- Let  $R \subset \mathbb{Z}$  be the sequence of rows and  $C \subset \mathbb{Z}$  be the sequence of columns.
- Let K be the domain for modifiers  $K = \{ADJ, ROW, COL\}$ .
- Let  $A_{c,r,k}$  be the solution matrix for column c, row r and modifier k.
- Let X be a set of points (c,r) which are a subset of the points in A. The points represent non-empty cells.
- Let hcon(c, r) be the set of horizontally connected cells for  $c, r \in X$  except for (c, r).
- Let vcon(c, r) be the set of vertically connected cells for  $c, r \in X$  except for (c, r).
- Let  $V(c,r) = \{(c-1,r), (c+1,r), (c,r-1), (c,r+1)\} \cap X$  and then  $\mathrm{adj}(c,r) = \sum_{(c',r') \in V(c,r)} A_{c',r',\mathtt{ADJ}} * 0.4.$
- Let  $\operatorname{row}(c,r) = \sum_{(c',r') \,\in\, \operatorname{hcon}(c,r)} A_{c',r',\mathtt{ROW}} * 0.25.$
- $\bullet \ \ \mathrm{Let} \ \mathrm{col}(c,r) = \sum_{(c',r') \, \in \, \mathrm{vcol}(c,r)} A_{c',r',\mathtt{COL}} * 0.25.$
- Let  $\operatorname{mul}(c, r) = 1 + \operatorname{adj}(c, r) + \operatorname{row}(c, r) + \operatorname{col}(c, r)$ .
- Let big M = 2.8.
- Let unmodified $(c,r) = 1 \left(\sum_{k \in K} A_{c',r',k}\right)$ .

$$\begin{array}{lll} \text{maximize} & \sum_{(c,r) \in X} w_{c,r} \\ \text{subject to} & \sum_{k \in K} A_{c,r,k} \leq 1, & \forall (c,r) \in X \\ & \sum_{k \in K} A_{c,r,k} = 0, & \forall (c,r) \in (C \times R) - X \\ & w_{c,r} \leq \text{mul}(c,r), & \forall (c,r) \in X \\ & \sum_{(c',r') \in V(c,r)} \text{unmodified}(c',r') \geq 3 * A_{c,r,\text{ADJ}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{hcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{ROW}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{hcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{(c',r') \in \text{vcon}(c,r)} \text{unmodified}(c',r') \geq 5 * A_{c,r,\text{COL}}, & \forall (c,r) \in X \\ & \sum_{($$