

1) • $x_0 = 4\sin^2\theta$, $x_{n+1} = 4x_n - x_n^2 \rightarrow x_{n+1} = 4\sin^2(2^n\theta)$

$$x_{0+1} = 4(4\sin^2\theta) - 4^2(\sin^2\theta)^2$$

$$= 16\sin^2\theta - 16(\sin^2\theta)^2$$

$$= 16(\sin^2\theta - (\sin^2\theta)^2)$$

$$= 16\sin^2\theta(1 - \sin^2\theta)$$

$$= 16\sin^2\theta \cos^2\theta \quad \begin{matrix} \cos^2\theta = 1 - \sin^2\theta \\ \sin(2\theta) = 2\sin\theta\cos\theta \end{matrix}$$

$$x_{0+1} = 4\sin^2(2\theta) = x_{n+1} = 4\sin^2(2^{n+1}\theta)$$

$$x_1 = 4\sin^2(2\theta), \quad \theta \in [0, \pi/2]$$

$$4\sin^2(2\theta) \text{ en } 0 \leq \theta \leq \pi/2, \quad \begin{matrix} \text{Valor máximo} = 4 \\ \text{Valor mínimo} = 0 \end{matrix}$$

• $x_0 = \sin^2\theta$, $x_{n+1} = 4x_n - 4x_n^2$

$$x_{0+1} = 4(\sin^2\theta) - 4(\sin^2\theta)^2$$

$$= 4(\sin^2\theta - (\sin^2\theta)^2)$$

$$= 4\sin^2\theta(1 - \sin^2\theta)$$

$$= 4\sin^2\theta\cos^2\theta$$

$$= \sin^2(2\theta), \quad \theta \in [0, \pi/2]$$

$$x_1 = \sin^2(2\theta) = x_{n+1} = \sin^2(2^{n+1}\theta)$$