MEMORY ANALYSIS OF THE KEEP STRATEGY

The keep algorithm assumes that  $m$  is big enough to keep at least a column of length  $B_k$ . As it has been explained, in 3D the buffer is then stretched in the  $j^{th}$  dimension and finally in the  $i^{th}$  dimension as long as there is enough main memory available to use the keep strategy. This section covers how we estimate the amount of memory required by the keep strategy in order to know how much we can stretch the buffer in each dimension.

Two pieces of information are required to know the worst case memory consumption of the keep algorithm: what is the maximum number of each overlap area/volume we will have to keep in memory during the algorithm and what is the maximum size that those overlap areas/volumes can have. In this analysis we express the overlap size in terms of the number of voxels that constitutes the overlap because the real quantity of memory used depends on the size of a voxel in memory. For convenience one can avoid this extra parameter by setting the number of bytes per voxel to 1.

### M. A “naive” buffer ordering algorithm

The maximum number of each overlap to keep in memory depends on the buffer order. Therefore, the buffer order defines the maximum amount of extra data we will have to keep in memory. As we do not know a good ordering which do not imply a compute-intensive algorithm (see section “Discussion”), let us define a naive ordering as follows (Algorithm 3):

---

#### Algorithm 3 Naive buffer ordering algorithm

---

- 1: **Inputs:** inputShape, outputShape
  - 2:  $overlap \leftarrow dict()$
  - 3:  $overlap \leftarrow getOverlapUpperBounds(inputShape, outputShape)$
  - 4:  $sort(overlap, by=values)$
  - 5: **return**  $overlap.keys()$
-

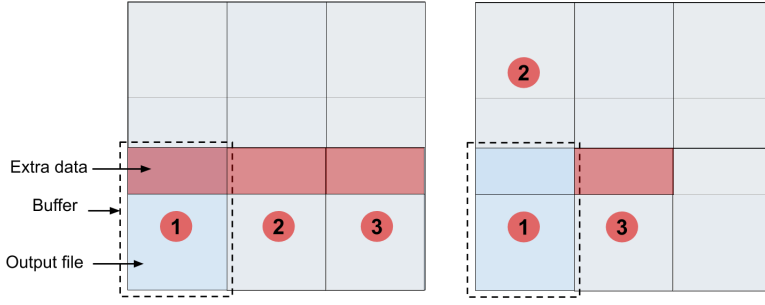


Fig. 11. Comparison of a bad buffer ordering (left side) against a good buffer ordering (right side), given an overlap in the  $k$  dimension. The red area represents the amount of extra data kept in memory after loading the third buffer. The right side order allowed to release the extra data from the first buffer after reading the second buffer.

This naive algorithm computes the overlap size in each dimension and returns an array of indices representing the dimensions, ordered by decreasing overlap size. If there is no overlap in a given dimension, then the overlap size is 0. The idea is to read the buffers in the direction where the overlap is the most important first, then read those columns of buffers in the order of the second dimension where the overlap is the biggest, etc. For example if the order is  $(j, k, i)$ , we will read the buffers in direction  $j$  first (see figure x). We evaluate the amount of overlap thanks to the function `getOverlapUpperBounds`. `getOverlapUpperBounds` returns, for each dimension, the amount of memory needed to keep the extra data in memory if we read a buffer row (a row of buffers in the reconstructed image) in this dimension.

According to this ordering, we can now find the formula of the maximum number of overlap areas/volumes that will be stored during the keep algorithm execution. We present the formulas for the 3D case, but it can be extended to the  $N$  dimensional case. Let us say that the ordering is  $[k, j, i]$ . We keep at a maximum

- one time the overlap in the first dimension of the buffer order:  $f_1$ .
- $n_k - 1$  times the overlap in the second dimension of the buffer order:  $(n_k - 1)(f_2 + f_3)$ .
- $F_1 + n_j(F_2 + F_3) + F_4(N_s - 1)$

#### N. Overlap sizes in 3D

According to the “keep” algorithm, the buffer is stretched in the storage order. As a consequence, only a set of possible overlaps may happen, as illustrated on Figure x. Let us define the amount of extra data to be stored in each case.

In a given dimension  $x$ , when loading the  $n^{th}$  buffer, the overlap length is  $C_x(n) = nB_x \bmod(O_x)$  with  $i \in [1, b_x]$  where  $b_x$  is the number of buffers in the direction  $x$ . Let us call the index of the buffer in dimension  $k, j, i$ :  $x, y$  and  $z$  respectively.

In 2D, the amount of extra data  $e$  is:

- $C_k(x)B_j$  while the  $a$  and  $b$  areas are not totally covered by the buffer ( $B_j < \Lambda_j$ ).
- $e = f_1 + f_2 + f_3$  else, with:

- Size of the  $a$  area:  $f_1 = C_k(x)(B_j - C_j(y))$
- Size of the  $b$  area:  $f_2 = C_k(x)C_j(y)$
- Size of the  $c$  area:  $f_3 = C_j(y)(B_k - C_k(x))$

Then, in 3D, the amount of extra data is:

- $e = (f_1 + f_2 + f_3)B_i$  while  $B_i < d_1$  (see Figure x)
- $e = (f_1 + f_2 + f_3)d_1 + B_jB_k(B_i - d_1)$  while  $B_i - d_1 < C_i(z)$
- $e = (f_1 + f_2 + f_3)d_1 + B_jB_kC_i(z)$ , else

When extending the buffer more than  $\Lambda$  we add  $I_x$  to the dimension  $x$  in which the amount of extra data is the most important while  $B_x < R_x$ . If there is still some memory available after  $B_x = R_x$ , we start adding  $I_y$  in the second dimension  $y$  with the biggest amount of extra data, etc. The above formulas still stands, it only changes the value of  $B$ .

By definition of the modulo, the maximum overlap length in a given dimension  $x$  is  $O_x$ .  $O_x$  is an upper bound as in some cases like in Figure x we may never reach this point. We could therefore compute  $C_x(k)$  for all  $k \in [1, b_x]$  to find the maximum if it is not too compute intensive in order to find the exact maximum length of the overlap in direction  $x$ . Now that we know how to compute the maximum  $C$  value we can replace it in the above formula.

#### O. Putting all together

We can use this analysis to compute the buffer shape according to the following algorithm:

#### IMPLEMENTATION

#### EXPERIMENTS

- *dask<sub>i</sub>o* vs naive with different shapes
- *dask<sub>i</sub>o* perfs with different memory buffer sizes
- *dask<sub>i</sub>o* perfs with different shapes



## RESULTS

## DISCUSSION

*P. Usage and support for MINC/Nifti file formats*

*Q. Comparison with previous work*

*R. Solution of the ordering problem*

*S. Extending the algorithm for ROI extraction*

*T. Distributed keep algorithm*

*U. Improvements*

- proof of optimality
- better ordering

## CONCLUSION

## ACKNOWLEDGMENTS

## REFERENCES

- [1] V. Hayot-Sasson, Y. Gao, Y. Yan, and T. Glatard, "Sequential algorithms to split and merge ultra-high resolution 3d images," in *2017 IEEE International Conference on Big Data (Big Data)*, pp. 415–424, Dec 2017.