

Artificial Intelligence :-
Final test:-

Vallamkonda Vishal
SS071029

1) Propositional Logic:-

$A \rightarrow$ "Carla goes to the party"
 $B \rightarrow$ "Diana goes to the party"
 $C \rightarrow$ "Mario goes to the party"
 $D \rightarrow$ "Bruno goes to the party"

Formulize the given sentence:-

- 1) $D \rightarrow \neg A \rightarrow \psi_1$
- 2) $(D \vee C) \vee (D \wedge C) \rightarrow \psi_2$
- 3) $C \rightarrow B \rightarrow \psi_3$
- 4) $A \rightarrow \neg B \rightarrow \psi_4$
- 5) $(A \vee B) \wedge (C \vee D)$ (The party is over atleast one

female and male friend are going $\rightarrow \emptyset$

Lets try resolving above Equations:-

$$\psi_1: D \rightarrow \neg A \equiv \boxed{(\neg D \vee \neg A)}$$

$$\psi_2: \boxed{(D \vee C) \vee (D \wedge C)}$$

$$\psi_3: C \rightarrow B \equiv \boxed{\neg C \vee B}$$

$$\psi_4: A \rightarrow \neg B \equiv \boxed{\neg A \vee \neg B}$$

Claes of $\varphi_1, \varphi_2, \varphi_3, \varphi_4$ are

1) $\neg D$ } φ_1

2) $\neg A$ }

3) D, C } φ_3

4) D, C }

5) $\neg C$ } φ_3

6) B }

7) $\neg A$ } φ_4

8) $\neg B$ }

To find whether the party will happen or not the $\varphi_1, \varphi_2, \varphi_3$ and φ_4 should satisfy ϕ . Where ϕ is $(A \vee B) \wedge (D \vee C)$

\therefore When the party is over when one male and female

friend are going.

The $\varphi_1, \varphi_2, \varphi_3$ and φ_4 are consistent because If they are not the every formula of ϕ is a logical consequence of them.

There are total 5 contrails. ($\varphi_1, \varphi_2, \varphi_3, \varphi_4, \phi$)

The party will be there only if it is satisfiable i.e. There is atleast one interpretation that can all the considered

($\varphi_1 \wedge \varphi_2 \wedge \varphi_3 \wedge \varphi_4 \wedge \varphi_5$ is \top).

$(A \vee B) \vee (C \vee D) \Rightarrow$

9) A, B }
10) C, D }

Considering the above statements considering is we consider the following interpretation. i.e. $A' = F$, $B' = T$, $C' = T$ and $D' = T$. Then the given logic is true to it satisfiable (ie) for the above interpretation $\psi_1 \wedge \psi_2 \wedge \psi_3 \wedge \psi_4 \wedge \psi_5 \rightarrow T$ and is satisfiable hence the party will be there only if carla does not goes to the party.

5) Relational Logics

Given that the Herbrand universe with two constants and the predicates P and Q .

- 1) $\forall x. P(x) \rightarrow \exists (y). P(y)$
- 2) $\forall x. \exists y. Q(x, y) \rightarrow \exists x \forall y. (x, y)$
- 3) $\exists y. P(y) \rightarrow \forall x. P(x)$
- 4) $\forall x. \forall y. (x, y) \rightarrow \exists x. P(x)$
- 5) $(\forall x. (P(x) \rightarrow \exists y. Q(x, y)) \wedge \exists z. P(z)) \rightarrow \exists x. \exists y. Q(x, y)$

By showing the following formulae we are that in a party its

satisfiable

$$i) \forall x. P(x) \xrightarrow{x=y} \exists (y). P(y) \text{ (satisfied)}$$

$y = z$

The logical constraint, the party of boed. in.

$$ii) \forall x \exists y \forall (x, y) \Rightarrow \exists x \forall y \forall (x, y) \text{ (not satisfied)}$$

$$\left. \begin{array}{l} \forall x = \forall y \\ \exists y = \exists x \end{array} \right\} \Rightarrow \text{Equation is solved.}$$

$$iii) \exists y P(y) \Rightarrow \forall x. P(x) \text{ (not satisfied)}$$

$$\exists y \supset \forall x \Rightarrow \text{if possible}$$

$$(iv) \forall x \forall y. \psi(x, y) \rightarrow \exists x P(x) \text{ (satisfied)}$$

\Downarrow

It is not possible.

(not satisfied)

$$(v) (\forall x (P(x) \rightarrow \exists y (R(x, y) \wedge \exists z P(z) \wedge (R(z, x) \vee R(x, z)))) \rightarrow \exists x \exists y \neg \psi(x, y)) -$$

$$\exists x \exists y. \neg \psi(x, y)$$

\Downarrow

It is not possible.

which is not proportional