

David Vallecampo

ID: 991487504

MATH18584 Fundamentals of Computer Mathematics

- Assignment #1
- This assignment will be graded out of 30
- This assignment is to be completed individually. Assignments copied in whole or in part will receive a grade of ZERO.
- You must show your work for full marks!
- Answers may only be submitted in the following formats:
 - Microsoft Word Document (.docx)
 - Adobe PDF Document (.pdf)
 - Do not submit external links. Scanned documents need to be legible and in pdf format.

1. Evaluate the following signed binary numbers. (3 marks each)

a)
$$\begin{array}{r} 01000100 \\ + 00101100 \\ \hline 01110100 \end{array}$$

b)
$$\begin{array}{r} 01110110 \\ - 00111101 \\ \hline 111001 \end{array}$$

c)
$$\begin{array}{r} 11011100 \\ - 00101110 \\ \hline 10101110 \end{array}$$

2. Solve. (2 marks each)

a)
$$\begin{array}{r} A459 \\ + 4CF6 \\ \hline F14F \end{array}$$

b)
$$\begin{array}{r} 8B3 \\ - 6C4 \\ \hline 20F \end{array}$$

3. Convert the following numbers. Show all your steps. (2 marks each)

a) 146_{dec} to binary

$$\begin{aligned} 146 - 2^7 &= 18 \\ 18 - 2^4 &= 2 \quad \therefore 146_{dec} = 10010010 \\ 2 - 2^1 &= 0 \end{aligned}$$

b) $5FA63_{hex}$ to binary

$$\begin{array}{cccccc} 5 & F & A & 6 & 3 & hex \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \\ 01011111 & 10100110 & 0011 & 0100 & 0011 & bin \end{array}$$

4. Natasha would like to buy a car that costs $57C6_{hex}$ dollars. She has \$20,000 in the bank and her brother will give her 100110100111_{bin} . Can she afford the car? (3 marks)

$$\begin{aligned} 20000 \div 16 &= 1250, R0 \\ 1250 \div 16 &= 78, R2 \\ 78 \div 16 &= 4, R14 \\ 4 \div 16 &= 0, R4 \\ \therefore &= 4E20_{hex} \end{aligned}$$

$$\begin{array}{ccc} 1001 & 1010 & 0111 \\ \hline 9 & A & 7_{hex} \end{array}$$

$$\begin{aligned} \text{Natasha's } \$ &= 4E20 + 9A7 \\ &= 57C7_{hex} \end{aligned}$$

\therefore Natasha can afford the car because $57C7_{hex} > 57C6_{hex}$

5. Which of the following is a negation for "Jim is inside and Jan is at the pool?" Explain. (2 marks)

- (a) Jim is inside or Jan is not at the pool.
 (b) Jim is inside or Jan is at the pool.
 (c) Jim is not inside or Jan is at the pool.
 (d) Jim is not inside and Jan is not at the pool.
 (e) Jim is not inside or Jan is not at the pool.

c) because Jim is not inside to negate and Jan is not at the pool to negate the statement. 'And' remains.

6. Find the truth value of each of the expressions below, using the truth values shown. Show all your steps. (2 marks)

$$F * \sim(E * D) \leftrightarrow \sim(D * E + F) * D, \text{ where } D = 1, E = 0, F = 1$$

$$1 * \sim(0 * 1) \leftrightarrow \sim(1 * 0 + 1) * 1$$

$$1 * \sim(0) \leftrightarrow \sim(1) * 1$$

$$1 \leftrightarrow 0$$

$$0$$

7. Using the Identities and Laws of Boolean Algebra, simplify the following expressions. List the specific law used for every simplification. (2 marks each)

a. $\sim(\sim B * A + \sim B) + A$

b) $AB(\sim C + 1) + A(C + 1) \quad T3$

b. $A * B * \sim C + A * B + A * C + A$

a) $\sim(\sim B(A + 1)) + A \quad T3$

$\sim(\sim B(1)) + A \quad T7$

$B + A \quad T10$

8. Evaluate using the equivalent binary numbers:
 (-6) - 5

(2 marks)