

UNIVERSIDADE FEDERAL FLUMINENSE



Programa de Mestrado e Doutorado em Engenharia de Produção

Forecasting

Lesson: 101

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# Presentation

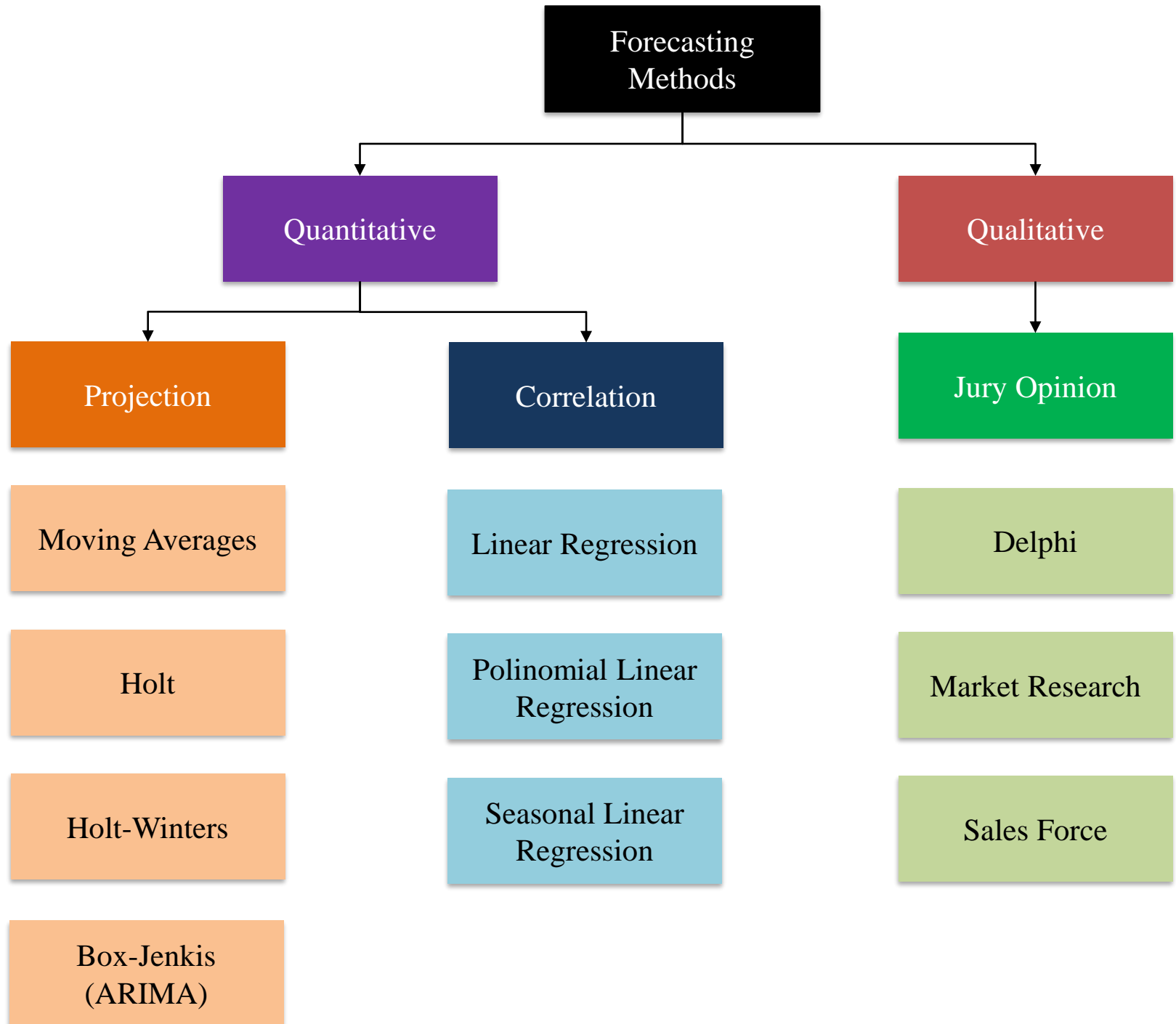
- **Graduation:** Production Engineering (UERJ)
- **Specialization:** Construction Engineering and Assembly (PROMINP / UFF)
- **Masters:** Production Engineering (UFF) - Emphasis on Technology and Innovation.
- **PhD:** Production Engineering (UFF) - Emphasis on Operational Research.

<b>Date</b>	<b>Lessons</b>
05/04/2018	Prediction Theory and Errors
12/04/2018	Test
19/04/2018	Decomposition of Time Series
26/04/2018	Test
03/05/2018	Holt Method
10/05/2018	Test
17/05/2018	Holt-Winters Method
24/05/2018	Test
<b>31/05/2018</b>	<b>RECESS</b>
07/06/2018	Linear Regression
14/06/2018	Test
21/06/2018	Seasonal Linear Regression
28/06/2018	Test
05/07/2018	Logistic Regression
12/07/2018	Test

<https://github.com/Valdecy/Forecasting>



Year	GM - Pontiac Aztek Sales
2000	11,201
2001	27,322
2002	27,793
2003	27,354
2004	20,588
2005	5,020
2006	347
2007	69



# Forecasting

**Forecasting** is a rational process of searching for information about the amount of item sales (or set of items) in the future. However forecasting methods do not lead to perfect results, and the chance of error increases as the planning horizon increases.

A **time series** can be defined as a set of observations of a variable arranged sequentially in time. Usually the time series are analyzed from their main movements described as: **trend**, **seasonality**, **cycle** and **random events** (prediction errors).

## TIME SERIES

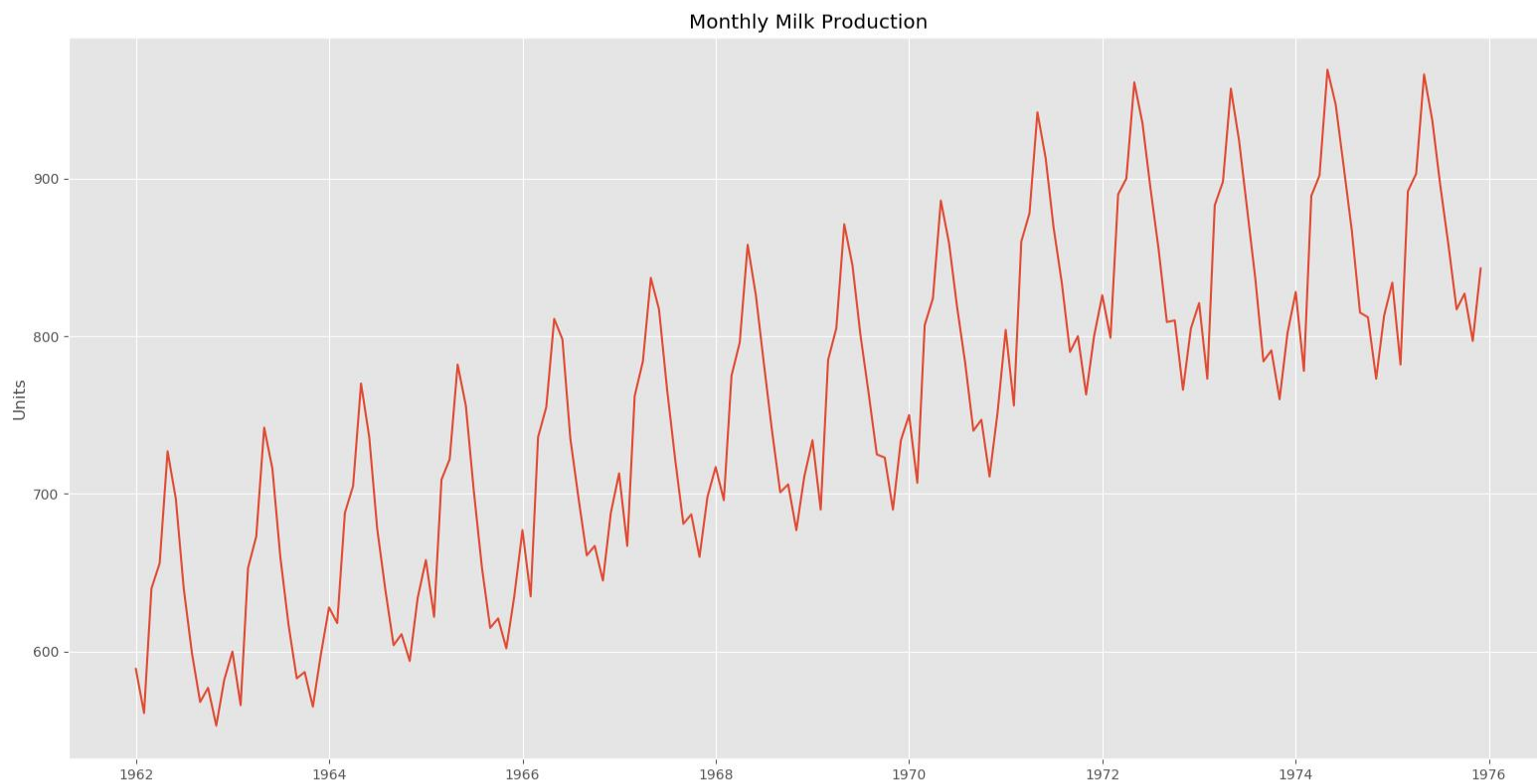
Trend

Seasonality

Cycle

Noise





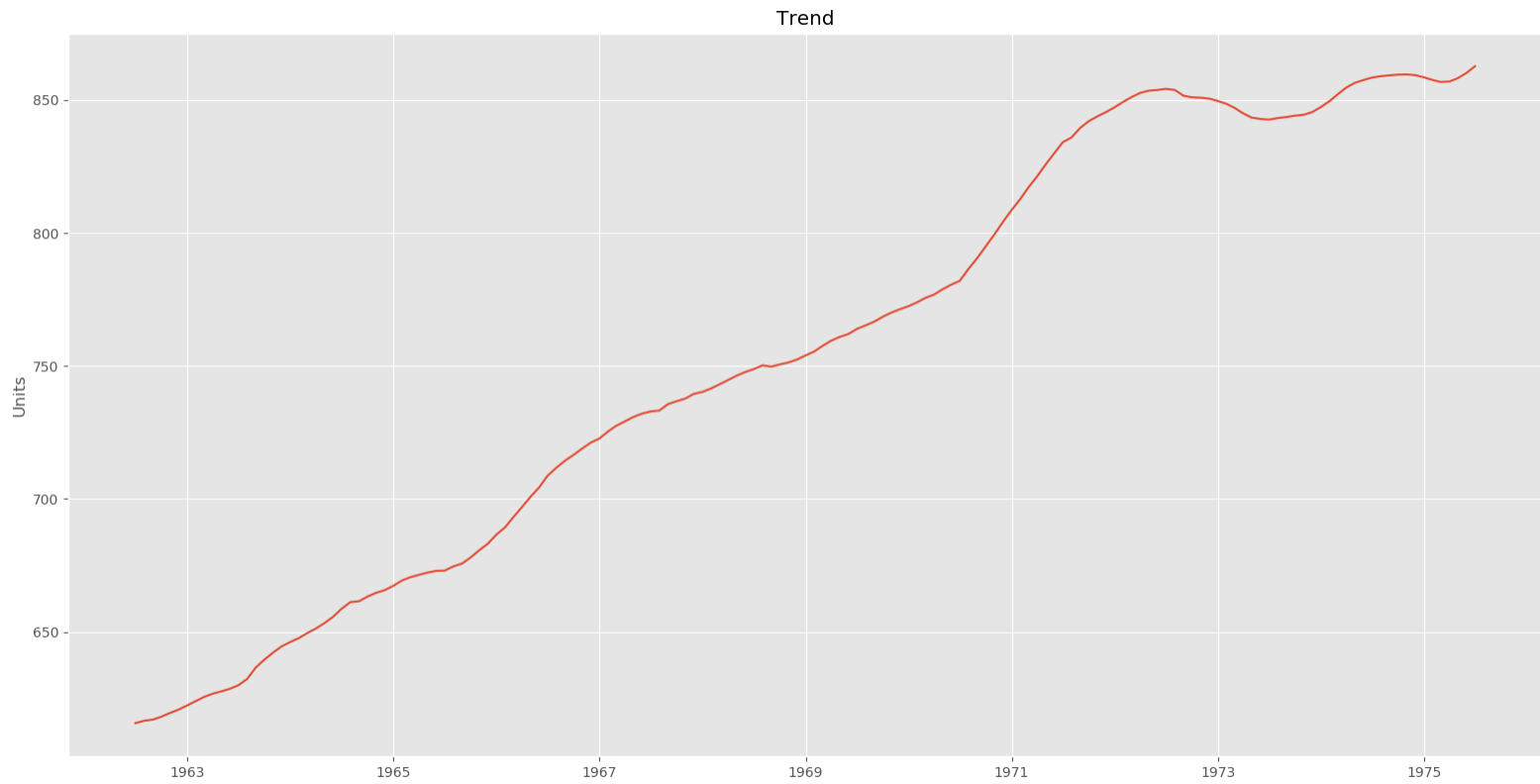
## TIME SERIES

Trend

Seasonality

Cycle

Noise



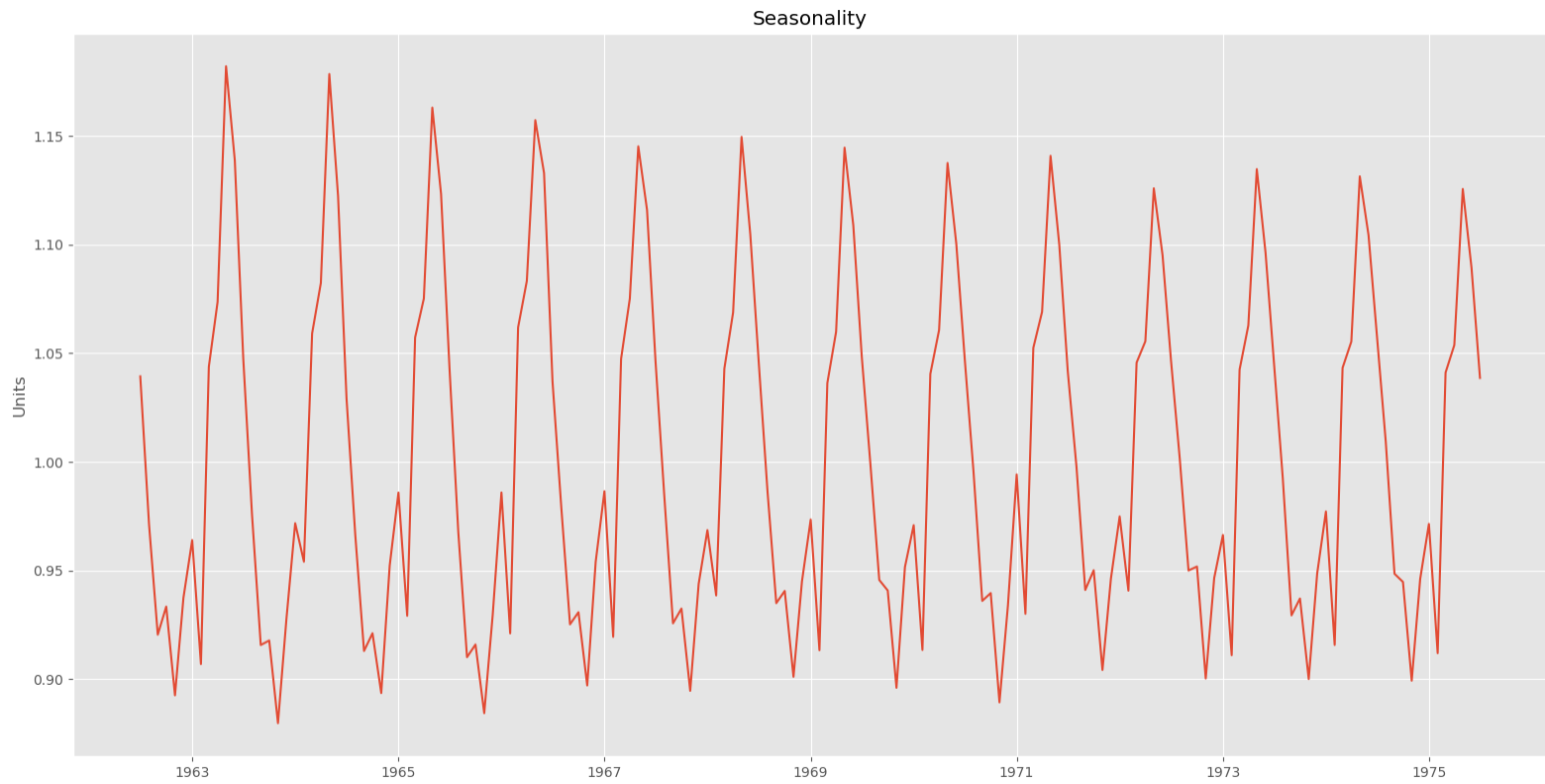
## TIME SERIES

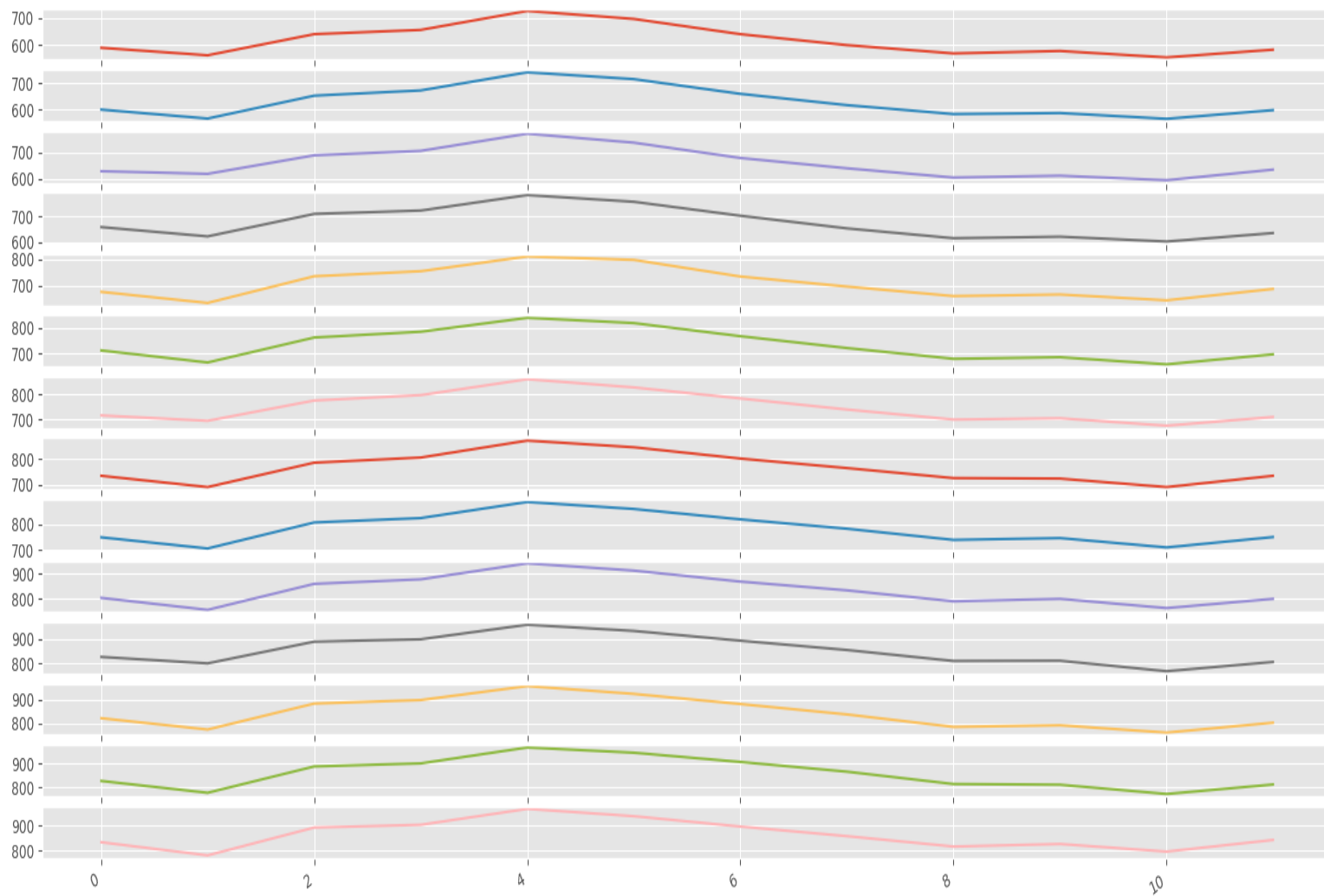
Trend

Seasonality

Cycle

Noise





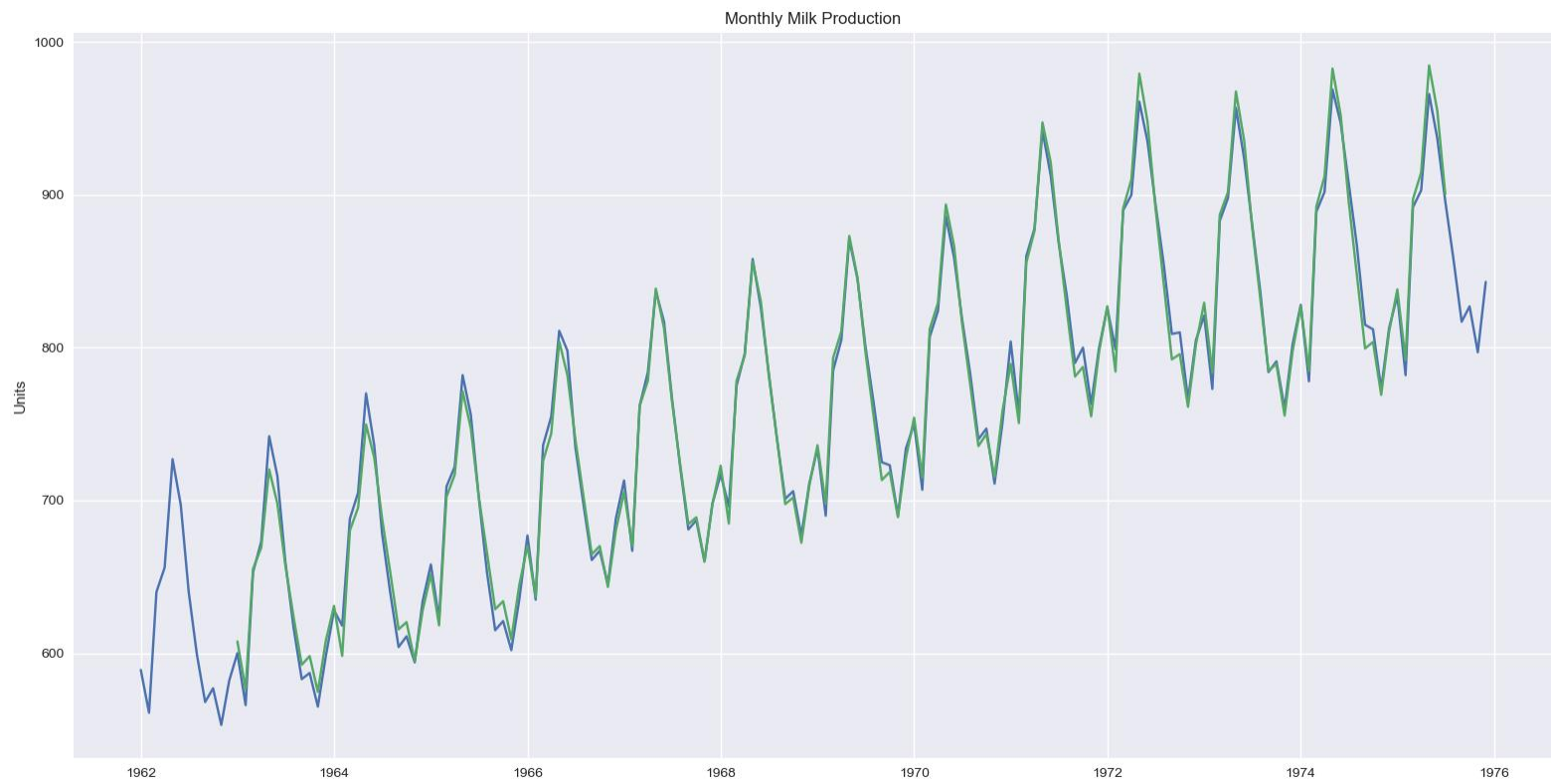
## TIME SERIES

Trend

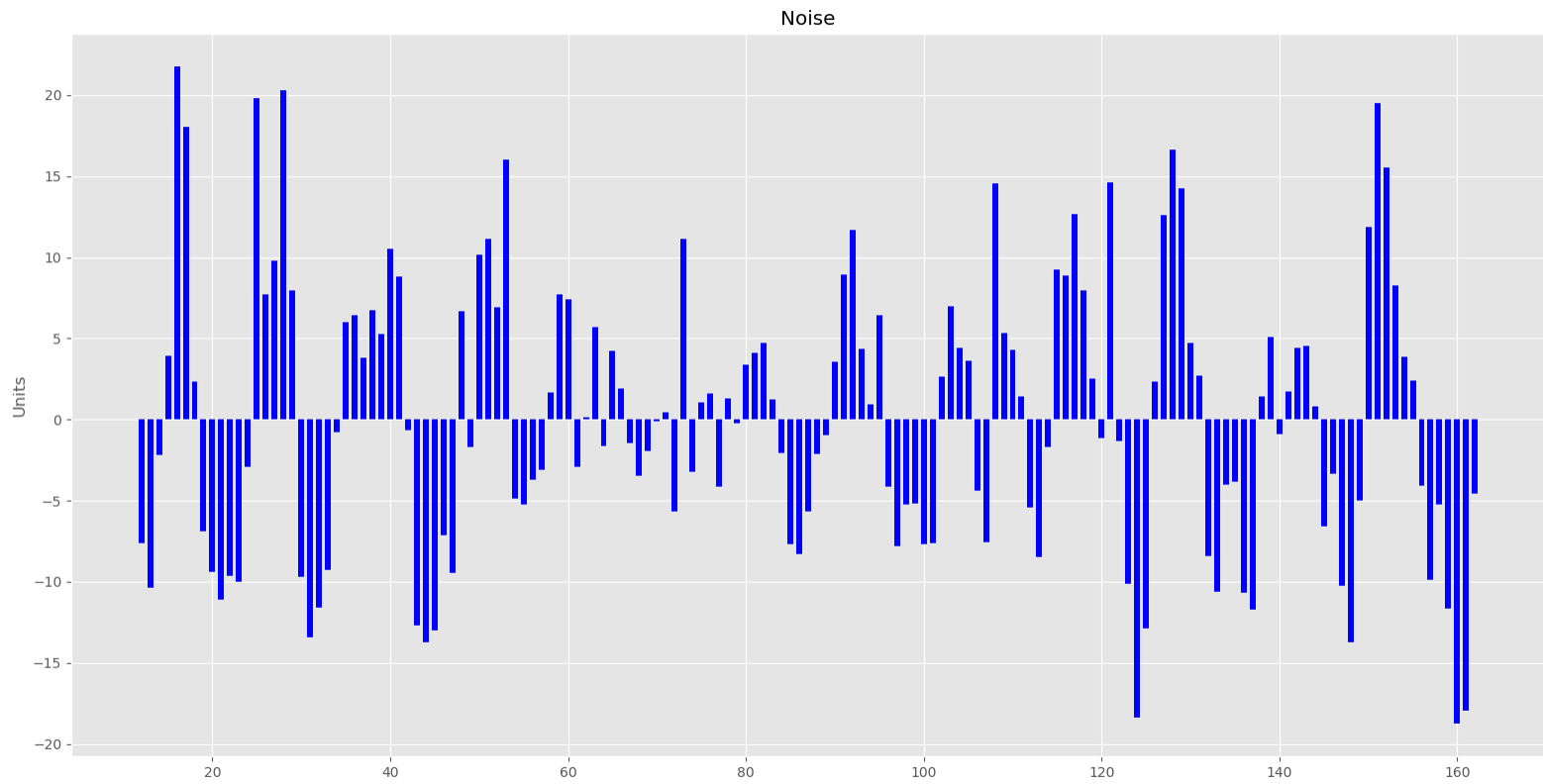
Seasonality

Cycle

Noise







# Forecasting

The **trend** ( $T$ ) represents a growth or fall in the consumption of a certain item during some representative period of time. A time series may have a **linear** or a **nonlinear trend**.

**Seasonality** ( $S$ ) is defined as the repetitive and predictable movement around the trend line within a year or less. It is detected visually within the time intervals that make up the year, such as: **days**, **weeks**, **months**, or **quarters**.

The **cycle** ( $C$ ) can only be perceived if it is considered a large period of time, for example decades, and can be understood as a repetition of the consumption behavior of a particular item or set of items.

Finally, **random events** or **prediction errors** ( $e$ ) are perturbations that may occur during the actual consumption period and affect it in some way. Prediction errors may also be correlated to variables not contemplated by the forecast model.

# Forecasting

The demand forecast ( $P$ ) can be calculated based on one of the following equations:

$$\text{Additive} \rightarrow P = (T) + (S) + (C) + (e)$$

$$\text{Multiplicative} \rightarrow P = (T)(S)(C)(e)$$

# Forecasting

GODNESS OF FIT

# Forecasting

To measure the **goodness of fit** of a model, the following measurements are used:

- a) CFE (Cumulative Forecasting Error)
- b) ME (Mean Error)
- c) MAE (Mean Absolute Error)
- d) MSE (Mean Squared Error)
- e) MPE (Mean Percentage Error)
- f) MAPE (Mean Absolute Percentage Error)
- g) U-Theil

# Forecasting

- The error is calculated as:

$$e = D - P$$

- The **Cumulative Forecasting Error (CFE)** reports the bias of the forecast errors and is given by:

$$CFE = \sum_{i=1}^n e_i$$

# Forecasting

- The **Mean Error (ME)** is given by:

$$ME = \frac{\sum_{i=1}^n e_i}{n}$$

- The **ME** will probably generate small values or be equal to zero (0) due to the trade-offs between the positive and negative values of the errors of each period. The **ME** also reports, on average, the bias of forecast errors.

# Forecasting

- The **Mean Absolut Error (MAE)** is given by:

$$MAE = \frac{\sum_{i=1}^n |e_i|}{n}$$

- The **MAE** turns all errors into positive values and then an average is calculated. Being easy to interpret results and easier to explain to non-specialists.



# Forecasting

- The **Mean Squared Error (MSE)** is given by:

$$MSE = \frac{\sum_{i=1}^n e_i^2}{n}$$

- The **MSE** turns all errors into positive values and then a mean is calculated. The **MSE** is not so easy to interpret but it manages to punish the model when large prediction errors occur.

# Forecasting

- The **MSE** can also be used to find confidence intervals for the forecast:

$$P_{i+1} \pm z\sqrt{MSE}$$

- The **MSE** provides an estimate of the variance so the square root of the **MSE** provides an estimate of the standard deviation of the prediction error. Therefore it is assumed that the errors are normally distributed and have zero mean (0).

# Forecasting

- The **Mean Percentage Error (MPE)** is given by:

$$MPE = \frac{\sum_{i=1}^n \left( \frac{D_i - P_i}{D_i} \right)}{n}$$

- The **MPE** allows to compare time series with different scales of magnitude, but it has the same disadvantages of the **ME** and can not be computed if the time series allows values equal to zero. Ex: Air temperature.

# Forecasting

- The **Mean Absolute Percentage Error (MAPE)** is given by:

$$MAPE = \frac{\sum_{i=1}^n \left| \left( \frac{D_i - P_i}{D_i} \right) \right|}{n}$$

- The **MAPE** has the same characteristics of the **MAE**, but it also can not be used in time series that allow the existence of the value zero (0). **MAPE** transmits more information than the previous error measures.

# Forecasting

- The **U-Theil Statistic** (developed by Theil in 1966) measures whether the model used is as good as the Naïve Forecast.

$$U = \sqrt{\frac{\sum_i^{n-1} \left( \frac{P_{i+1} - D_{i+1}}{D_i} \right)^2}{\sum_i^{n-1} \left( \frac{D_{i+1} - D_i}{D_i} \right)^2}}$$

# Forecasting

- $U = 1 \rightarrow$  The evaluated model is as good as the Naïve Forecast.
- $U < 1 \rightarrow$  The evaluated model is better than the Naïve Forecast. The lower the value, the better the model.
- $U > 1 \rightarrow$  The evaluated model is worse than the Naïve Forecast. The higher the value, the worse the model.

# References

- MAKRIDAKIS, S.G., WHEELWRIGHT, S.C, HYNDMAN, R.J. **Forecasting: Methods and Application.** 3rd Edition