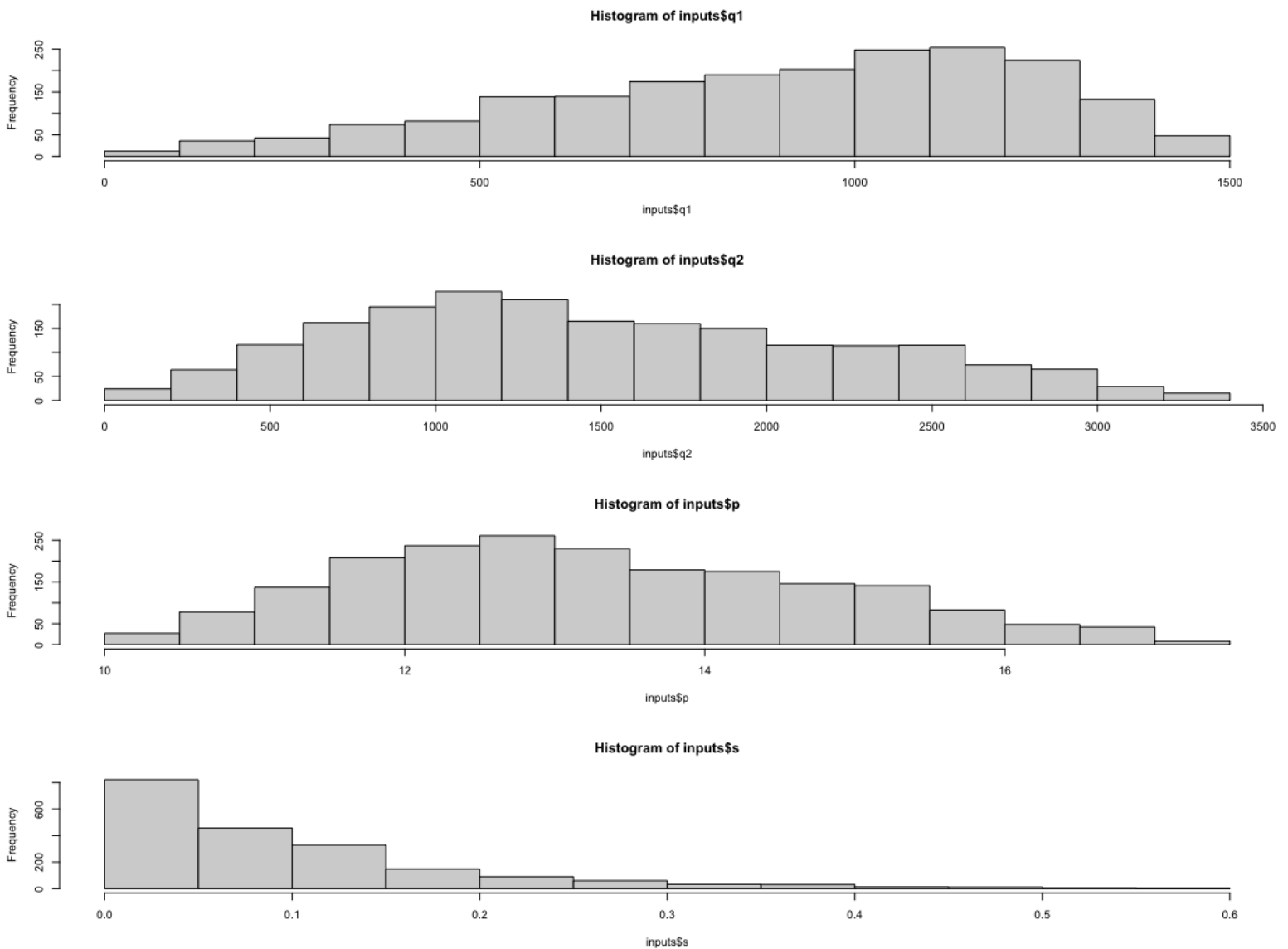


CAP4830 HW3

1) Create a data frame named **inputs** with the following column names (q1, q2, p, s) and each column has 2000 rows with the following data:

- q1 -> 2000 random variables that have a triangle distribution with $A = 0$, $B = 1500$, $C = 1200$
- q2 -> 2000 random variables that have a triangle distribution with $A = 0$, $B = 3500$, $C = 1000$
- p -> 2000 random variables that have a triangle distribution with $A = 10$, $B = 17.50$, $C = 12.50$
- s -> 2000 random variables that have an exponential distribution with $\lambda = 10$

2) Plot the histogram in a single window of each column of the **inputs** data frame. Hint use `par(mfrow=c(4, 1))`



3) Create a data frame named **outputs** with a column name **value** that stores the output of the following model:

$$f(q1, q2, p, s) = (2700 - q1 - q2) * p - (s * p)$$


4) Run a Monte Carlo Simulation 1000 times of the model shown in #3, and store the results in the **value** column of the data frame **outputs**


Environment


History

Connections


Tutorial








Import Dataset



183 MiB



R

Global Environment

Data

inputs

2000 obs. of 4 variables

outputs

3000 obs. of 1 variable

Values

i

1000L

p

12.5049614562915

q1

1375.3122340112

q2

1088.55126282974

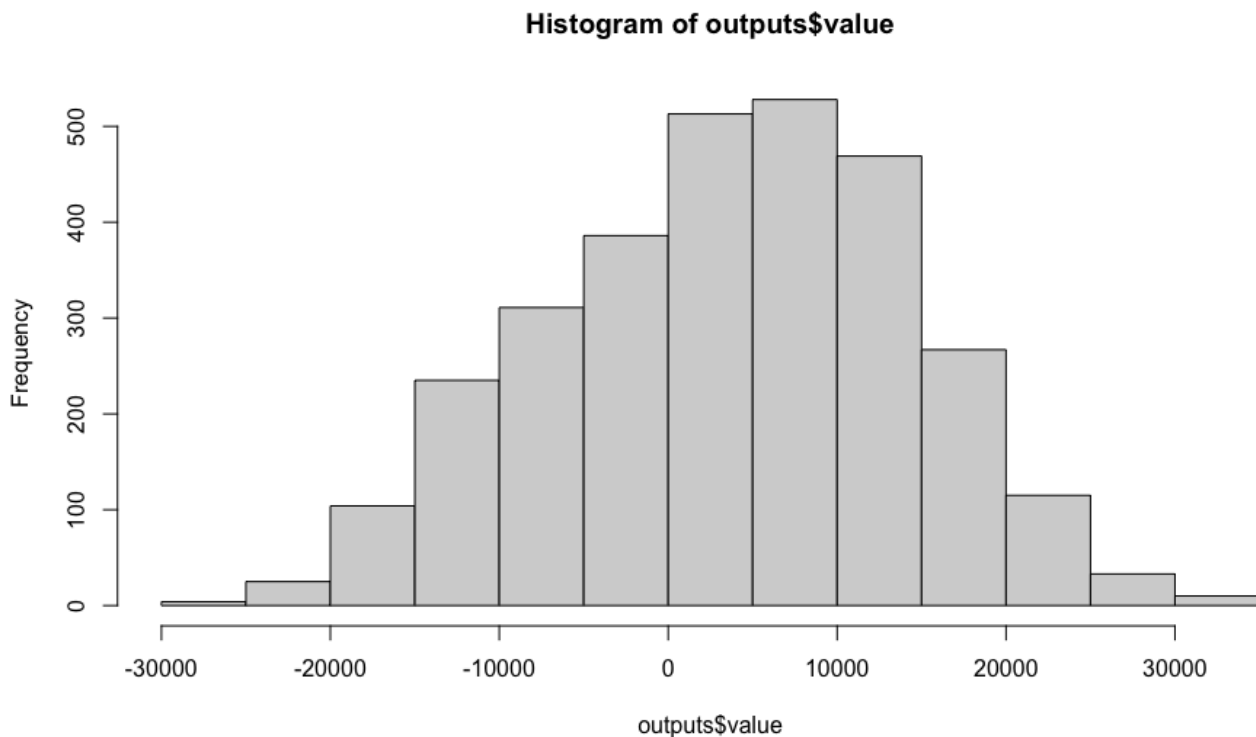
s

0.0173549974880483

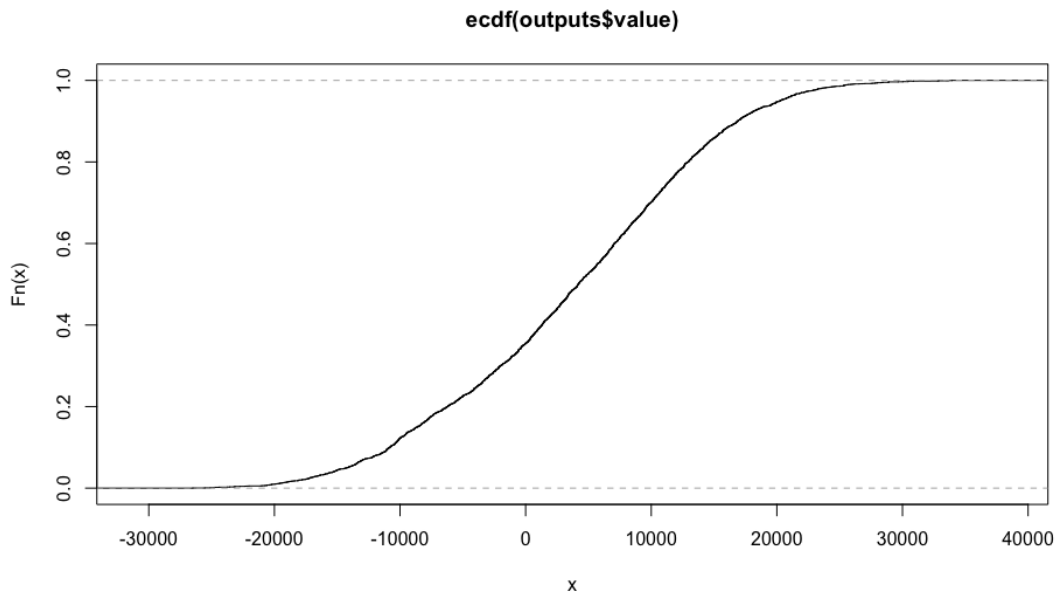
value

2952.66084685292

5) Plot the histogram of outputs\$value



6) Create the empirical CDF of outputs\$value and plot this CDF



7) Calculate the P0, P10, P20, P30, ... P90, P100 and output these values on the R-Console

```

60 #7 calculate the P0,P10... and output values on R-Console
61 quantile(outputs$value, probs = c(seq(0,1,by = 0.1)))
62
63 #8 find P20 to P80 interval values
64
65 px <- data.frame (values = quantile(outputs$value, probs = c(seq(0,1,by = 0.1))))
66
61:54 # (Untitled)
R Script

```

```

+ # store the results with outputs
+ q1 <- sample(inputs$q1 , 1)
+ q2 <- sample(inputs$q2 , 1)
+ p <- sample(inputs$p , 1)
+ s <- sample(inputs$s , 1)
+
+ value <- ((2700 - q1 - q2) * p - (s*p))
+
+ # store the results within outputs
+ outputs <- rbind(outputs, data.frame(value))
+ }
> hist(outputs$value)
> hist(outputs$value)
> empiricalCDF <- ecdf(outputs$value)
> plot(empiricalCDF)
> quantile(outputs$value, probs = c(seq(0,1,by = 0.1)))
      0%      10%      20%      30%      40%      50%      60%      70%      80%      90%     100%
-26495.888 -10836.816 -6206.979 -1997.033  1304.400  4190.421  7060.896  9940.221 12922.506 16884.749 33940.706
>

```

8) Find the P20 to P80 interval values from the empirical CDF.

```

63 #8 find P20 to P80 interval values
64
65 px <- data.frame (values = quantile(outputs$value, probs = c(seq(0,1,by = 0.1))))
66
67 sprintf("Interval of Interest: [ %.2f , %.2f ]", px$values[3], px$values[9])
68
69 #9 create matrix named storage that stores 100 samples
70
71 storage <- matrix(ncol = 100, nrow = 250)
72
73 for(i in 1:100){
68:1 (Untitled) R Script

```

```

R 4.2.2 ~|
+ p <- sample(inputs$p, 1)
+ s <- sample(inputs$s, 1)
+
+ value <- ((2700 - q1 - q2) * p - (s*p))
+
+ # store the results within outputs
+ outputs <- rbind(outputs, data.frame(value))
+ }
> hist(outputs$value)
> hist(outputs$value)
> empiricalCDF <- ecdf(outputs$value)
> plot(empiricalCDF)
> quantile(outputs$value, probs = c(seq(0,1,by = 0.1)))
      0%      10%      20%      30%      40%      50%      60%      70%      80%      90%     100%
-26495.888 -10836.816 -6206.979 -1997.033  1304.400  4190.421  7060.896  9940.221 12922.506 16884.749 33940.706
> px <- data.frame (values = quantile(outputs$value, probs = c(seq(0,1,by = 0.1))))
>
> sprintf("Interval of Interest: [ %.2f , %.2f ]", px$values[3], px$values[9])
[1] "Interval of Interest: [ -6206.98 , 12922.51 ]"
>

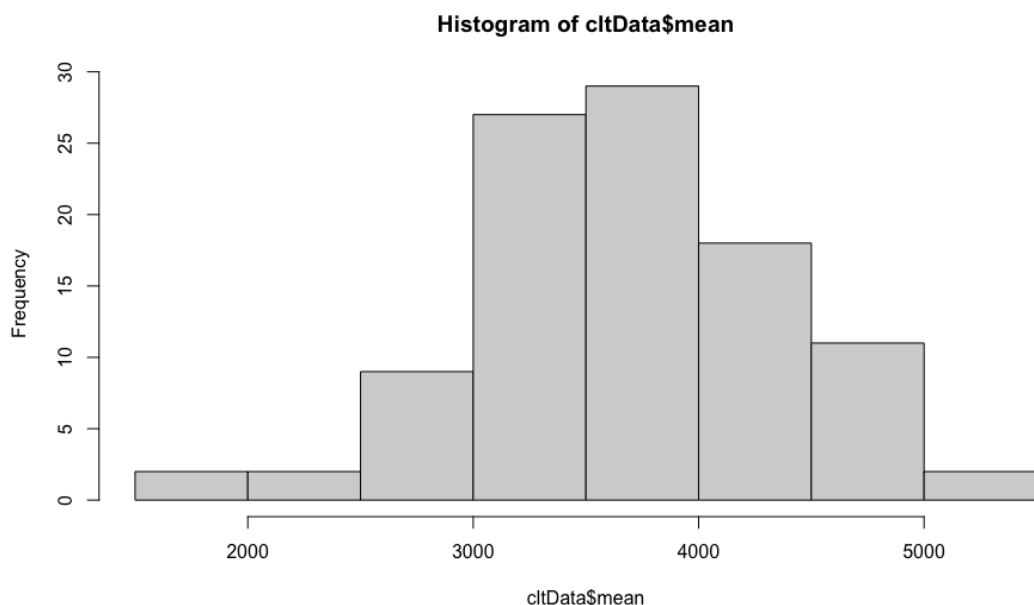
```

9) Create a matrix named **storage** that stores 100 samples of the Monte Carlo simulation of the model in #3. Each Monte Carlo simulation will have 250 realizations.

10) Convert the **storage** matrix into a data frame named **storage**.

11) Create a data frame named **cltData** that stores all the means of each column of the **storage** data frame.

12) Plot the histograms of the data within **cltData**





13) Check if the data within **cltData** is normally distributed. Hint use a normal test for this.

```
102 #13 Use Shapiro test to check if cltdata is normally distributed
```

```
103  
104 shapiro.test(cltData$mean)
```

```
105  
106 #14 state if the data in cltData is normally distributed
```

```
107  
104:1 # (Untitled) ↕
```

```
Console Terminal × Background Jobs ×  
R 4.2.2 · ~/    
+ s <- sample(inputs$s, 1)  
+  
+ value <- ((2700 - q1 - q2) * p - (s*p))  
+  
+ outputData <- rbind(outputData, data.frame(value))  
+ }  
+ storage[, i] <- outputData$value  
+ }  
> storage <- data.frame(storage)  
> cltData <- data.frame(mean = colMeans(storage))  
> par(mfrow=c(1,1))  
> hist(cltData$mean)  
> shapiro.test(cltData$mean)
```

Shapiro-Wilk normality test

```
data: cltData$mean  
W = 0.98514, p-value = 0.3252
```






14) State in your code using a comment if the data in cltData is normal distributed or not and why.

```
106 #14 state if the data in cltData is normally distributed
```

```
107  
108 sprintf("Considering that the p-value is %.4f it is less than 0.5, which means its significantly different from normal distri  
109 shapiro.test(cltData$mean)$p)
```

```
110  
111 #15 calculate the 80% confidence interval and output the lower and upper bounds  
112
```

```
110:1 # (Untitled) ↕ R Script ↕
```

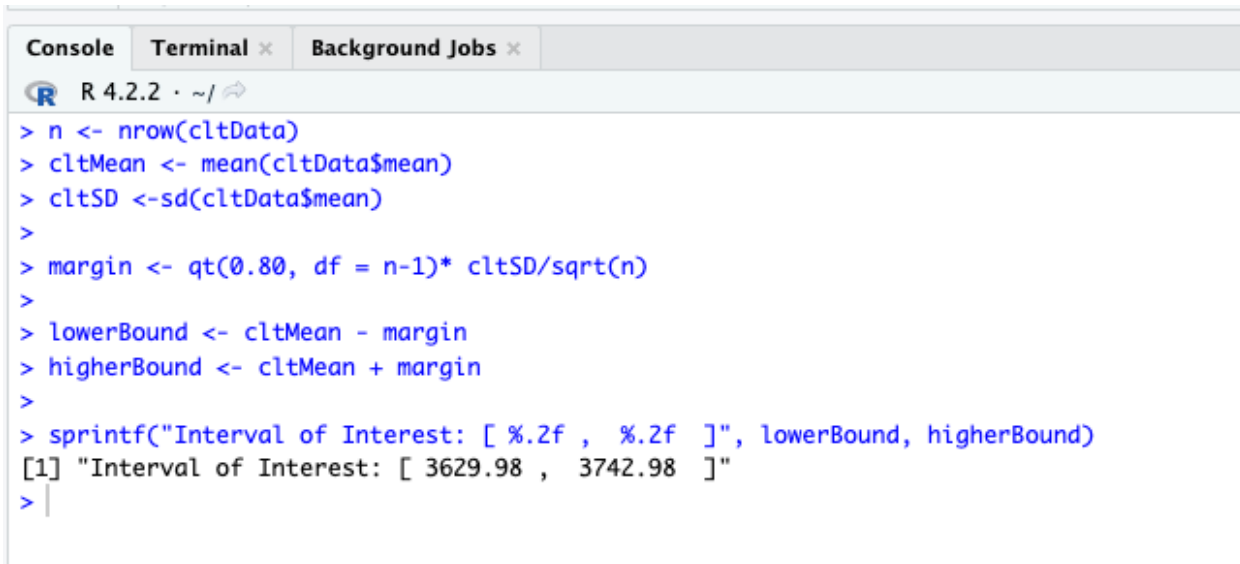
```
Console Terminal × Background Jobs ×    
R 4.2.2 · ~/     
> shapiro.test(cltData$mean)
```

Shapiro-Wilk normality test

```
data: cltData$mean  
W = 0.98514, p-value = 0.3252
```

```
> sprintf("Considering that the p-value is %.4f it is less than 0.5, which means its significantly different from normal distributio  
1.",  
+ shapiro.test(cltData$mean)$p)  
[1] "Considering that the p-value is 0.3252 it is less than 0.5, which means its significantly different from normal distribution."  
>
```

15) Calculate the 80% confidence interval and output the lower and upper bounds of this interval on the R-console



The screenshot shows an R console window with the following tabs: Console, Terminal, and Background Jobs. The console output is as follows:

```
R 4.2.2 · ~/
> n <- nrow(cltData)
> cltMean <- mean(cltData$mean)
> cltSD <- sd(cltData$mean)
>
> margin <- qt(0.80, df = n-1)* cltSD/sqrt(n)
>
> lowerBound <- cltMean - margin
> higherBound <- cltMean + margin
>
> sprintf("Interval of Interest: [ %.2f , %.2f ]", lowerBound, higherBound)
[1] "Interval of Interest: [ 3629.98 , 3742.98 ]"
>
```