

# Standard GAN vs W-GAN for image colorization

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- 1 Introduction
- 2 Data pre-processing
- 3 cGAN architecture
- 4 W GAN
- 5 Results
- 6 Conclusions

**Image colorization:** The goal is to assign plausible colors to each pixel of a grayscale image.

In this project, we have implemented two generative models:

- 1 Based on the **PatchGAN architecture** developed by Isola et al. in 2016 <sup>1</sup>
- 2 Variation of the previous one introducing the **Wasserstein distance** as the objective function

## Dataset

**Tiny-ImageNet-200**, composed by images with  $64 \times 64$  pixels resolution.

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<sup>1</sup>P. Isola, J. Zhu, T. Zhou, and A. A. Efros, “Image-to-image translation with conditional adversarial networks,” CoRR, vol. abs/1611.07004, 2016.

- The images were transformed from the RGB to the *Lab* color space.
- Grayscale input images were created by isolating the *Luminance channel*, which was duplicated twice to preserve the original image structure of  $64 \times 64 \times 3$ .
- All images were *normalized* to the range of  $[-1,1]$ .

## Data Loading

- *Training set*: 100k images, divided into 500 per class.
- *Testing set*: 1k images, divided into 50 per class.
- *Batch size*: 128.

A **Generative Adversarial Network (GAN)** consists of two neural networks, a generator and a discriminator, which are trained **one against the other** to improve their performance.

- The **generator** produces fake samples from noise:  $G : \mathbf{z} \rightarrow \mathbf{y}$ .

## Colorization task

To predict colored images from grayscale ones, not from noise!

### Conditional GANs:

- The **generator** takes both noise and an observed **grayscale image  $\mathbf{x}$**  as inputs:  $G : \{\mathbf{z}, \mathbf{x}\} \rightarrow \mathbf{y}$ .
- The **discriminator** distinguishes between real and fake samples, returning a **probability value  $p$**  for the candidate colored image  $\mathbf{y}'$ :  $D : \{\mathbf{y}', \mathbf{x}\} \rightarrow p$ .

The general loss equation of a cGAN model is:

$$L_{cGAN}(G, D) = \mathbb{E}_{\mathbf{x}, \mathbf{y}} [\log D(\mathbf{x}, \mathbf{y})] + \mathbb{E}_{\mathbf{x}, \mathbf{z}} [\log (1 - D(\mathbf{x}, G(\mathbf{x}, \mathbf{z})))] \quad (1)$$

$$\min_G \max_D L_{cGAN}(G, D) \quad (2)$$

- Adding also **L1**, the Generator produces images that are **closer to the ground truth**:

$$L_{cGAN, tot}(G, D) = L_{cGAN}(G, D) + \lambda \mathbb{E}_{\mathbf{x}, \mathbf{y}, \mathbf{z}} [\|\mathbf{y} - G(\mathbf{x}, \mathbf{z})\|_1] \quad (3)$$

- In Isola et al. study, it was observed that the model learned to simply ignore the noise  $\rightarrow \mathbf{z} = \mathbf{0}$ .

In practice, **Binary Cross Entropy** has been used:

$$BCE(\alpha, \beta) = \frac{1}{m} \sum_{i=1}^m [\alpha_i \times \log \beta_i + (1 - \alpha_i) \times \log (1 - \beta_i)] \quad (4)$$

■ For the **Discriminator**:

- \* **Real** images:  $\beta = D(\mathbf{x}, \mathbf{y})$ , the desired label is  $\alpha = 1$ .
- \* **Fake** images:  $\beta = D(\mathbf{x}, G(\mathbf{x}, \mathbf{z} = 0))$ , the desired label is  $\alpha = 0$ .
- \*  $D_{loss} = \frac{BCE_{fake} + BCE_{true}}{2}$

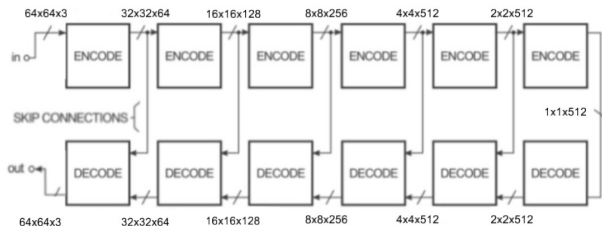
■ For the **Generator**:

- \*  $\beta = D(\mathbf{x}, G(\mathbf{x}, \mathbf{z} = 0))$  but  $\alpha = 1$  because the Generator aims to **fool** the Discriminator.
- \* **L1** loss with  $\lambda = 100$ .

## U-Net based architecture:

**Skip connections** between downsampling and upsampling layers.

**Hyperbolic tangent** as activation function in the last layer, predictions in the input range  $[-1, 1]$ .



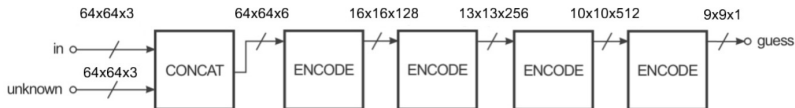


## PatchGAN architecture:

Type of CNN which  
classify small  $N \times N$   
patches of the input  
image at time, rather than  
the full image.

$$N \times N = 46 \times 46.$$

Sigmoid activation  
function in the last layer,  
results in range of  
probabilities  $[0, 1]$ .



## Wasserstein GANs

Generative model implemented to improve original GANs.

- $P_r$ : probability distribution of real images.
- $P_g$ : probability distribution computed by the generator,

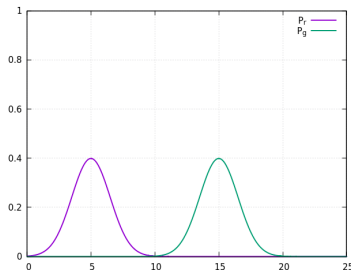
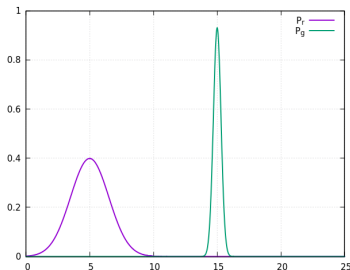
GOAL: make these distributions as similar as possible.



Jensen-Shannon distance:

$$JS(P_r, P_g) = \int \log \frac{P_r(x)}{P_m(x)} P_r(x) d\mu(x) + \int \log \frac{P_g(x)}{P_m(x)} P_g(x) d\mu(x), \quad (5)$$

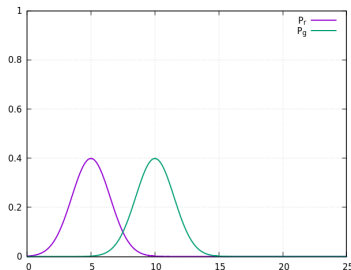
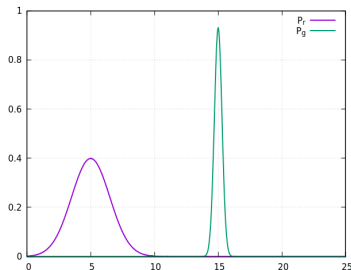
where  $P_m = \frac{P_r + P_g}{2}$ .



Wasserstain's distance:

$$W(P_r, P_g) = \max_{||f|| < 1} \mathbb{E}_{x \sim P_r}[f(x)] - \mathbb{E}_{x \sim P_g}[f(x)]; \quad (6)$$

- **Discriminator:** aims to *maximize* the separation between these two terms
- **Generator:** tries to *minimize* their difference



## Implementation:

- Discriminator  $\Rightarrow$  Critic: no sigmoid function,
- Lipschitz continuous  $f \Rightarrow$  weight clipping  $C = 0.01$ ,
- more training of Critic function.

## PROS

- 1 meaningful loss: termination criteria,
- 2 training stability,
- 3 prevent mode collaps.

## CONS

- 1 longer training time.

Experiment settings:

- Train for 100 epochs
- NVIDIA T4 Tensor Core GPU

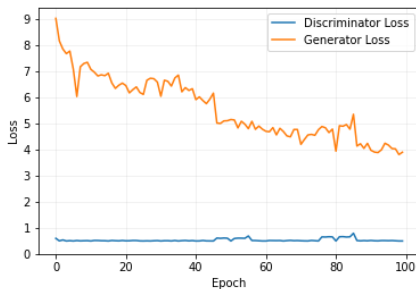
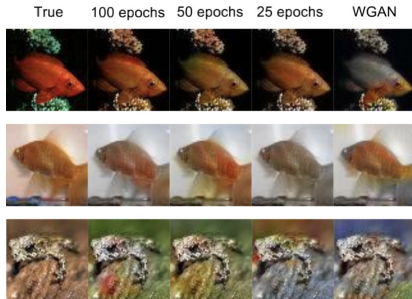


Figure: Loss values for different epochs of training for patchGAN model

# PatchGAN image comparison



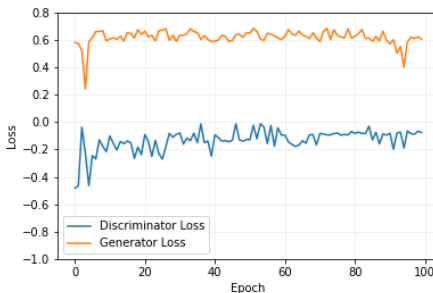
**Figure:** Good predictions results from the patchGAN model on the test set, according to the epoch of training



**Figure:** Wrong predictions for patchGAN

Experiment settings:

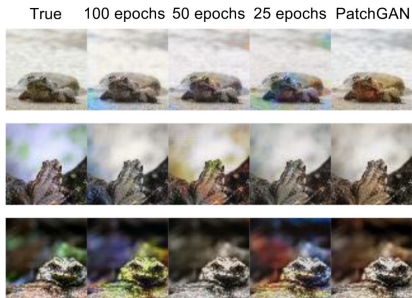
- Train for 100 epochs
- NVIDIA T4 Tensor Core GPU



**Figure:** Loss values for different epochs of training for WGAN model



# WGAN image comparison



**Figure:** Good predictions results from the WGAN model on the test set, according to the epoch of training



**Figure:** Wrong predictions results for WGAN

What has been achieved:

- 1 implementation of a full *Generative Adversarial Network* for image colorization,
- 2 patchGAN vs WGAN:
  - mode collapse prevent, ✓
  - lack of meaning. ✗
- 3 Simplicity of code, easy to train.

Further future enhancements:

- tuning of patch-sizes,
- tuning of other hyperparameters,
- incorporation of a pretrained model for image reconition.