

# Concurrency again

*Sistemi di Calcolo 2*

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Software solutions for  
synchronization

# Dijkstra's Algorithm

```
/* global storage */
boolean interested[N]      = {false, ..., false}
boolean passed[N]         = {false, ..., false}
int k = <any>               // k ∈ {0, 1, ..., N-1}

/* local info */
int i = <entity ID> // i ∈ {0, 1, ..., N-1}
1.  interested[i] = true
2.  while (k != i) {
3.    passed[i] = false
4.    if (!interested[k]) then k = i
    }
5.  passed[i] = true
6.  for j in 1 ... N except i do
7.    if (passed[j]) then goto 2
8.  <critical section>
9.  passed[i] = false; interested[i] = false
```

# Dijkstra characteristics

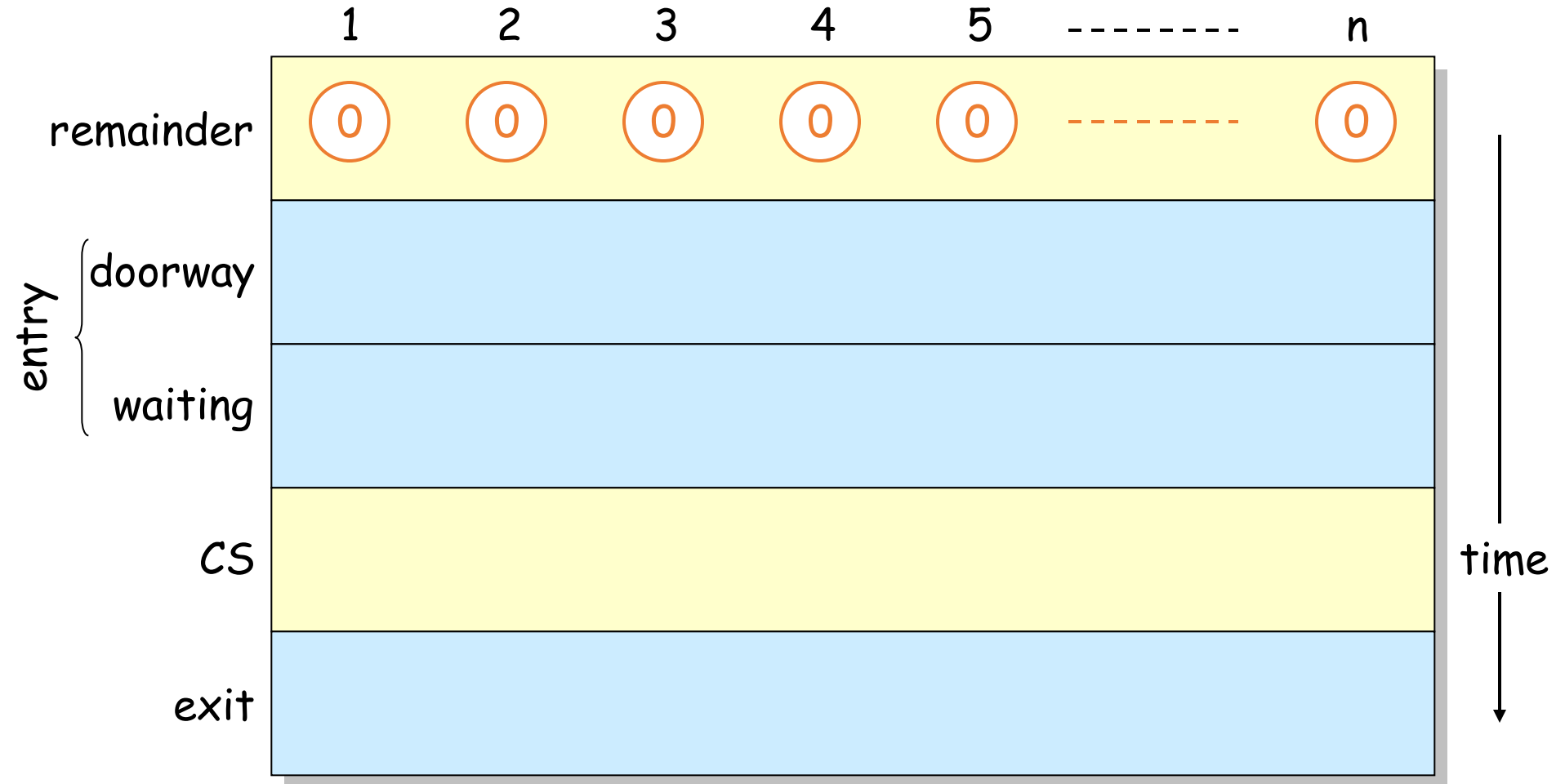
- Mutual Exclusion
- No deadlock
- No starvation?
  - Not guaranteed
- Other problems:
  - Needs atomic read/write
  - Needs memory sharing for k

# Bakery Algorithm

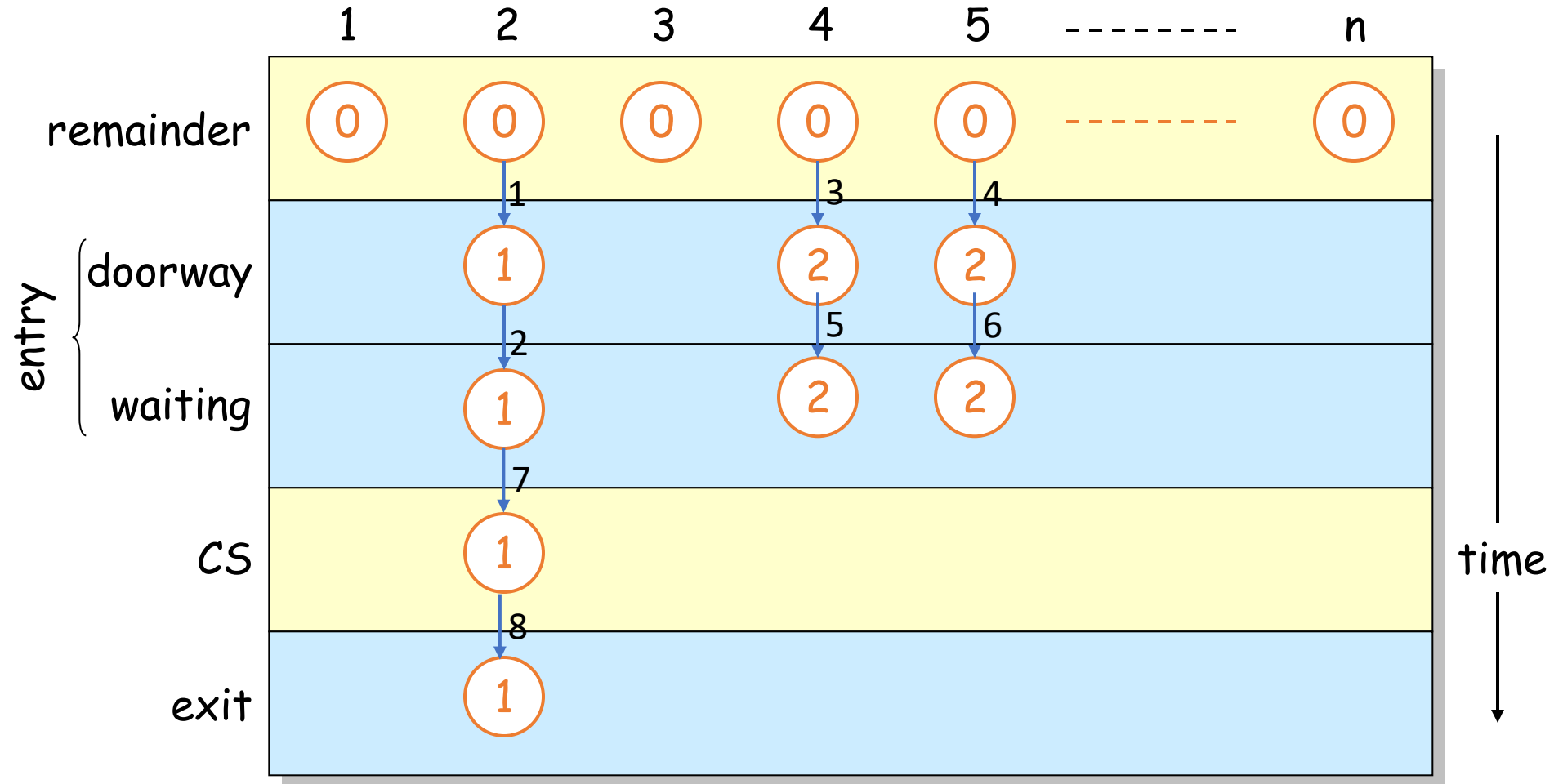
## Lamport (1975)

- Concept:
  - Think of a popular store with a crowded counter
    - People take a ticket from a machine
    - If nobody is waiting, tickets don't matter
    - When several people are waiting, ticket order determines order in which they can make purchases

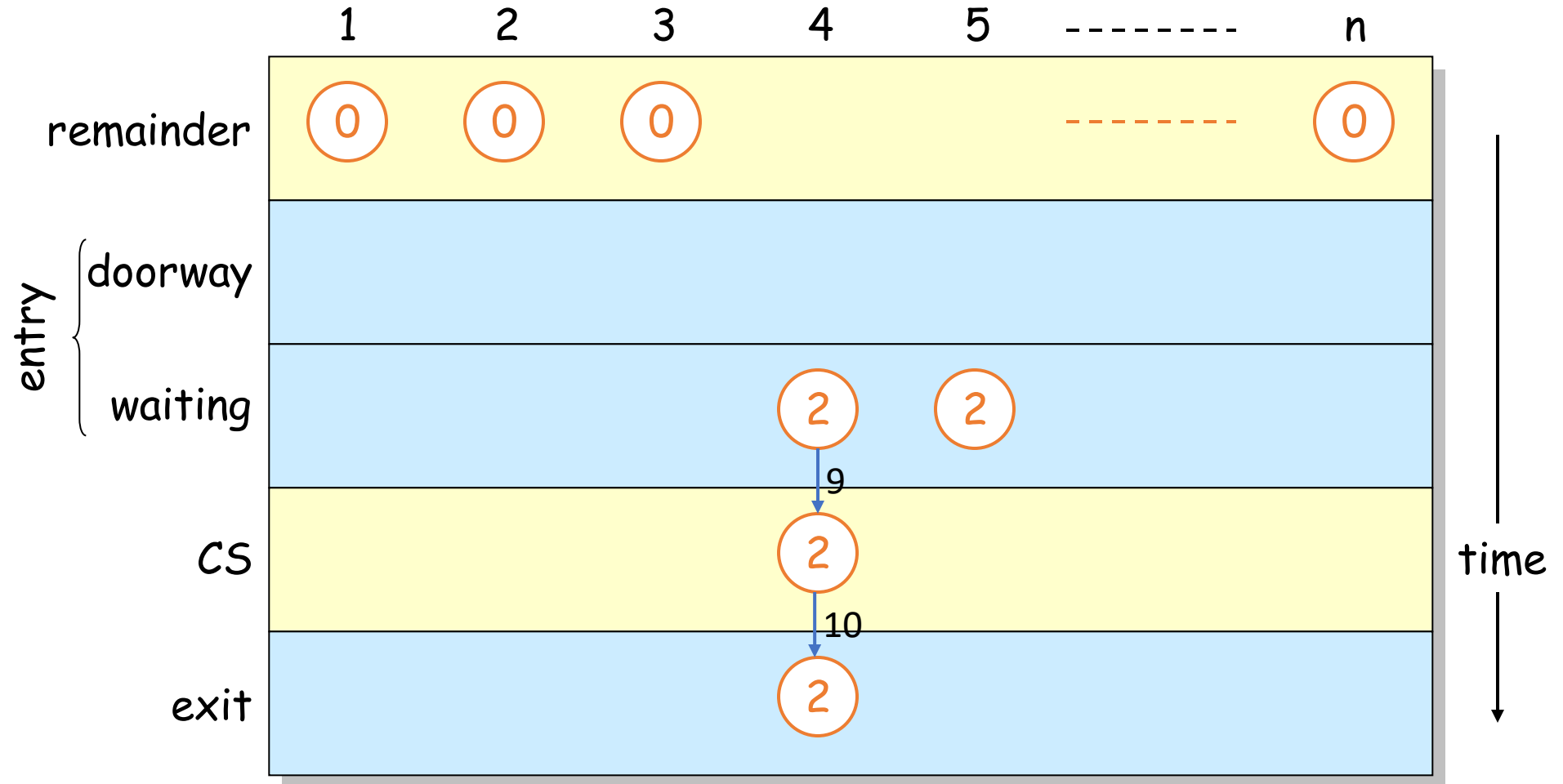
# The Bakery Algorithm



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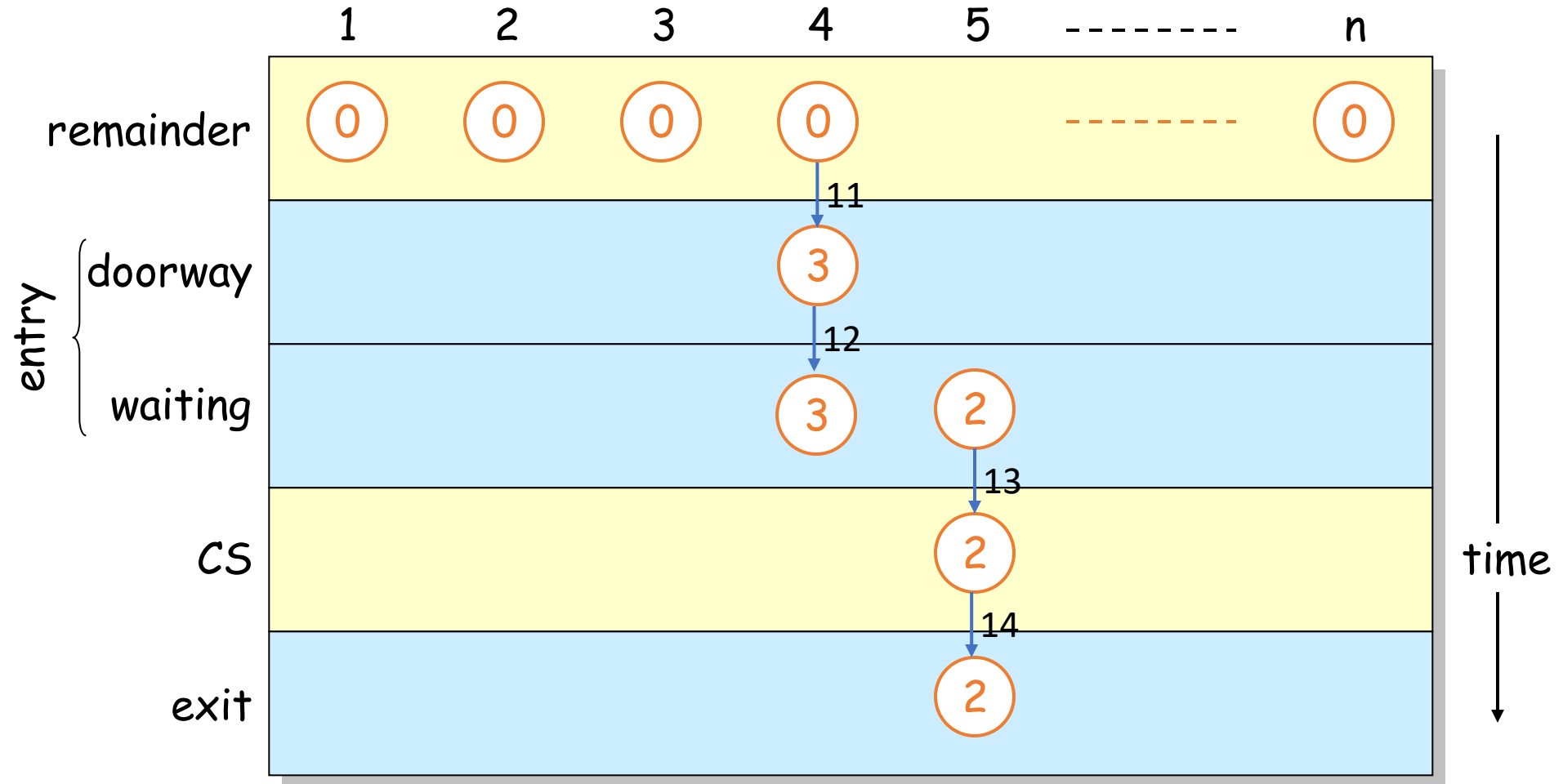


# The Bakery Algorithm





# The Bakery Algorithm



# Implementation 1

code of process  $i$ ,  $i \in \{1, \dots, n\}$

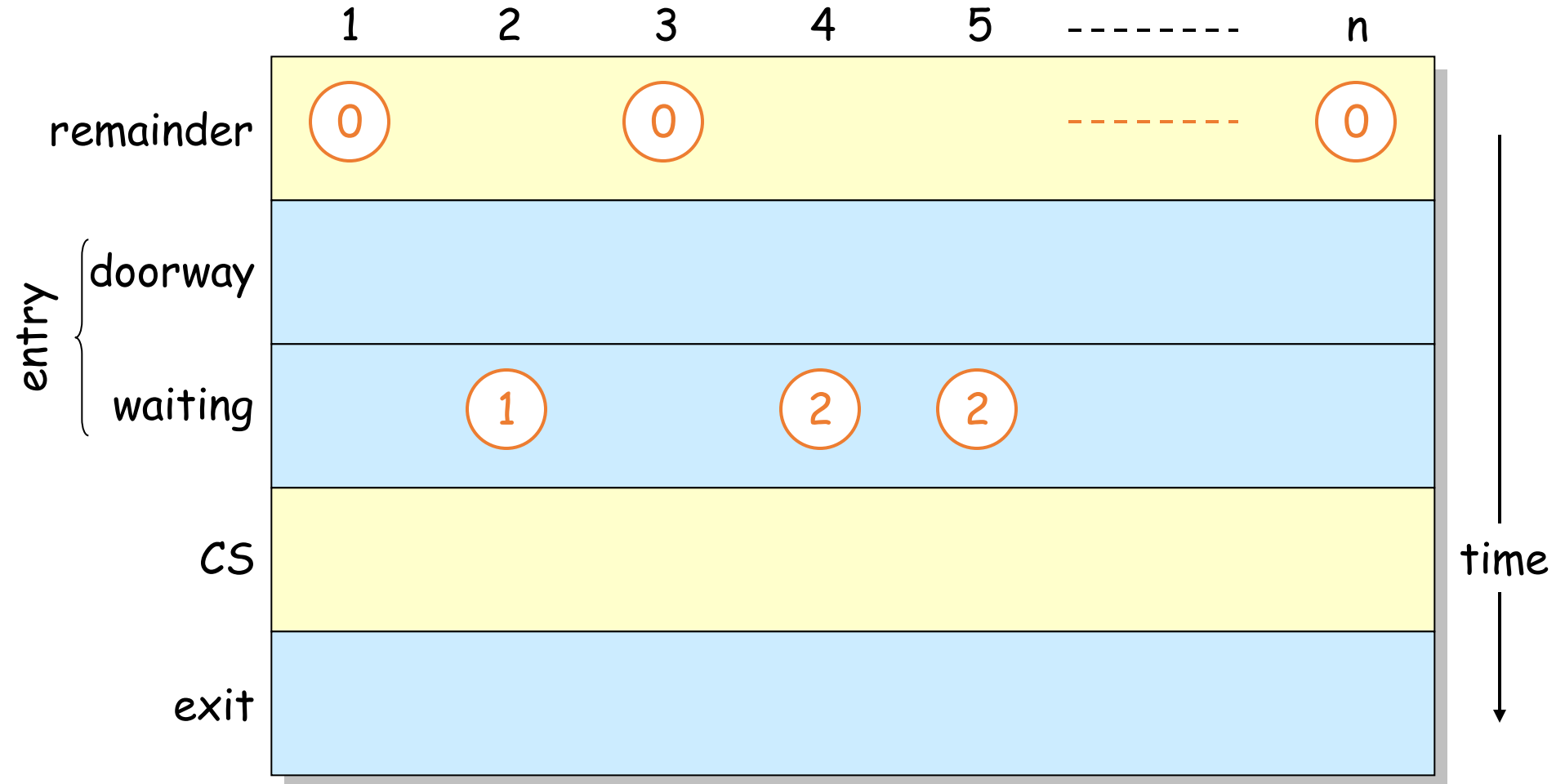
```
while (1){  
    /*NCS*/  
    number[i] = 1 + max {number[j] | (1 ≤ j ≤ N) except i}  
    for j in 1 .. N except i {  
        while (number[j] != 0 && number[j] < number[i]);  
    }  
    /*CS*/  
    number[i] = 0;  
}
```

//Doorway  
↓  
//Bakery  
↑

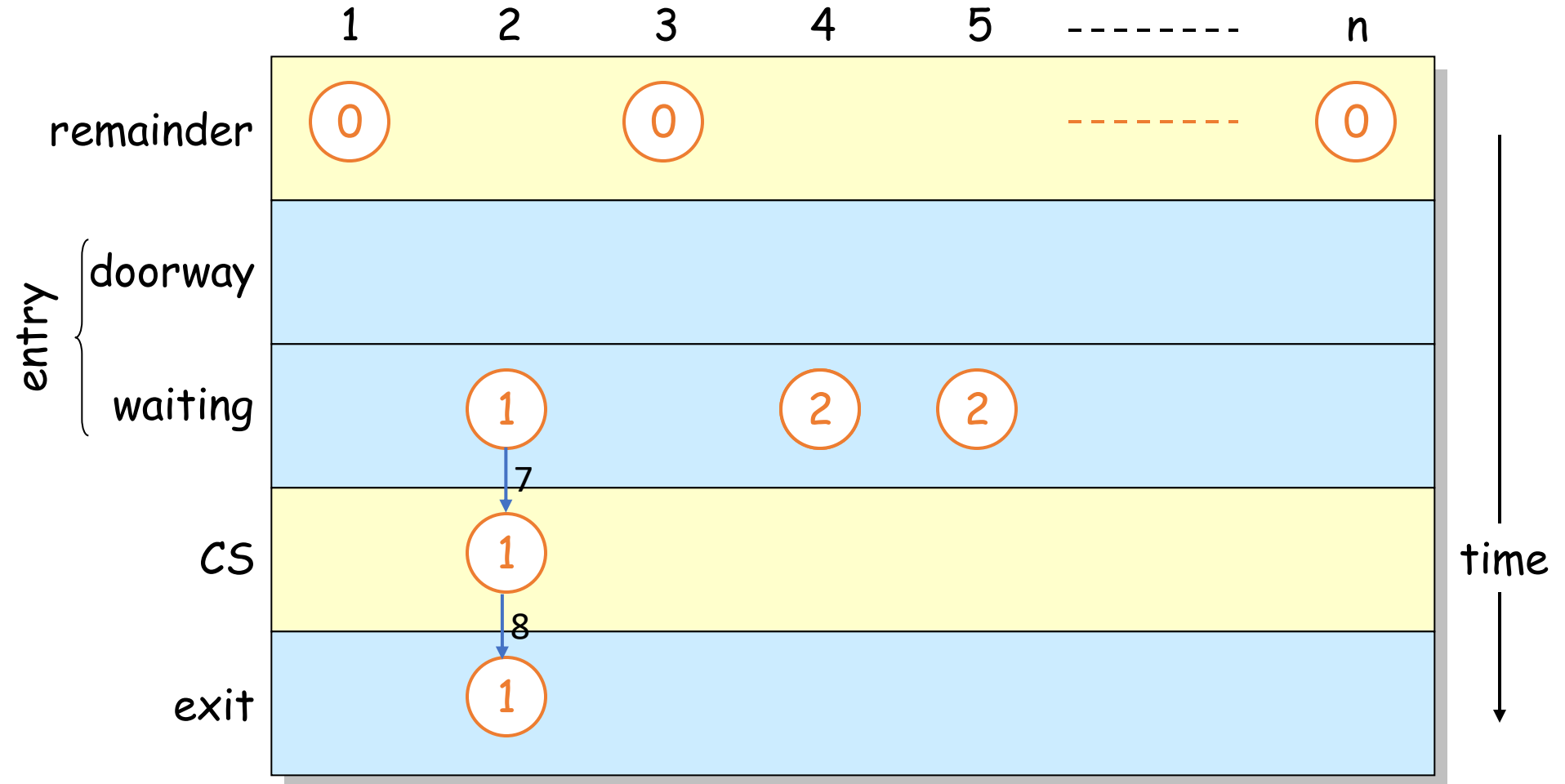
	1	2	3	4	-----	n	
number	0	0	0	0	0	0	integer

Answer: does not satisfy mutual exclusion

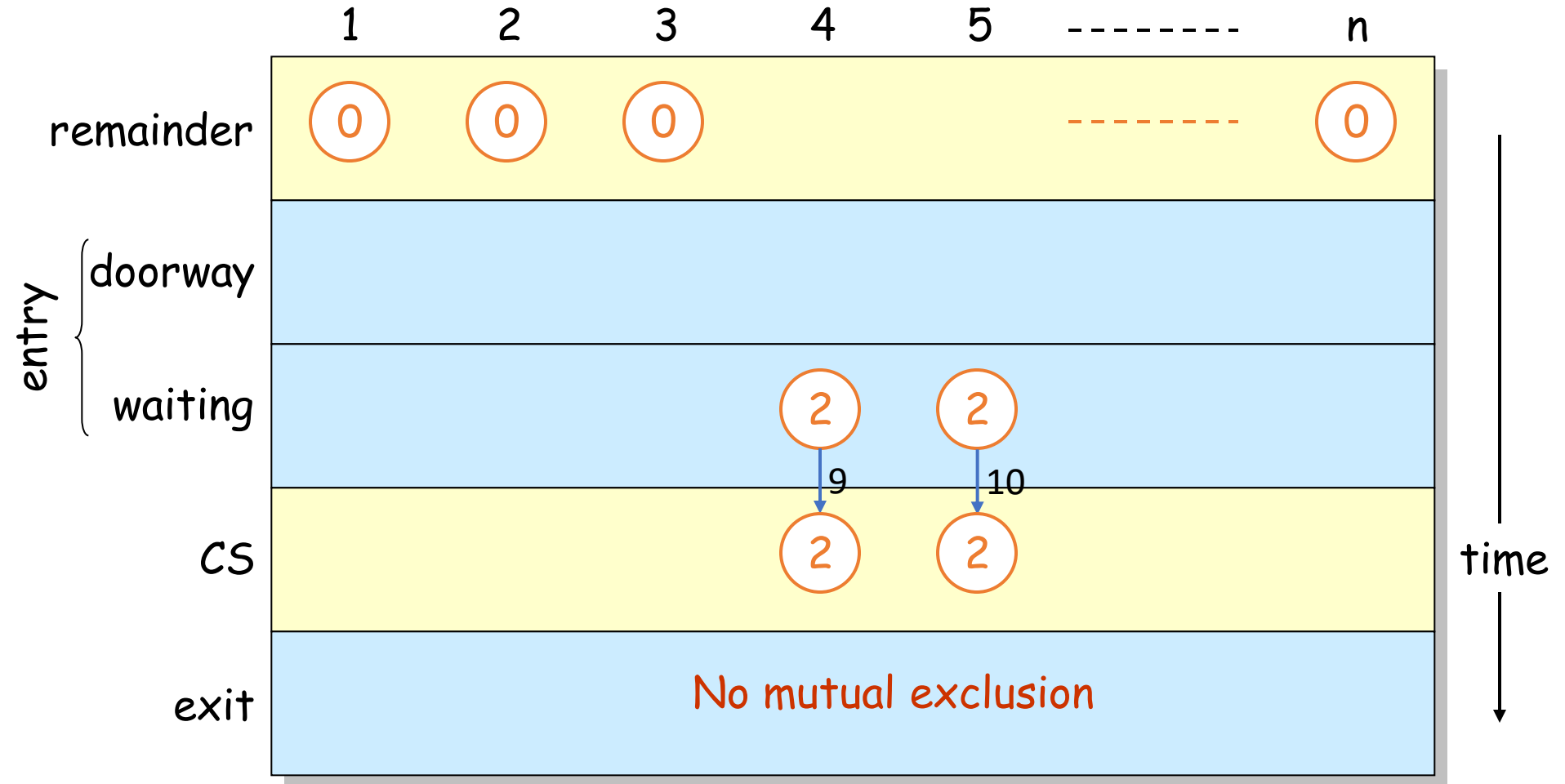
## Implementation 1: deadlock



# Implementation 1: deadlock



# Implementation 1: deadlock

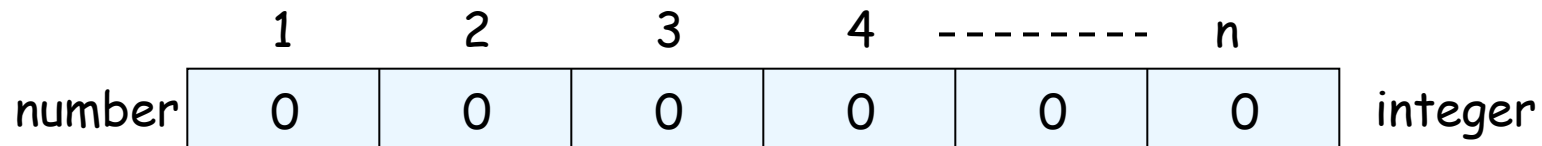


# Implementation 1

code of process  $i$ ,  $i \in \{1, \dots, n\}$

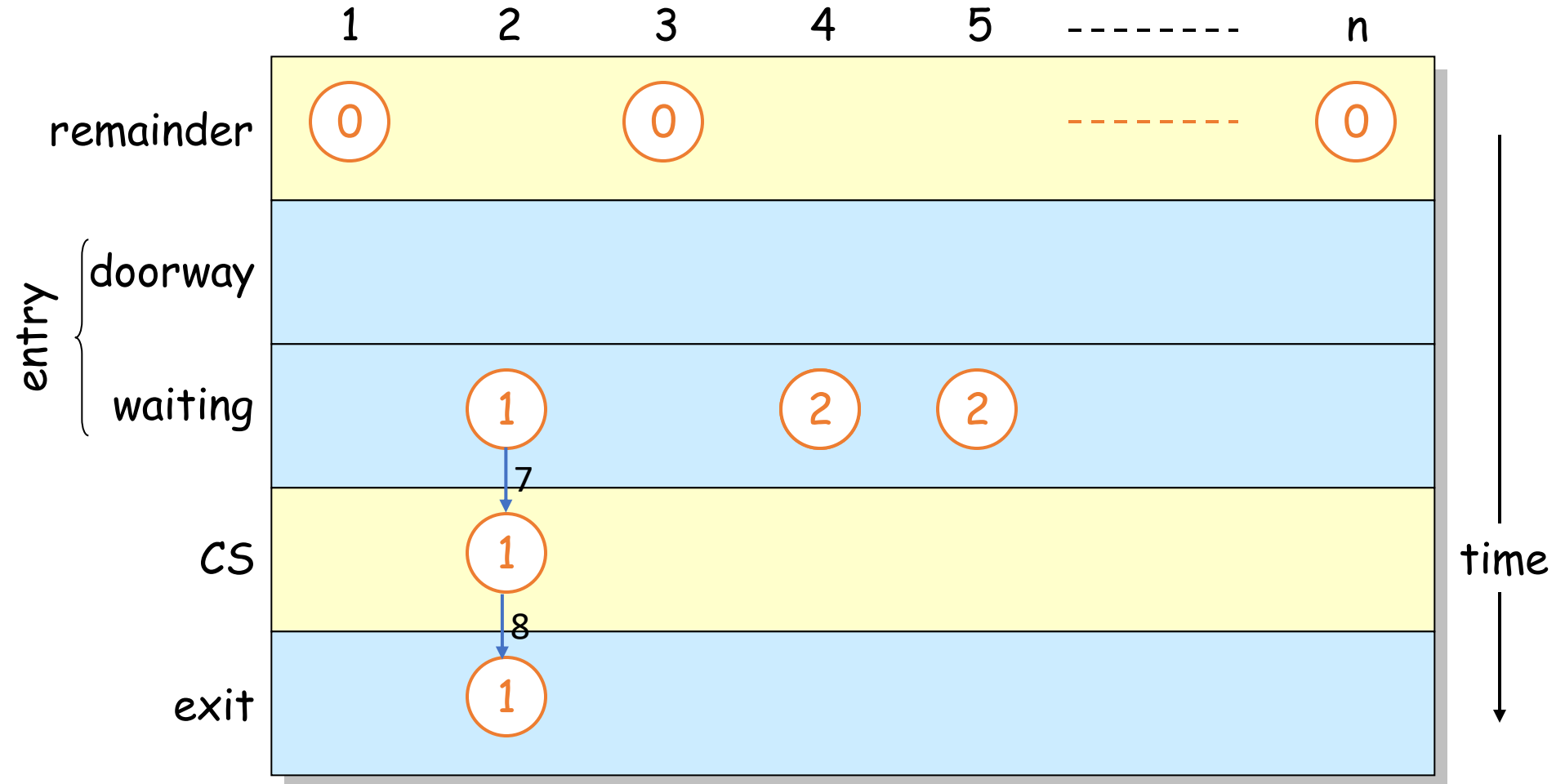
```
while (1){  
    /*NCS*/  
    number[i] = 1 + max {number[j] | (1 ≤ j ≤ N) except i}  
    for j in 1 .. N except i {  
        while (number[j] != 0 && number[j] < number[i]);  
    }  
    /*CS*/  
    number[i] = 0;  
}
```

What if we replace  $<$  with  $\leq$ ?

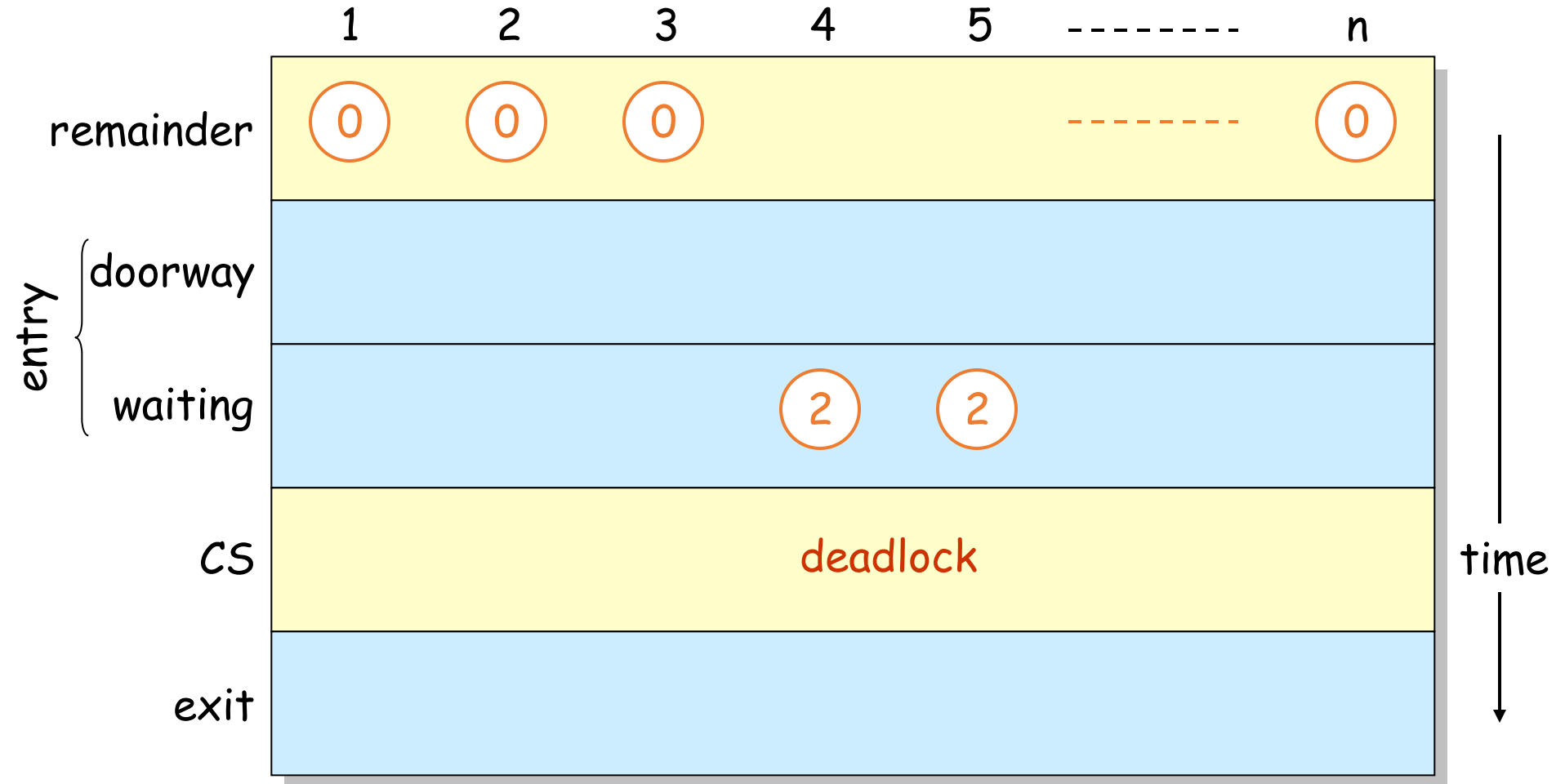


Answer: No! can deadlock

# Implementation 1: deadlock



## Implementation 1: deadlock





# Implementation 2

code of process  $i$ ,  $i \in \{1, \dots, n\}$

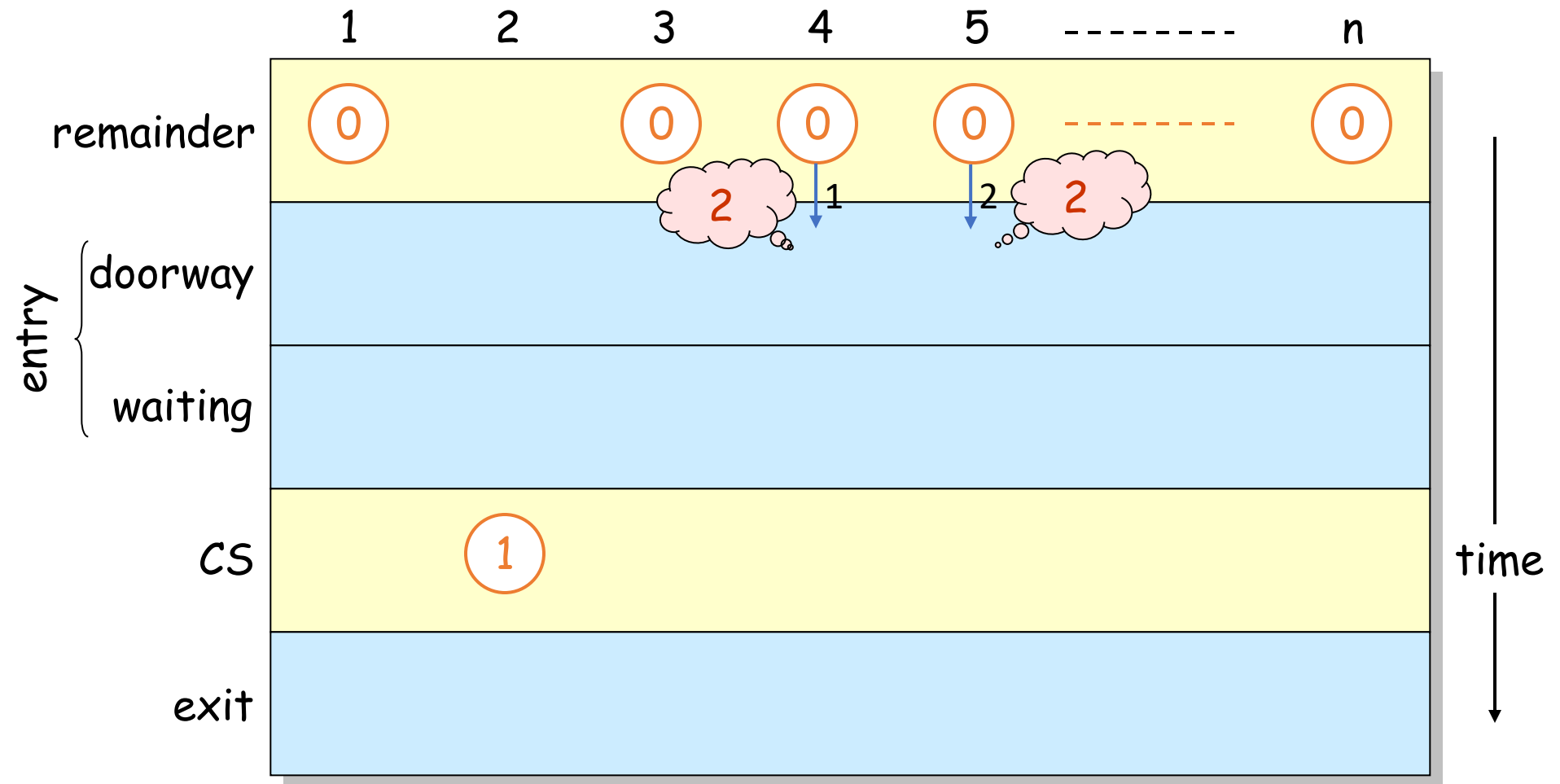
```
while (1){  
    /*NCS*/  
    number[i] = 1 + max {number[j] |  $(1 \leq j \leq N)$  except i}  
    for j in 1 .. N except i {  
        while (number[j] != 0 && (number[j],j) < (number[i],i));  
    }  
    /*CS*/  
    number[i] = 0;  
}
```

// lexicographical order:  $(B,j) < (A,i)$  means  $(B < A \mid \mid (B == A \ \&\& \ j < i))$

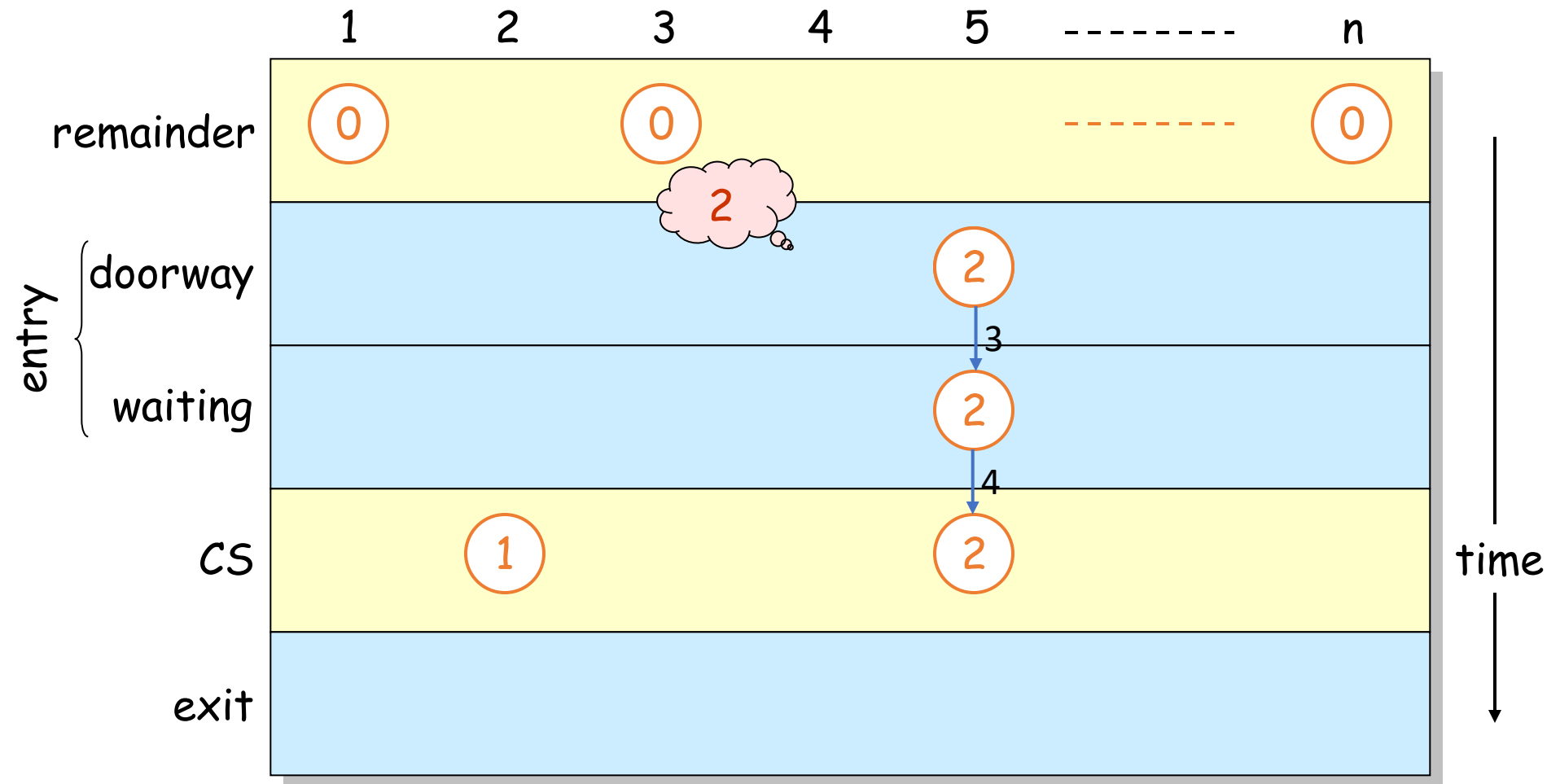
	1	2	3	4	-----	n	
number	0	0	0	0	0	0	integer

Answer: does not satisfy mutual exclusion

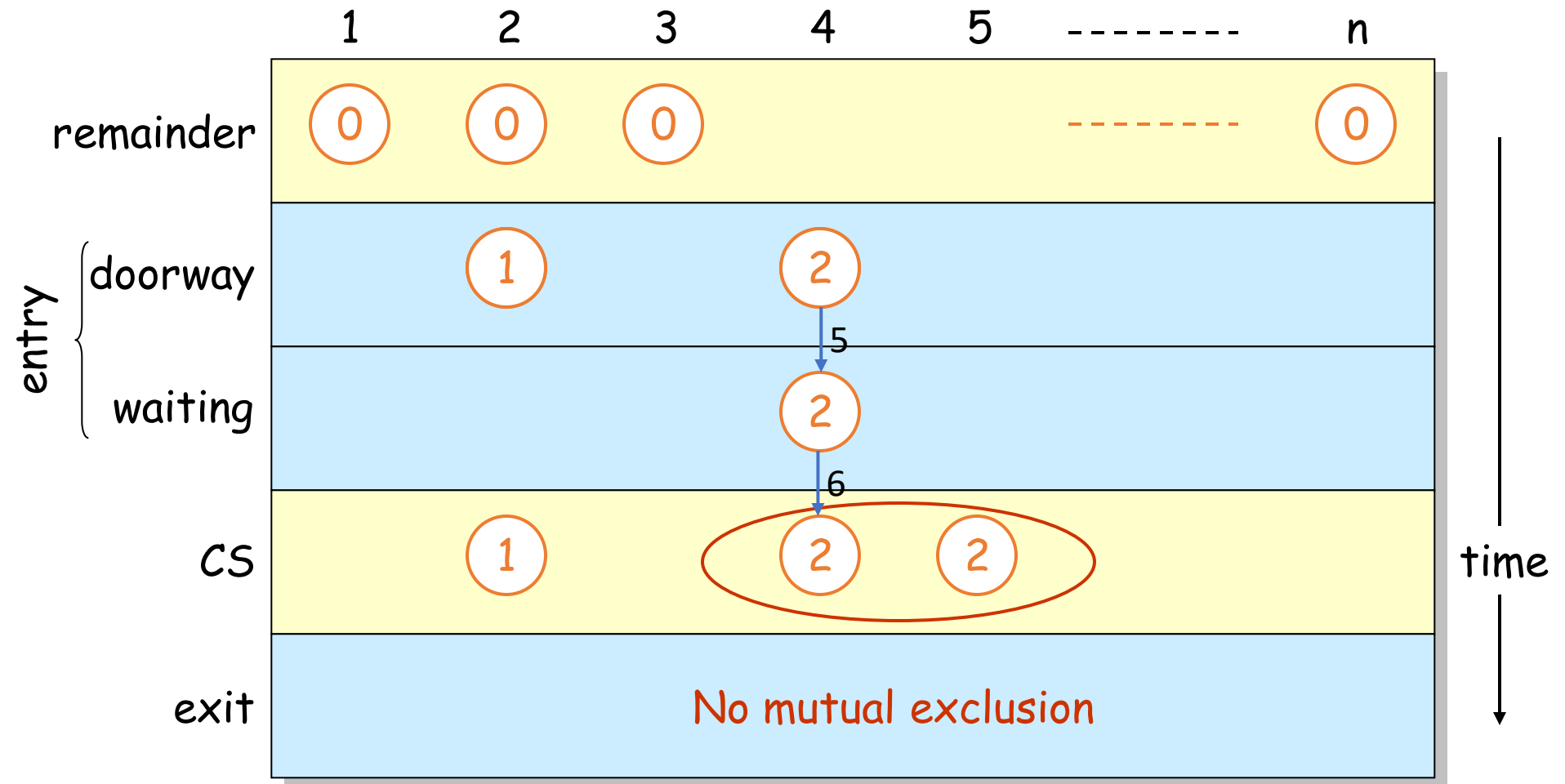
## Implementation 2: no mutual exclusion



## Implementation 2: no mutual exclusion



## Implementation 2: no mutual exclusion



# The Bakery Algorithm

code of process  $i$ ,  $i \in \{1, \dots, n\}$

```
while (1){  
    /*NCS*/  
    choosing[i] = true;  
    number[i] = 1 + max {number[j] | (1 ≤ j ≤ N) except i}  
    choosing[i] = false;  
    for j in 1 .. N except i {  
        while (choosing[j] == true);  
        while (number[j] != 0 && (number[j],j) < (number[i],i));  
    }  
    /*CS*/  
    number[i] = 0;  
}
```

	1	2	3	4	-----	n	
choosing	false	false	false	false	false	false	bits
number	0	0	0	0	0	0	integer

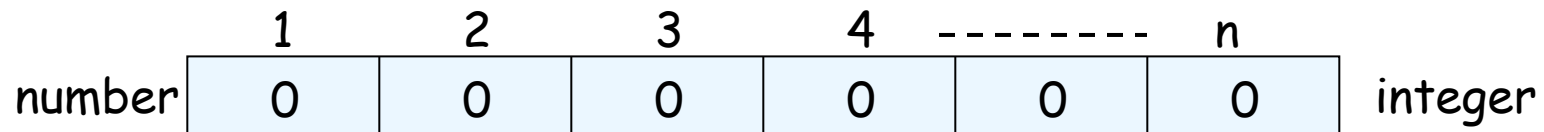
# Computing the Maximum

code of process  $i$ ,  $i \in \{1, \dots, n\}$

Correct implementation

```
number[i] = 1 + max {number[j] | (1 ≤ j ≤ N)}
```

```
local1 = 0;  
for local2 in 1 .. N {  
    local3 = number[local2];  
    if (local1 < local3)  
        local1 = local3;  
}  
number[i] = 1 + local1
```



# The Bakery Algorithm with bounded numbers

code of process  $i$ ,  $i \in \{1, \dots, n\}$

```
while (1){
    /*NCS*/
    while(number[i] == 0){
        choosing[i] = true;
        number[i] = (1 + max {number[j] | (1 ≤ j ≤ N) except i}) % MAXIMUM
        choosing[i] = false;
    }
    for j in 1 .. N except i {
        while (choosing[j] == true);
        while (number[j] != 0 && (number[j],j) < (number[i],i));
    }
    /*CS*/
    number[i] = 0;
}
```

# Bakery algorithm characteristics

- Processes communicate by writing/reading shared variables (as Dijkstra)
- Read/write are not atomic operations
  - Reader can read while writer is writing
  - None receives any notification
- Any shared variable is owned by a process that can write it, others can read it
- No process can perform two concurrent writings
- Execution times are not correlated



# The Bakery Algorithm in client/server app.

code of process  $i$ ,  $i \in \{1, \dots, n\}$

```
while (1){ //client thread
    /*NCS*/
    choosing = true; //doorway
    for j in 1 .. N except i {
        send(Pj,num);
        receive(Pj,v);
        num = max(num,v);
    }
    num = num+1;
    choosing = false;
    for j in 1 .. N except i { //backery
        do{
            send(Pj,choosing);
            receive(Pj,v);
        }while (v == true);
        do{
            send(Pj,v);
            receive(Pj,v);
        }while (v != 0 && (v,j) < (num,i));
    }
    /*CS*/
    num = 0;
}
```

```
//global variable
//inicialization:
int num = 0;
boolean choosing = false;
// and process ip/ports
```

```
while (1){ //server thread
    receive(Pj,message);
    if (message is a number)
        send(Pj,num);
    else
        send(Pj,choosing);
}
```

Assumptions:

- Finite response time
- Reliable communication channels