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# Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions

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**Abstract.** Many observations of pedestrian dynamics, including various self-organization phenomena, have been reproduced successfully by different models. But the empirical databases for quantitative calibration are still insufficient, e.g. the fundamental diagram as one of the most important relationships displays non-negligible differences among various studies. To improve this situation, experiments in straight corridors and T-junctions are performed. Four different measurement methods are defined to study their effects on the fundamental diagram. It is shown that they have minor influences for  $\rho < 3.5 \text{ m}^{-2}$  but only the Voronoi method is able to resolve the fine structure of the fundamental diagram. This enhanced measurement method permits us to observe the occurrence of a boundary-induced phase transition. For corridors of different widths we found that the specific flow concept works well for  $\rho < 3.5 \text{ m}^{-2}$ . Moreover, we illustrate the discrepancies between the fundamental diagrams of a T-junction and a straight corridor.

**Keywords:** traffic and crowd dynamics

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### 1. Introduction

During the last few decades, research on pedestrian and traffic flow became popular and attracted a lot of attention [1]–[6]. The investigation of pedestrian motion plays an important role in guaranteeing the safety of pedestrians in complex buildings or at mass events. A large number of models have been developed in the past. Most of them are able to reproduce phenomena of pedestrian movement qualitatively. Before using a model to predict quantitative results like the total evacuation time, it needs to be calibrated thoroughly and quantitatively using empirical data. However, this is still difficult due to a lack of reliable experimental data. In addition, the small number of available datasets show surprisingly large differences [7, 8].

In recent years, several well-controlled pedestrian experiments [9]–[13] and field studies [14]–[16] have been performed. One of the most important characteristics of pedestrian dynamics is the fundamental diagram which states the relationship between pedestrian flow and density. Several researchers, in particular Fruin and Pauls [17], Predtechenskii and Milinskii [18], Weidmann [19] and Helbing *et al* [20], have collected information about the relation of occupant density and velocity. But there exists considerable disagreement among these data. In the comparison performed in [21] the density  $\rho_0$ , where the velocity approaches zero due to overcrowding, ranges from 3.8 to  $10 \text{ m}^{-2}$ , while the density  $\rho_c$  where the flow reaches its maximum ranges from 1.75 to  $7 \text{ m}^{-2}$ . Several explanations for these discrepancies have been proposed, including cultural factors [22], and differences between unidirectional and multidirectional flow [23, 24].

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For single-file movements it was found that even the measurement method has a large influence on the fundamental diagram and could be responsible for the observed deviations [21]. For identical facilities (e.g. corridors, stairs, doors) with different width it is usually assumed that the fundamental diagrams are unified in a single diagram for specific flow  $J_s$ . The study of Hankin *et al* [25] in the London subway shows that above a certain minimum of about four feet the maximum flow in subway stations is directly proportional to the width of the corridor. Besides, it is still not clear whether or not the fundamental diagrams for other scenarios like bottlenecks or T-junctions are the same.

Facing such questions, a series of well-controlled laboratory experiments are carried out. The goals of this study are to improve the database related to pedestrian dynamics, to determine the influence of measurement methods on the fundamental diagram, and to check whether or not the fundamental diagram for different types of facilities can be unified in a single diagram.

In section 2, the experiment set-up will be briefly described. The measurement methods used in this paper are introduced and defined in section 3. The main results of the work are in section 4. Finally, we make some concluding remarks in section 5.

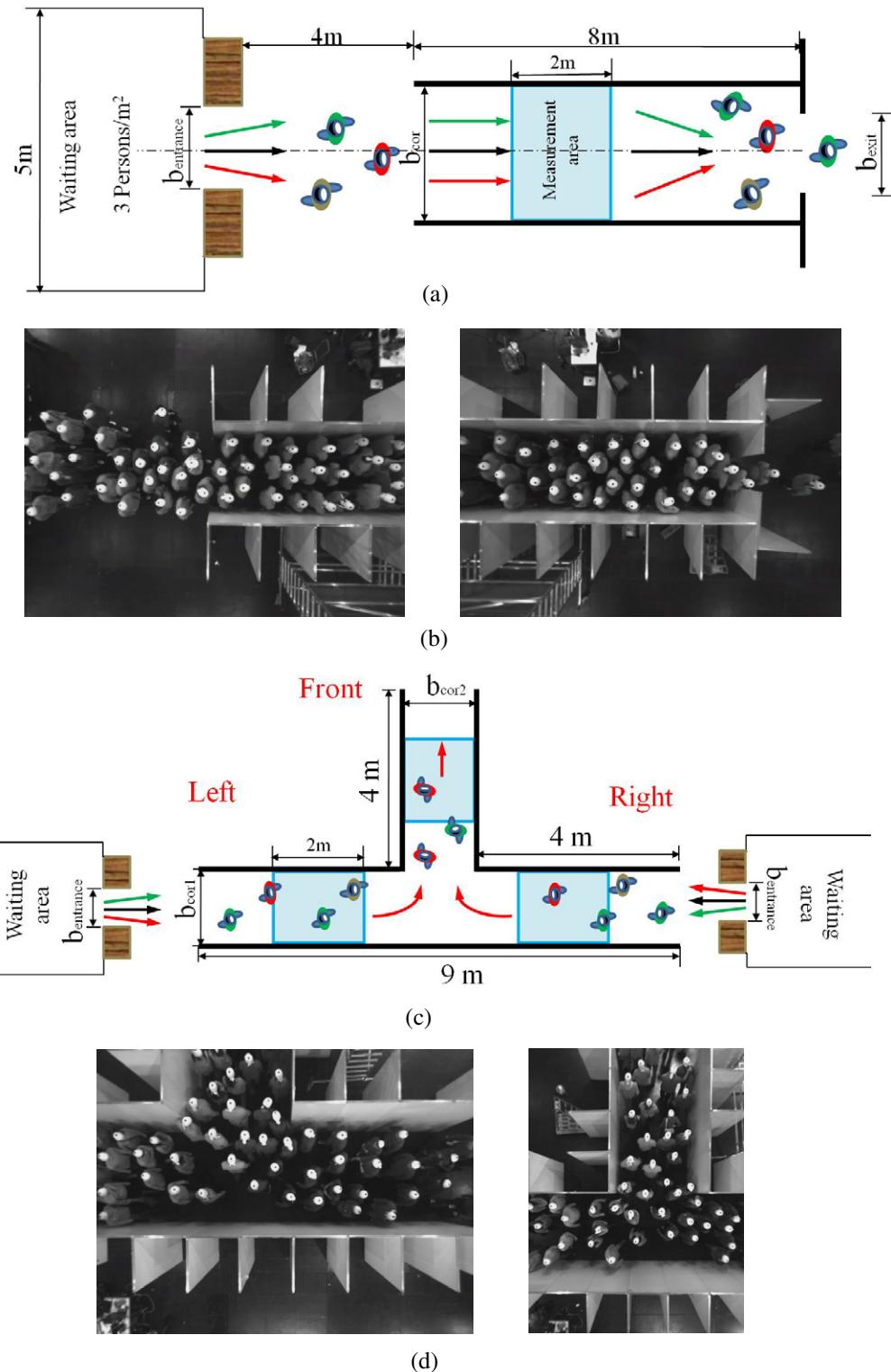
## 2. Experiment set-up

The experiments were performed in Hall 2 of the fairground Düsseldorf (Germany) in May 2009. They are part of the Hermes project [26] in which the data resulting from the experiments will be used to calibrate and test pedestrian movement models. The experiments were conducted with up to 350 participants. They were composed mostly of students and each of them was paid 50 € per day. The mean age and height of the participants were  $25 \pm 5.7$  years and  $1.76 \pm 0.09$  m, respectively. The free velocity  $v_0 = 1.55 \pm 0.18$  m s<sup>-1</sup> was obtained by measuring 42 participants' free movement.

Figure 1 shows the sketches of the set-ups and some snapshots during the experiments. Two types of geometries, straight corridor (C) and T-junction (T), were used in the experiment. 28 runs (see table 2) were performed in straight corridors with widths of 1.8 m, 2.4 m and 3.0 m, respectively. Seven runs for the T-junction with a corridor width of 2.4 m were carried out (see table 3). To regulate the pedestrian density in the corridor, the width of the entrance  $b_{\text{entrance}}$  and the exit  $b_{\text{exit}}$  was changed in each run. For details, see figure 1, tables 2 and 3. At the beginning, the participants were held within a waiting area. Equal densities for different runs were arranged by partitioning the waiting area and counting the number of people in the parts. Standing in the waiting area, they pass through a 4 m passage into the corridor. The passage was used as a buffer to minimize the effect of the entrance. In this way, the pedestrian flow in the corridor was nearly homogeneous over its entire width. When a pedestrian leaves through an exit, he or she returns to the waiting area for the next run.

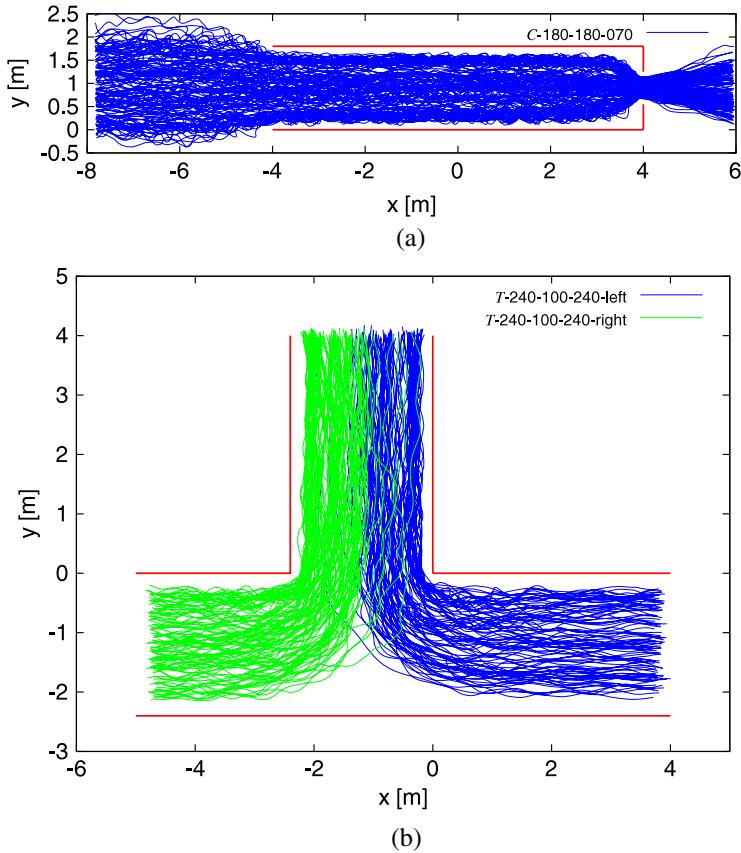
The experiments were recorded by two cameras mounted at the rack of the ceiling of the hall. To cover the complete region, the left and the right part of the corridor were recorded by the two cameras separately. The pedestrian trajectories were automatically extracted from video recordings using the software *PeTrack* [27]. Finally, the trajectory data from the two cameras were corrected manually and combined automatically. The frame rate of the trajectory data corresponds to 16 fps. Figure 2 shows the trajectories

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**Figure 1.** Sketch of the experimental set-up ((a) and (c)) and snapshots of the experiment from the two cameras, respectively ((b) and (d)). The shaded regions in (a) and (c) are the chosen measurement areas 2 m in length.

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**Figure 2.** The trajectories for all pedestrians in the experiment. The data are extracted from the video recording by the free software *PeTrack* [27].

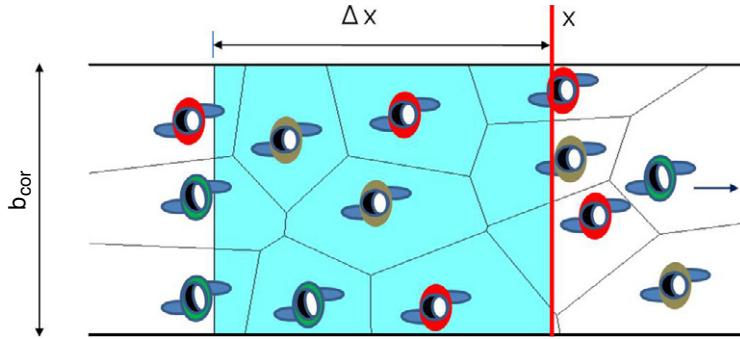
of the head of each pedestrian in two runs of the experiment. From these trajectories, pedestrian characteristics including flow, density and velocity are determined.

### 3. Measurement methods

For vehicular traffic it is well known that different measurement methods lead to different fundamental diagrams [28, 29]. The results presented in [21] using pedestrian trajectories of single-file movement have also shown how large variations induced by different measurement methods could be. In previous studies of pedestrian streams, different measurement methods were used, limiting the comparability of the data. Helbing *et al* proposed a Gaussian, distance-dependent weight function [20] to measure the local density and local velocity. Predtechenskii and Milinskii [18] used a dimensionless definition to consider different body sizes and Fruin introduced the ‘pedestrian area module’ [17]. All of these definitions have their advantages and disadvantages. To analyze all of them goes beyond the scope of this paper. To enable a detailed analysis, we study the influence of several measurement methods on the fundamental diagram and analyze which methods lead to the smallest fluctuations.

In this study four measurement methods were used to calculate the basic quantities: flow, density and velocity. Some terminologies used here are taken from [21] and [30].

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**Figure 3.** Illustration of different measurement methods. Method A is a kind of local measurement at cross section with position  $x$  averaged over a time interval  $\Delta t$ , while Methods B–D measure at a certain time and average the results over space  $\Delta x$ . Note that for Method D, the Voronoi diagrams are generated according to the spatial distributions of pedestrians frame by frame.

### 3.1. Method A

Method A calculates the mean value of flow and density over time. A reference location  $x$  in the corridor is taken and studied over a fixed period of time  $\Delta t$  (as shown in figure 3). We refer to this average by  $\langle \cdot \rangle_{\Delta t}$ . Using this method we can obtain the pedestrian flow  $J$  and the velocity  $v_i$  of each pedestrian passing  $x$  directly. Thus, the flow over time  $\langle J \rangle_{\Delta t}$  and the time mean velocity  $\langle v \rangle_{\Delta t}$  can be calculated as

$$\langle J \rangle_{\Delta t} = \frac{N_{\Delta t}}{t_{N_{\Delta t}}} \quad \text{and} \quad \langle v \rangle_{\Delta t} = \frac{1}{N_{\Delta t}} \sum_{i=1}^{N_{\Delta t}} v_i(t) \quad (1)$$

where  $N_{\Delta t}$  is the number of persons passing the location  $x$  during the time interval  $\Delta t$ .  $t_{N_{\Delta t}}$  is the time between the first and the last of the  $N_{\Delta t}$  pedestrians. Thus  $t_{N_{\Delta t}}$  is the actual time that the  $N_{\Delta t}$  pedestrians used for passing the location. It can be different from  $\Delta t$ . The time mean velocity  $\langle v \rangle_{\Delta t}$  is defined as the mean value of the instantaneous velocities  $v_i(t)$  of the  $N_{\Delta t}$  persons according to equation (2). We calculate  $v_i(t)$  by use of the displacement of pedestrian  $i$  in a small time interval  $\Delta t'$  around  $t$ :

$$v_i(t) = \frac{x_i(t + \Delta t'/2) - x_i(t - \Delta t'/2)}{\Delta t'}. \quad (2)$$

### 3.2. Method B

The second method measures the mean value of velocity and density over space and time. The spatial mean velocity and density are calculated by taking a segment  $\Delta x$  in the corridor as the measurement area. The velocity  $\langle v \rangle_i$  of each person is defined as the length  $\Delta x$  of the measurement area divided by the time he or she needs to cross the area (see equation (3)):

$$\langle v \rangle_i = \frac{\Delta x}{t_{\text{out}} - t_{\text{in}}} \quad (3)$$

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where  $t_{\text{in}}$  and  $t_{\text{out}}$  are the times a person enters and exits the measurement area, respectively. The density  $\rho_i$  for each person is calculated with equation (4):

$$\langle \rho \rangle_i = \frac{1}{t_{\text{out}} - t_{\text{in}}} \int_{t_{\text{in}}}^{t_{\text{out}}} \frac{N'(t)}{b_{\text{cor}} \Delta x} dt \quad (4)$$

where  $b_{\text{cor}}$  is the width of the measurement area while  $N'(t)$  is the number of persons in this area at a time  $t$ .

### 3.3. Method C

The third measurement method is the classical method. The density  $\langle \rho \rangle_{\Delta x}$  is defined as the number of pedestrians divided by the area of the measurement section:

$$\langle \rho \rangle_{\Delta x} = \frac{N}{b_{\text{cor}} \Delta x}. \quad (5)$$

The spatial mean velocity is the average of the instantaneous velocities  $v_i(t)$  for all pedestrians in the measurement area at time  $t$ :

$$\langle v \rangle_{\Delta x} = \frac{1}{N} \sum_{i=1}^N v_i(t). \quad (6)$$

### 3.4. Method D

This method is based on the use of Voronoi diagrams [31] which are a special kind of decomposition of a metric space determined by distances to a specified discrete set of objects in the space. At any time the positions of the pedestrians can be represented as a set of points, from which the Voronoi diagram (see figure 3) can be generated. The Voronoi cell area,  $A_i$ , for each person  $i$  can be obtained. Then, the density and velocity distribution of the space,  $\rho_{xy}$  and  $v_{xy}$ , can be defined as

$$\rho_{xy} = 1/A_i \quad \text{and} \quad v_{xy} = v_i(t) \quad \text{if } (x, y) \in A_i \quad (7)$$

where  $v_i(t)$  is the instantaneous velocity of each person, see equation (2). The Voronoi density and velocity for the measurement area is defined as [30]

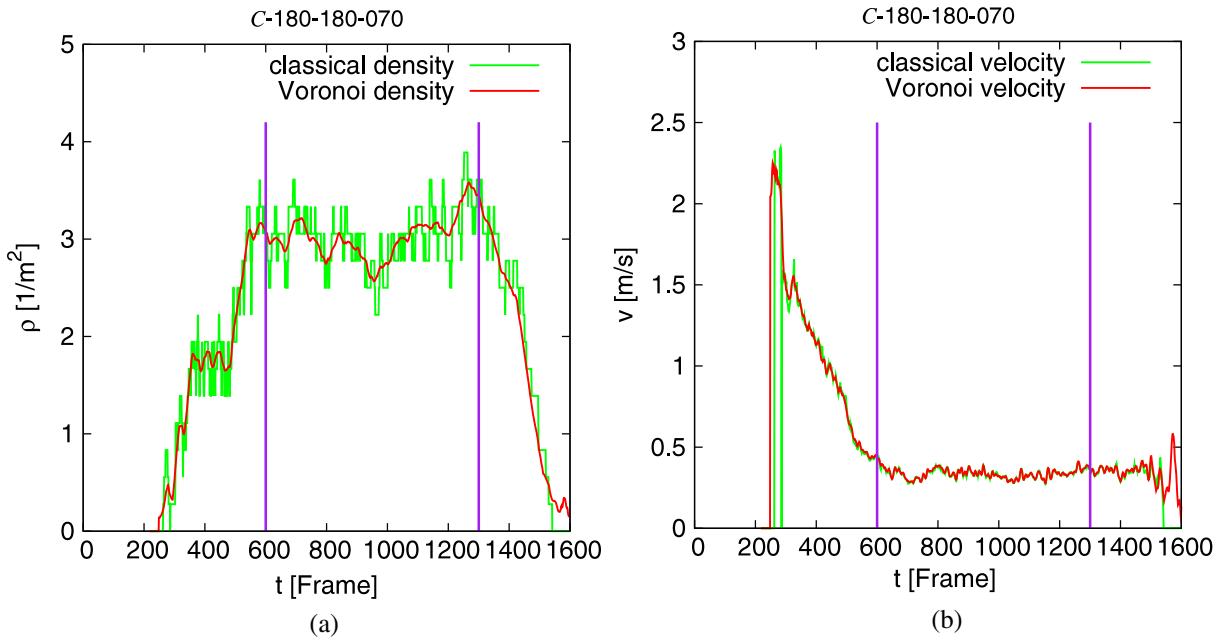
$$\langle \rho \rangle_v = \frac{\iint \rho_{xy} dx dy}{b_{\text{cor}} \Delta x} \quad (8)$$

$$\langle v \rangle_v = \frac{\iint v_{xy} dx dy}{b_{\text{cor}} \Delta x}. \quad (9)$$

## 4. Results

We calculate the fundamental diagram for the straight corridor experiments using the methods introduced in section 5. To facilitate a comparison among these four methods, we use the hydrodynamic flow equation  $J = \rho v b$ .

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**Figure 4.** Time series of density and velocity using Methods C and D. The two vertical lines indicate the beginning and the end of stationary states.

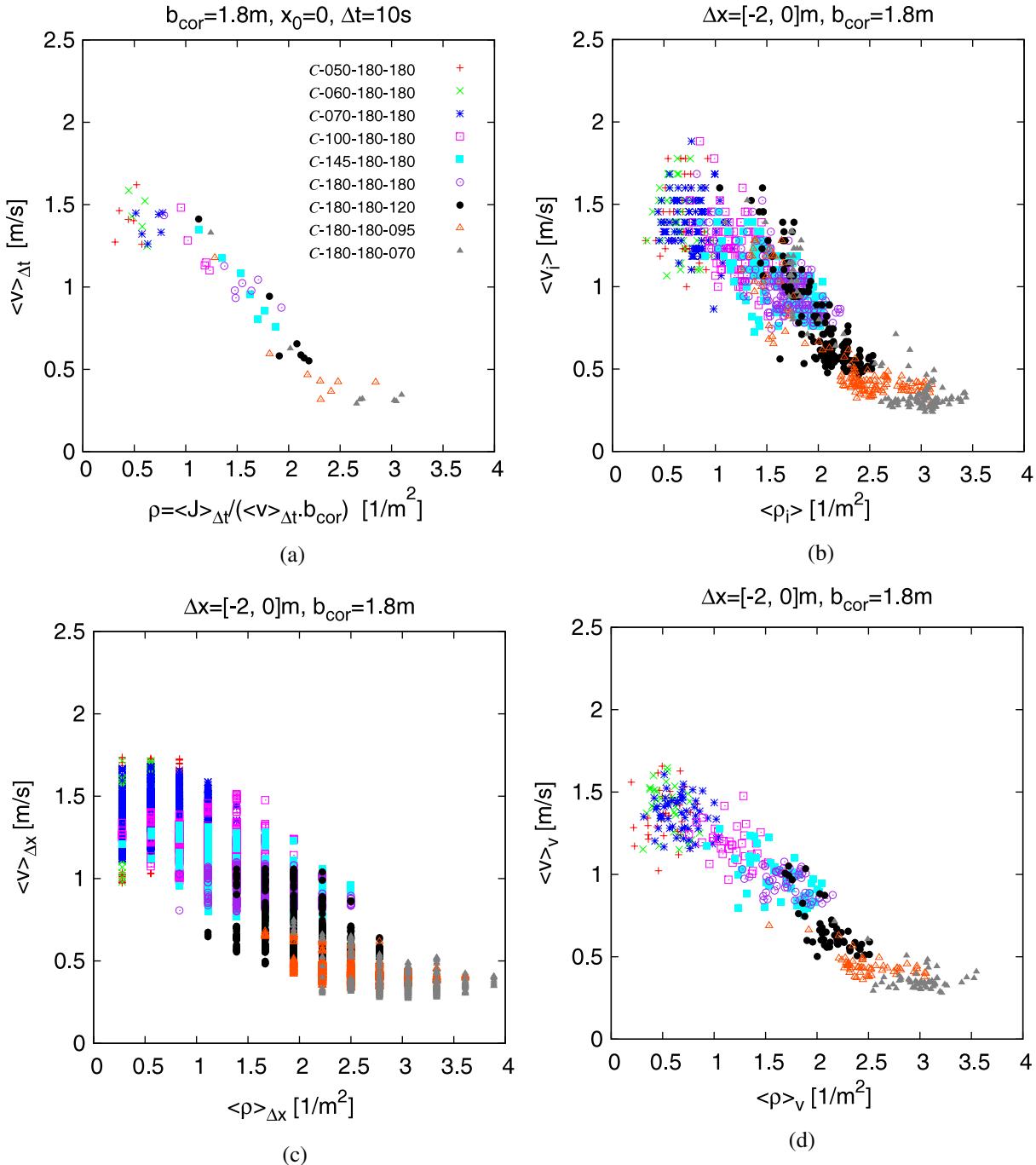
#### 4.1. Influence of the measurement method

For Method A we choose the time interval  $\Delta t = 10$  s,  $\Delta t' = 0.625$  s (corresponding to ten frames) and the measurement position at  $x = 0$  (see figure 2). For the other three methods a rectangle with length 2 m from  $x = -2$  m to 0 and the width of the corridor is chosen as the measurement area. We calculate the densities and velocities every frame with a frame rate of 16 fps. All data below are obtained from the trajectories. To determine the fundamental diagram only data at stationary states, which were selected manually by analyzing the time series density and velocity (see figure 4), were used. For Method D we use one frame per second to decrease the number of data points and to represent the data more clearly.

Figure 5 shows the relationship between density and velocity obtained from different methods. Using Method A the flow and mean velocity can be obtained directly. To get the relationship between density and flow, the equation  $\rho = \langle J \rangle_{\Delta t} / (\langle v \rangle_{\Delta t} b_{\text{cor}})$  was adopted to calculate the density. For Methods B, C and D the mean density and velocity can be obtained directly since they are mean values over space. There exists a similar trend of the fundamental diagram obtained using different methods. However, their influence on the scatter of the results is obvious. Table 1 shows the standard deviation of velocities in certain density intervals for different measurement methods. Compared to the other approaches, the fluctuations in Methods B and C are larger.

Another criterion for the quality of the methods is the resolution in time and space. Even if Method A provides a smaller standard deviation than Method D, the low resolution in time smears the transition at  $\rho = 2 \text{ m}^{-2}$  clearly visible in figure 5(d). The density in Method C has a strong dependence on the size of the measurement area  $A_m = b_{\text{cor}} \Delta x$ . The interval between two density values is  $1/A_m$ , which indicates that the measurement

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**Figure 5.** The fundamental diagrams, the relationship between density and velocity, measured on the same set of trajectories but with different methods. Except for the density in (a), which is calculated using  $\rho = J/(b\Delta x)$ , all data are determined directly from the trajectories. The legends in (b), (c) and (d) are the same as in (a).

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**Table 1.** Standard deviation of velocities in certain density interval for different methods.

Density interval (m <sup>-2</sup> )	Method A (m s <sup>-1</sup> )	Method B (m s <sup>-1</sup> )	Method C (m s <sup>-1</sup> )	Method D (m s <sup>-1</sup> )
$\rho \in [0.8, 1.2]$	0.119	0.169	0.175	0.120
$\rho \in [1.6, 2.0]$	0.086	0.144	0.175	0.111

**Table 2.** Parameters for the straight corridor experiments.

Experiment index	Name	$b_{\text{entrance}}$ (m)	$b_{\text{cor}}$ (m)	$b_{\text{exit}}$ (m)	$N$
1	C-050-180-180	0.50	1.80	1.80	61
2	C-060-180-180	0.60	1.80	1.80	66
3	C-070-180-180	0.70	1.80	1.80	111
4	C-100-180-180	1.00	1.80	1.80	121
5	C-145-180-180	1.45	1.80	1.80	175
6	C-180-180-180	1.80	1.80	1.80	220
7	C-180-180-120	1.80	1.80	1.20	170
8	C-180-180-095	1.80	1.80	0.95	159
9	C-180-180-070	1.80	1.80	0.70	148
10	C-065-240-240	0.65	2.40	2.40	70
11	C-080-240-240	0.80	2.40	2.40	118
12	C-095-240-240	0.95	2.40	2.40	108
13	C-145-240-240	1.45	2.40	2.40	155
14	C-190-240-240	1.90	2.40	2.40	218
15	C-240-240-240	2.40	2.40	2.40	246
16	C-240-240-160	2.40	2.40	1.60	276
17	C-240-240-130	2.40	2.40	1.30	247
18	C-240-240-100	2.40	2.40	1.00	254
19	C-080-300-300	0.80	3.00	3.00	119
20	C-100-300-300	1.00	3.00	3.00	100
21	C-120-300-300	1.20	3.00	3.00	163
22	C-180-300-300	1.80	3.00	3.00	208
23	C-240-300-300	2.40	3.00	3.00	296
24	C-300-300-300	3.00	3.00	3.00	349
25	C-300-300-200	3.00	3.00	2.00	351
26	C-300-300-160	3.00	3.00	1.60	349
27	C-300-300-120	3.00	3.00	1.20	348
28	C-300-300-080	3.00	3.00	0.80	270

**Table 3.** Parameters for the T-junction experiments.

Experiment index	Name	$b_{\text{cor1}}$ (m)	$b_{\text{entrance}}$ (m)	$b_{\text{cor2}}$ (m)	$N$
1	T-240-050-240	2.40	0.50	2.40	134
2	T-240-060-240	2.40	0.60	2.40	132
3	T-240-080-240	2.40	0.80	2.40	228
4	T-240-100-240	2.40	1.00	2.40	208
5	T-240-120-240	2.40	1.20	2.40	305
6	T-240-150-240	2.40	1.50	2.40	305
7	T-240-240-240	2.40	2.40	2.40	302

area should not be too small using this method. But large areas cannot provide a detailed spatial resolution. Method D can reduce the density and velocity scatter [30]. The reduced fluctuation of Method D is combined with a good resolution in time and space, which reveal a phenomenon that is not observable with Methods A, B and C. In figure 5(d) it seems that there is a discontinuity of the fundamental diagram when the density is about  $2 \text{ m}^{-2}$ . This will be analyzed in detail in section 4.3.

Figure 6 shows the relationship between the density and flow obtained from different methods. The pedestrian flow shows small fluctuations at low densities and high fluctuations at high densities. The fluctuations for Method A and Method D are smaller than those for other methods. However, there is a major difference between the results. While the fundamental diagrams obtained using Method A and Method C are smooth, fundamental diagrams obtained with Method B and Method D show a clear discontinuity at a density of about  $2 \text{ m}^{-2}$ . The average over a time interval of Method A and the large scatter of Method C blur this discontinuity. In disagreement with the results in [21], no marked differences occur among the fundamental diagrams produced by different methods (see figure 5). In [21], single-file movement in a corridor with periodic boundary was studied. In that experiment, distinct stop waves occurred at high densities and lead to large inhomogeneities in the trajectories. Possibly the differences of different methods will be larger in the cases where stop waves occur or when the characteristic of the pedestrian flow is not laminar.

#### 4.2. Influence of the corridor width

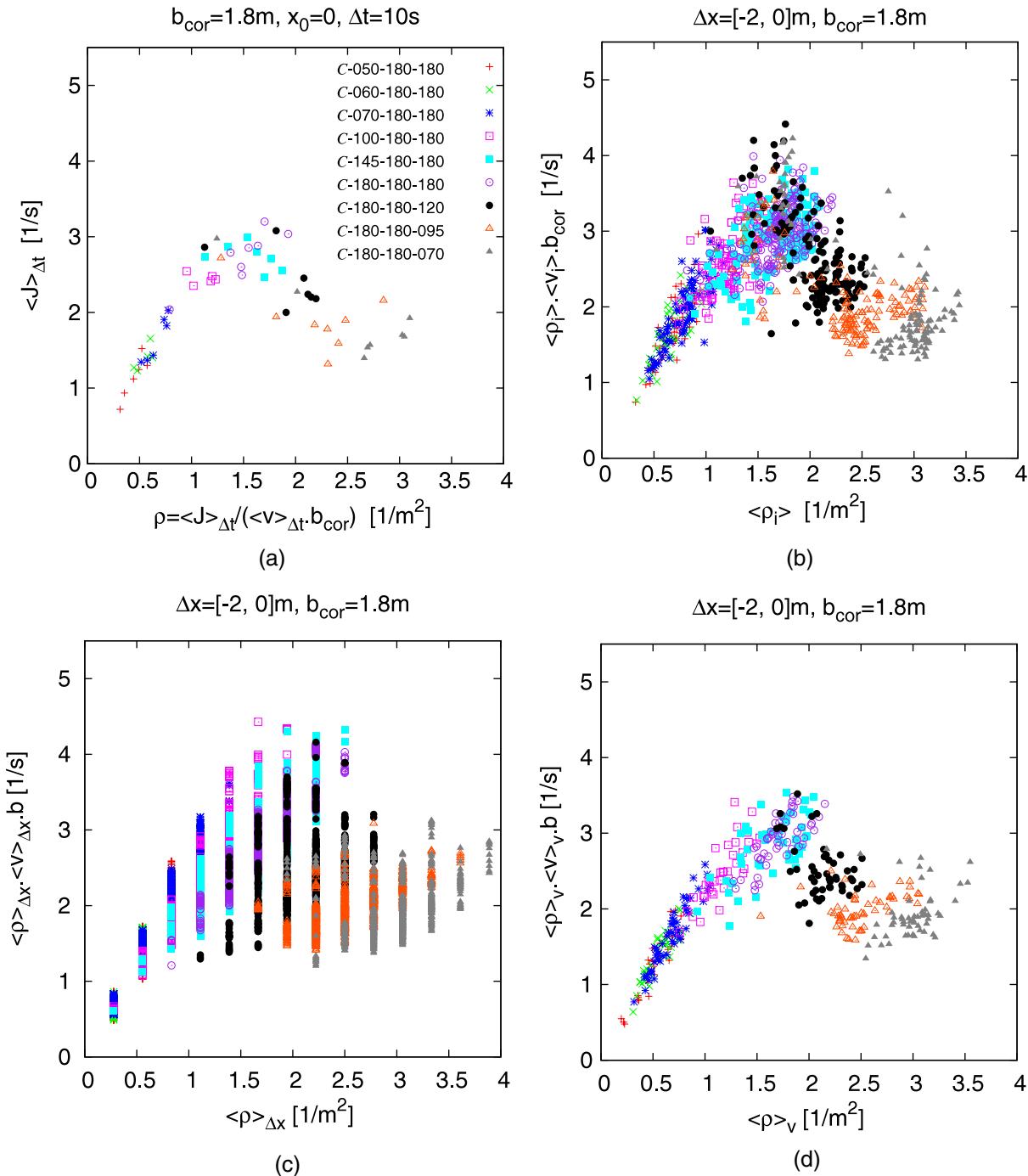
From the above analysis it can be concluded that there is no large influence of different methods on the results for the density region without the stop wave phenomenon. We have shown that the results with the smallest fluctuations are provided by Methods A and D. Thus we analyze the other unidirectional experiments with corridor widths 2.4 and 3.0 m using Method A and Method D.

Figure 7 shows the relationship between density, velocity and flow using these two methods. The fundamental diagram of the same type of corridor but with different widths are compared. The fundamental diagrams for these three widths agree well for both methods. This result is in conformance with Hankin's findings [25]. He found that above a certain minimum of about 4 ft (about 1.22 m) the maximum flow in subways is directly proportional to the width of the corridor. Our results agree with the assumption that the specific flow  $J_s = J/b$  is independent of the width of the facility. However, it is possible that for small corridors or very high densities  $J_s$  becomes dependent on  $b$ .

#### 4.3. Discontinuous trend of the fundamental diagram

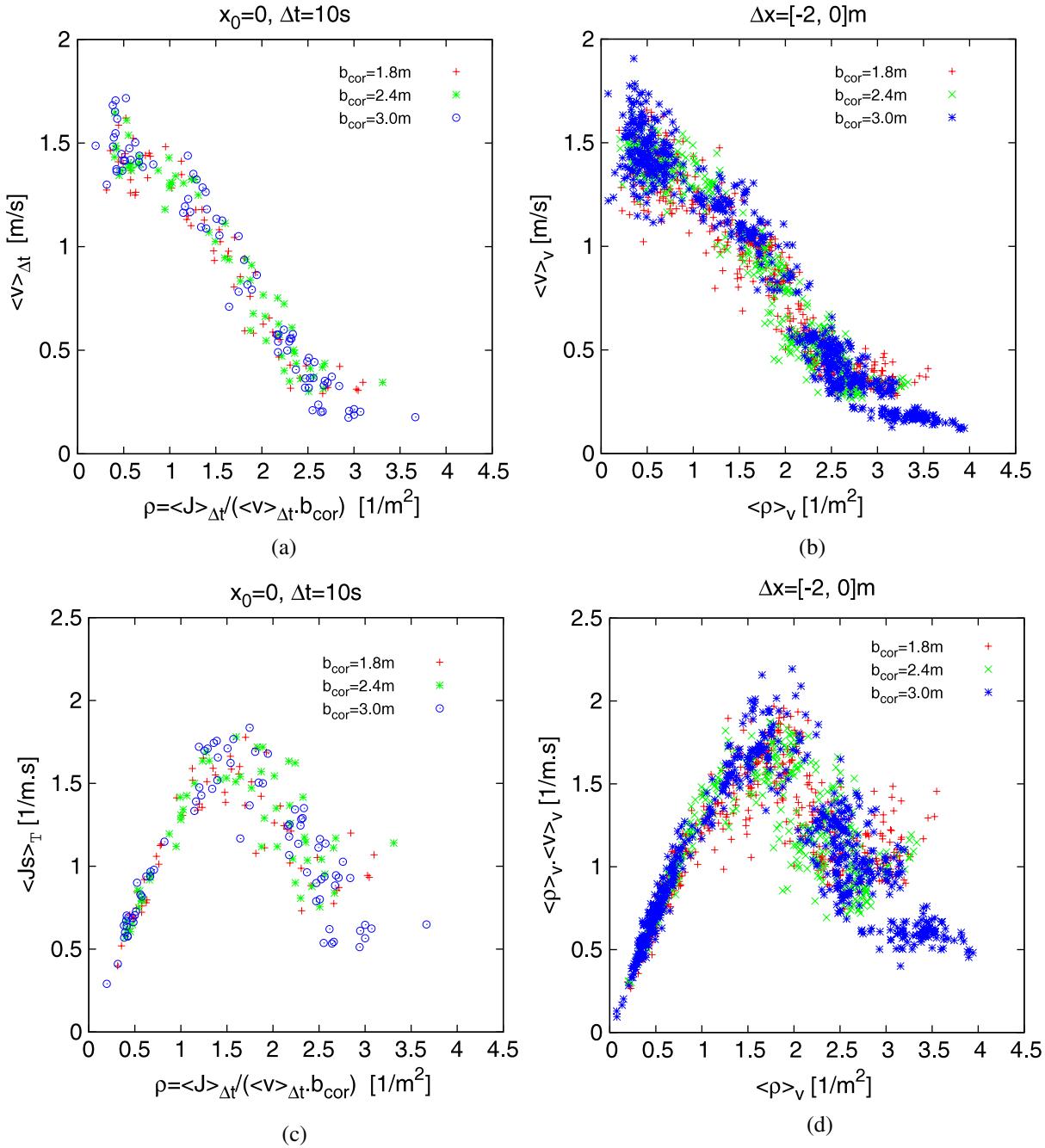
In figures 5(b) and (d) a discontinuity occurs at  $\rho \approx 2 \text{ m}^{-2}$ , separating the function  $J_s(\rho)$  in a region  $\rho < 2 \text{ m}^{-2}$  with negative curvature and a region  $\rho > 2 \text{ m}^{-2}$  with positive curvature. Moreover, for Method D a gap occurs around  $v = 0.7 \text{ m s}^{-1}$ . This transition is also found in the experiments with  $b_{\text{cor}} = 2.4 \text{ m}$  and  $b_{\text{cor}} = 3.0 \text{ m}$ . The fundamental diagram changes qualitatively when the width  $b_{\text{exit}}$  of the exit is modified. The modification of the exit width was necessary to achieve high densities. However, it seems that this slight change in the experimental set-up causes a significant change in the flow-density relation. This point becomes obvious in the velocity-density relation,

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**Figure 6.** The fundamental diagrams, the relationship between density and flow, measured at the same set of trajectories but with different methods. The density in (a) is calculated indirectly using  $\rho = J/(b\Delta x)$ , while the flows in (b), (c) and (d) are obtained by adopting the equation  $J = \rho vb$ . The legends in (b), (c) and (d) are the same as in (a).

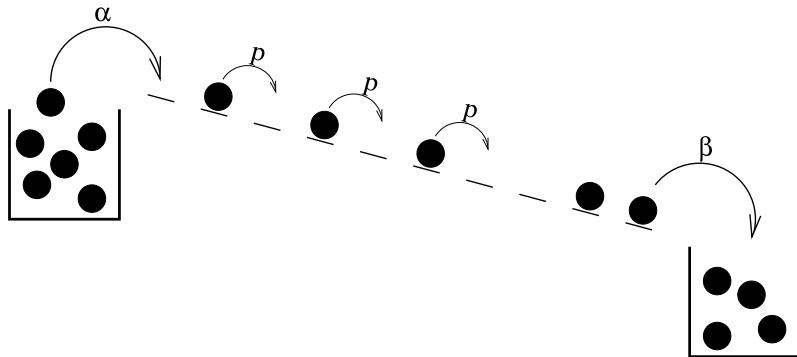
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**Figure 7.** Comparison of the fundamental diagram in different corridor widths.

especially in figure 5(d) which is obtained from Method D. Although the measurement area in the corridor is 4 m away from the exit, the influence of the change of the exit on the fundamental diagram is sensitive. The decreasing of the exit width limits the outflow of pedestrians and leads to a discontinuity in the fundamental diagram. This can be interpreted in terms of the well-established theory of boundary-induced phase transitions, see section 4.4.

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**Figure 8.** Open system with particle input at the left boundary with rate  $\alpha$  and particle output at the right boundary with rate  $\beta$ .

#### 4.4. Interpretation in terms of boundary-induced phase transitions

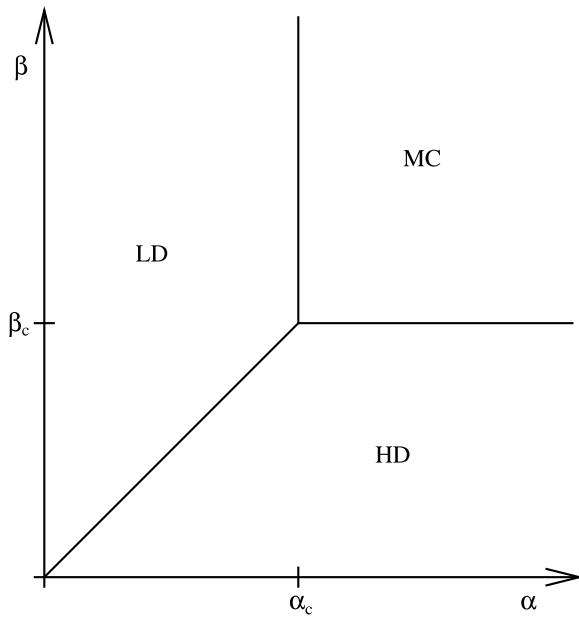
Some of the results can be interpreted in terms of the well-established theory of boundary-induced phase transitions [6, 32]. In nonequilibrium systems phase transitions (in the bulk) can be induced by changing boundary conditions, generically input and output rates in the case of transport systems. A mesoscopic theory has been developed which allows us to derive the phase diagram of an open system (allowing input and output of particles at the boundaries, see figure 8) from the fundamental diagram of the periodic system [33]. This theory even makes quantitative predictions on the basis of an extremal principle [34].

The phase diagram as a function of the boundary rates  $\alpha$  and  $\beta$  has a generic structure. The number of phases observed depends only on the number of local maxima in the fundamental diagram. For generic traffic systems it has only one maximum and the  $\alpha$ - $\beta$  phase diagram consists of three phases, the high-density phase (HD), the low-density phase (LD) and the maximum current phase (MC), see figure 9. When the supply rate  $\alpha$  of the particles is larger than the removal rate  $\beta$  and  $\beta < \beta_c$ , the particle extraction is the limiting process resulting in a high-density phase where the current is independent of  $\alpha$ . When the particles are supplied not too fast,  $\alpha < \alpha_c$  and  $\beta > \alpha$ , a low-density phase is formed which is limited by particle supply. Here the current is independent of  $\alpha$ . There is a discontinuous phase transition along the line  $\alpha = \beta < \alpha_c$ . When particles are supplied and removed sufficiently rapidly,  $\alpha > \alpha_c$  and  $\beta > \beta_c$ , a continuous phase transition into a maximum current phase for which transport is bulk-dominated [32] occurs where the current is independent of both  $\alpha$  and  $\beta$ .

The experiments in the corridor geometry can effectively be described by such a scenario. The input rate  $\alpha$  into the corridor is controlled by the width  $b_{\text{entrance}}$  of the entrance whereas the output rate  $\beta$  is controlled by the width  $b_{\text{exit}}$  of the exit. Therefore the  $\alpha$ - $\beta$  phase diagram corresponds in our case to a  $b_{\text{entrance}}-b_{\text{exit}}$  diagram. The width  $b_{\text{cor}}$  of the corridor, on the other hand, controls the maximal possible bulk flow in the system, given by the maximal flow  $J_{\max}$  in the fundamental diagram.

For the experiments with  $b_{\text{exit}} = b_{\text{cor}}$  the flow through the system is not limited by the exit (see figure 6), corresponding to the case  $\beta > \beta_c$ . The system is then in the low-density phase. Here the flow is controlled by the inflow into the system, i.e. effectively by  $b_{\text{entrance}}$ . At  $b_{\text{entrance}} \approx 1.45$  m a transition into the maximum current phase can be

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**Figure 9.** Generic form of the phase diagram for an open system with input rate  $\alpha$  and output rate  $\beta$ . In the LD phase the current has the form  $J = J(\alpha; p)$  and in the HD phase  $J = J(\beta; p)$ . In the MC phase, the current is independent of  $\alpha$  and  $\beta$  and corresponds to the maximum of the fundamental diagram:  $J = J_{\max}(p)$ .

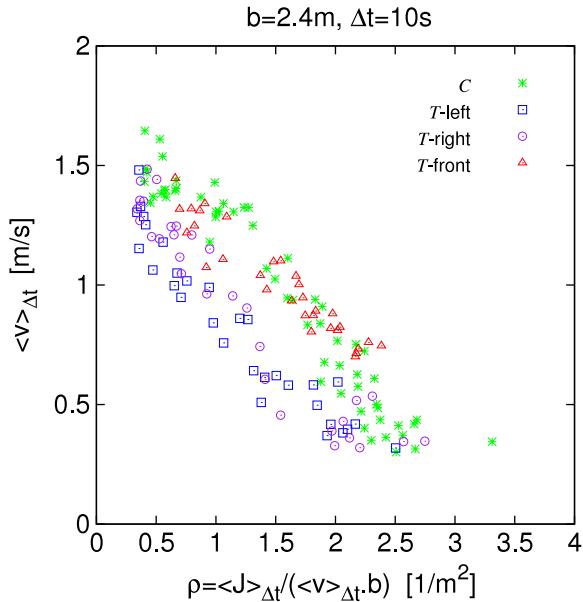
observed (see especially figure 6(a)). For  $b_{\text{entrance}} = b_{\text{cor}}$  and  $b_{\text{exit}} < b_{\text{cor}}$  the system is in the high-density phase. The phase diagram will be investigated in more detail in a separate publication [35].

#### 4.5. Comparison of straight corridor with T-junction

In this section, we compare the fundamental diagrams for a straight corridor (C) and T-junction (T) with channel width  $b = 2.4$  m.

Figure 10 shows the results obtained from the experiments C and T using Method A. The data assigned with ‘T-left’ and ‘T-right’ are measured in the area before the stream merge (see figure 1(c)). The data assigned with ‘T-front’ are measured in the region where the streams already merged. The comparison shows that the fundamental diagram of the unidirectional flow agrees with the fundamental diagram of the T-junction in the ‘front’ part (T-front). But for the density region  $\rho$  from 0.5 to  $2 \text{ m}^{-2}$  the velocities at the ‘right’ and ‘left’ parts of the T-junction (T-left and T-right) are significantly lower. For densities higher than  $2 \text{ m}^{-2}$  the difference is smaller. The differences in the fundamental diagram could be interpreted in the following way. The dynamics in the region after the merging of the streams is comparable with the unidirectional pedestrian flow in an open corridor. But in front of the merging the velocities are significantly lower, indicating that the dynamics of the stream changes due to the change of the geometry and the merging of the streams.

Transitions in pedestrian fundamental diagrams of straight corridors and T-junctions



**Figure 10.** Comparison of the fundamental diagrams between straight corridor and T-junction.

## 5. Summary

A series of well-controlled laboratory pedestrian experiments were performed in straight corridors and T-junctions in this study. Up to 350 persons participated in these activities and the whole processes of the experiment were recorded using two video cameras. The trajectories of each pedestrian are extracted with high accuracy from the video recordings automatically using *PeTrack*. Four measurement methods are adopted in this study and their influences on the fundamental diagram are investigated. It is found that the results obtained from different methods agree well and the main differences are the range of the fluctuations and the resolution in time of the results. The influence of the corridor width on the results is also investigated. It is shown that fundamental diagrams for the same type of facility but different widths agree well and can be unified in one diagram for specific flow. From the comparison of the fundamental diagrams between straight corridor and T-junction, it is indicated that the fundamental diagrams for different facilities are not comparable. The reason for this difference may be the equilibration between the inflow and outflow of pedestrians in the corridor. When the outflow and the inflow are not equal, a transition between low and high densities appears in the pedestrian flow. This transition can also be observed in the fundamental diagram.

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