



# Causal ML for predicting treatment outcomes

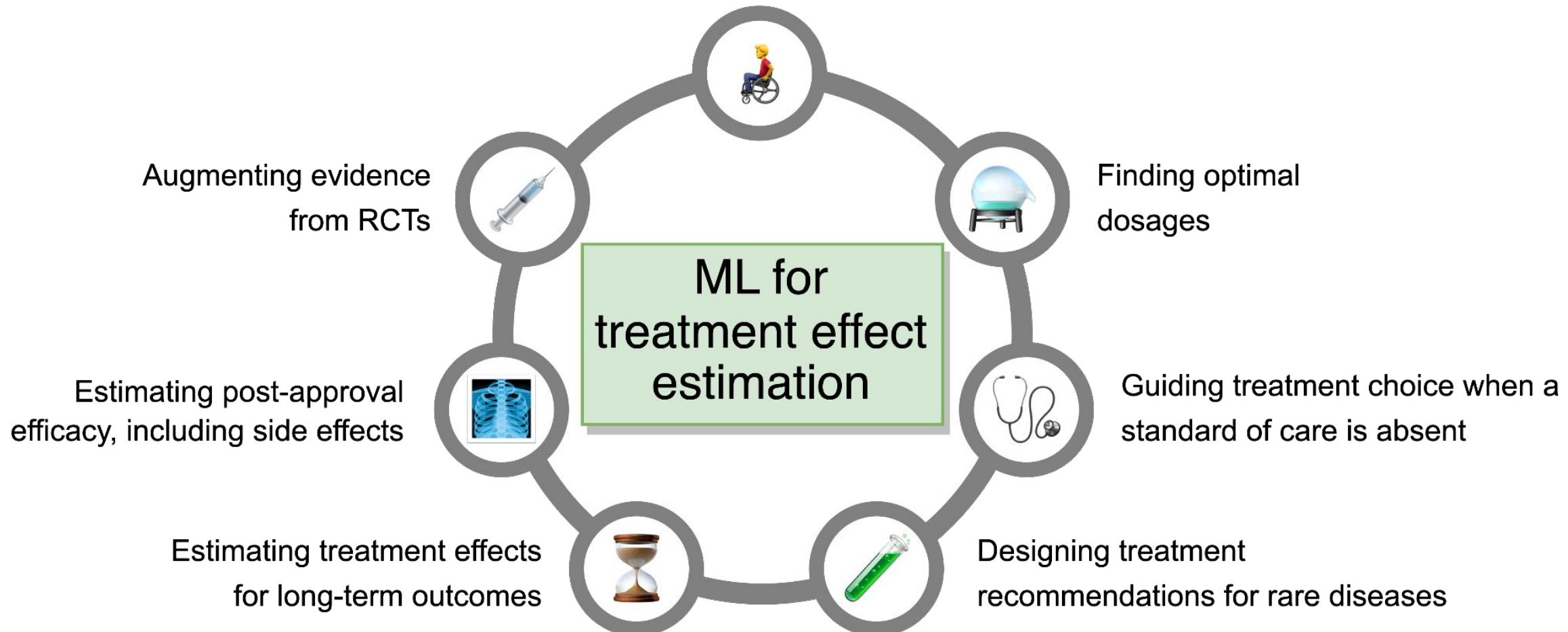
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LMU Munich  
<https://www.ai.bwl.lmu.de>



## Promises of Causal ML

Estimating treatment effects for vulnerable groups



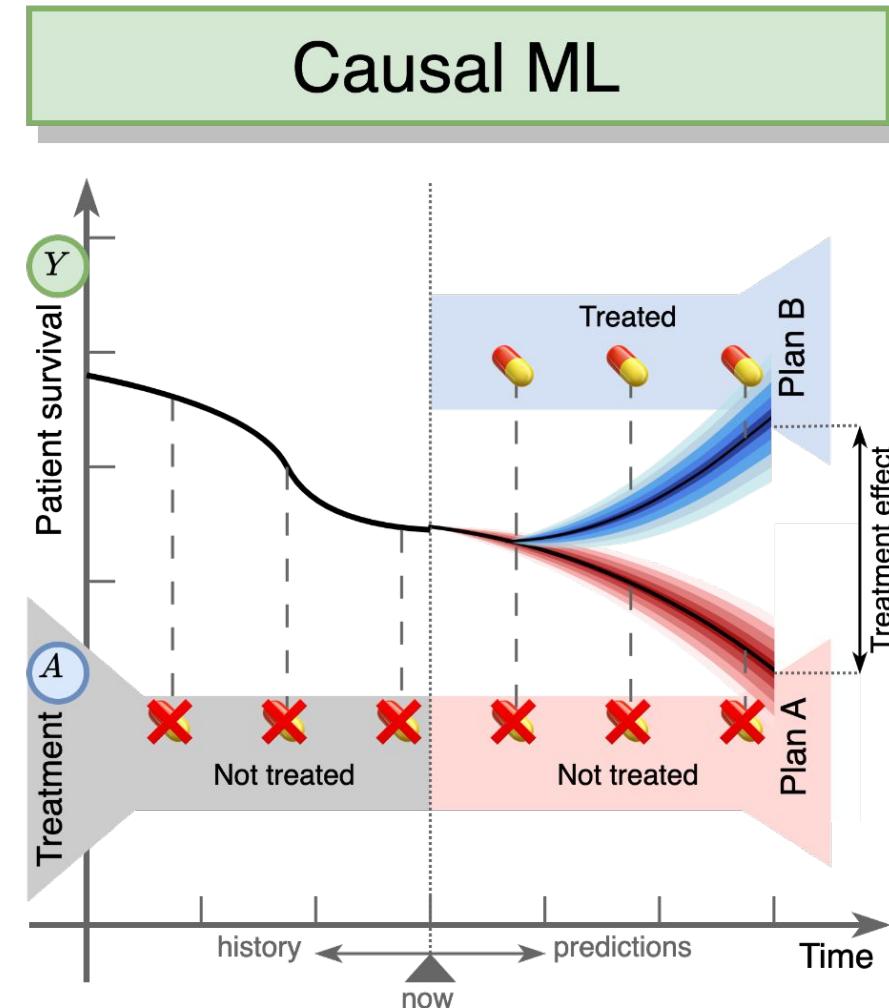
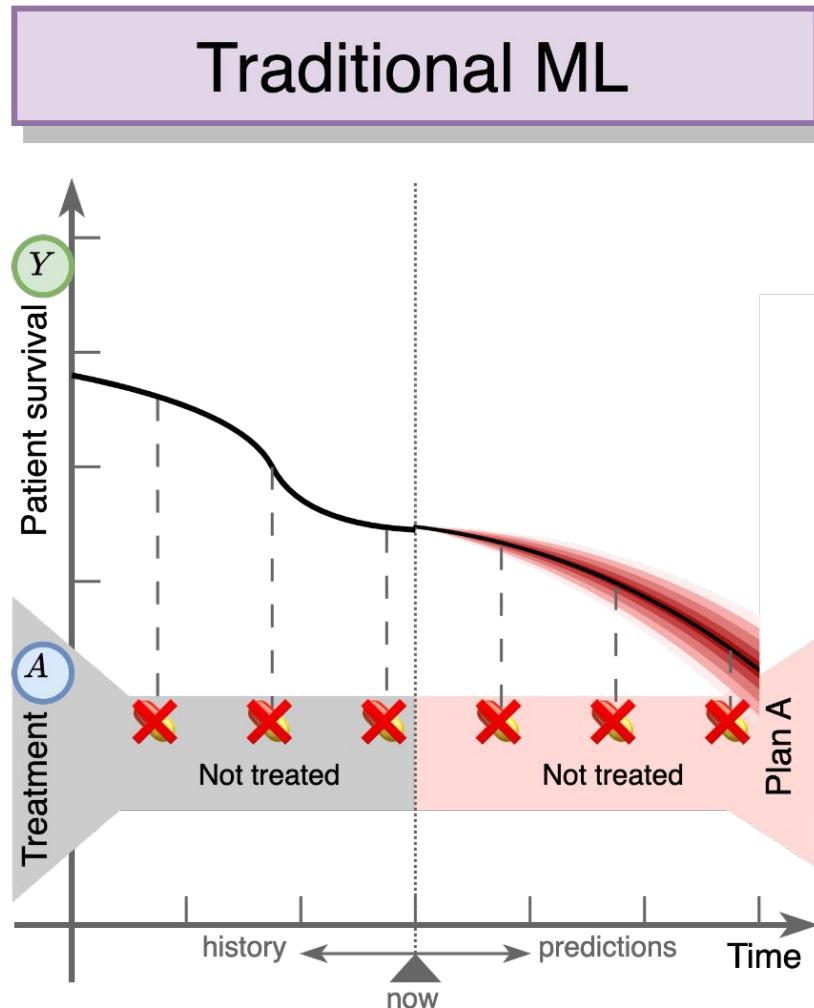


# Why do we need Causal ML in medicine?

## Reference:

Feuerriegel, S., Frauen, D., Melnychuk, V., Schweisthal, J., Hess, K., Curth, A., Bauer, S., Kilbertus, N., Kohane, I.S. and van der Schaar, M., 2024. Causal machine learning for predicting treatment outcomes. Nature Medicine, 30(4), pp.958-968.

## Moving from diagnostics to therapeutics: Estimating treatment effects with ML



## TERMINOLOGY

# Real-world data (RWD) vs. real-world evidence (RWE) to support medicine

The US Food and Drug Administration (FDA) defines <sup>1,2,3</sup>:



## Real-world data (RWD)

- Data relating to patient health status and the delivery of healthcare
- **Examples:** electronic health records (EHRs), claims and billing activities, disease registries, ...
- Naming: observational data ( $\neq$  experimental data)



## Real-world evidence (RWE)

- Analysis of RWD regarding usage and effectiveness
- Vision: greater personalization of care
- Disclaimer: should not replace but augment RCTs

1) Real-World Evidence — Where Are We Now? <https://www.nejm.org/doi/full/10.1056/NEJMp2200089>

2) Real-World Evidence — What Is It and What Can It Tell Us? <https://www.nejm.org/doi/full/10.1056/nejmsb1609216>

3) Real-World Evidence and Real-World Data for Evaluating Drug Safety and Effectiveness <https://jamanetwork.com/journals/jama/fullarticle/2697359>

## TERMINOLOGY

# Real-world data (RWD) vs. real-world evidence (RWE) to support medicine

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## Real-world evidence (RWE)

- **Aim:** estimate treatment effectiveness
- **Challenges:** representativeness (selection bias), no proper randomization, ...
- **Custom methodologies:** target trial emulation, **causal machine learning**, ...

- Analysis of RWD regarding usage and effectiveness
- Vision: greater personalization of care
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## Real-world data (RWD) vs. real-world evidence (RWE) to support medicine

Why is getting a **meaningful** RWE challenging?



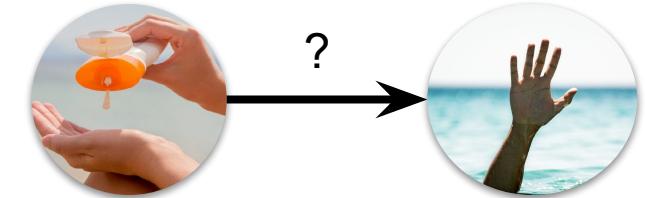
Real-world  
(observational) data  
(RWD)

- Observational data of
  - sunscreen usage (binary treatment)
  - number of drowning-related deaths (outcome)



Real-world evidence  
(RWE)

- Aim: effect of sunscreen on the chance of drowning



- Evidence: The higher the usage of sunscreen -> the more likely is the chance of drowning
- This is counterintuitive: Is there something we didn't account for?

## Real-world data (RWD) vs. real-world evidence (RWE) to support medicine

Why is getting a **meaningful RWE** challenging? -> **Hidden confounding**



### Real-world data (RWD)



### Real-world evidence (RWE)

- Observational data of
  - sunscreen usage (binary treatment)
  - number of drowning-related deaths (outcome)
  - **intensity of sunlight (covariates)**

- **Aim:** effect of sunscreen on the chance of drowning for **different intensities of sunlight**

- Evidence: no association between sunscreen usage and chance of drowning in each group of sunlight
- Comparing with the previous slide: Intensity of sunlight is a **confounder**



## Application scenarios of RWD

RWD helps to guide decision-making (beyond RCTs):

### 1 ... in the absence of a standard of care

- Specific subtypes of diseases with no standard of care yet (e.g., oncology)
- New or experimental drugs (e.g., orphan drugs, is Biontech vs. Moderna vaccine more effective for subcohort X?)

### 2 ... in complex, high-dimensional decision problems

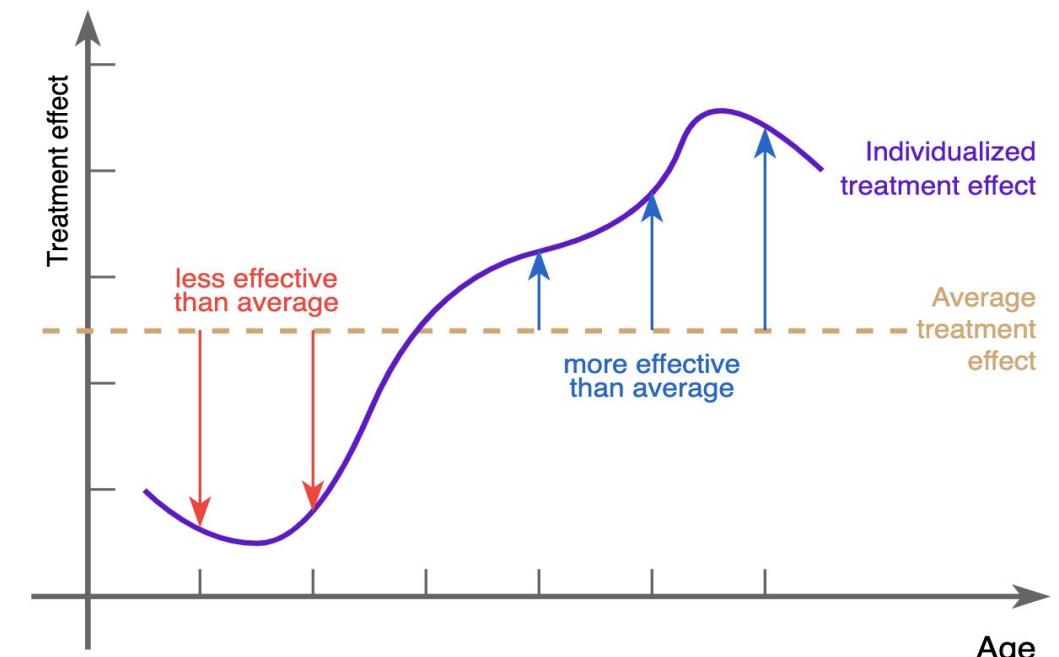
- Complex dosaging problems

### 3 ... when RCTs are unethical

- Vulnerable populations (e.g., pregnant women)<sup>1</sup>

### 4 ... when a greater personalization is desired

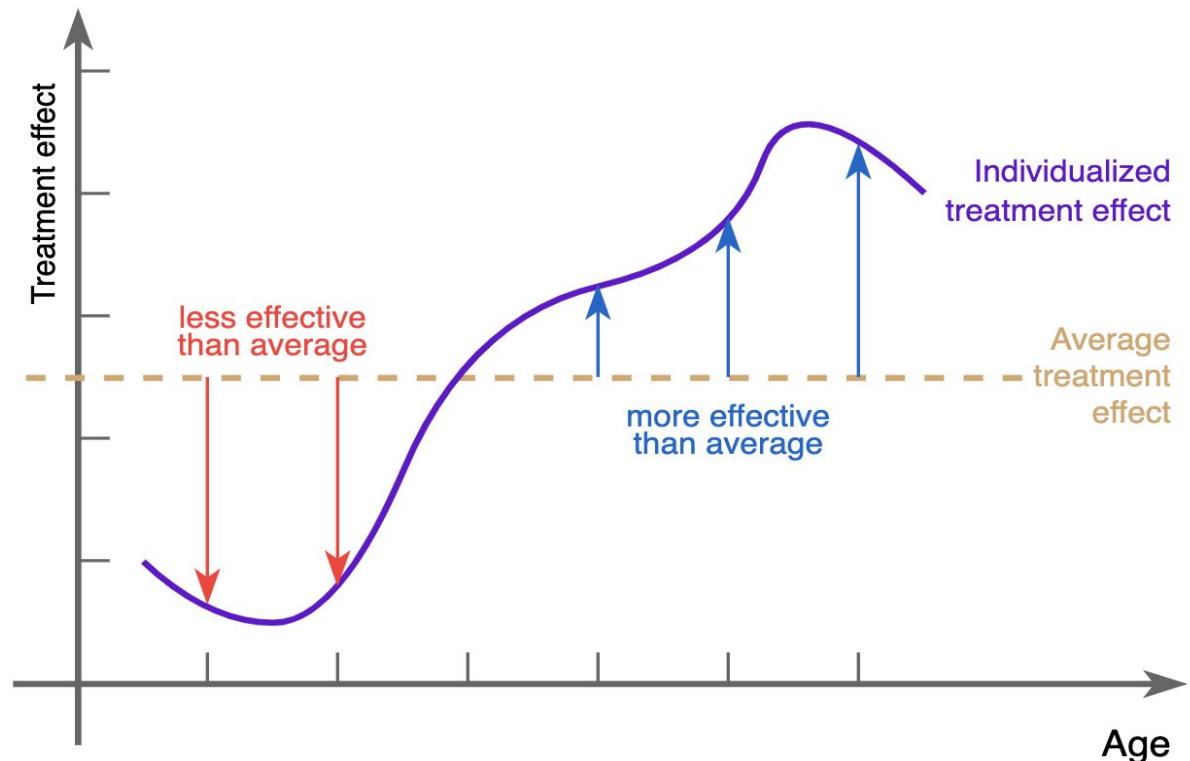
- Highly granular subpopulations that cannot be really placed in RCTs (e.g., women, above 60, with comorbidity etc.)
- Personalization based on genome data (e.g., precision medicine)



1) The Effectiveness of Right Heart Catheterization in the Initial Care of Critically Ill Patients <https://jamanetwork.com/journals/jama/article-abstract/407990>

## Understanding heterogeneity in the treatment effect

- Focus is often on **average** treatment effect (ATE)
- ATE is aggregated across the population
- ATE **cannot** tell whether a treatment works for some or not  
→ e.g., medication works only for women but not for men, but RCT was done with all patients
- NB: both RCTs and target trial emulation focus on ATEs



To personalize treatment recommendations, we need to understand the **individualized treatment effect (ITE)**



# Short introduction to causal machine learning

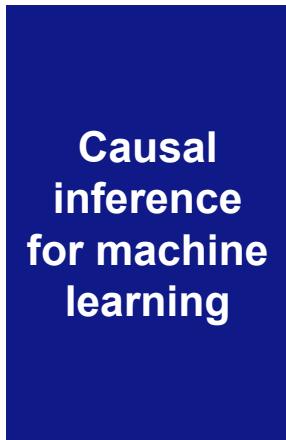
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## PRIMER

## Ambiguity of the definition

“Causal ML” could be both:



### Causal inference concepts



### ML / DL problems

- Explainability
- Fairness
- Algorithmic recourse
- Robustness / domain adaptation
- ...



### Causal inference problems

- Predicting treatment outcomes
- Counterfactual inference
- Causal discovery
- ...



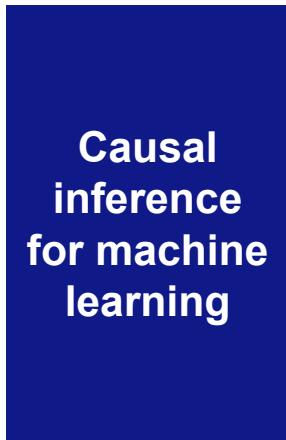
### ML / DL tools



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### ML / DL tools



### Causal inference problems

- Predicting treatment outcomes
- Counterfactual inference
- Causal discovery
- ...



## Ladder of causation

### Pearl's layers of causation

Level (Symbol)	Typical Activity	Typical Questions	Examples
1. Association $P(y x)$	Seeing	What is? How would seeing $X$ change my belief in $Y$ ?	What does a symptom tell me about a disease? What does a survey tell us about the election results?
2. Intervention $P(y do(x), z)$	Doing Intervening	What if? What if I do $X$ ?	What if I take aspirin, will my headache be cured? What if we ban cigarettes?
3. Counterfactuals $P(y_x x', y')$	Imagining, Retrospection	Why? Was it $X$ that caused $Y$ ? What if I had acted differently?	Was it the aspirin that stopped my headache? Would Kennedy be alive had Oswald not shot him? What if I had not been smoking the past 2 years?



**Causal Hierarchy Theorem:** statistical inference for a layer requires the information from the same or higher layer. For the inference from lower layer data, we need to make **additional assumptions**.

<sup>1</sup> Elias Bareinboim et al. "On Pearl's hierarchy and the foundations of causal inference". In: Probabilistic and Causal Inference: The Works of Judea Pearl. Association for Computing Machinery, 2022, pp. 507–556.

## PRIMER

## Ladder of causation

Pearl's  
layers of  
causation

Level (Symbol)	Typical Activity	Typical Questions	Examples	Traditional ML
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## Ladder of causation

Pearl's  
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Level (Symbol)	Typical Activity	Typical Questions	Examples
1. Association $P(y x)$	Seeing	What is? How would seeing $X$ change my belief in $Y$ ?	What does a symptom tell me about a disease? What does a stock price tell me about the election?
2. Intervention $P(y do(x), z)$	Doing Intervening	What if? What if I do $X$ ?	What if I take aspirin, will my headache be cured? What if we ban cigarettes?
3. Counterfactuals $P(y_x x', y')$	Imagining, Retrospection	Why? Was it $X$ that caused $Y$ ? What if I had acted differently?	Was it the aspirin that stopped my headache? Would Kennedy be alive had Oswald not shot him? What if I had not been smoking the past 2 years?

Causal ML



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## TREATMENT OUTCOMES

# Predicting treatment outcomes (treatment effects or potential outcome)

### Problem formulation

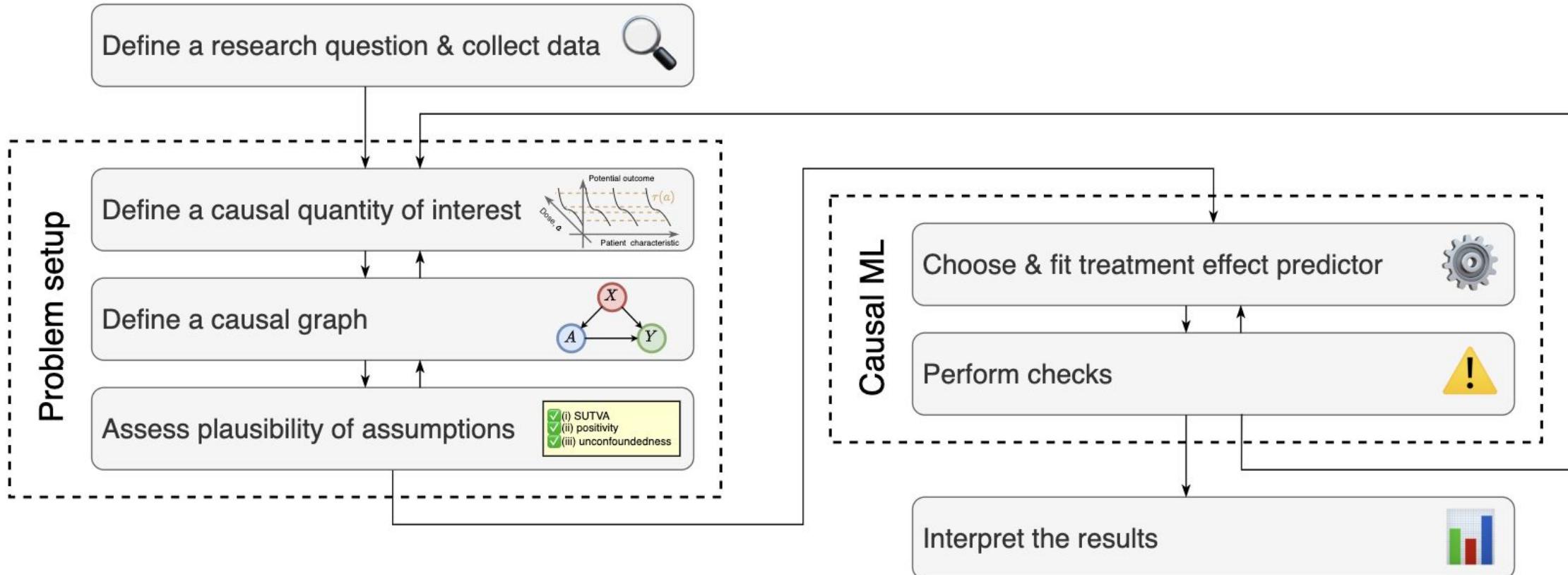
- Given i.i.d. observational dataset  $\mathcal{D} = \{x_i, a_i, y_i\}_{i=1}^n \sim \mathbb{P}(X, A, Y)$ 
  - $X$  covariates
  - $A$  (binary) treatments
  - $Y$  continuous (factual) outcomes
- We want to identify & estimate treatment outcomes:
  - treatment effects**  $Y[1] - Y[0]$
  - potential outcomes** (separately)  $Y[0]$   $Y[1]$
- Fundamental problem:** never observing both potential outcomes!

Patient	Covariates $X$	Treatment $A$	Outcome $Y = Y(0)$	Outcome $Y = Y(1)$
...	...	0	-1.0	
...	...	1		2.3
...	...	1		0.3
...	...	...	...	...

Patient	Covariates $X$	Potential outcomes $Y(0)$	$Y(1)$	Treatment effect $Y(1) - Y(0)$
...	...	?	?	?
...	...	?	?	?
...	...	...	...	...

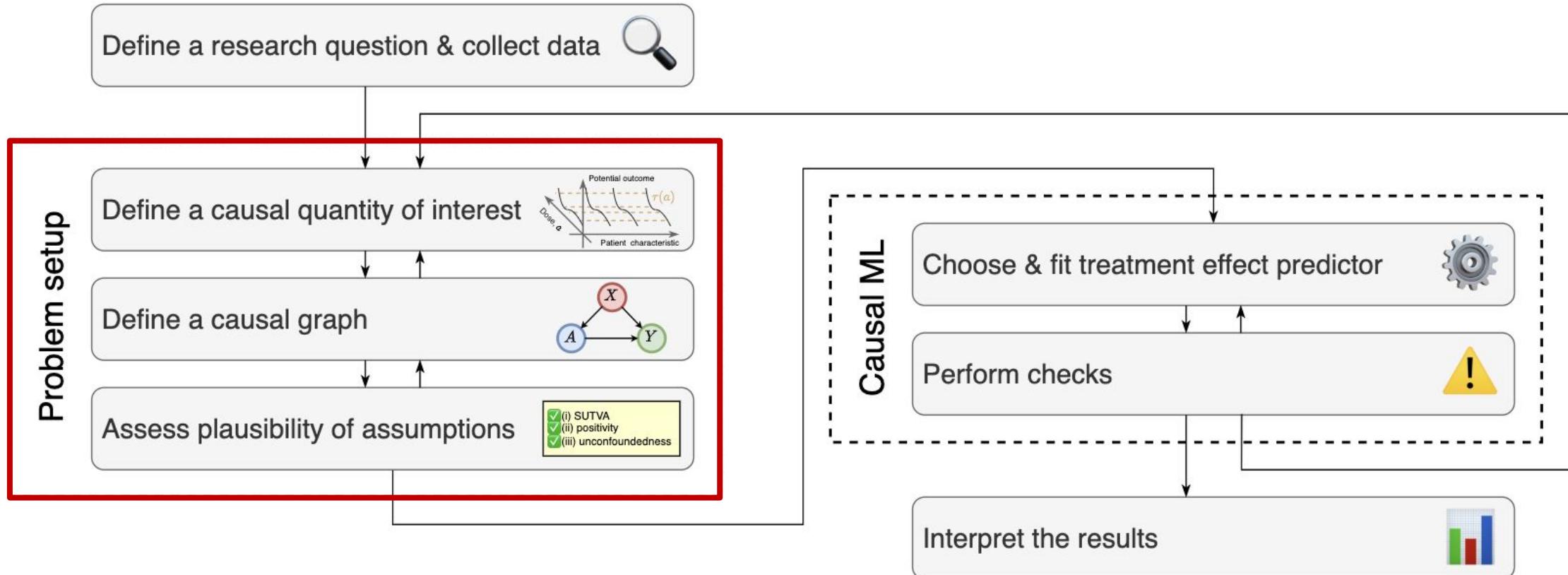
## TREATMENT OUTCOMES

# Causal ML Workflow



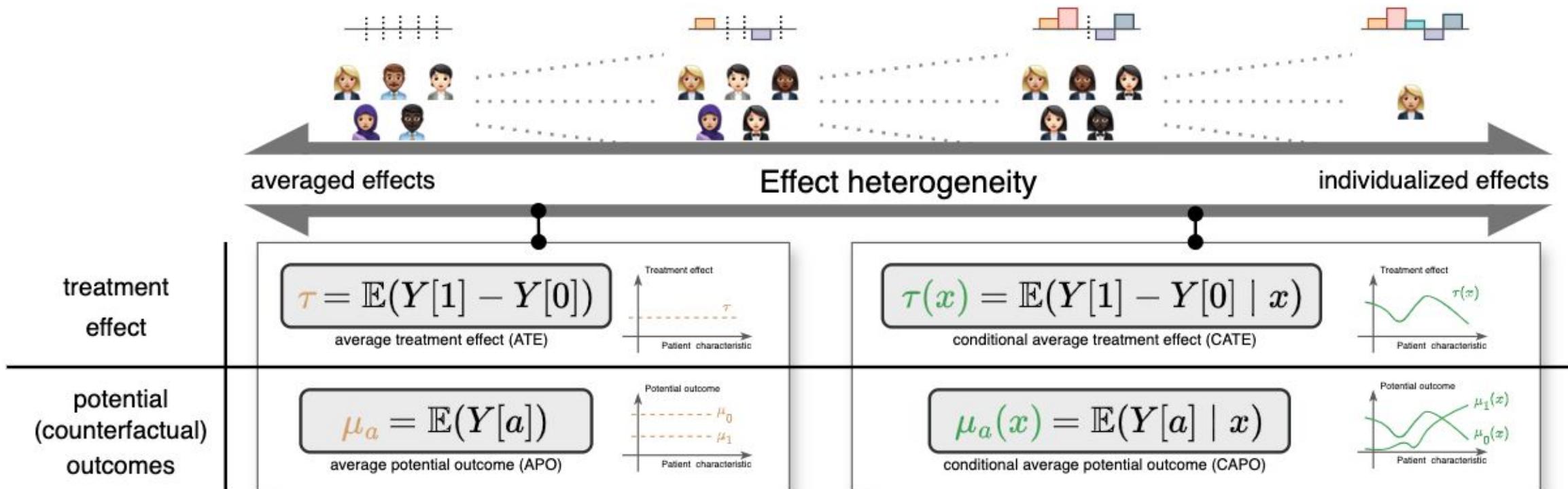
## TREATMENT OUTCOMES

# Causal ML Workflow



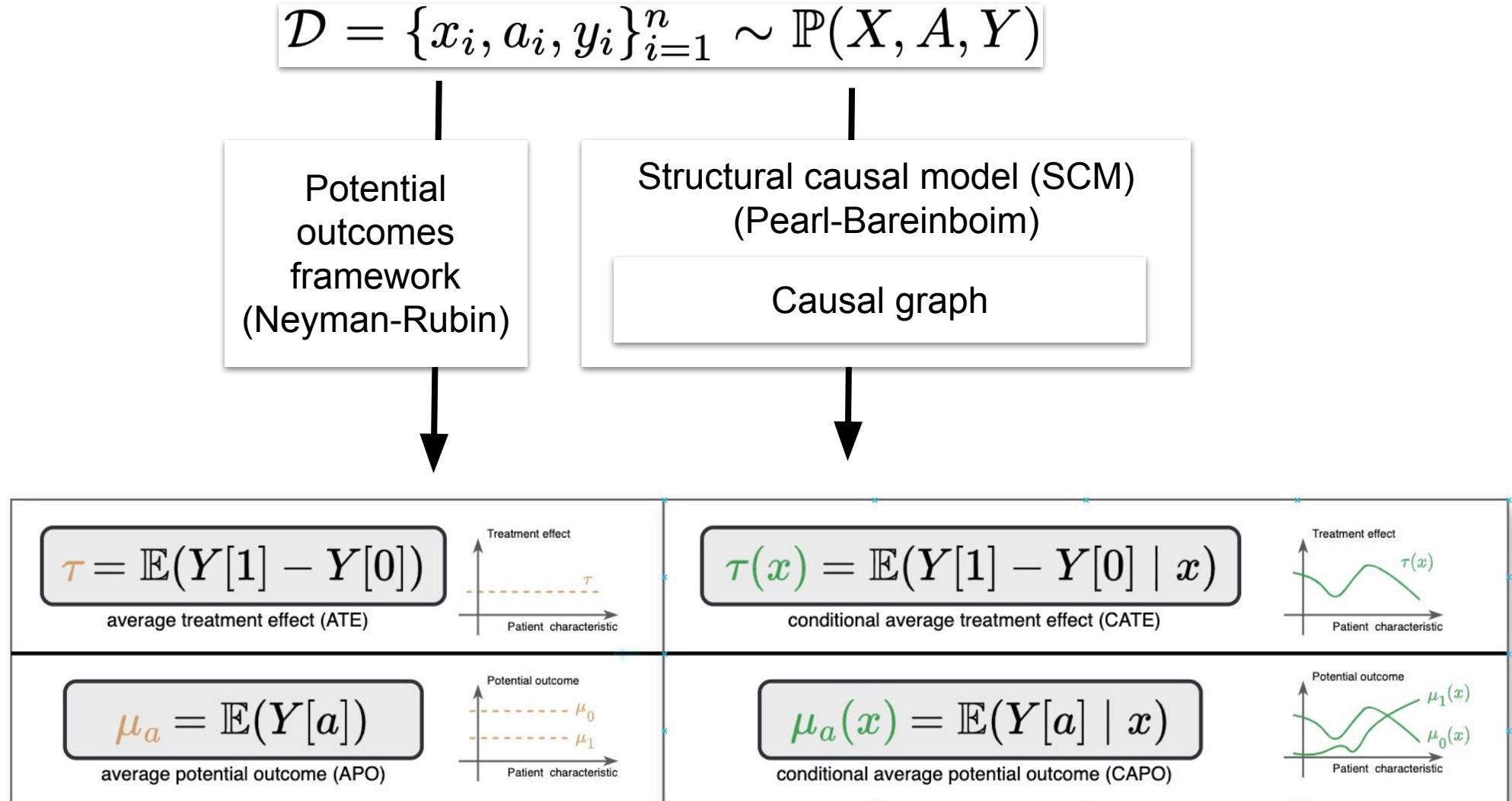
## PROBLEM SETUP

# Causal quantities of interest



## PROBLEM SETUP

### Assumption frameworks



## PROBLEM SETUP

### Assumption frameworks: SCMs and causal graphs

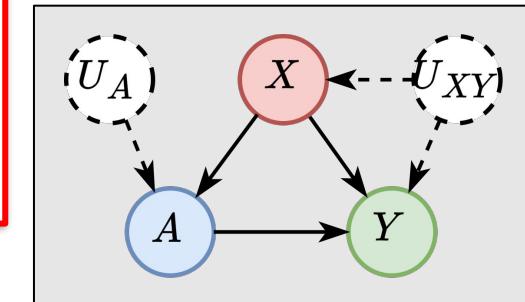
$$\mathcal{D} = \{x_i, a_i, y_i\}_{i=1}^n \sim \mathbb{P}(X, A, Y)$$

Potential outcomes framework (Neyman-Rubin)

Structural causal model (SCM) (Pearl-Bareinboim)

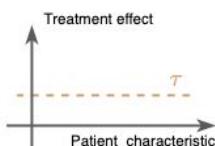
Causal graph

Assumptions stem from structural knowledge



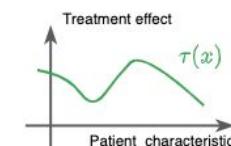
$$\tau = \mathbb{E}(Y[1] - Y[0])$$

average treatment effect (ATE)



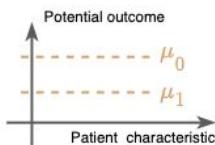
$$\tau(x) = \mathbb{E}(Y[1] - Y[0] | x)$$

conditional average treatment effect (CATE)



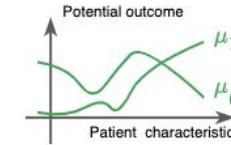
$$\mu_a = \mathbb{E}(Y[a])$$

average potential outcome (APO)



$$\mu_a(x) = \mathbb{E}(Y[a] | x)$$

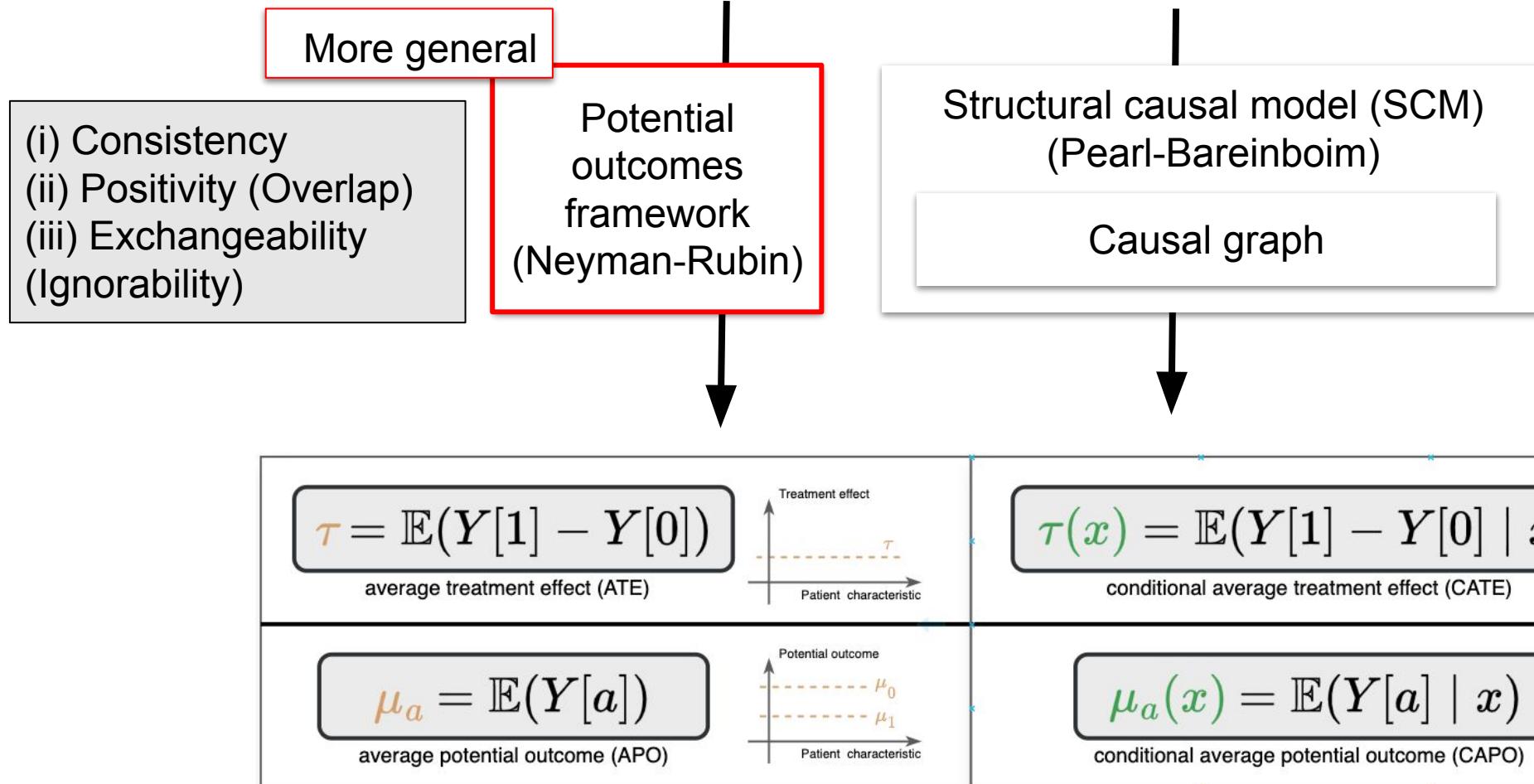
conditional average potential outcome (CAPO)



## PROBLEM SETUP

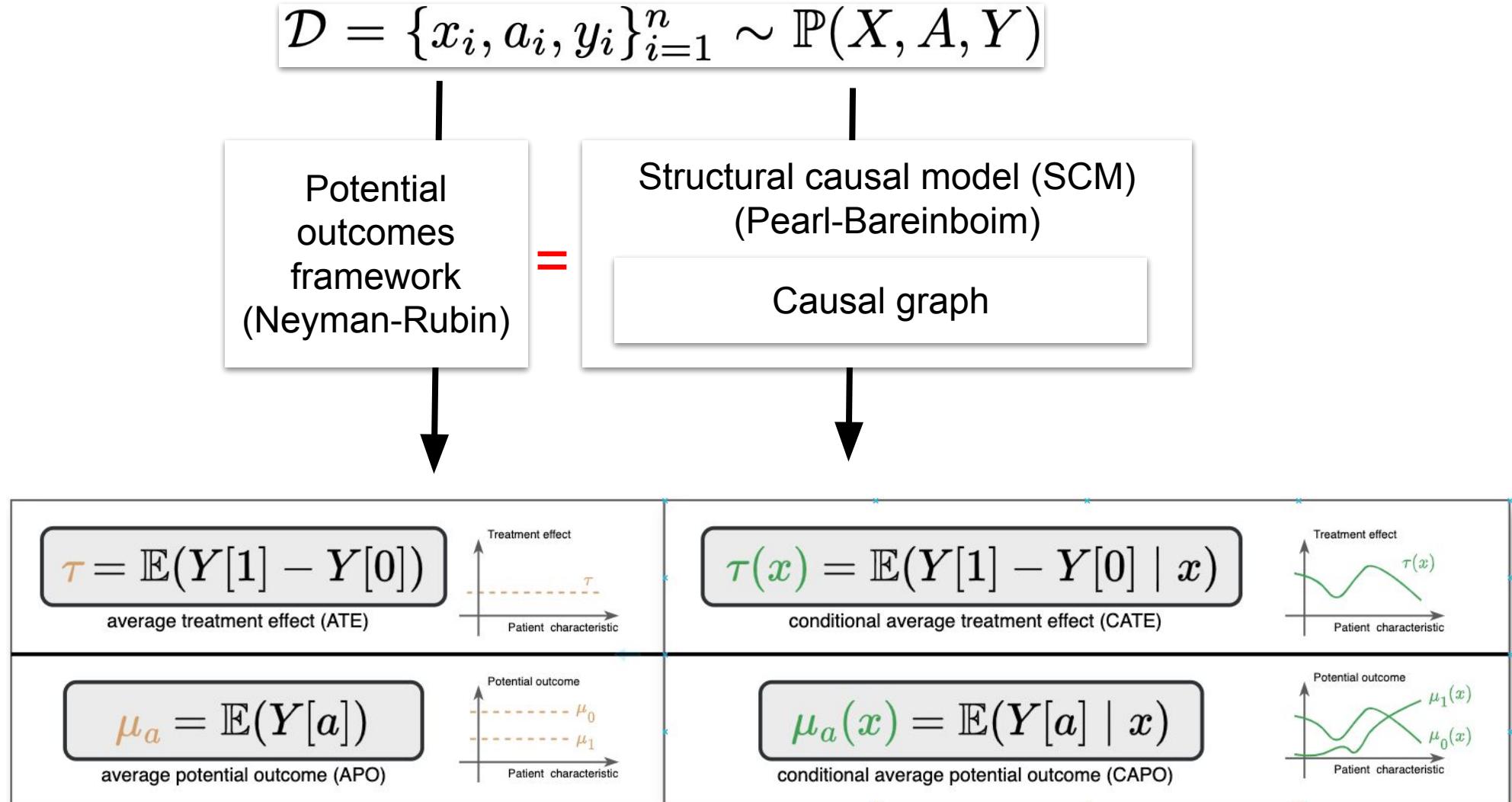
# Assumption frameworks: Potential outcomes framework

$$\mathcal{D} = \{x_i, a_i, y_i\}_{i=1}^n \sim \mathbb{P}(X, A, Y)$$



## PROBLEM SETUP

### Assumption frameworks

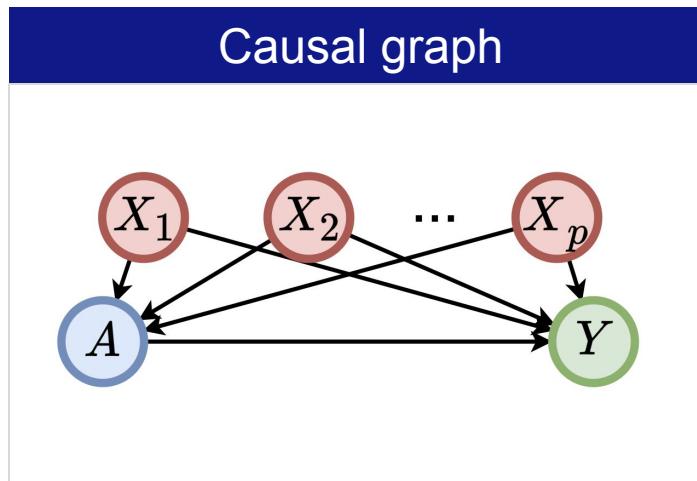


## PROBLEM SETUP

### Example of a case study

**Aim:** estimate heterogeneous treatment effect of development aid on SDG outcomes

- **Treatment A:** development aid earmarked to end the HIV/AIDS epidemic
- **Outcome Y:** relative reduction in HIV infection rate
- **Covariates X:** control for differences in country characteristics



Causal quantity of interest

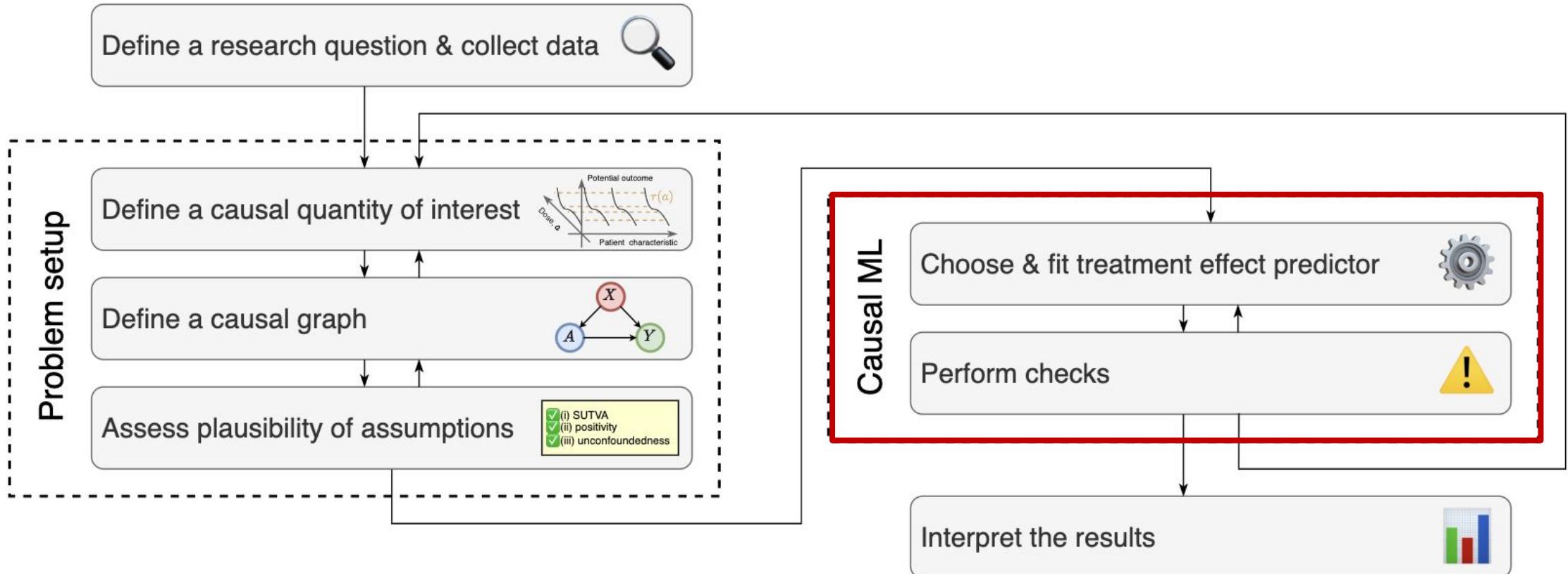
$$\mu_a(x) = \mathbb{E}(Y[a] \mid x)$$

conditional average potential outcome (CAPO)

Assumptions
Potential outcomes framework (Neyman-Rubin)
Consistency: $Y = Y(a)$ if $A = a$
Positivity: $0 < p(A = a \mid X = x) < 1, \forall a \in \mathcal{A}$
Ignorability: $Y(a) \perp\!\!\!\perp A \mid X = x, \forall a \in \mathcal{A}$

## TREATMENT OUTCOMES

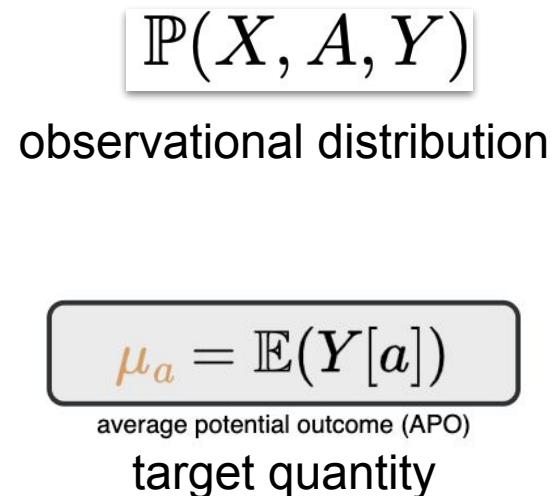
# Causal ML Workflow



## CAUSAL ML

## Identification vs. estimation / learning

**Identification  
(infinite data)**



Potential outcomes framework (Neyman-Rubin)

$$\mu_a = \mathbb{E}(\mathbb{E}[Y | a, X])$$

back-door adjustment

$$\mu_a = \mathbb{E}\left[\frac{1(A=a)}{\pi_a(X)} Y\right]$$

inverse propensity of treatment weighting (IPTW)

identification formulas

**Estimation  
(finite data)**

$\mathcal{D} = \{x_i, a_i, y_i\}_{i=1}^n \sim \mathbb{P}(X, A, Y)$

sample from observational distribution

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$$\mu_a = \mathbb{E}\left[\frac{1(A=a)}{\pi_a(X)} Y\right]$$

identification formulas

Semi-parametric efficiency theory / Neyman-orthogonal learning

$$\hat{\mu}_{a,A\text{-IPTW}} = \frac{1}{n} \sum_{i=1}^n \frac{a_i=a}{\hat{\pi}_a(x_i)} \left( y_i - \hat{\mu}_a(x_i) \right) + \hat{\mu}_a(x_i)$$

$$\hat{\eta} = \{\hat{\mu}_a(x) = \hat{\mathbb{E}}[Y | A = a, X = x]; \\ \hat{\pi}_a(x) = \hat{\mathbb{P}}[A = a | X = x]\}$$

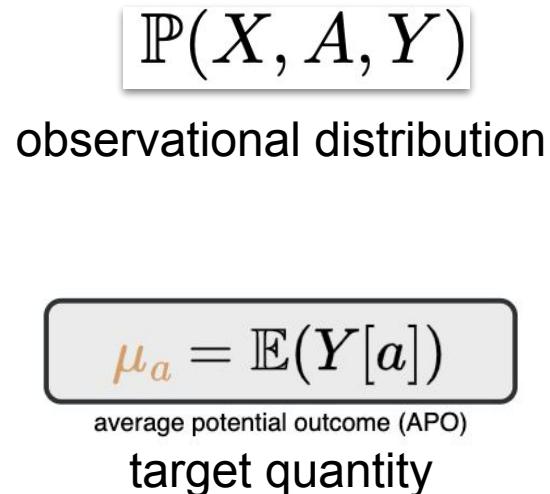
augmented inverse propensity of treatment weighting (A-IPTW)

efficient estimator

CAUSAL ML

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augmented inverse propensity of treatment weighting (A-IPTW)

efficient estimator

## Challenges and open questions fitting an ML model

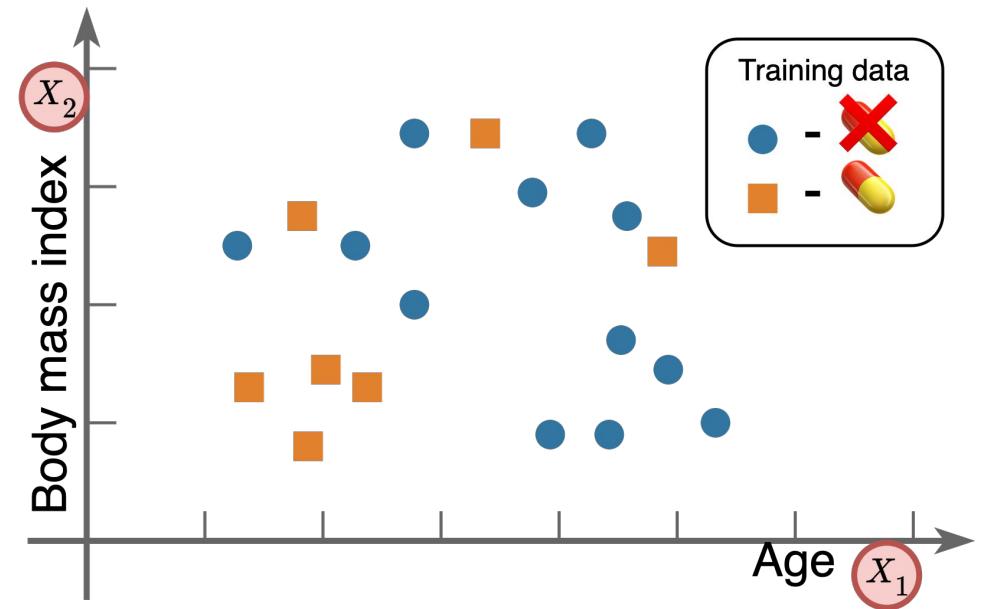
$$\mu_a(x) = \mathbb{E}(Y[a] \mid x)$$

### conditional average potential outcome (CAPO)

$$\tau(x) = \mathbb{E}(Y[1] - Y[0] \mid x)$$

### conditional average treatment effect (CATE)

## Challenges



## Challenges and open questions fitting an ML model

### Challenges

$$\mu_a(x) = \mathbb{E}(Y[a] | x)$$

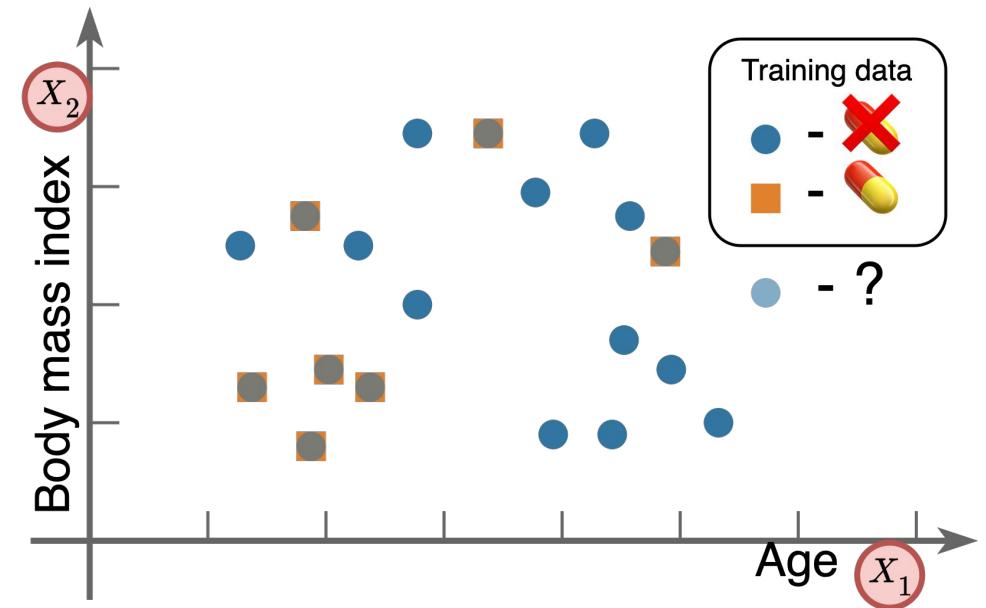
conditional average potential outcome (CAPO)

- **Selection bias:** parts of the population rarely gets treated

$$\tau(x) = \mathbb{E}(Y[1] - Y[0] | x)$$

conditional average treatment effect (CATE)

- **Selection bias:** parts of the population rarely gets treated



# Challenges and open questions fitting an ML model

## Challenges

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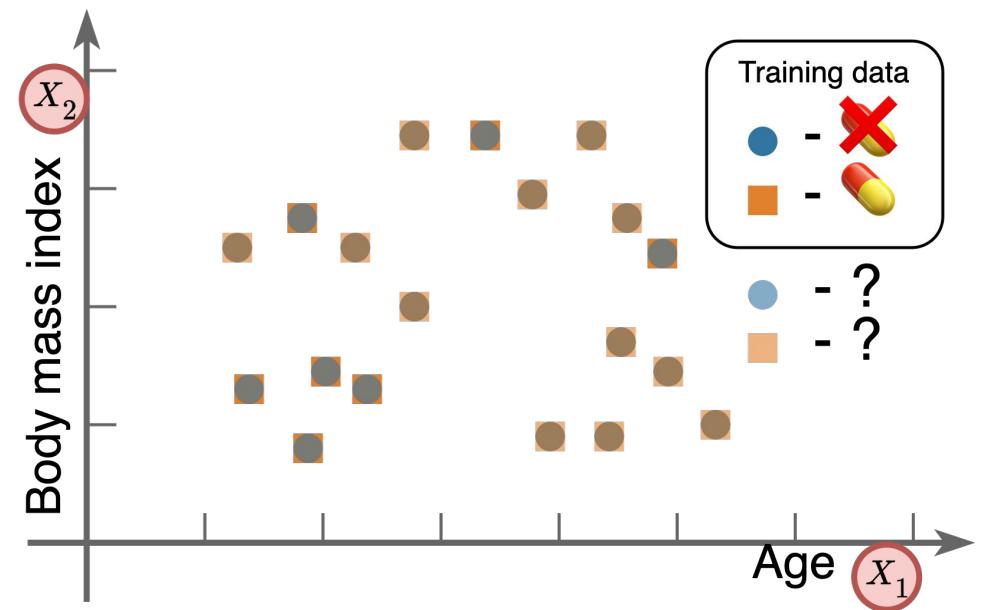
conditional average potential outcome (CAPO)

- **Selection bias:** parts of the population rarely gets treated

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conditional average treatment effect (CATE)

- **Selection bias:** parts of the population rarely gets treated
- **Fundamental problem:** never observing a difference of potential outcomes



# Challenges and open questions fitting an ML model

## Challenges

$$\mu_a(x) = \mathbb{E}(Y[a] | x)$$

conditional average potential outcome (CAPO)

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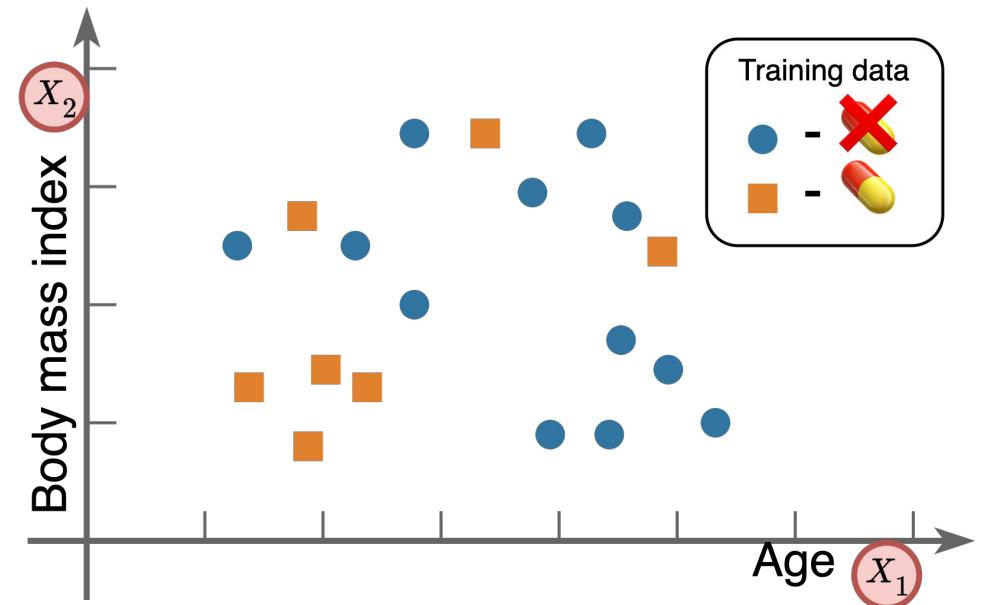
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conditional average treatment effect (CATE)

- **Selection bias:** parts of the population rarely gets treated
- **Fundamental problem:** never observing a difference of potential outcomes

## Open problems

- How to effectively address selection bias?
- How to incorporate inductive biases, e.g., regularize CAPO / CATE models?



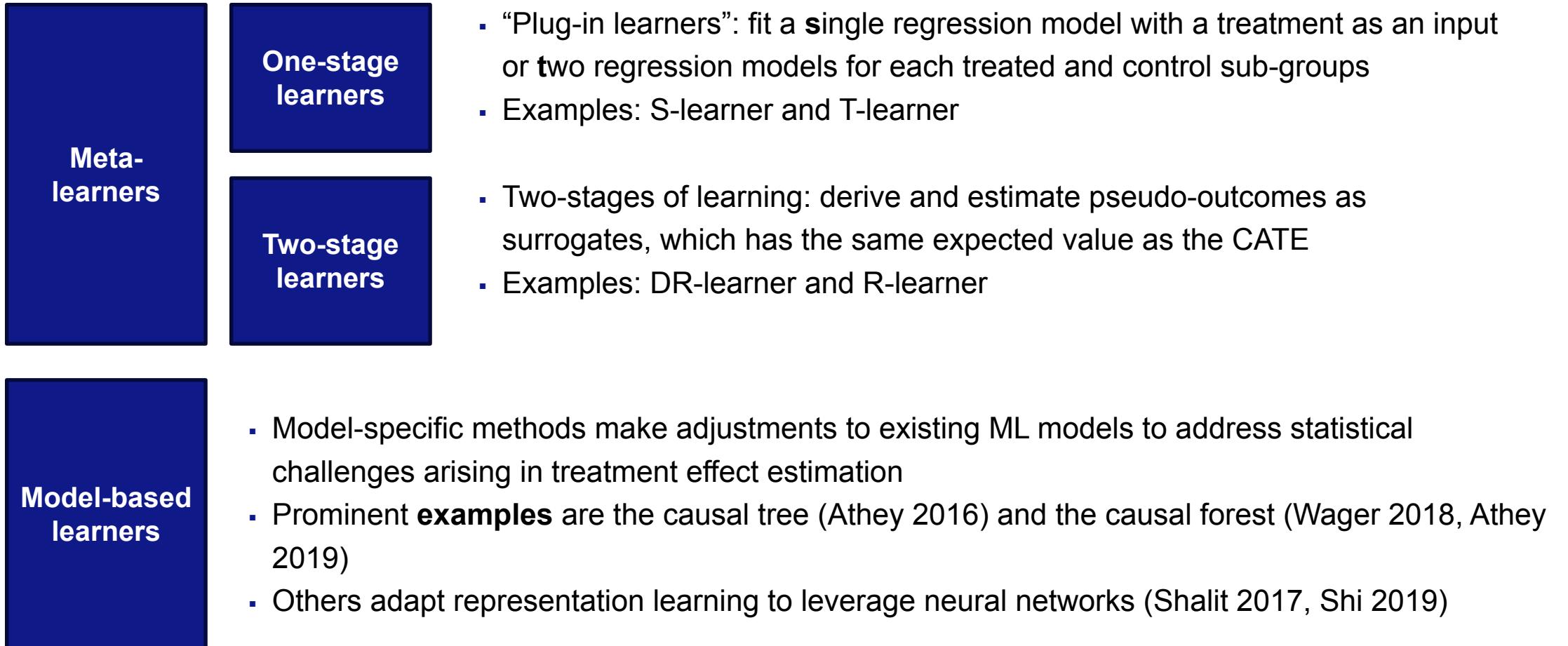
### Meta- learners

- Meta-learners (Kunzel 2019) are model-agnostic methods for CATE estimation
- Can be used for treatment effect estimation in combination with an arbitrary ML model of choice (e.g., a decision tree, a neural network)

### Model-based learners

- Model-specific methods make adjustments to existing ML models to address statistical challenges arising in treatment effect estimation
- Prominent **examples** are the causal tree (Athey 2016) and the causal forest (Wager 2018, Athey 2019)
- Others adapt representation learning to leverage neural networks (Shalit 2017, Shi 2019)

1. Künzel, Sören R., et al. "Metalearners for estimating heterogeneous treatment effects using machine learning." *Proceedings of the national academy of sciences* 116.10 (2019): 4156-4165.
2. Athey, Susan, and Guido Imbens. "Recursive partitioning for heterogeneous causal effects." *Proceedings of the National Academy of Sciences* 113.27 (2016): 7353-7360.
3. Athey, Susan, and Stefan Wager. "Estimating treatment effects with causal forests: An application." *Observational studies* 5.2 (2019): 37-51.
4. Shalit, Uri, Fredrik D. Johansson, and David Sontag. "Estimating individual treatment effect: generalization bounds and algorithms." *International conference on machine learning*. PMLR, 2017.
5. Shi, Claudia, David Blei, and Victor Veitch. "Adapting neural networks for the estimation of treatment effects." *Advances in neural information processing systems* 32 (2019).



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4. Shalit, Uri, Fredrik D. Johansson, and David Sontag. "Estimating individual treatment effect: generalization bounds and algorithms." *International conference on machine learning*. PMLR, 2017.
5. Shi, Claudia, David Blei, and Victor Veitch. "Adapting neural networks for the estimation of treatment effects." *Advances in neural information processing systems* 32 (2019).

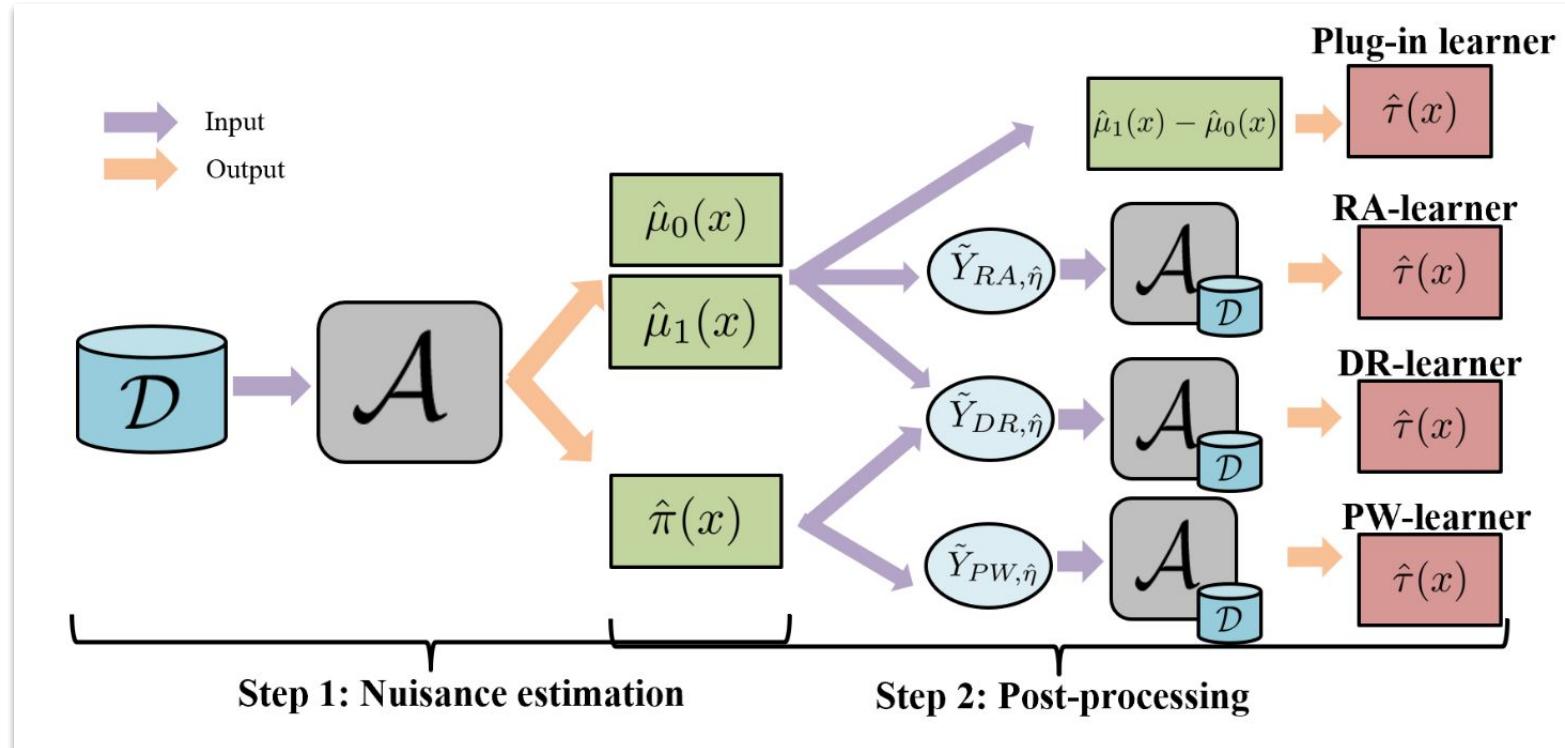
## One-stage and two-stage meta-learners

**Example:** meta-learners for CATE

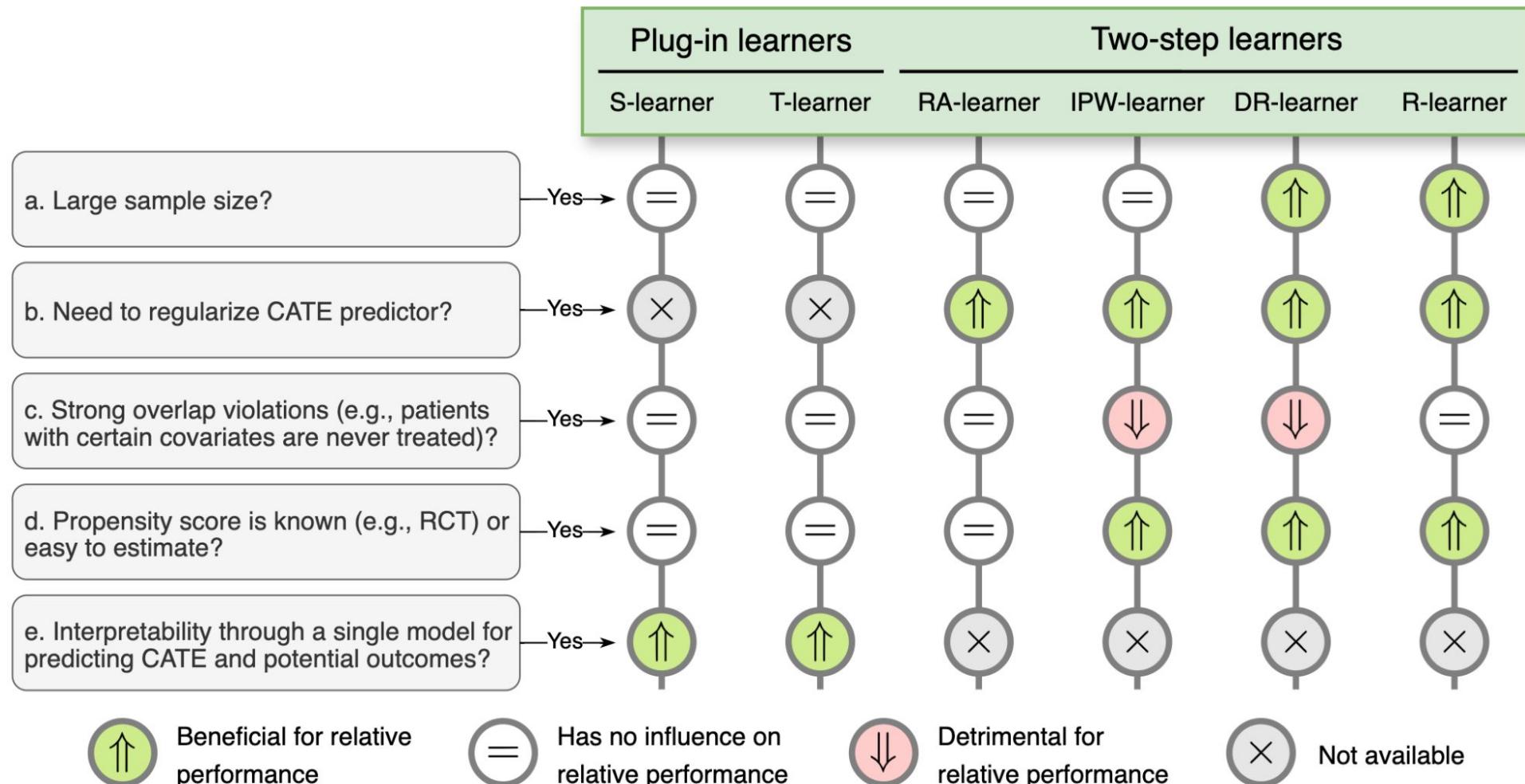
$$\tau(x) = \mathbb{E}(Y[1] - Y[0] \mid x)$$

conditional average treatment effect (CATE)

**Method:** Using any ML model to fit relevant parts of the observed distribution, namely, **nuisance functions**. Then, we can use the nuisance functions estimators for the final CATE model.



# Comparison of meta-learners



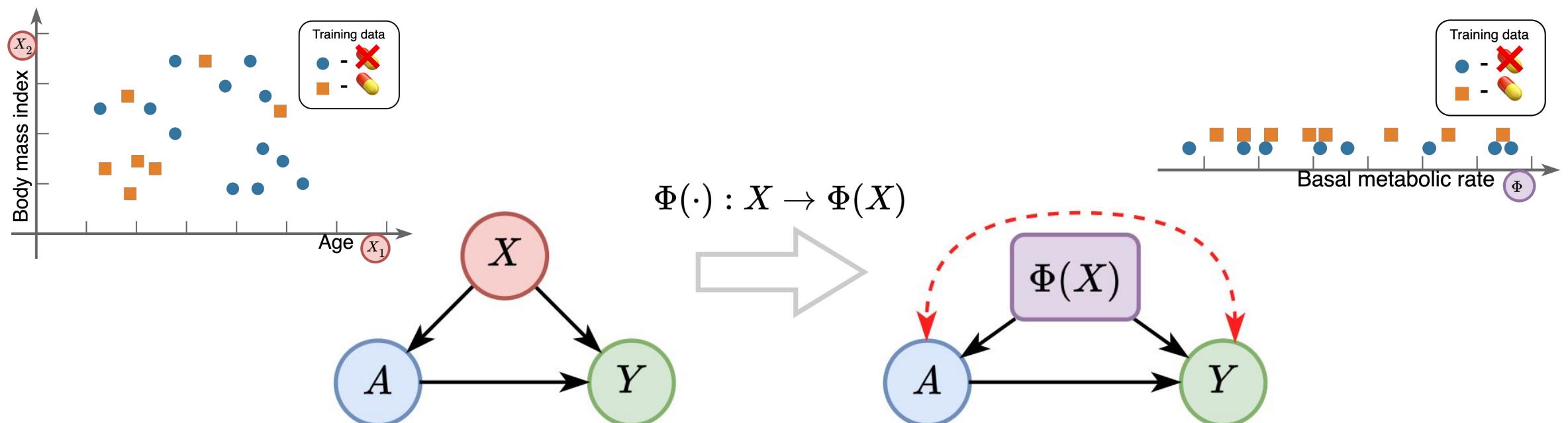
## Model-based learners: Representation learning

Example: TarNET / CFRNet for CATE

$$\tau(x) = \mathbb{E}(Y[1] - Y[0] \mid x)$$

conditional average treatment effect (CATE)

**Method:** Learning a low-dimensional (balanced) representation  $\Phi(\cdot)$  of high-dimensional covariates. Then, we can fit a CATE model based on the representations.



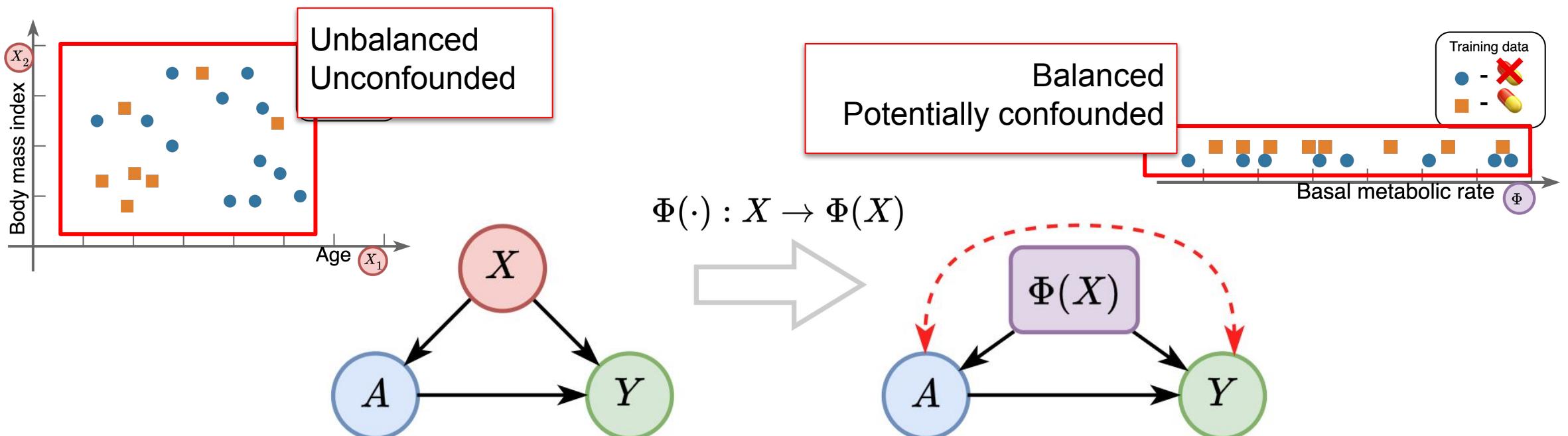
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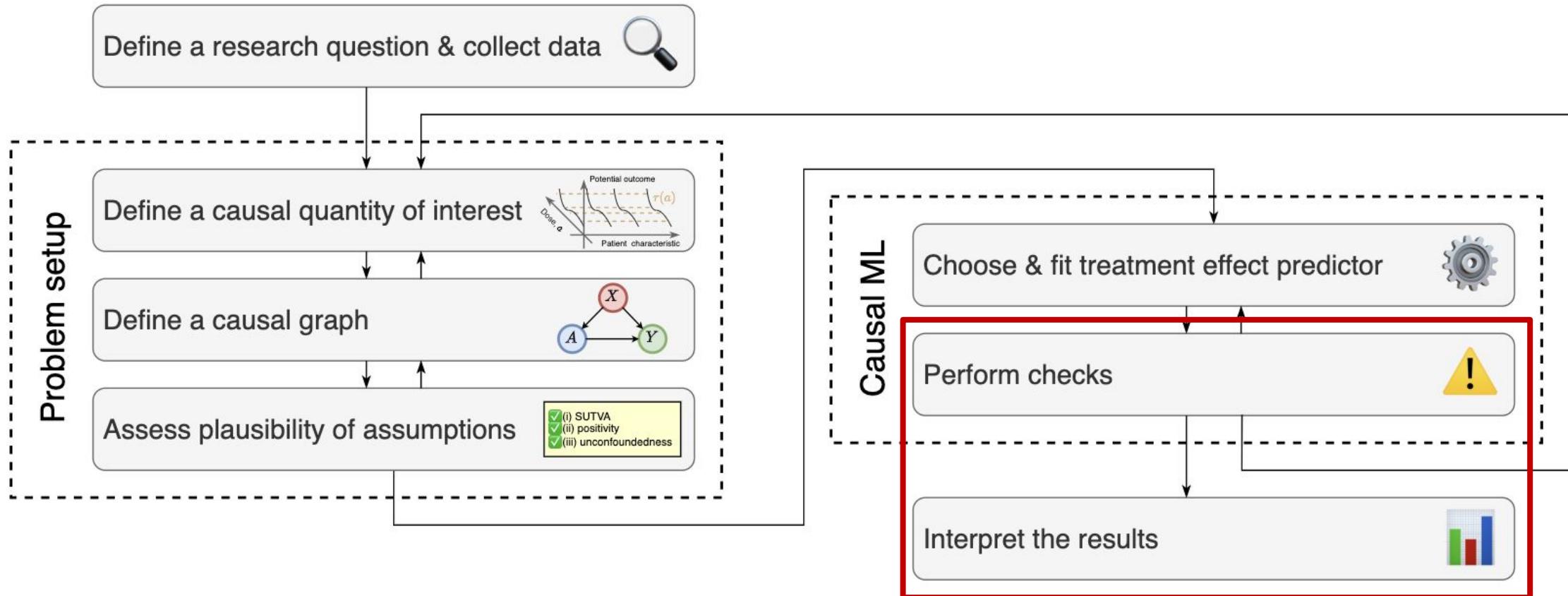


# Where we are (and what is still needed): Current state of causal ML research



## PRIMER

# Causal ML Workflow



# Extensions & Open research problems

## 1 Model validity

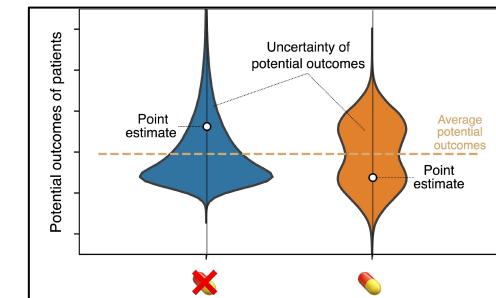
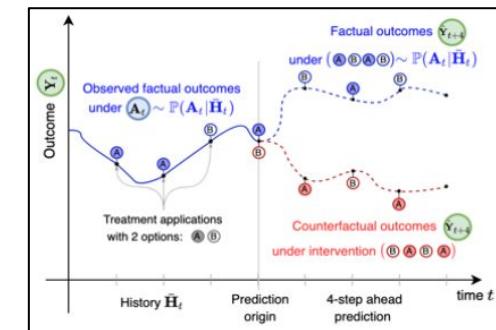
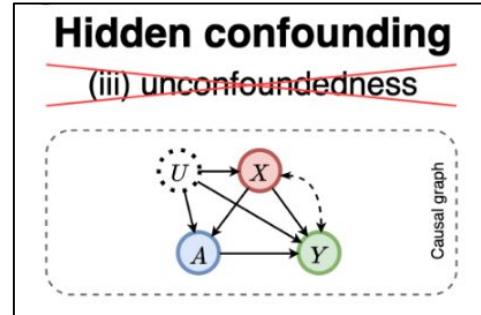
- Selection and validation of CATE models
  - Unlike traditional ML, we do not have a ground truth validation subset
- Robustness checks wrt. violation of assumptions
  - Sensitivity models
  - Spillover effects

## 2 Flexibility

- Extensions to more complicated settings
  - continuous / high-dimensional treatments
  - time-varying potential outcomes and treatment effects
- Data fusion from multiple environments
- Constrained ML: interpretability, privacy enforcement

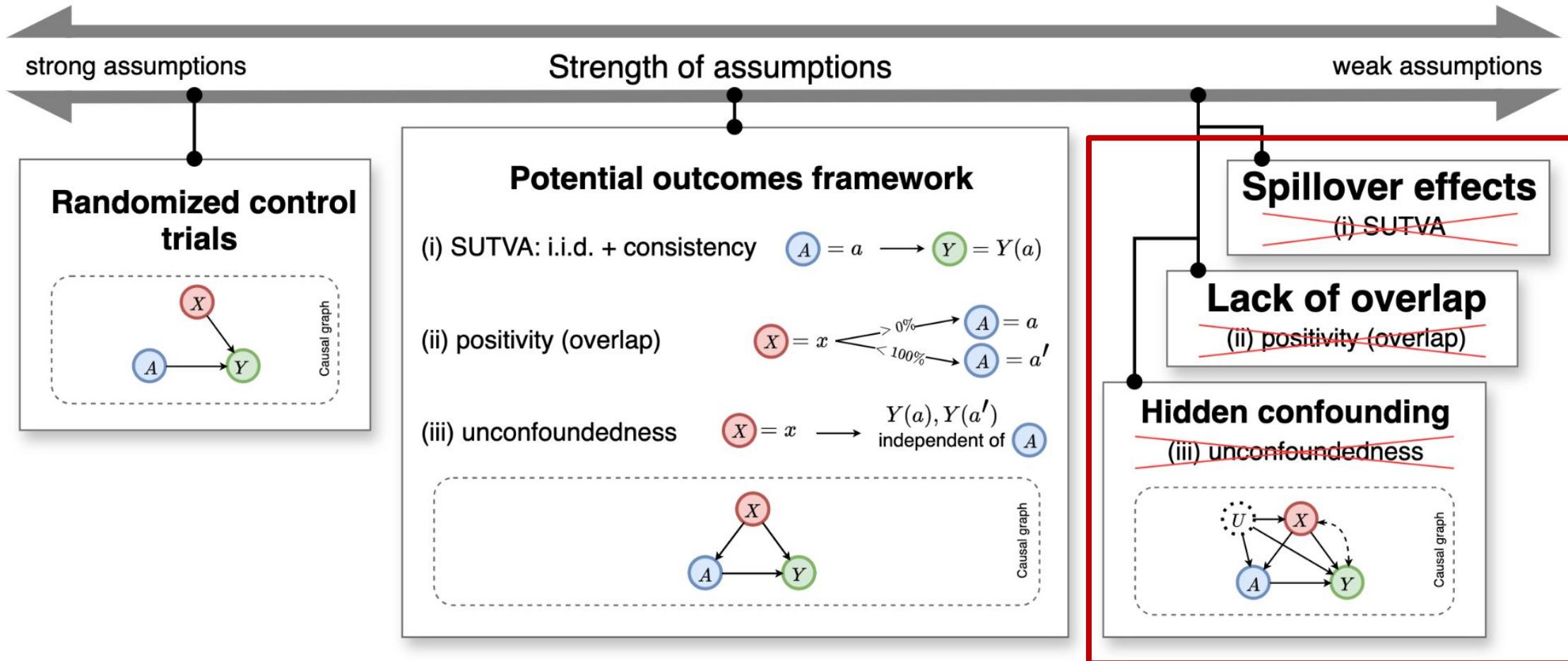
## 3 Uncertainty quantification

- Uncertainty quantification
  - uncertainty of estimation (aka confidence intervals)
  - predictive uncertainty (aka predictive intervals)



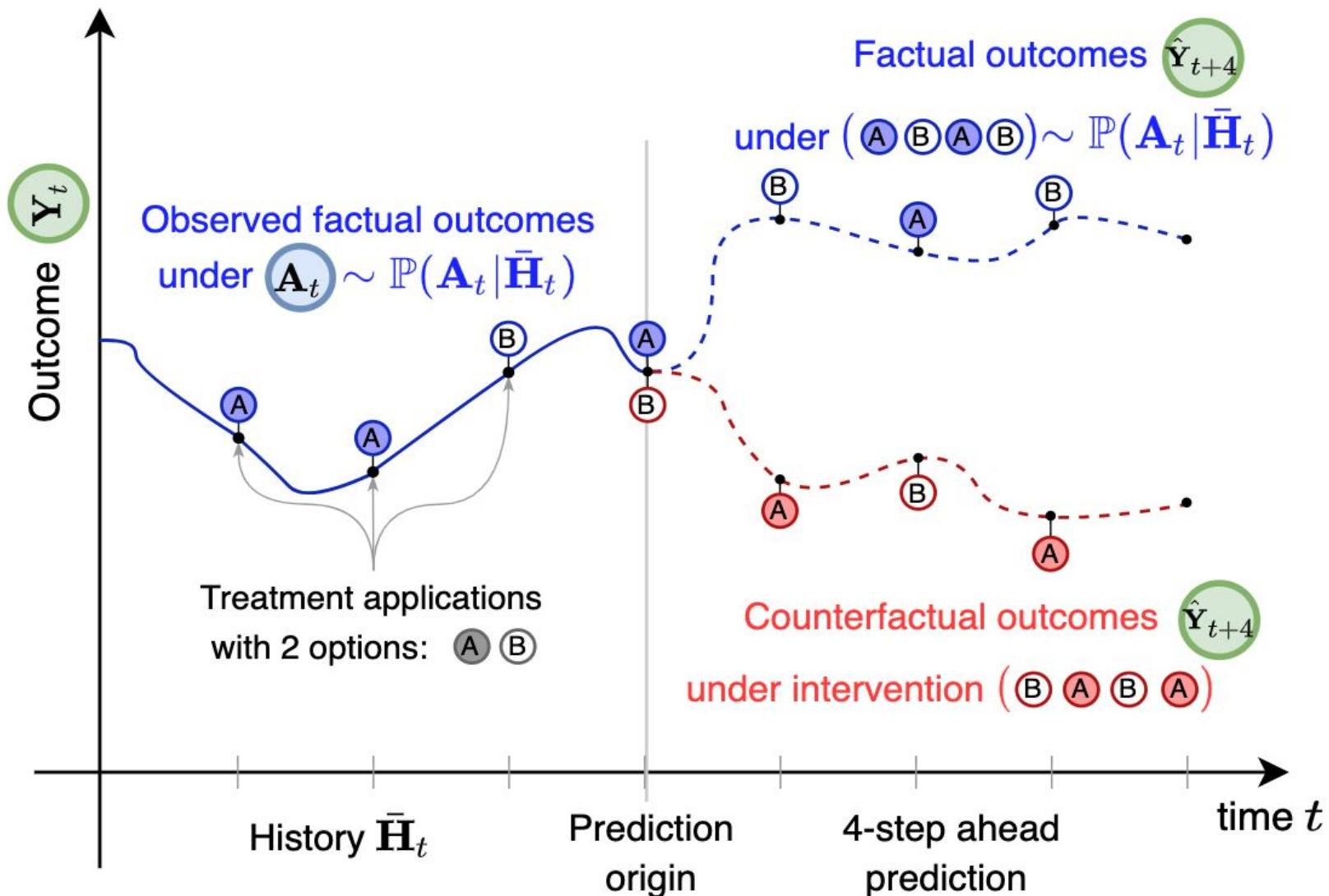
## **EXTENSIONS & OPEN RESEARCH QUESTIONS**

## Model validity: Robustness checks wrt. violation of assumptions



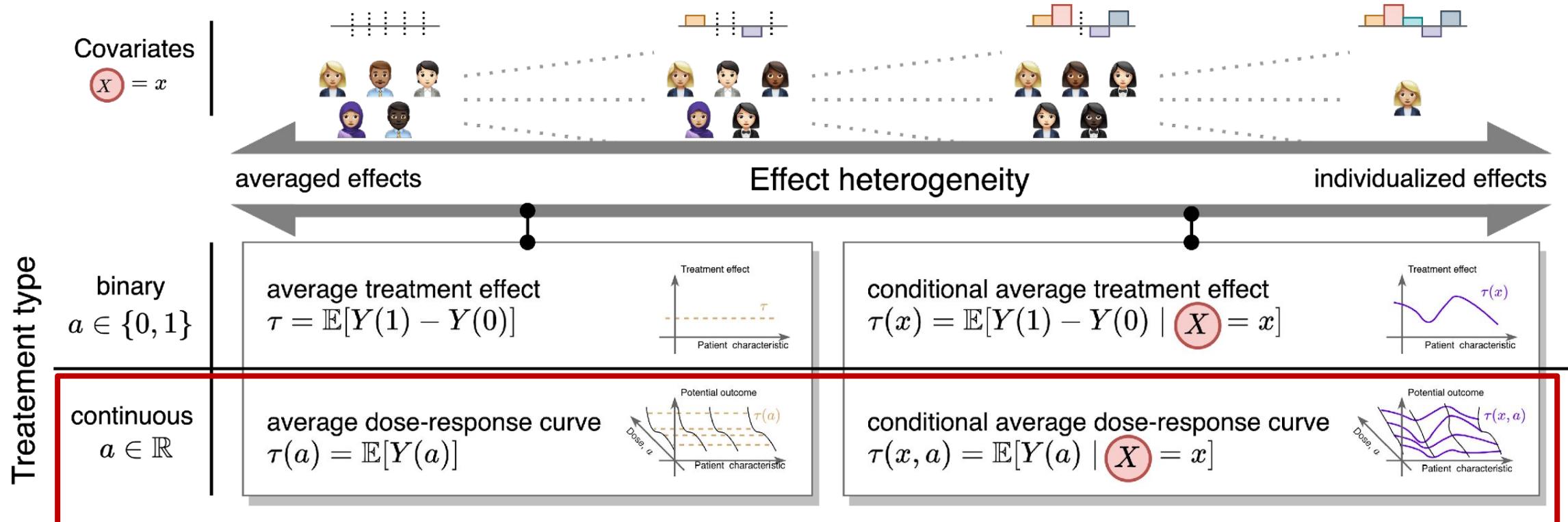
## EXTENSIONS & OPEN RESEARCH QUESTIONS

### Flexibility: Causal ML for predicting outcomes over time

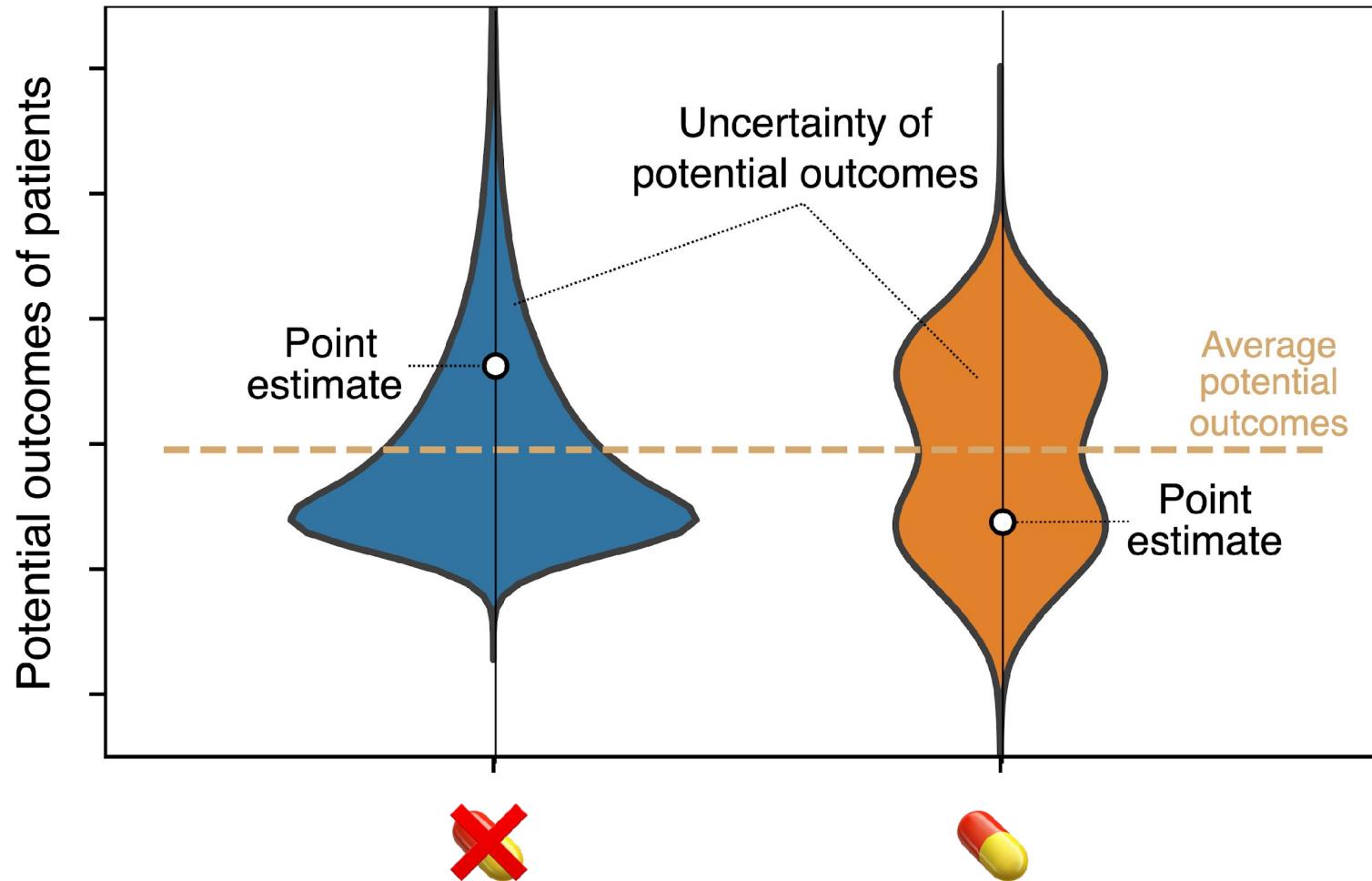


## EXTENSIONS & OPEN RESEARCH QUESTIONS

# Flexibility: Continuous / high-dimensional treatments

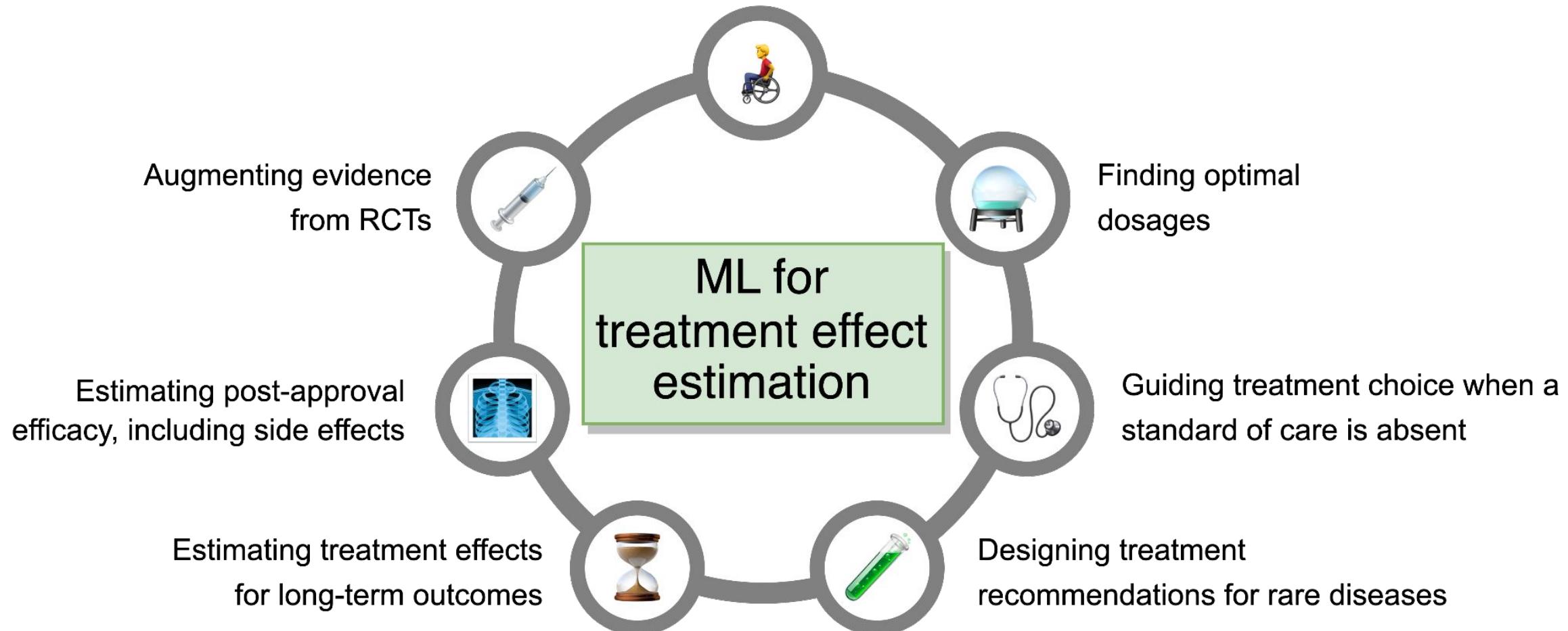


## Uncertainty quantification



## Promises of Causal ML

Estimating treatment effects for vulnerable groups





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