

# Regression Analysis (MATH 1312)

## Final Project

“What’s driving the health insurance up, in the US?”

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# Table of Contents

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Introduction.....	3
Dataset .....	3
Target Feature .....	3
Descriptive Features (Predictors) .....	3
Data-Preprocessing .....	3
Data Exploration .....	4
Methodology .....	6
Linear Regression .....	6
Ridge Regression .....	7
Lasso Regression (Least absolute shrinkage selector operator).....	8
Model Selection.....	8
Predictors Selection.....	9
Model Building .....	11
First Model .....	11
Model diagnostic for first model .....	11
Prediction for first model .....	12
Second Model.....	12
Model diagnostic for second model .....	12
Prediction for second model .....	14
Third model .....	14
Model diagnostic for third model.....	14
Prediction for Third model .....	15
Results .....	15
Evaluating Interpretation .....	15
Discussion .....	17
References .....	17
Appendix.....	17

# Introduction

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As per the saying- “A sound mind lives in a healthy body”. With the increase in health-related problems, People have become more aware about maintaining an insured life to avoid any financial risks. But the fact that getting a health insurance comes at a high cost, is one of the concerns. I have come across an article about the same, published by [CNBC](#) in 2018, addressing the concern over high health care costs for the individuals in the United States and factors involved. The United States is one of those countries that overspends on an average ~\$9,500 Mn on its healthcare expenditure. This report will scrutinize all those parameters that are responsible for the variation in the costs of health-insurance.

During my proposal I will try and answer the following two questions:

- Within the United States, is it true that the insurance premium cost is high based on the location?
- If not, then what are the key variables apart from the regions explaining higher insurance costs?

## Dataset

---

To support my idea, I have searched related datasets on various public data sites and found “Medical cost personal dataset” to be the most suitable according to my requirements for further analysis. The data is sourced from [Kaggle](#). The dataset comprises 7 variables (predictors) and 1338 observations. All the further actions will be taken out on this dataset. The variables in this dataset are sex, BMI, children, smoker, region, and target variable charges.

### Target Feature

The target feature for this dataset is ‘**Charges**’ variable. ‘Charges’ has chosen as a response variable because it is the medical cost for an individual, that is dependent on other features/predictors. It varies based on the factors affecting the cost of insurance.

### Descriptive Features (Predictors)

The description of the attributes that has been chosen for descriptive features are readily comprehensible and are as follows-

**Age**- age of primary beneficiary

**Sex**- gender of the insurer, female, male

**bmi** - Body mass index, providing an understanding of body, weights that are relatively high or low relative to height, objective index of body weight ( $\text{kg} / \text{m}^2$ ) using the ratio of height to weight, ideally 18.5 to 24.9.

**children**: Number of children covered by health insurance / Number of dependents

**smoker**: Smoking

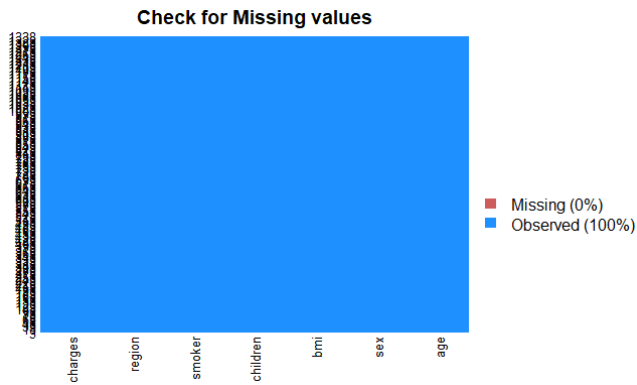
**region**: the beneficiary's residential area in the US, northeast, southeast, southwest, northwest.

## Data-Preprocessing

---

Data has been imported to R, using `read.csv()` function and named it as “US\_health”. The size of the data is confirmed using ‘`dim()`’ function. The structure of the data is viewed by using ‘`str()`’ function, in order to display list contents compactly. To scan the data quickly on the basis of statistics, `summary()` function is used.

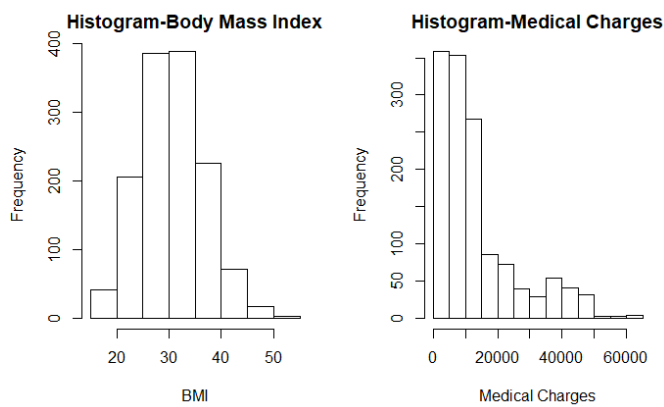
It is very important that the dataset should not contain any missing and NA values. A miss map is created to check the missing values in the data. The map shows that there is no missing value present in the data. Also, `colSums(is.na())` is used to check for the NA values, and the result shows that there is no NA value as well.



## Data Exploration

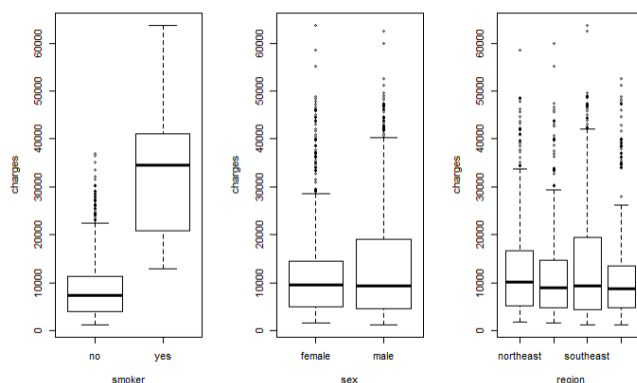
To support the hypothesis and to apprehend the dataset statistically, it is always better to visualize the data. So, histograms are used for "Univariate Visualization", whereas, "Box plot", "Double bar graph" and "scatter plot" are used for "Multi-variate Visualizations".

### 1.) Univariate Visualization

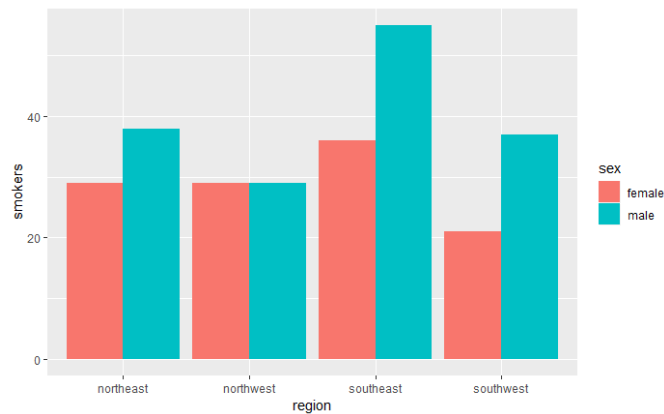


From the above histogram for BMI, it can be seen that it is normally distributed. Although, it is rightly skewed for the medical charges, showing that in this dataset, the observations with high medical costs are lesser.

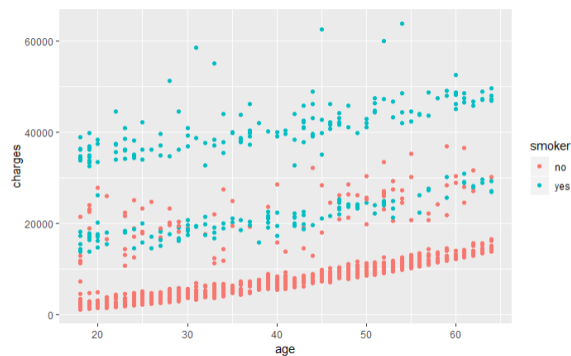
### 2.) Multivariate Visualization



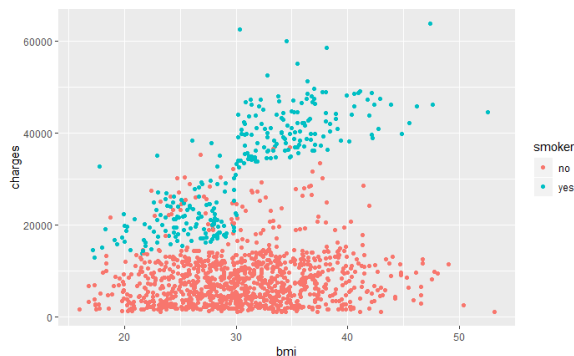
The above boxplots for gender and region are having more outliers for that of high charges than comparatively lower charges. The medians for region and genders are almost the same. The most expected point to note here is medical costs are very high for the people who smoke.



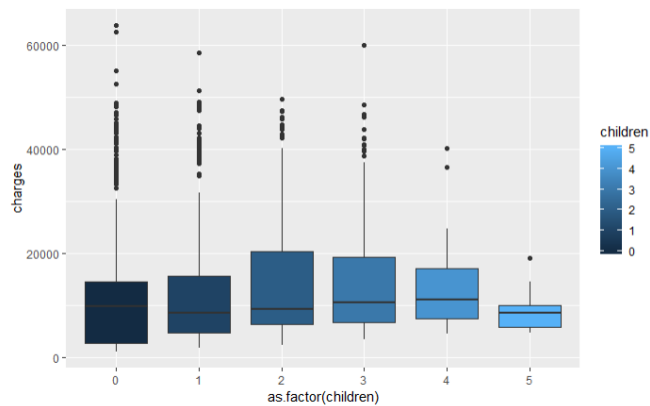
From the above double bar graph, it can be observed that both male and female equal smokers in almost all the 4 regions. Although, in southeast male smokers are more than that of female.



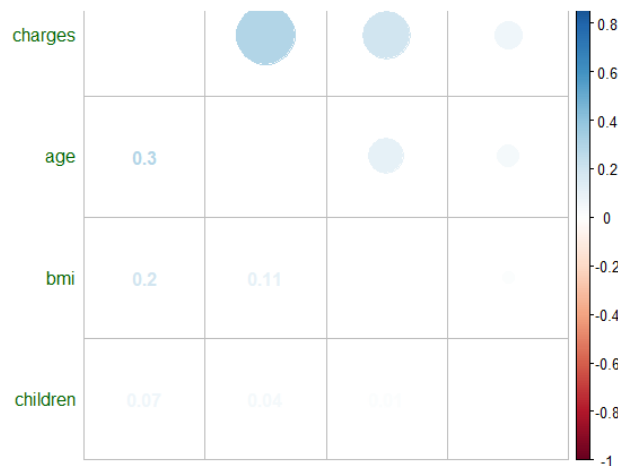
The above scatter plot is showing that higher charges are directly proportional to old-aged smokers. In other words, as the age increases for the smokers so do their health-related issues, that eventually results in higher medical costs.



Based on the above plot, it is found out that those smokers who have higher BMI tend to pay higher for the insurance premiums. In other words, the higher bmi smokers are more vulnerable to diseases, and hence will pay higher medical costs.



The above boxplot is giving an idea that people having 2 or 3 children are paying higher insurance charges than those having lesser or a greater number of children. Again, all the medians are almost at the same level.



Using correlation plot, it can be figured out that medical cost is highly correlated with 'age'. In other words, as the age increase the medical cost also increases. With the help of visualisation it can be concluded that 'charges' is highly dependent on 'customer related data'.

## Methodology

In order to understand the relationship between independent variables and dependent variable 'target'. Regression analysis on data set is performed using Linear regression, Lasso Regression (Least absolute shrinkage selector operator), and Ridge regression.

### Linear Regression

Linear regression is among the simplest and most widely used technique for predictive modeling. Linear regression model looks for statistical relationship and not for deterministic relationship<sup>[1]</sup>, where the main objective is to obtain a line of best fit for the data. The line of best is a diagonal line for which the prediction errors are very small as possible.

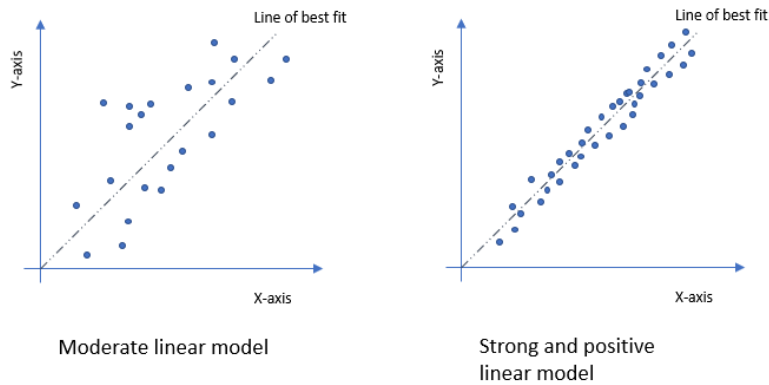


Figure 1, Linear regression model type

The closer the data point are closer to the line of best fit, the better is the model with less variation which is explained by adjusted  $R^2$  value. A scatterplot shown above determines the strength of the relationship between two variables, and numerical measurement of association between two variables is generally explained by coefficient of correlations, between -1 and 1.

Linear regression equation is:  $Y = a + bX$ . Where,  $a$  is the intercept,  $Y$  is the dependent variable, slope is  $b$  and  $X$  is the explanatory variable.

## Ridge Regression

Multiple regression data which has multicollinearity, ridge regression is a technique that is commonly used. If there is multicollinearity present then there is an unbiasedness in their least square estimates, but they might be placed far away from their actual values which is explained by higher variation. As it is known that multicollinearity creates inaccurate estimates for the coefficients by inflating the standard errors. Therefore, by adding a parameter or a degree of bias to the estimates, the standard errors explained by higher variance is minimized.

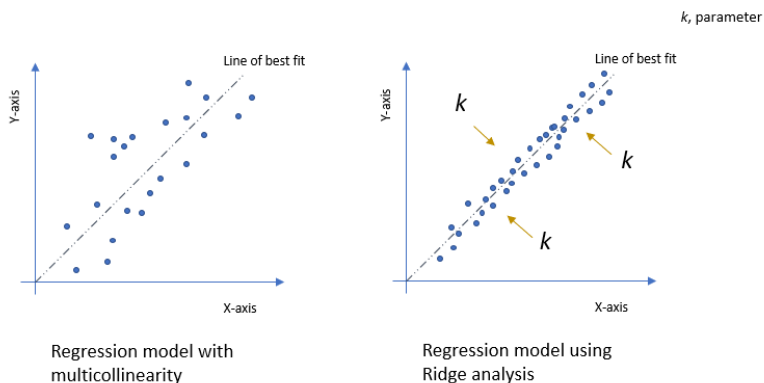


Figure 2, Ridge regression model type

Ridge Regression equation is:  $Y = a + b\bar{e}$ . Where,  $a$  is the intercept,  $Y$  is the dependent variable, slope is  $b$  and  $\bar{e}$  represents the errors are residuals.

## Lasso Regression (Least absolute shrinkage selector operator)

Lasso regression is very similar to the ridge analysis, where Lasso selects only the best features while reducing the coefficients of less important features to 0, generally this practice is known as feature selection. Lasso uses L1 regression technique and is generally preferred when there are large number of variable present in the dataset. However, one of the challenge during the Lasso regression is that even if there are variables with smaller correlation, the lasso model will set the value for that feature to 0. As a result, it will lead to loss of information which further would lead to poor model performance.

## Model Selection

For model building, the first step is to split the data into 70-30 train and test.

```
##{r}
set.seed(10)
Ind <- sample(2,nrow(US_health),replace= TRUE,prob=c(0.7,0.3))
train_health <- US_health[Ind==1,]
test_health <- US_health[Ind==2,]
##
```

A linear regression model is then built based on this split. The summary statistics for the same is below for the train set.

```
Call:
lm(formula = train_health$charges ~ ., data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-11090.8  -3115.8   -951.6   1525.4  30446.4

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -12478.26   1223.49  -10.199 < 2e-16 ***
age           254.56     14.74   17.265 < 2e-16 ***
sexmale     -171.20     413.98   -0.414  0.67931
bmi          369.80     35.36   10.458 < 2e-16 ***
children     428.85     169.92    2.524  0.01178 *
smokeryes    23777.71    510.49   46.578 < 2e-16 ***
regionnorthwest -633.69    592.50   -1.070  0.28512
regionsoutheast -1664.15    589.47   -2.823  0.00486 **
regionsouthwest -1027.20    598.50   -1.716  0.08645 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6244 on 913 degrees of freedom
Multiple R-squared:  0.743,    Adjusted R-squared:  0.7408
F-statistic: 330 on 8 and 913 DF, p-value: < 2.2e-16
```

A sample data is the created, in which, the 'x' is containing all the variables but the target variable and the 'y' is containing only the target variable. The sample train set is then divided into half and the sample test set is made to consist everything but the sample train set. Linear and ridge models were then tried to fit, and the differences came out to be nominal. Hence, ridge model was used to check whether it can improve the OLS estimations. After checking the ridge model for the coefficients, it turned out to be not significant as the coefficients estimates were coming out to be conservative. So, lasso model then tried to fit and check for the coefficients again. Lasso model, as expected, set the unimportant variables to zero and gave preferences to the three most important predictors, i.e., age, bmi and smokers. Lasso can be chosen as the best model, but it needs to have the lowest MSE value. Post checking the MSE values for the three models, linear regression model came out to be with least MSE score, hence, it is selected as the best model among the three.



```
#Checking MSE for linear model
mean((lm_predict-y_test)^2)
...

```

```
[1] 36825120
```

```
```{r}
#Checking MSE for ridge model
mean((ridge_predict-y_test)^2)
...

```

```
[1] 39616462
```

```
```{r}
#Checking MSE for Lasso Model
mean((lasso_predict-y_test)^2)
...

```

```
[1] 43500867
```

## Predictors Selection

Summary() function is used to get the descriptive statistics and the coefficients estimates in order to get the equation of the best fit for linear model. The equation came out to be-

$$y = -11544.86 + (236.65 * \text{age}) + (477.06 * \text{sexmale}) + (354.18 * \text{bmi}) + (500.36 * \text{children}) + (22107.37 * \text{smokeryes}) - (1101.03 * \text{regionnorthwest}) - (1409.71 * \text{regionsoutheast}) - (1363.39 * \text{regionsouthwest})$$

To select the best predictors among all the predictors, 5 methods are used, and those are, ANOVA, All possible subset regression, Forward regression, Backward regression and Stepwise regression. According to ANOVA statistics, age, BMI and smoker variables are the most significant ones. Stepwise and backward regression returned the same results, i.e., age, BMI, smoker and children are the best predictors. And, Forward and all possible subset regression gave the same results, i.e., all the predictors but sex are the best ones. So, to summarize, it can be said that, 3 possible models can be built, and those are-

1. MODEL 1- Based on ANOVA- age, bmi and smoker

Anova Table (Type II tests)

Response: US\_health\$charges

	Sum Sq	Df	F value	Pr(>F)	
age	7.0698e+09	1	184.5342	< 2e-16	***
sex	3.7256e+07	1	0.9724	0.32443	
bmi	2.7522e+09	1	71.8364	< 2e-16	***
children	2.3629e+08	1	6.1675	0.01326	*
smoker	5.4934e+10	1	1433.8560	< 2e-16	***
region	2.1251e+08	3	1.8489	0.13698	
Residuals	2.5286e+10	660			

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

## 2. MODEL 2- Based on Stepwise and backward- age, bmi, smoker and children

```

Step: AIC=11689.46
US_health$charges ~ age + bmi + children + smoker

              Df Sum of Sq      RSS      AIC
<none>                2.5549e+10 11690
- children    1  2.3349e+08  2.5783e+10 11694
- bmi         1  2.7725e+09  2.8322e+10 11756
- age         1  7.1431e+09  3.2692e+10 11852
- smoker      1  5.5639e+10  8.1189e+10 12461

Call:
lm(formula = US_health$charges ~ age + bmi + children + smoker,
    data = US_health, subset = train_new)

Residuals:
    Min       1Q   Median       3Q      Max
-10032   -3246   -1064    1246   31329

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -11845.57    1364.71   -8.680  <2e-16 ***
age           237.40      17.42    13.625  <2e-16 ***
bmi           338.98      39.93     8.488  <2e-16 ***
children      495.71     201.23     2.463   0.014 *
smokeryes     22134.76    582.09    38.026  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6203 on 664 degrees of freedom
Multiple R-squared:  0.7124,    Adjusted R-squared:  0.7107
F-statistic: 411.2 on 4 and 664 DF,  p-value: < 2.2e-16

```

## 3. MODEL 3- Based on Forward and all possible subset regression- age, bmi, smoker, children and region

Model FPE	R-Square HSP	Adj. R-Square APC	Pred R-Square	C(p)	AIC	SBIC	SBC	MSEP
1	0.6198	0.6195	0.618	611.9889	27667.4636	23868.9391	27683.0604	55887669.4102
55887544.4451		41800.8466	0.3814					
2	0.7214	0.7210	0.7196	93.8304	27253.3244	23455.8677	27274.1201	41010413.6993
41010184.4505		30673.4926	0.2799					
3	0.7475	0.7469	0.7455	-37.6245	27123.8359	23327.0363	27149.8306	37227691.7503
37227317.1643		27844.2284	0.2540					
4	0.7497	0.7489	0.7474	-46.9727	27114.0352	23317.3965	27145.2288	36956206.6446
36955628.2045		27641.1727	0.2522					
5	0.7509	0.7496	0.7475	-51.0596	27113.6624	23313.1716	27160.4528	36891265.6918
36890440.8009		27592.6006	0.2514					
6	0.7509	0.7494	0.7471	-49.2088	27115.5058	23315.1156	27167.4951	36942459.0871
36941343.9390		27630.8903	0.2517					

```

Start: AIC=11690.53
US_health$charges ~ age + sex + bmi + children + smoker + region

Call:
lm(formula = US_health$charges ~ age + sex + bmi + children +
    smoker + region, data = US_health, subset = train_new)

Residuals:
    Min       1Q   Median       3Q      Max
 -9872   -3015   -1107    1305   31561

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -11544.86    1416.98   -8.148 1.86e-15 ***
age           236.65      17.42    13.584  < 2e-16 ***
sexmale       477.06     483.77     0.986   0.3244
bmi           354.18      41.79     8.476  < 2e-16 ***
children      500.36     201.48     2.483   0.0133 *
smokeryes     22107.37    583.83    37.866  < 2e-16 ***
regionnorthwest -1101.03    688.29   -1.600   0.1102
regionsoutheast -1409.71    686.01   -2.055   0.0403 *
regionsouthwest -1363.39    686.14   -1.987   0.0473 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6190 on 660 degrees of freedom
Multiple R-squared:  0.7154,    Adjusted R-squared:  0.7119
F-statistic: 207.4 on 8 and 660 DF,  p-value: < 2.2e-16

```

# Model Building

## First Model

First model is built on the basis of ANOVA results with three of the best predictors, i.e., age, bmi, smoker. On the basis of summary the equation came out to be-

$$y = -12037.77 + (256.42 \cdot \text{age}) + (338.80 \cdot \text{bmi}) + (23670.40 \cdot \text{smoker})$$

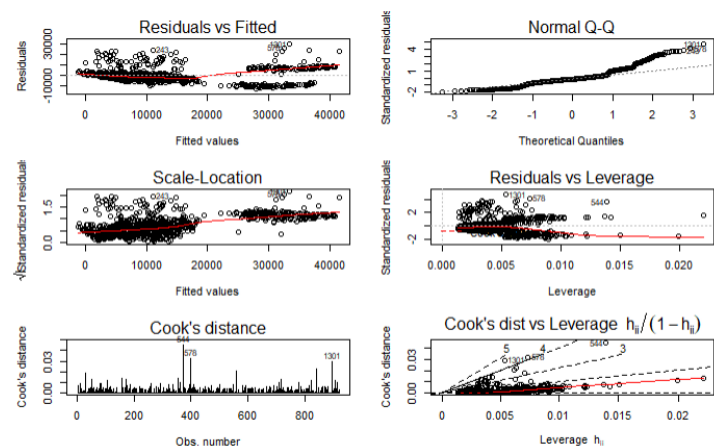
## Model diagnostic for first model

Firstly, the multicollinearity was diagnosed using VIF scores. There are no major differences noticed in the results, and all the values are closed to 1. Hence, it can be said that Multicollinearity is not present among the variables.

```
# Checking the Multicollinearity
car::vif(bestmodel_anova)
...
```

age	bmi	smoker
1.012844	1.012897	1.000052

Residuals assumptions are applied to this model, and 6 graphs are plotted. It can be noticed that all the variables are independent with zero mean and are mostly normally distributed. Therefore, residuals assumptions are fulfilled.



With the 'Non-constant variance score test', the p-value is less than alpha 0.05, therefore the null hypothesis is rejected stating that the residuals variance is constant.

```
car::ncvTest(bestmodel_anova)
...
```

```
Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 151.619, Df = 1, p = < 2.22e-16
```

Next, is the durbin Watson test for testing the autocorrelated errors. With p-value greater than 0.05, the null hypothesis is not rejected, confirming that NO autocorrelation is present in the model.

```
durbinwatsonTest(bestmodel_anova)
```

```
***
```

```
lag Autocorrelation D-W Statistic p-value  
1 0.006906446 1.98215 0.778  
Alternative hypothesis: rho != 0
```

Although by shapiro wilk normality test, the p-value is less than 0.05, hence rejecting the null hypothesis, which states that the data is normally distributed. Hence, for this model the data is not normally distributed.

```
shapiro.test(bestmodel_anova$residuals)
```

```
***
```

```
Shapiro-wilk normality test
```

```
data: bestmodel_anova$residuals  
W = 0.89898, p-value < 2.2e-16
```

## Prediction for first model

The prediction for the models are done by using predict() function. In order to solve probabilities of prediction, type is set to "response". Residual is set with this predict result subtracted from the target variable. A prediction is then made by setting actual and predicted parameters, and accuracy is calculated.

```
ME RMSE MAE MPE MAPE  
Test set 60.4786 5667.741 4005.492 -19.5216 45.08702
```

## Second Model

Second model is built on the basis of stepwise and backward regression results with four of the best predictors, i.e., age, bmi, smoker and children. On the basis of summary the equation came out to be-

$y = -12565.34 + (255.28 * \text{age}) + (341.87 * \text{bmi}) + (23675.65 * \text{smokeryes}) + (421.95 * \text{children})$

## Model diagnostic for second model

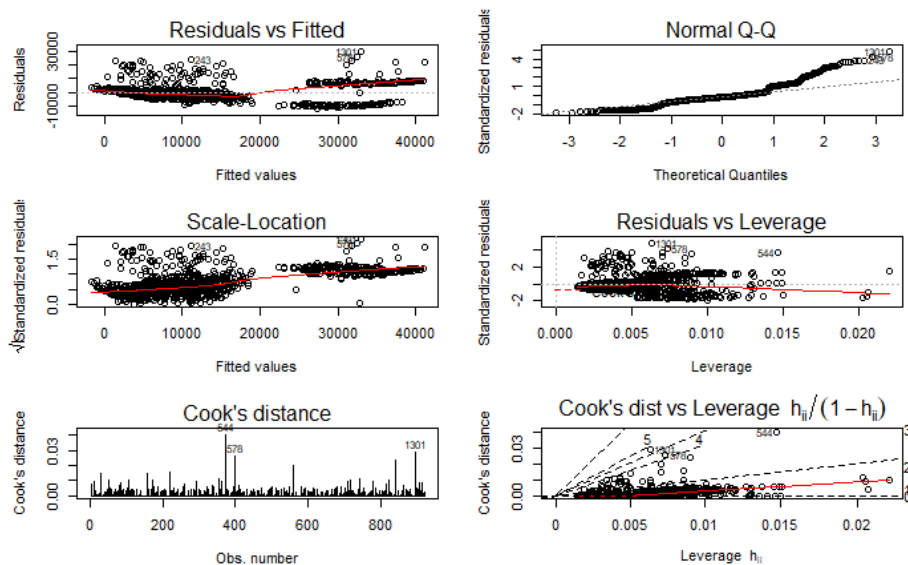
Again, There are no major differences noticed in the VIF score results, and all the values are closed to 1. Hence, it can be said that Multicollinearity is not present among the variables.

```
car::vif(bestmodel_StepBack)
```

```
***
```

```
age bmi smoker children  
1.013816 1.014245 1.000070 1.002078
```

Residuals assumptions are applied to this model, and 6 graphs are plotted. It can be noticed that all the variables are independent with zero mean and are mostly normally distributed. Therefore, residuals assumptions are fulfilled.



With the 'Non-constant variance score test', the p-value is less than alpha 0.05, therefore the null hypothesis is rejected stating that the residuals variance is constant.

```
car::ncvTest(bestmodel_stepBack)

...

Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 156.9308, Df = 1, p = < 2.22e-16
```

With p-value greater than 0.05, the null hypothesis is not rejected, confirming that NO autocorrelation is present in the model, by durbin Watson test for testing the autocorrelated errors.

```
durbinwatsonTest(bestmodel_stepBack)

...

lag Autocorrelation D-w Statistic p-value
1 0.002167906 1.992042 0.882
Alternative hypothesis: rho != 0
```

Although by shapiro wilk normality test, the p-value is less than 0.05, hence rejecting the null hypothesis, which states that the data is normally distributed. Hence, for this model the data is not normally distributed.

```
shapiro.test(bestmodel_stepBack$residuals)

...

Shapiro-wilk normality test

data: bestmodel_stepBack$residuals
W = 0.89561, p-value < 2.2e-16
```

## Prediction for second model

The prediction for the second model is done by the same process. The statistics that came out from this prediction is-

	ME	RMSE	MAE	MPE	MAPE
Test set	107.7915	5628.947	3972.476	-16.4929	43.83209

## Third model

Third model is built on the basis of forward and all possible subset regression results with five of the best predictors, i.e., age, bmi, smoker, region and children. On the basis of summary the equation came out to be-

$$y = -12546.15 + (254.74 * \text{age}) + (369.25 * \text{bmi}) + (23756.57 * \text{smokeryes}) + (428.42 * \text{children}) - (638.41 * \text{regionnorthwest}) - (1668.87 * \text{regionsoutheast}) - (1030.88 * \text{regionsouthwest})$$

## Model diagnostic for third model

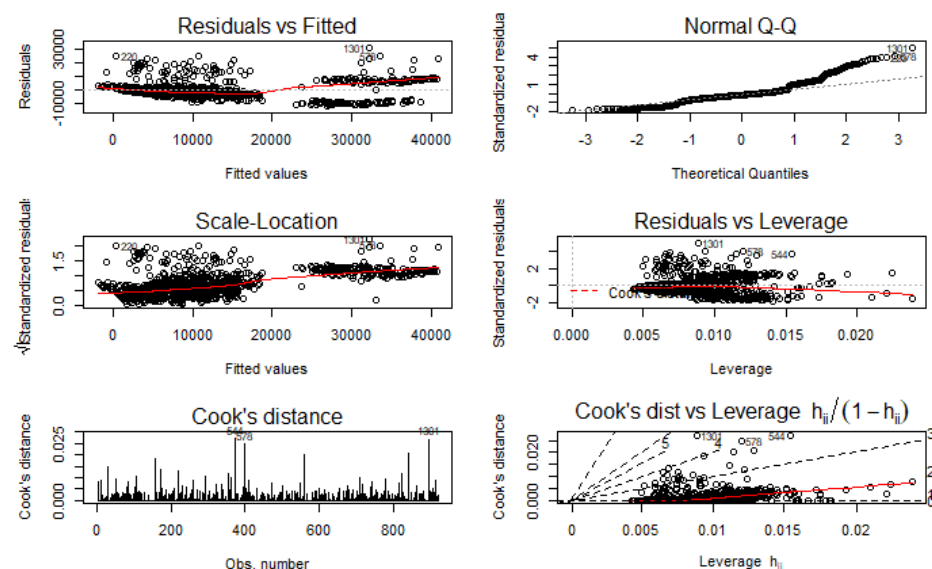
Yet again, There are no major differences noticed in the VIF score results, and all the values are closed to 1. Hence, it can be said that Multicollinearity is not present among the variables.

```
car::vif(bestmodel_fwd)
```

```
***
```

	GVIF	Df	GVIF <sup>1/(2*Df)</sup>
age	1.015301	1	1.007622
bmi	1.102430	1	1.049967
smoker	1.005959	1	1.002975
children	1.005435	1	1.002714
region	1.097810	3	1.015674

Residuals assumptions are applied to this model, and 6 graphs are plotted. It can be noticed that all the variables are independent with zero mean and are mostly normally distributed. Therefore, residuals assumptions are fulfilled.



With the 'Non-constant variance score test', the p-value is less than alpha 0.05, therefore the null hypothesis is rejected stating that the residuals variance is constant.

```
car::ncvTest(bestmodel_fwd)
```

```
...
```

```
Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 153.8316, Df = 1, p = < 2.22e-16
```

With p-value greater than 0.05, the null hypothesis is not rejected, confirming that NO autocorrelation is present in the model, by durbin Watson test for testing the autocorrelated errors.

```
durbinwatsonTest(bestmodel_fwd)
```

```
...
```

```
lag Autocorrelation D-w Statistic p-value
1 -0.0008177996 1.997969 0.942
Alternative hypothesis: rho != 0
```

Although by shapiro wilk normality test, the p-value is less than 0.05, hence rejecting the null hypothesis, which states that the data is normally distributed. Hence, for this model the data is not normally distributed.

```
shapiro.test(bestmodel_fwd$residuals)
```

```
...
```

```
shapiro-wilk normality test
data: bestmodel_fwd$residuals
W = 0.89578, p-value < 2.2e-16
```

## Prediction for Third model

The prediction for the second model is done by the same process. The statistics that came out from this prediction is-

	ME	RMSE	MAE	MPE	MAPE
Test set	102.2186	5665.428	4017.834	-14.77523	43.3282

## Results

---

The test assumptions for all the three models are almost the same for 'Non-constant variance score test', 'durbin Watson test', 'shapiro wilk normality test', residual analysis and VIF scores.

Hence, on this basis the best model can't be selected. Summary statistics will come into the picture now.

## Evaluating Interpretation

From the **summary statistics** for the three models, the 3 key evaluators are-

```
summary(bestmodel_anova)
...

Call:
lm(formula = train_health$charges ~ age + bmi + smoker, data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-12095   -3184   -1032    1515   29136

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -12037.77   1164.32   -10.34 <2e-16 ***
age           256.42    14.80     17.33 <2e-16 ***
bmi           338.80    34.05      9.95 <2e-16 ***
smokeryes    23670.40   509.11    46.49 <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6277 on 918 degrees of freedom
Multiple R-squared:  0.7389,    Adjusted R-squared:  0.738
F-statistic: 865.8 on 3 and 918 DF,  p-value: < 2.2e-16
```

```
summary(bestmodel_StepBack)
...

Call:
lm(formula = train_health$charges ~ age + bmi + smoker + children,
    data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-11588   -3122   -1026    1491   29616

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -12565.34   1180.38   -10.645 <2e-16 ***
age           255.28    14.76     17.292 <2e-16 ***
bmi           341.87    33.98     10.062 <2e-16 ***
smokeryes    23675.65   507.69    46.634 <2e-16 ***
children      421.95    170.06     2.481  0.0133 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6259 on 917 degrees of freedom
Multiple R-squared:  0.7406,    Adjusted R-squared:  0.7395
F-statistic: 654.6 on 4 and 917 DF,  p-value: < 2.2e-16
```

```
summary(bestmodel_fwd)
...

Call:
lm(formula = train_health$charges ~ age + bmi + smoker + children +
    region, data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-11165.7   -3111.7   -979.4    1507.6   30377.4

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -12546.15   1211.88   -10.353 < 2e-16 ***
age           254.74    14.73     17.294 < 2e-16 ***
bmi           369.25    35.32     10.454 < 2e-16 ***
smokeryes    23756.57   507.70    46.793 < 2e-16 ***
children      428.42    169.84     2.522  0.01182 *
regionnorthwest -638.41    592.12   -1.078  0.28124
regionsoutheast -1668.87    589.10   -2.833  0.00471 **
regionsouthwest -1030.88    598.17   -1.723  0.08516 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6241 on 914 degrees of freedom
Multiple R-squared:  0.743,    Adjusted R-squared:  0.741
F-statistic: 377.4 on 7 and 914 DF,  p-value: < 2.2e-16
```

**Residuals-** Residuals are actuals negatively predicted. The lowest the “max error”, the better it is. Among the three models, the lowest max errors are for ANOVA based model and Stepwise/Backward regression-based model, and those are 29136 and 29616, respectively. In other words, approximately \$29136 and \$29616 max errors are substantial, as per the model underprediction.

**p-value-** The smallest the p-value, the better relationship with the response variable “charges” and also the non-zero coefficient. The p-value is less than 0.05 for all the three models, according to the summary. But, the coefficients are the highest significant for ANOVA based best model and next for Stepwise/Backward regression-based model.

**Multiple R-squared value-** It explains the measurement of variation can be explained by the data. All the three models are having close to 74%, i.e., approximately 74% of the variance can be explained by the model. Hence, ANOVA based model can still be chosen according to this.

So, the results are narrowed down to two of the models that are better than the third, and those are, ANOVA based model and Stepwise/Backward regression-based model.

The **deciding factor** can be the **Root mean squared error (RMSE)** values that came from the prediction and accuracy results of the three models. The lowest the RMSE value the better the model is. The lowest RMSE value is noticed from the Stepwise/Backward regression-based model with 5628.947.

Hence, **Stepwise/Backward regression-based model**, i.e., **the second model** can be concluded as the best model among the three models. So, the best regressors/predictors are **age, bmi, smoker and children**.

The equation of best fit for the best model is-

$$y = -12565.34 + (255.28 * \text{age}) + (341.87 * \text{bmi}) + (23675.65 * \text{smokeryes}) + (421.95 * \text{children})$$



## Discussion

---

Based on the regression results, it can be well concluded that the insurance charges tends to be on the higher side if an individual is a smoker, whether is underweight, overweight or obese, and is directly proportional to the age, which means as age increases the insurance charges tend to increase as well. However, based on all the linear regression analysis techniques, it can be concluded that “smoker” has the most significance as compared to other predictors in determining insurance charges for an individual in the US.

## References

---

[1] Linear Regression — Detailed View

Towards Data Science. (2018). Linear Regression — Detailed View.

Available at: <https://towardsdatascience.com/linear-regression-detailed-view-ea73175f6e86>

## Appendix

---

# Regression Analysis-Final Project

Vamika Pardeshi-s3701024

June 5, 2019

## DATA IMPORT

Hide

```
setwd("C:\\Regression Analysis")
US_health <- read.csv("US_healthinsurance.csv")
head(US_health, n=10)
```

	age	sex	bmi	children	smoker	region	charges
	<int>	<fctr>	<dbl>	<int>	<fctr>	<fctr>	<dbl>
1	19	female	27.900	0	yes	southwest	16884.924
2	18	male	33.770	1	no	southeast	1725.552
3	28	male	33.000	3	no	southeast	4449.462
4	33	male	22.705	0	no	northwest	21984.471
5	32	male	28.880	0	no	northwest	3866.855
6	31	female	25.740	0	no	southeast	3756.622
7	46	female	33.440	1	no	southeast	8240.590
8	37	female	27.740	3	no	northwest	7281.506
9	37	male	29.830	2	no	northeast	6406.411
10	60	female	25.840	0	no	northwest	28923.137

1-10 of 10 rows

Hide

```
# checking the data size
dim(US_health)
```

[1] 1338 7

Hide

```
#checking the data structure
str(US_health)
```

```
'data.frame': 1338 obs. of 7 variables:
 $ age      : int 19 18 28 33 32 31 46 37 37 60 ...
 $ sex      : Factor w/ 2 levels "female","male": 1 2 2 2 2 1 1 1 2 1 ...
 $ bmi      : num 27.9 33.8 33 22.7 28.9 ...
 $ children: int 0 1 3 0 0 0 1 3 2 0 ...
 $ smoker   : Factor w/ 2 levels "no","yes": 2 1 1 1 1 1 1 1 1 1 ...
 $ region   : Factor w/ 4 levels "northeast","northwest",...: 4 3 3 2 2 3 3 2 1 2 ...
 $ charges  : num 16885 1726 4449 21984 3867 ...
```

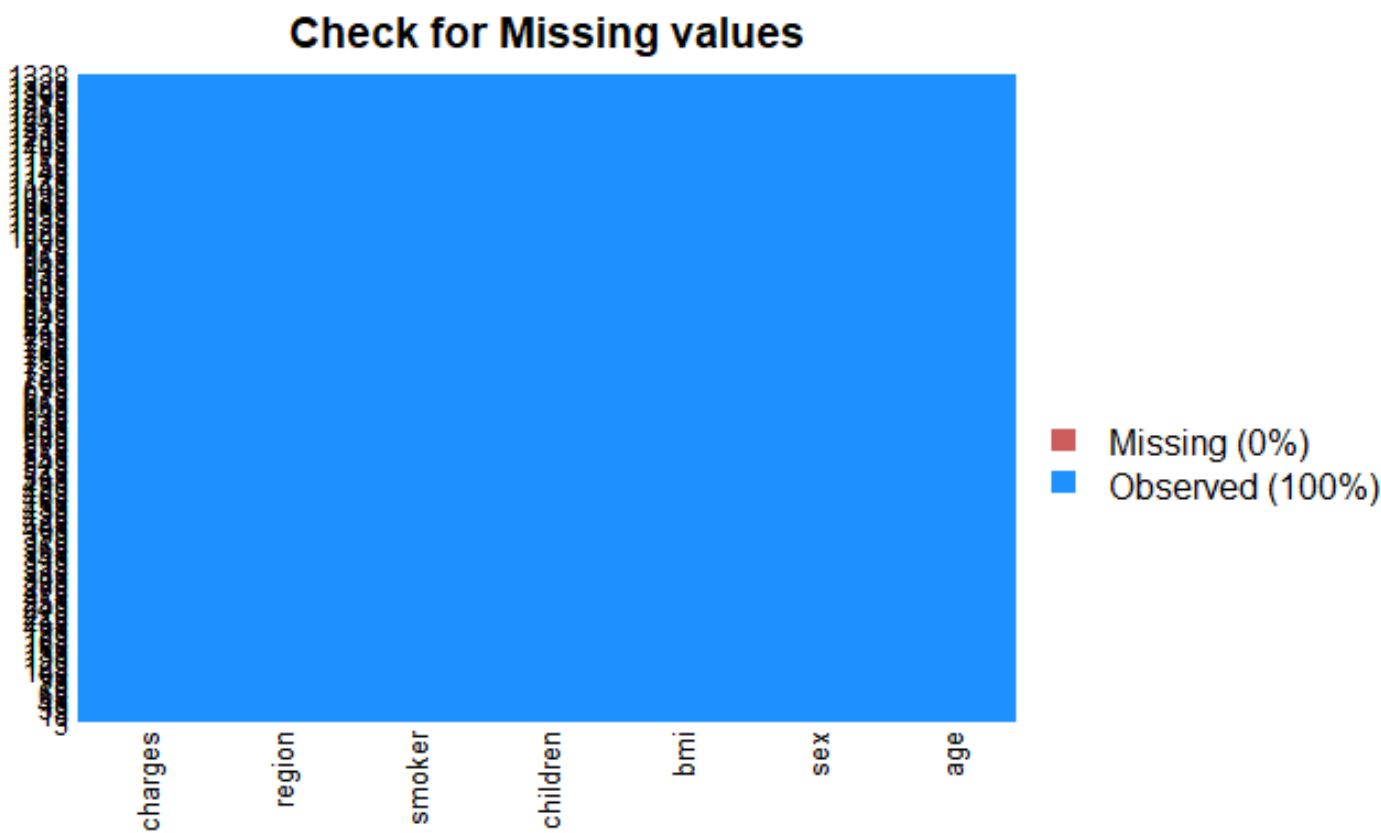
Hide

```
summary(US_health)
```

age	sex	bmi	children	smoker	region	charges
Min. :18.00	female:662	Min. :15.96	Min. :0.000	no :1064	northeast:324	Min. : 1122
1st Qu.:27.00	male :676	1st Qu.:26.30	1st Qu.:0.000	yes: 274	northwest:325	1st Qu.: 4740
Median :39.00		Median :30.40	Median :1.000		southeast:364	Median : 9382
Mean :39.21		Mean :30.66	Mean :1.095		southwest:325	Mean :13270
3rd Qu.:51.00		3rd Qu.:34.69	3rd Qu.:2.000			3rd Qu.:16640
Max. :64.00		Max. :53.13	Max. :5.000			Max. :63770

Hide

```
missmap(US_health, main = "Check for Missing values")
```



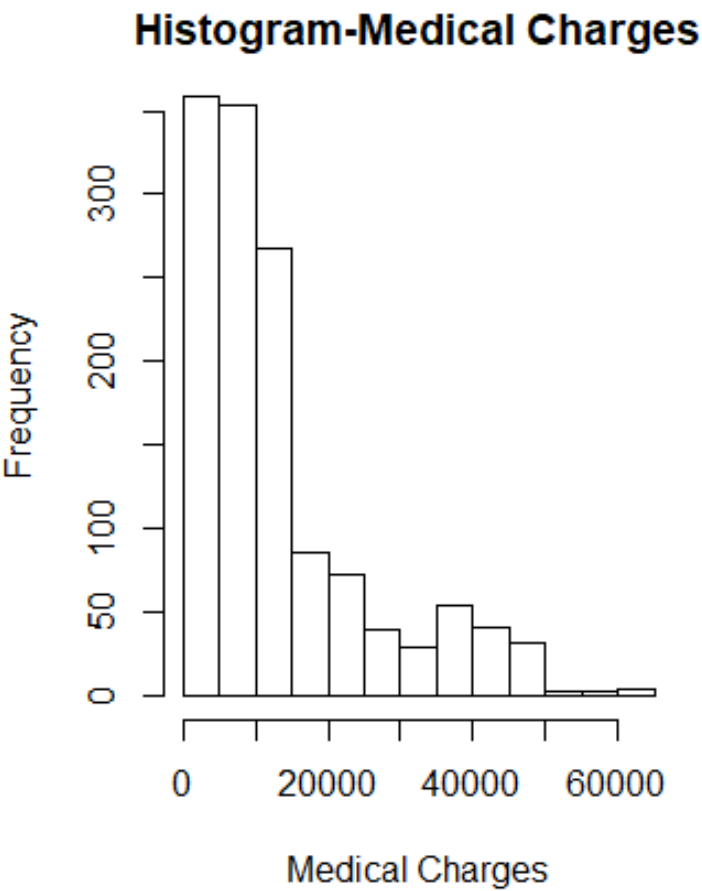
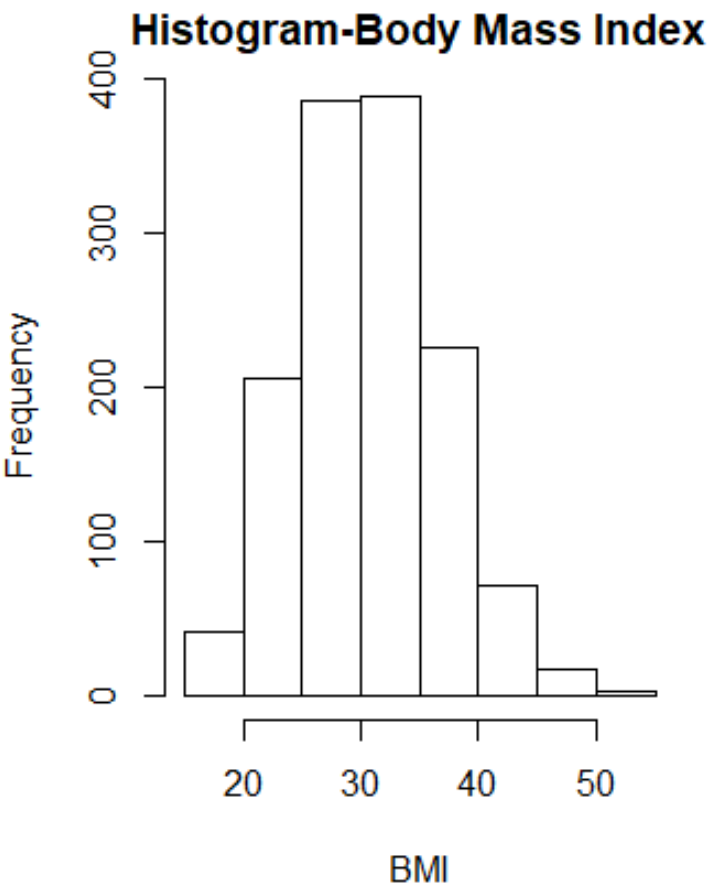
Hide

```
# checking for NA values
colSums(is.na(US_health))
```

age	sex	bmi	children	smoker	region	charges
0	0	0	0	0	0	0

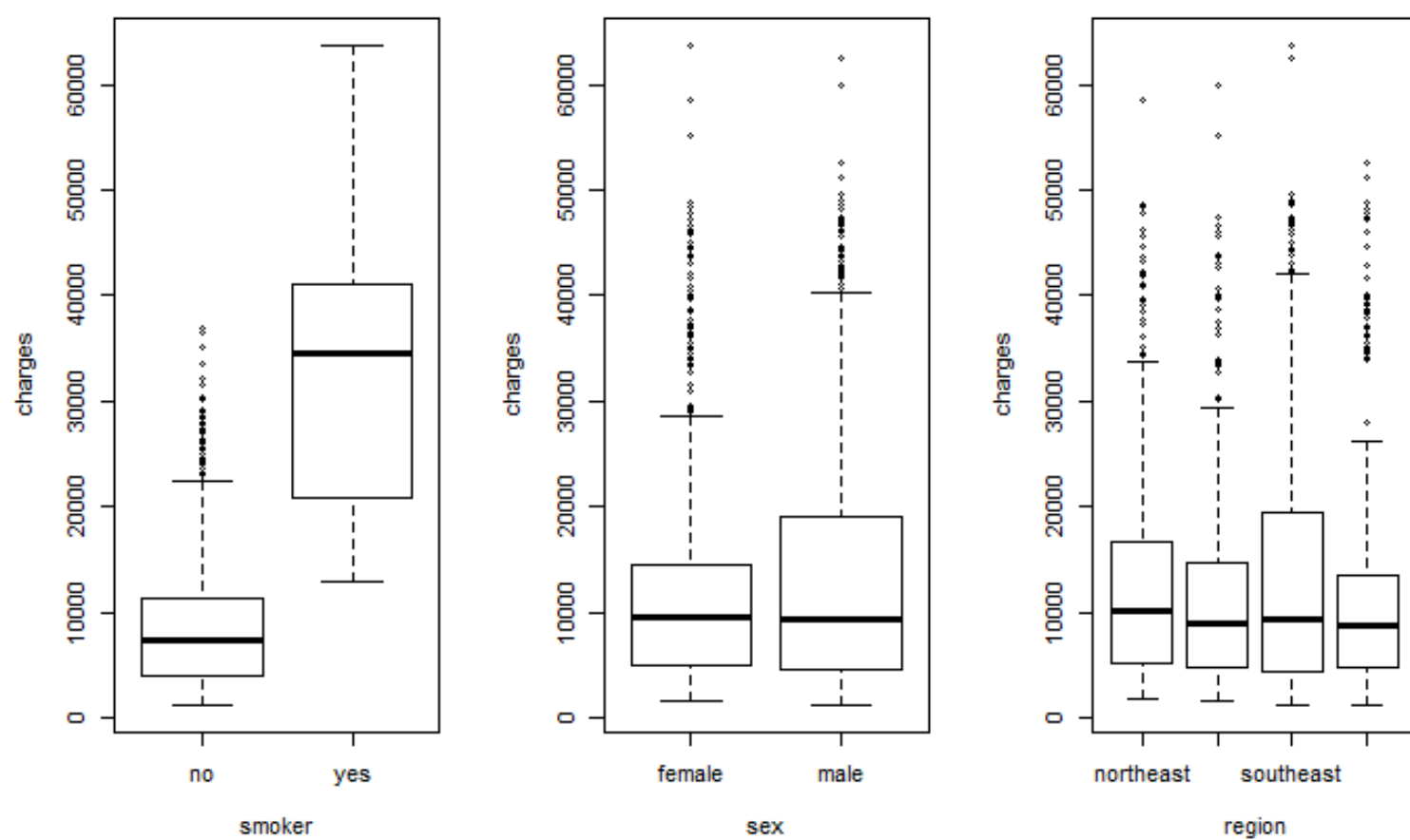
Hide

```
par(mfrow=c(1,2))
hist(US_health$bmi, xlab = "BMI",
     main = "Histogram-Body Mass Index")
hist(US_health$charges, xlab = "Medical Charges",
     main = "Histogram-Medical Charges")
```

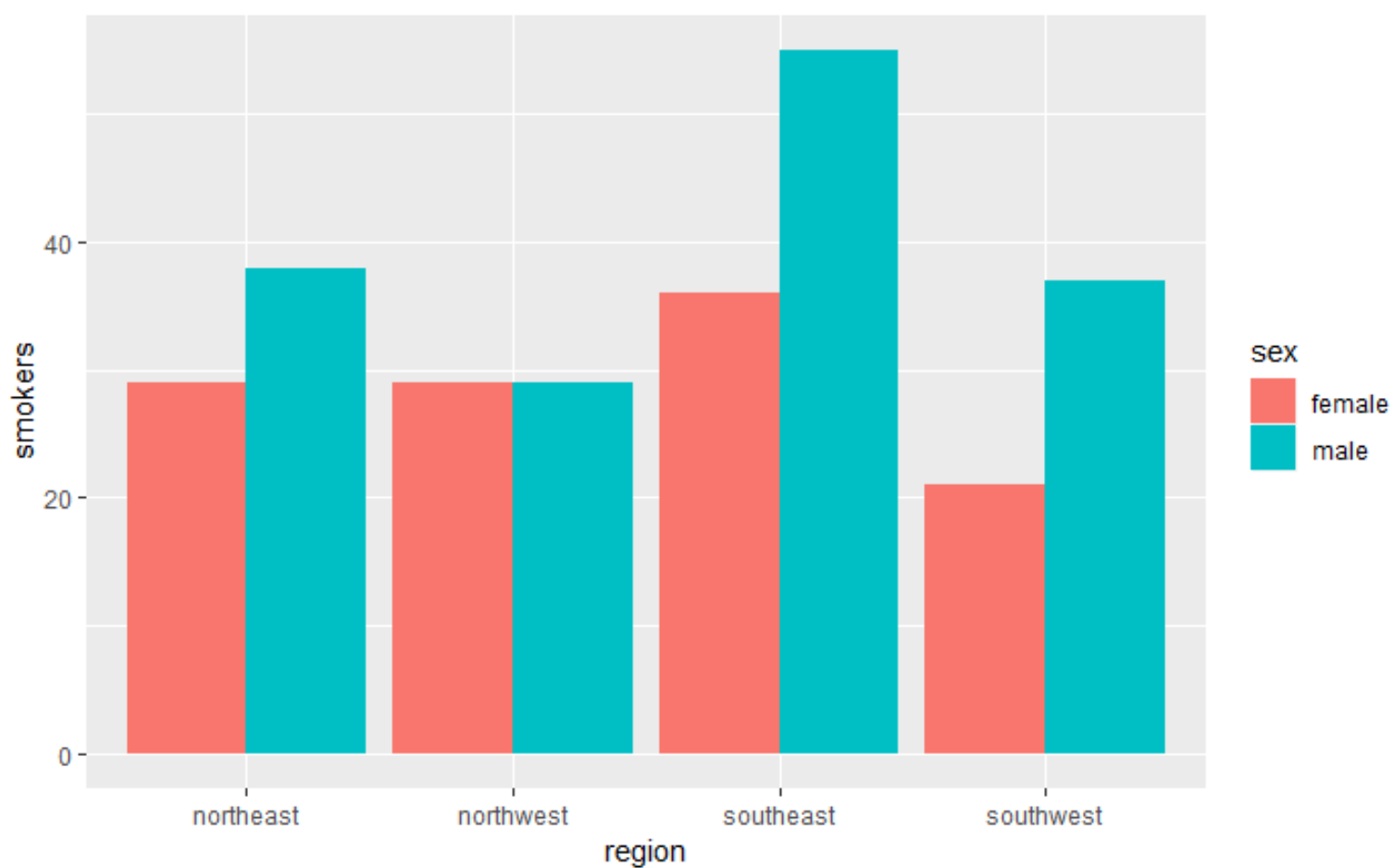


Hide

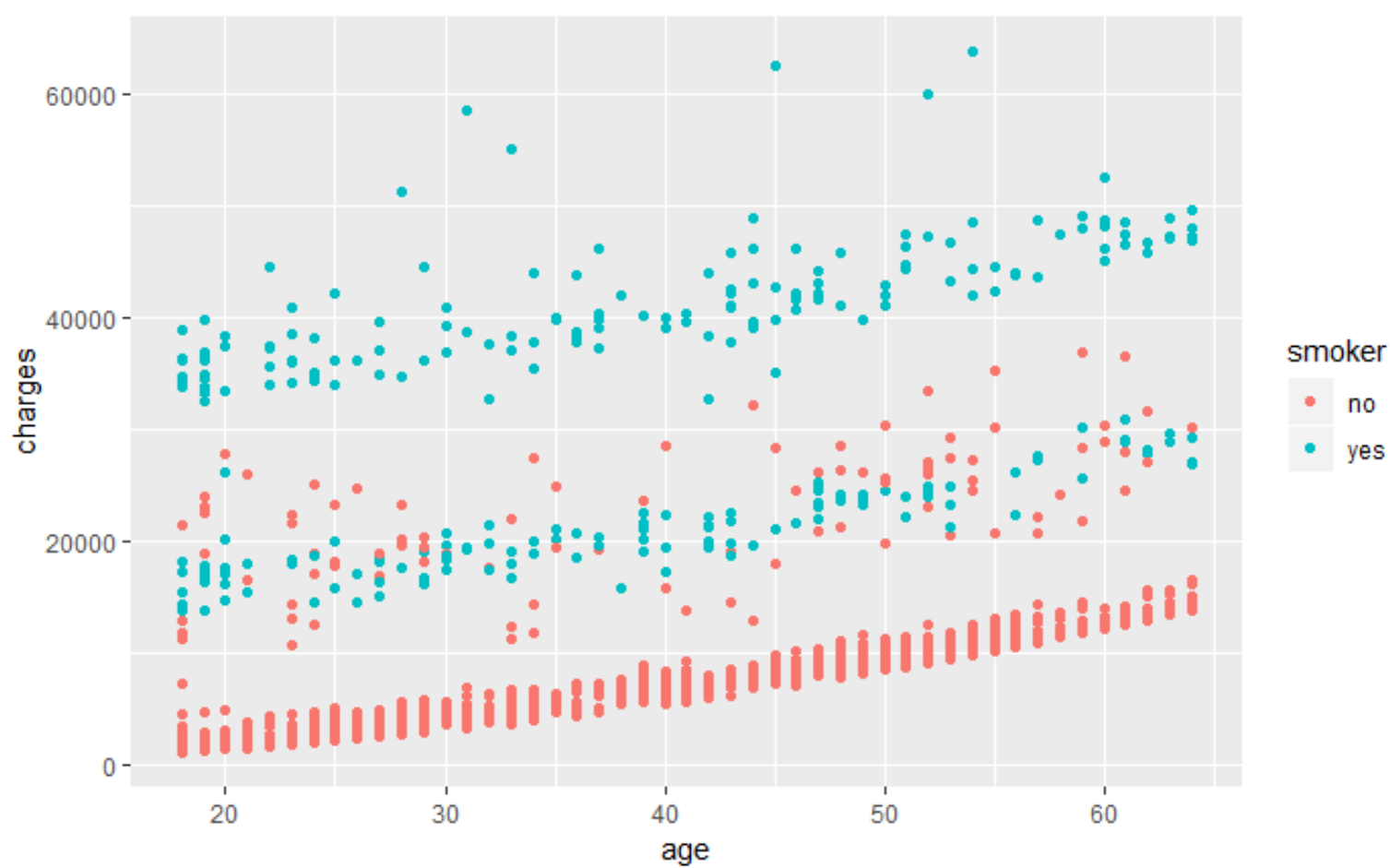
```
#plotting of charges against other factors like sex and smoker and region
par(mfrow=c(1,3))
with(US_health, plot(charges ~ smoker + sex + region))
```


[Hide](#)

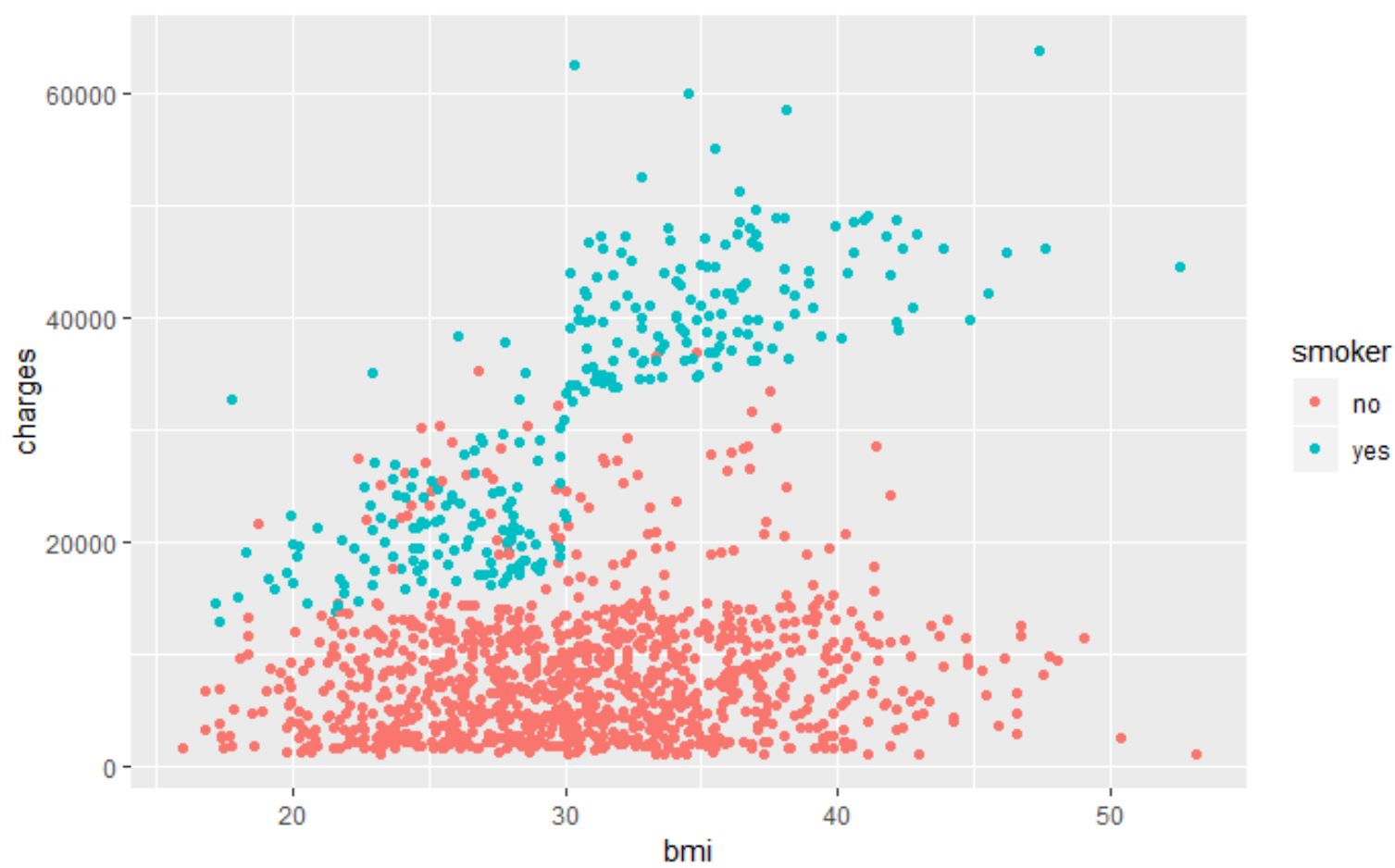
```
US_health %>% group_by(sex,region) %>% summarise(smokers=sum(smoker=="yes")) %>% ggplot(aes(x=region,y=smokers,fill=sex))+geom_bar(stat = "identity",position = "dodge")
```


[Hide](#)

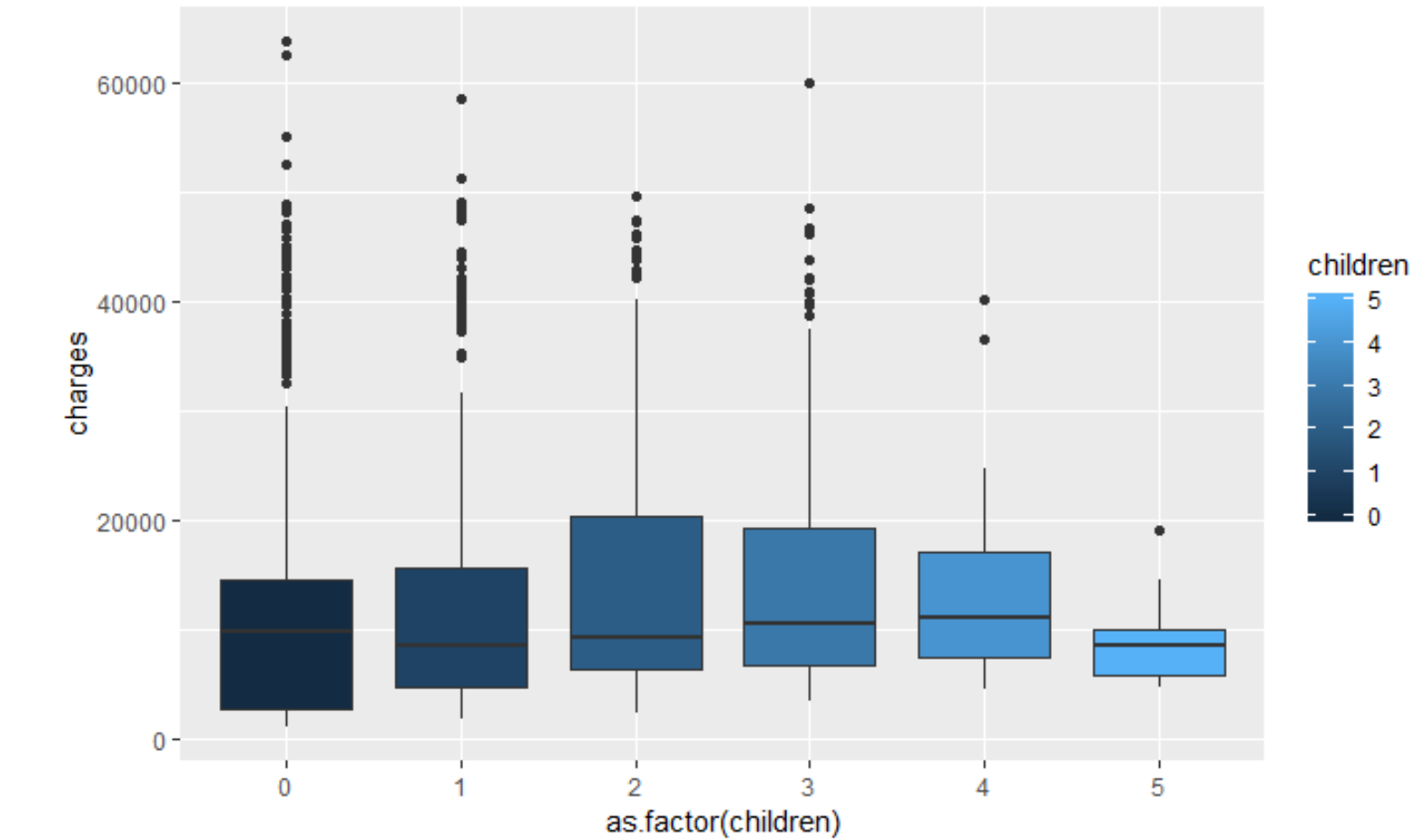
```
ggplot(US_health, aes(x = age, y = charges)) +  
  geom_point(aes(color = smoker))
```


[Hide](#)

```
ggplot(US_health, aes(x = bmi, y = charges)) +  
  geom_point(aes(color = smoker))
```


[Hide](#)

```
ggplot(data = US_health, aes(x=as.factor(children), y=charges))+geom_boxplot(aes(fill=children))
```



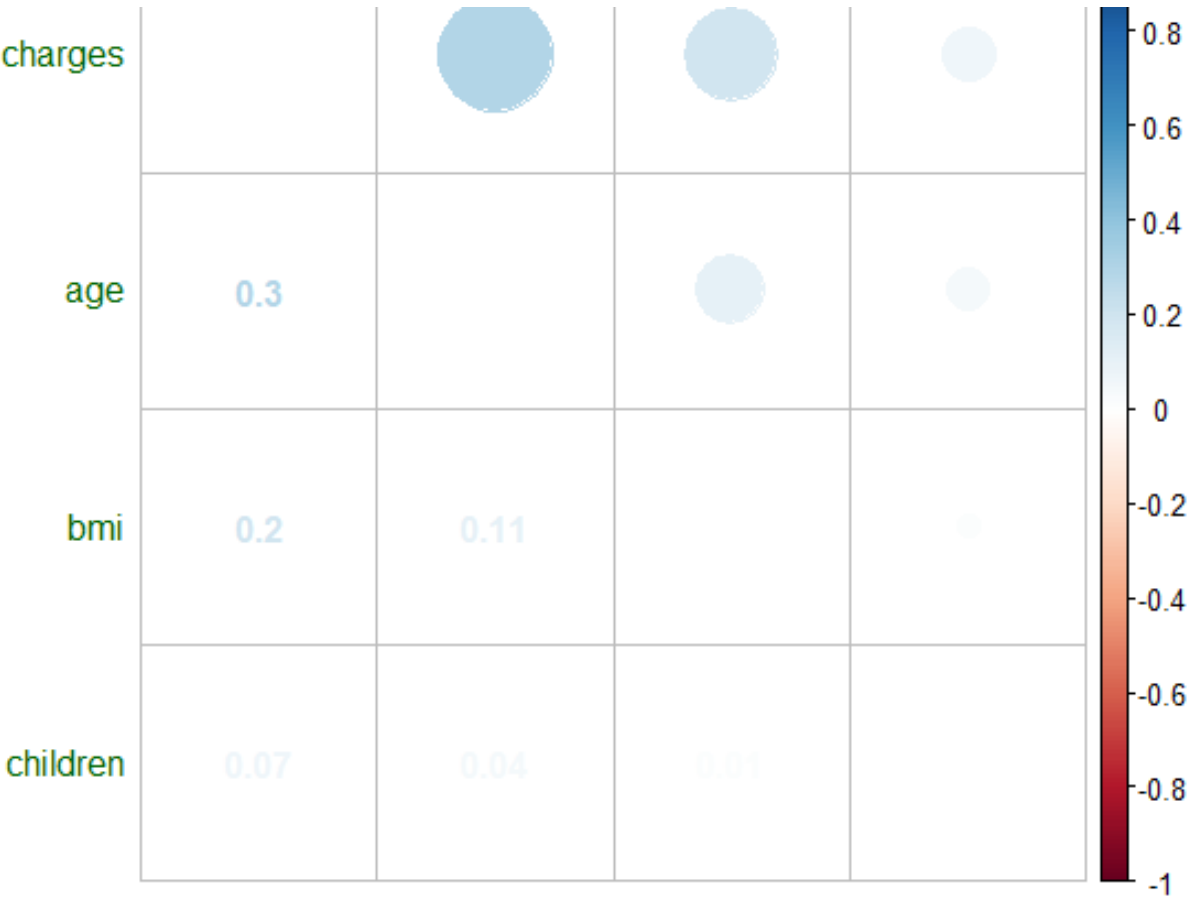
Hide

```
numeric_Var <- which(sapply(US_health, is.numeric)) #index vector numeric variables
numeric_VarNames <- names(numeric_Var) #saving names vector for use later on
cat('There are', length(numeric_Var), 'numeric variables')
```

There are 4 numeric variables

Hide

```
US_health_numVar <- US_health[, numeric_Var]
cor_health <- cor(US_health_numVar, use="pairwise.complete.obs") #correlations of all numeric variables
#sorting on decreasing correlations with SalePrice
cor_sorted_health <- as.matrix(sort(cor_health[, 'charges'], decreasing = TRUE))
#selecting only high corelations
Cor_High <- names(which(apply(cor_sorted_health, 1, function(x) abs(x)>0)))
cor_health <- cor_health[Cor_High, Cor_High]
corrplot.mixed(cor_health, tl.col="dark green", tl.pos = "lt")
```



- Conversions

Hide

```
US_health$age<-as.numeric(US_health$age)
US_health$children<-as.numeric(US_health$children)
US_health$sex<-as.factor(US_health$sex)
US_health$smoker<-as.factor(US_health$smoker)
US_health$region<-as.factor(US_health$region)
```

## Creating train and test data

Hide

```
set.seed(10)
Ind <- sample(2,nrow(US_health),replace= TRUE,prob=c(0.7,0.3))
train_health <- US_health[Ind==1,]
test_health <- US_health[Ind==2,]
```

## Linear, Ridge and Lasso Models

Hide

```
# Linear regression
lm_health <- lm(train_health$charges~., data =train_health)
```

Hide

```
summary(lm_health)
```

```
Call:
lm(formula = train_health$charges ~ ., data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-11090.8  -3115.8   -951.6   1525.4  30446.4

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  -12478.26    1223.49  -10.199  < 2e-16 ***
age             254.56      14.74   17.265  < 2e-16 ***
sexmale       -171.20     413.98   -0.414  0.67931
bmi            369.80      35.36   10.458  < 2e-16 ***
children       428.85     169.92    2.524  0.01178 *
smokeryes     23777.71     510.49  46.578  < 2e-16 ***
regionnorthwest  -633.69     592.50   -1.070  0.28512
regionsoutheast -1664.15     589.47   -2.823  0.00486 **
regionsouthwest -1027.20     598.50   -1.716  0.08645 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6244 on 913 degrees of freedom
Multiple R-squared:  0.743, Adjusted R-squared:  0.7408
F-statistic: 330 on 8 and 913 DF, p-value: < 2.2e-16
```

Hide

```
#making predictions
predict_lm <-predict(lm_health, test_health, type = "response")
residual <- test_health$charges - predict_lm
predict_linreg <- data.frame("Predicted"= predict_lm, "Actual" =test_health$charges, "Residuals" = residual)
accuracy(predict_lm, test_health$charges)
```

```
ME      RMSE      MAE      MPE      MAPE
Test set 104.9532 5665.485 4012.258 -14.62795 43.18357
```

Hide

```
x <- model.matrix(US_health$charges~., US_health)[,-1]
y <- US_health$charges
lambda_val <-10^seq(10, -2, length = 100)
```

Hide

```
set.seed(489)
train_new = sample(1:nrow(x), nrow(x)/2)
test_new = (-train_new)
y_test = y[test_new]
```

- Fitting the models

Hide

```
linear_RegModel <- lm(US_health$charges~., data= US_health)
coef(linear_RegModel)
```

(Intercept)	age	sexmale	bmi	children	smokeryes	regionnorthwest
-11938.5386	256.8564	-131.3144	339.1935	475.5005	23848.5345	-352.9639
regionsoutheast	regionsouthwest					
-1035.0220	-960.0510					

Hide

```
# Ridge model
ridge_model <- glmnet(x, y, alpha = 0, lambda = lambda_val)
coef(ridge_model)
```

9 x 100 sparse Matrix of class "dgCMatrix"

```
[[ suppressing 100 column names <U+393C><U+3E31>s0<U+393C><U+3E32>, <U+393C><U+3E31>s1<U+393C><U+3E32>, <U+393C><U+3E31>s
2<U+393C><U+3E32> ... ]]
```



(Intercept)	1.327039e+04	1.327038e+04	1.327036e+04	1.327034e+04	1.327032e+04	1.327028e+04
age	3.119854e-04	4.124261e-04	5.452028e-04	7.207255e-04	9.527558e-04	1.259486e-03
sexmale	1.679238e-03	2.219849e-03	2.934507e-03	3.879241e-03	5.128119e-03	6.779057e-03
bmi	4.768017e-04	6.303034e-04	8.332235e-04	1.101471e-03	1.456079e-03	1.924847e-03
children	8.269116e-04	1.093128e-03	1.445050e-03	1.910269e-03	2.525260e-03	3.338241e-03
smokeryes	2.858823e-02	3.779195e-02	4.995871e-02	6.604242e-02	8.730412e-02	1.154108e-01
regionnorthwest	-1.363637e-03	-1.802645e-03	-2.382988e-03	-3.150164e-03	-4.164321e-03	-5.504971e-03
regionsoutheast	2.436197e-03	3.220505e-03	4.257312e-03	5.627906e-03	7.439742e-03	9.834869e-03
regionsouthwest	-1.476582e-03	-1.951953e-03	-2.580365e-03	-3.411086e-03	-4.509248e-03	-5.960947e-03

(Intercept)	1.327024e+04	1.327018e+04	1.327010e+04	1.327000e+04	1.326986e+04	1.326968e+04
age	1.664963e-03	2.200979e-03	2.909556e-03	3.846248e-03	5.084489e-03	6.721352e-03
sexmale	8.961489e-03	1.184652e-02	1.566032e-02	2.070188e-02	2.736642e-02	3.617638e-02
bmi	2.544530e-03	3.363710e-03	4.446610e-03	5.878130e-03	7.770493e-03	1.027205e-02
children	4.412949e-03	5.833643e-03	7.711707e-03	1.019438e-02	1.347628e-02	1.781471e-02
smokeryes	1.525660e-01	2.016829e-01	2.666121e-01	3.524443e-01	4.659083e-01	6.158994e-01
regionnorthwest	-7.277217e-03	-9.620001e-03	-1.271698e-02	-1.681095e-02	-2.222280e-02	-2.937675e-02
regionsoutheast	1.300106e-02	1.718654e-02	2.271942e-02	3.003344e-02	3.970192e-02	5.248269e-02
regionsouthwest	-7.879997e-03	-1.041685e-02	-1.377039e-02	-1.820352e-02	-2.406377e-02	-3.181050e-02

(Intercept)	1.326944e+04	1.326913e+04	1.326871e+04	1.326816e+04	1.326743e+04	1.326646e+04
age	8.885157e-03	1.174552e-02	1.552666e-02	2.052493e-02	2.713205e-02	3.586576e-02
sexmale	4.782230e-02	6.321697e-02	8.356685e-02	1.104665e-01	1.460233e-01	1.930222e-01
bmi	1.357890e-02	1.795025e-02	2.372872e-02	3.136719e-02	4.146421e-02	5.481084e-02
children	2.354975e-02	3.113094e-02	4.115251e-02	5.439986e-02	7.191108e-02	9.505814e-02
smokeryes	8.141759e-01	1.076281e+00	1.422759e+00	1.880767e+00	2.486199e+00	3.286496e+00
regionnorthwest	-3.883349e-02	-5.133410e-02	-6.785807e-02	-8.969984e-02	-1.185700e-01	-1.567287e-01
regionsoutheast	6.937743e-02	9.171010e-02	1.212305e-01	1.602511e-01	2.118276e-01	2.799976e-01
regionsouthwest	-4.205094e-02	-5.558769e-02	-7.348161e-02	-9.713478e-02	-1.284002e-01	-1.697266e-01

(Intercept)	1.326519e+04	1.326351e+04	1.326128e+04	13258.3379786	13254.4500899	13249.3124272
age	4.741028e-02	6.266987e-02	8.283935e-02	0.1094973	0.1447291	0.1912886
sexmale	2.551428e-01	3.372470e-01	4.457563e-01	0.5891511	0.7786265	1.0289552
bmi	7.245252e-02	9.577065e-02	1.265904e-01	0.1673227	0.2211517	0.2922813
children	1.256541e-01	1.660949e-01	2.195460e-01	0.2901889	0.3835463	0.5069097
smokeryes	4.344359e+00	5.742645e+00	7.590841e+00	10.0336014	13.2620066	17.5284060
regionnorthwest	-2.071620e-01	-2.738137e-01	-3.618918e-01	-0.4782708	-0.6320206	-0.8351008
regionsoutheast	3.700950e-01	4.891645e-01	6.465081e-01	0.8544036	1.1290484	1.4917971
regionsouthwest	-2.243495e-01	-2.965434e-01	-3.919547e-01	-0.5180392	-0.6846394	-0.9047424

(Intercept)	13242.5240529	13233.5560069	13221.7129155	13206.0734859	13185.4304440	13158.196213	13122.289322
age	0.2528115	0.3340958	0.4414681	0.5832707	0.7704837	1.017547	1.343416
sexmale	1.3596187	1.7962890	2.3715131	3.1312837	4.1328904	5.452140	7.187735
bmi	0.3862596	0.5104046	0.6743201	0.8907604	1.1763970	1.553147	2.049720
children	0.6699023	0.8852177	1.1695710	1.5450189	2.0405305	2.694159	3.555764
smokeryes	23.1659554	30.6143089	40.4531668	53.4469986	70.6019409	93.241167	123.101644
regionnorthwest	-1.1032674	-1.4572559	-1.9240799	-2.5397732	-3.3508992	-4.418316	-5.820966
regionsoutheast	1.9707785	2.6030020	3.4367976	4.5362694	5.9845223	7.890007	10.393270
regionsouthwest	-1.1954737	-1.5793987	-2.0862193	-2.7549756	-3.6368880	-4.798992	-6.328738

(Intercept)	13074.988008	13012.745783	12930.963093	12823.711554	12683.412902	12500.485945	12262.994539
age	1.772919	2.338475	3.082253	4.058811	5.338241	7.009754	9.185478
sexmale	9.467545	12.456108	16.363231	21.453138	28.052937	36.557977	47.429828
bmi	2.703607	3.563578	4.692744	6.172210	8.105248	10.621757	13.882457
children	4.690487	6.183110	8.143420	10.712612	14.070635	18.444032	24.113304
smokeryes	162.458395	214.282252	282.437288	371.922933	489.162336	642.330915	841.704835
regionnorthwest	-7.660598	-10.067258	-13.205239	-17.278848	-22.536601	-29.271435	-37.812943
regionsoutheast	13.675247	17.966780	23.558774	30.811639	40.161279	52.116799	67.241940
regionsouthwest	-8.339713	-10.978607	-14.433408	-18.942552	-24.804288	-32.384688	-42.121533

(Intercept)	11956.36133	11563.25834	11063.84443	10436.58011	9659.88054	8714.82196	7588.87936	6280.36190
age	12.00398	15.63261	20.26717	26.12676	33.44096	42.42645	53.25166	65.99073
sexmale	61.18000	78.32937	99.33034	124.43852	153.52734	185.85694	219.85020	252.96212
bmi	18.08186	23.44839	30.23933	38.72771	49.17820	61.81036	76.75172	93.98643
children	31.41794	40.75598	52.57336	67.33678	85.48304	107.34055	133.02488	162.32629
smokeryes	1099.98485	1432.51321	1857.24840	2394.29966	3064.76806	3888.63531	4881.55493	6050.69209
regionnorthwest	-48.50575	-61.66639	-77.51055	-96.04658	-116.94202	-139.39357	-162.05491	-183.11601
regionsoutheast	86.10821	109.20348	136.77757	168.61107	203.71191	239.98326	273.96817	300.83254
regionsouthwest	-54.51960	-70.13100	-89.51275	-113.15484	-141.37747	-174.21011	-211.28585	-251.80762

(Intercept)	4802.54248	3186.12989	1478.6367	-260.0970	-1965.6512	-3578.10842	-5049.9191	-6350.5215
age	80.57454	96.75251	114.0831	131.9667	149.7213	166.68272	182.3005	196.2001
sexmale	281.78433	302.48564	311.5830	306.8431	287.9656	256.72668	216.5038	171.3997
bmi	113.31386	134.33142	156.4539	178.9706	201.1302	222.23197	241.7037	259.1504

children	194.62222	228.86208	263.6618	297.5080	329.0177	357.16348	381.3889	401.5927
smokeryes	7390.27714	8878.11422	10474.6259	12125.6745	13769.2223	15344.30308	16799.6853	18099.7508
regionnorthwest	-200.59470	-212.84374	-219.1324	-220.0468	-217.4614	-214.02250	-212.3444	-214.2764
regionsoutheast	314.76429	309.86710	281.4145	227.0899	147.7435	47.35415	-67.7787	-190.2895
regionsouthwest	-294.64493	-338.58342	-382.6653	-426.4698	-470.1649	-514.26261	-559.1882	-604.8915
(Intercept)	-7466.7598	-8401.41371	-9167.47509	-9784.484455	-10274.86693	-10659.65076	-10959.15937	
age	208.1990	218.29113	226.59309	233.299398	238.64038	242.84061	246.11513	
sexmale	125.3218	81.41197	41.70534	7.235238	-21.73044	-45.51947	-64.67286	
bmi	274.3772	287.33732	298.14103	306.984003	314.09328	319.76338	324.22789	
children	418.0355	431.13606	441.43086	449.436892	455.59573	460.34268	463.97570	
smokeryes	19226.3817	20177.32061	20962.21848	21598.183619	22105.79019	22506.07587	22818.74744	
regionnorthwest	-221.4758	-231.93110	-245.15889	-259.759219	-273.03313	-286.89587	-299.37951	
regionsoutheast	-313.6773	-430.85248	-537.91813	-632.333475	-712.06061	-779.55490	-834.83818	
regionsouthwest	-651.1356	-696.03828	-738.51354	-777.352941	-810.94950	-840.51147	-865.34297	
(Intercept)	-11190.71705	-11368.80675	-11505.2282	-11609.7400	-11689.0845	-11749.4027	-11795.2145	
age	248.64992	250.60136	252.0974	253.2430	254.1142	254.7769	255.2804	
sexmale	-79.86839	-91.78835	-101.0581	-108.1978	-113.7048	-117.9232	-121.1441	
bmi	327.71268	330.41397	332.4964	334.0786	335.3032	336.2391	336.9520	
children	466.74827	468.85984	470.4655	471.6675	472.5949	473.2997	473.8342	
smokeryes	23061.16918	23248.04042	23391.4488	23501.1325	23584.7922	23648.4783	23696.8861	
regionnorthwest	-310.15567	-319.17689	-326.5525	-331.2598	-336.0847	-339.9782	-343.0190	
regionsoutheast	-879.34796	-914.70014	-942.4755	-963.1377	-979.9854	-993.0471	-1003.0750	
regionsouthwest	-885.74495	-902.21370	-915.3187	-924.9009	-933.0189	-939.3750	-944.2809	
(Intercept)	-11829.9759	-11856.3328	-11876.3059	-11891.4349	-11902.8910	-11911.6778	-11918.2301	-11923.1768
age	255.6625	255.9522	256.1719	256.3382	256.4642	256.5612	256.6331	256.6875
sexmale	-123.5978	-125.4637	-126.8809	-127.9562	-128.7715	-129.3659	-129.8386	-130.1973
bmi	337.4941	337.9058	338.2181	338.4549	338.6344	338.7666	338.8696	338.9482
children	474.2391	474.5458	474.7780	474.9538	475.0869	475.1834	475.2598	475.3182
smokeryes	23733.6381	23761.5163	23782.6492	23798.6608	23810.7874	23819.9703	23826.9207	23832.1809
regionnorthwest	-345.3705	-347.1790	-348.5643	-349.6221	-350.4281	-350.7814	-351.2510	-351.6529
regionsoutheast	-1010.7430	-1016.5910	-1021.0422	-1024.4253	-1026.9936	-1028.7303	-1030.2104	-1031.3687
regionsouthwest	-948.0466	-950.9268	-953.1239	-954.7965	-956.0678	-956.8744	-957.6090	-958.1937
(Intercept)	-11926.9172	-11929.7467	-11931.8874	-11933.5069	-11934.7321	-11935.6591	-11936.3603	-11936.8907
age	256.7286	256.7597	256.7832	256.8010	256.8145	256.8247	256.8324	256.8382
sexmale	-130.4690	-130.6747	-130.8304	-130.9482	-131.0373	-131.1048	-131.1558	-131.1944
bmi	339.0078	339.0530	339.0872	339.1131	339.1326	339.1474	339.1586	339.1671
children	475.3625	475.3961	475.4216	475.4408	475.4553	475.4663	475.4747	475.4810
smokeryes	23836.1615	23839.1736	23841.4527	23843.1770	23844.4815	23845.4684	23846.2151	23846.7799
regionnorthwest	-351.9680	-352.2092	-352.3924	-352.5313	-352.6365	-352.7162	-352.7765	-352.8221
regionsoutheast	-1032.2543	-1032.9269	-1033.4365	-1033.8223	-1034.1143	-1034.3353	-1034.5025	-1034.6290
regionsouthwest	-958.6431	-958.9849	-959.2440	-959.4403	-959.5889	-959.7014	-959.7865	-959.8509
(Intercept)	-11937.2920	-11937.5956	-11937.8252	-11937.9990	-11938.1304	-11938.2298	-11938.3050	-11938.3619
age	256.8426	256.8460	256.8485	256.8504	256.8519	256.8530	256.8538	256.8544
sexmale	-131.2236	-131.2457	-131.2624	-131.2751	-131.2846	-131.2919	-131.2974	-131.3015
bmi	339.1735	339.1784	339.1821	339.1848	339.1869	339.1885	339.1897	339.1906
children	475.4857	475.4893	475.4921	475.4941	475.4957	475.4969	475.4978	475.4984
smokeryes	23847.2072	23847.5304	23847.7750	23847.9600	23848.0999	23848.2057	23848.2858	23848.3464
regionnorthwest	-352.8566	-352.8827	-352.9025	-352.9174	-352.9288	-352.9373	-352.9438	-352.9487
regionsoutheast	-1034.7247	-1034.7971	-1034.8519	-1034.8933	-1034.9247	-1034.9484	-1034.9663	-1034.9799
regionsouthwest	-959.8996	-959.9365	-959.9643	-959.9854	-960.0014	-960.0135	-960.0226	-960.0295
(Intercept)	-11938.4049	-11938.4375	-11938.4621	-11938.4807	-11938.4948	-11938.5055	-11938.5135	-11938.5196
age	256.8549	256.8552	256.8555	256.8557	256.8559	256.8560	256.8561	256.8561
sexmale	-131.3046	-131.3070	-131.3088	-131.3101	-131.3112	-131.3119	-131.3125	-131.3130
bmi	339.1913	339.1918	339.1922	339.1925	339.1928	339.1929	339.1931	339.1932
children	475.4990	475.4993	475.4996	475.4999	475.5000	475.5002	475.5002	475.5003
smokeryes	23848.3922	23848.4269	23848.4531	23848.4729	23848.4879	23848.4993	23848.5079	23848.5144
regionnorthwest	-352.9524	-352.9552	-352.9573	-352.9589	-352.9601	-352.9610	-352.9617	-352.9623
regionsoutheast	-1034.9902	-1034.9979	-1035.0038	-1035.0082	-1035.0116	-1035.0141	-1035.0161	-1035.0175
regionsouthwest	-960.0348	-960.0387	-960.0417	-960.0440	-960.0457	-960.0470	-960.0479	-960.0487

- Here, the differences came out to be nominal. Hence, using ridge in order to check whether it can improve the OLS estimation.

[Hide](#)

```
# Creating linear and ridge models based on x and y train/test split
linear_RegModel <- lm(US_health$charges~., data = US_health, subset = train_new)
ridge_model <- glmnet(x[train_new,], y[train_new], alpha = 0, lambda = lambda_val)
#Finding out best lambda value from the list via cross-validation.
CV_out <- cv.glmnet(x[train_new,], y[train_new], alpha =0)
lambda_best <- CV_out$lambda.min
```

Hide

```
# Making predictions based on best lambda
# Linear model prediction
lm_predict <- predict(linear_RegModel, newdata = US_health[test_new,])
# Ridge model prediction
ridge_predict <- predict(ridge_model, s= lambda_best, newx = x[test_new,])
```

Hide

```
# looking for coefficients
out_ridge <-glmnet(x[train_new,], y[train_new], alpha = 0)
predict(ridge_model, type = "coefficients", s= lambda_best)[1:6,]
```

(Intercept)	age	sexmale	bmi	children	smokeryes
-9585.4564	216.4560	584.9393	318.8245	492.4345	20305.3594

- MMost of the coefficients estimates are coming out to be conservative.
- So, trying to fit lasso as it takes absolute values for coefficients estimates.

Hide

```
#Lasso Model
lasso_model <- glmnet(x[train_new,],y[train_new], alpha = 1, lambda = lambda_val)
lasso_predict <- predict(lasso_model, s= lambda_best, newx = x[test_new,])
```

Hide

```
lasso_coef <- predict(lasso_model, type= "coefficients", s= lambda_best)[1:6]
lasso_coef
```

```
[1] -3651.569    171.284      0.000    190.056      0.000 19538.071
```

- As expected, lasso set the value to 0 for unimportant variables and set the values high for the important ones, i.e., age, bmi, smoker. So, lasso model can be chosen. Let's, confirm it with MSE values.

## Selection of best model among linear, ridge and lasso

Hide

```
#Checking MSE for linear model
mean((lm_predict-y_test)^2)
```

```
[1] 36825120
```

Hide

```
#Checking MSE for ridge model
mean((ridge_predict-y_test)^2)
```

```
[1] 39616462
```

Hide

```
#Checking MSE for Lasso Model
mean((lasso_predict-y_test)^2)
```

```
[1] 43500867
```

- Since, linear regression model has the least MSE, therefore, it is the best model among the three models.

# SELECTION OF BEST PREDICTORS BASED ON LINEAR REGRESSION MODEL

Hide

```
summary(linear_RegModel)
```

```
Call:
lm(formula = US_health$charges ~ ., data = US_health, subset = train_new)

Residuals:
    Min       1Q   Median       3Q      Max
-9872  -3015  -1107   1305  31561

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  -11544.86   1416.98  -8.148 1.86e-15 ***
age             236.65     17.42  13.584 < 2e-16 ***
sexmale        477.06     483.77   0.986  0.3244
bmi            354.18     41.79   8.476 < 2e-16 ***
children       500.36     201.48   2.483  0.0133 *
smokeryes     22107.37    583.83  37.866 < 2e-16 ***
regionnorthwest -1101.03    688.29  -1.600  0.1102
regionsoutheast -1409.71    686.01  -2.055  0.0403 *
regionsouthwest -1363.39    686.14  -1.987  0.0473 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6190 on 660 degrees of freedom
Multiple R-squared:  0.7154,    Adjusted R-squared:  0.7119
F-statistic: 207.4 on 8 and 660 DF,  p-value: < 2.2e-16
```

- From the above summary(), the equation came out to be:
- $y = -11544.86 + (236.65age) + (477.06sexmale) + (354.18bmi) + (500.36children) + (22107.37smokeryes) - (1101.03regionnorthwest) - (1409.71regionsoutheast) - (1363.39regionsouthwest)$

## Anova

Hide

```
Anova(linear_RegModel)
```

```
Anova Table (Type II tests)

Response: US_health$charges
              Sum Sq Df  F value  Pr(>F)
age          7.0698e+09  1  184.5342 < 2e-16 ***
sex           3.7256e+07  1    0.9724 0.32443
bmi           2.7522e+09  1   71.8364 < 2e-16 ***
children      2.3629e+08  1    6.1675 0.01326 *
smoker        5.4934e+10  1 1433.8560 < 2e-16 ***
region        2.1251e+08  3    1.8489 0.13698
Residuals    2.5286e+10 660
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

## All possible subset regression

Hide

```
All_subset <- lm(linear_RegModel, data = US_health)
ols_step_best_subset(All_subset)
```

Best Subsets Regression									
Model	Index	Predictors							
	1	smoker							
	2	age smoker							
	3	age bmi smoker							
	4	age bmi children smoker							
	5	age bmi children smoker region							
	6	age sex bmi children smoker region							
Subsets Regression Summary									
Model	R-Square	Adj. R-Square	Pred R-Square	C(p)	AIC	SBIC	SBC	MSEP	FPE
HSP	APC								
1	0.6198	0.6195	0.618	611.9889	27667.4636	23868.9391	27683.0604	55887669.4102	5588754
4.4451	41800.8466	0.3814							
2	0.7214	0.7210	0.7196	93.8304	27253.3244	23455.8677	27274.1201	41010413.6993	4101018
4.4505	30673.4926	0.2799							
3	0.7475	0.7469	0.7455	-37.6245	27123.8359	23327.0363	27149.8306	37227691.7503	3722731
7.1643	27844.2284	0.2540							
4	0.7497	0.7489	0.7474	-46.9727	27114.0352	23317.3965	27145.2288	36956206.6446	3695562
8.2045	27641.1727	0.2522							
5	0.7509	0.7496	0.7475	-51.0596	27113.6624	23313.1716	27160.4528	36891265.6918	3689044
0.8009	27592.6006	0.2514							
6	0.7509	0.7494	0.7471	-49.2088	27115.5058	23315.1156	27167.4951	36942459.0871	3694134
3.9390	27630.8903	0.2517							
AIC: Akaike Information Criteria									
SBIC: Sawa's Bayesian Information Criteria									
SBC: Schwarz Bayesian Criteria									
MSEP: Estimated error of prediction, assuming multivariate normality									
FPE: Final Prediction Error									
HSP: Hocking's Sp									
APC: Amemiya Prediction Criteria									

## Forward Regression

Hide

```
Model_ForwardReg <- step(linear_RegModel , direction = "forward")
```

```
Start:  AIC=11690.53
US_health$charges ~ age + sex + bmi + children + smoker + region
```

Hide

```
summary(Model_ForwardReg)
```

```
Call:
lm(formula = US_health$charges ~ age + sex + bmi + children +
    smoker + region, data = US_health, subset = train_new)

Residuals:
    Min       1Q   Median       3Q      Max
-9872  -3015  -1107   1305  31561

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)   -11544.86    1416.98  -8.148 1.86e-15 ***
age             236.65      17.42   13.584 < 2e-16 ***
sexmale        477.06      483.77    0.986  0.3244
bmi            354.18      41.79    8.476 < 2e-16 ***
children       500.36     201.48    2.483  0.0133 *
smokeryes     22107.37     583.83   37.866 < 2e-16 ***
regionnorthwest -1101.03     688.29  -1.600  0.1102
regionsoutheast -1409.71     686.01  -2.055  0.0403 *
regionsouthwest -1363.39     686.14  -1.987  0.0473 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6190 on 660 degrees of freedom
Multiple R-squared:  0.7154,    Adjusted R-squared:  0.7119
F-statistic: 207.4 on 8 and 660 DF,  p-value: < 2.2e-16
```

# Backward Regression

Hide

```
Model_BackwardReg <- step(linear_RegModel , direction = "backward")
```

```
Start:  AIC=11690.53
US_health$charges ~ age + sex + bmi + children + smoker + region

              Df Sum of Sq      RSS   AIC
- sex          1  3.7256e+07 2.5323e+10 11690
- region        3  2.1251e+08 2.5498e+10 11690
<none>                                2.5286e+10 11690
- children      1  2.3629e+08 2.5522e+10 11695
- bmi           1  2.7522e+09 2.8038e+10 11758
- age           1  7.0698e+09 3.2356e+10 11854
- smoker        1  5.4934e+10 8.0219e+10 12461

Step:  AIC=11689.51
US_health$charges ~ age + bmi + children + smoker + region

              Df Sum of Sq      RSS   AIC
- region        3  2.2628e+08 2.5549e+10 11690
<none>                                2.5323e+10 11690
- children      1  2.4049e+08 2.5564e+10 11694
- bmi           1  2.8350e+09 2.8158e+10 11758
- age           1  7.0387e+09 3.2362e+10 11852
- smoker        1  5.5663e+10 8.0986e+10 12465

Step:  AIC=11689.46
US_health$charges ~ age + bmi + children + smoker

              Df Sum of Sq      RSS   AIC
<none>                                2.5549e+10 11690
- children      1  2.3349e+08 2.5783e+10 11694
- bmi           1  2.7725e+09 2.8322e+10 11756
- age           1  7.1431e+09 3.2692e+10 11852
- smoker        1  5.5639e+10 8.1189e+10 12461
```

Hide

```
summary(Model_BackwardReg)
```

```
Call:
lm(formula = US_health$charges ~ age + bmi + children + smoker,
    data = US_health, subset = train_new)

Residuals:
    Min       1Q   Median       3Q      Max
-10032  -3246  -1064   1246   31329

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -11845.57    1364.71  -8.680  <2e-16 ***
age           237.40      17.42   13.625  <2e-16 ***
bmi           338.98      39.93    8.488  <2e-16 ***
children      495.71     201.23    2.463   0.014 *
smokeryes     22134.76     582.09   38.026  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6203 on 664 degrees of freedom
Multiple R-squared:  0.7124,    Adjusted R-squared:  0.7107
F-statistic: 411.2 on 4 and 664 DF,  p-value: < 2.2e-16
```

# Stepwise Regression

Hide

```
Model_StepwiseReg <- step(linear_RegModel , direction = "both")
```

Start: AIC=11690.53  
US\_health\$charges ~ age + sex + bmi + children + smoker + region

	Df	Sum of Sq	RSS	AIC
- sex	1	3.7256e+07	2.5323e+10	11690
- region	3	2.1251e+08	2.5498e+10	11690
<none>			2.5286e+10	11690
- children	1	2.3629e+08	2.5522e+10	11695
- bmi	1	2.7522e+09	2.8038e+10	11758
- age	1	7.0698e+09	3.2356e+10	11854
- smoker	1	5.4934e+10	8.0219e+10	12461

Step: AIC=11689.51  
US\_health\$charges ~ age + bmi + children + smoker + region

	Df	Sum of Sq	RSS	AIC
- region	3	2.2628e+08	2.5549e+10	11690
<none>			2.5323e+10	11690
+ sex	1	3.7256e+07	2.5286e+10	11690
- children	1	2.4049e+08	2.5564e+10	11694
- bmi	1	2.8350e+09	2.8158e+10	11758
- age	1	7.0387e+09	3.2362e+10	11852
- smoker	1	5.5663e+10	8.0986e+10	12465

Step: AIC=11689.46  
US\_health\$charges ~ age + bmi + children + smoker

	Df	Sum of Sq	RSS	AIC
<none>			2.5549e+10	11690
+ region	3	2.2628e+08	2.5323e+10	11690
+ sex	1	5.1028e+07	2.5498e+10	11690
- children	1	2.3349e+08	2.5783e+10	11694
- bmi	1	2.7725e+09	2.8322e+10	11756
- age	1	7.1431e+09	3.2692e+10	11852
- smoker	1	5.5639e+10	8.1189e+10	12461

Hide

```
summary(Model_StepwiseReg)
```

```
Call:
lm(formula = US_health$charges ~ age + bmi + children + smoker,
    data = US_health, subset = train_new)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-10032	-3246	-1064	1246	31329

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-11845.57	1364.71	-8.680	<2e-16 ***
age	237.40	17.42	13.625	<2e-16 ***
bmi	338.98	39.93	8.488	<2e-16 ***
children	495.71	201.23	2.463	0.014 *
smokeryes	22134.76	582.09	38.026	<2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6203 on 664 degrees of freedom  
Multiple R-squared: 0.7124, Adjusted R-squared: 0.7107  
F-statistic: 411.2 on 4 and 664 DF, p-value: < 2.2e-16

# BEST MODEL ACCORDING TO ANNOVA

Hide

```
bestmodel_anova <- lm(train_health$charges~ age + bmi + smoker, data =train_health)
summary(bestmodel_anova)
```

```
Call:
lm(formula = train_health$charges ~ age + bmi + smoker, data = train_health)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-12095	-3184	-1032	1515	29136

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-12037.77	1164.32	-10.34	<2e-16 ***
age	256.42	14.80	17.33	<2e-16 ***
bmi	338.80	34.05	9.95	<2e-16 ***
smokeryes	23670.40	509.11	46.49	<2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6277 on 918 degrees of freedom  
Multiple R-squared: 0.7389, Adjusted R-squared: 0.738  
F-statistic: 865.8 on 3 and 918 DF, p-value: < 2.2e-16

- From the above summary(), the equation came out to be:
- $y = -12037.77 + (256.42age) + (338.80bmi) + (23670.40 \times smokeryes)$

# Model Diagnostic Tests for annova based fit model

Hide

```
# Checking the Multicollinearity
car::vif(bestmodel_anova)
```

	age	bmi	smoker
	1.012844	1.012897	1.000052

Hide

```
par(mfrow = c(3, 2))
plot(bestmodel_anova, which=1) #Plotted Residuals v/s fitted graph
plot(bestmodel_anova, which=2) # Normality plot for residuals
```

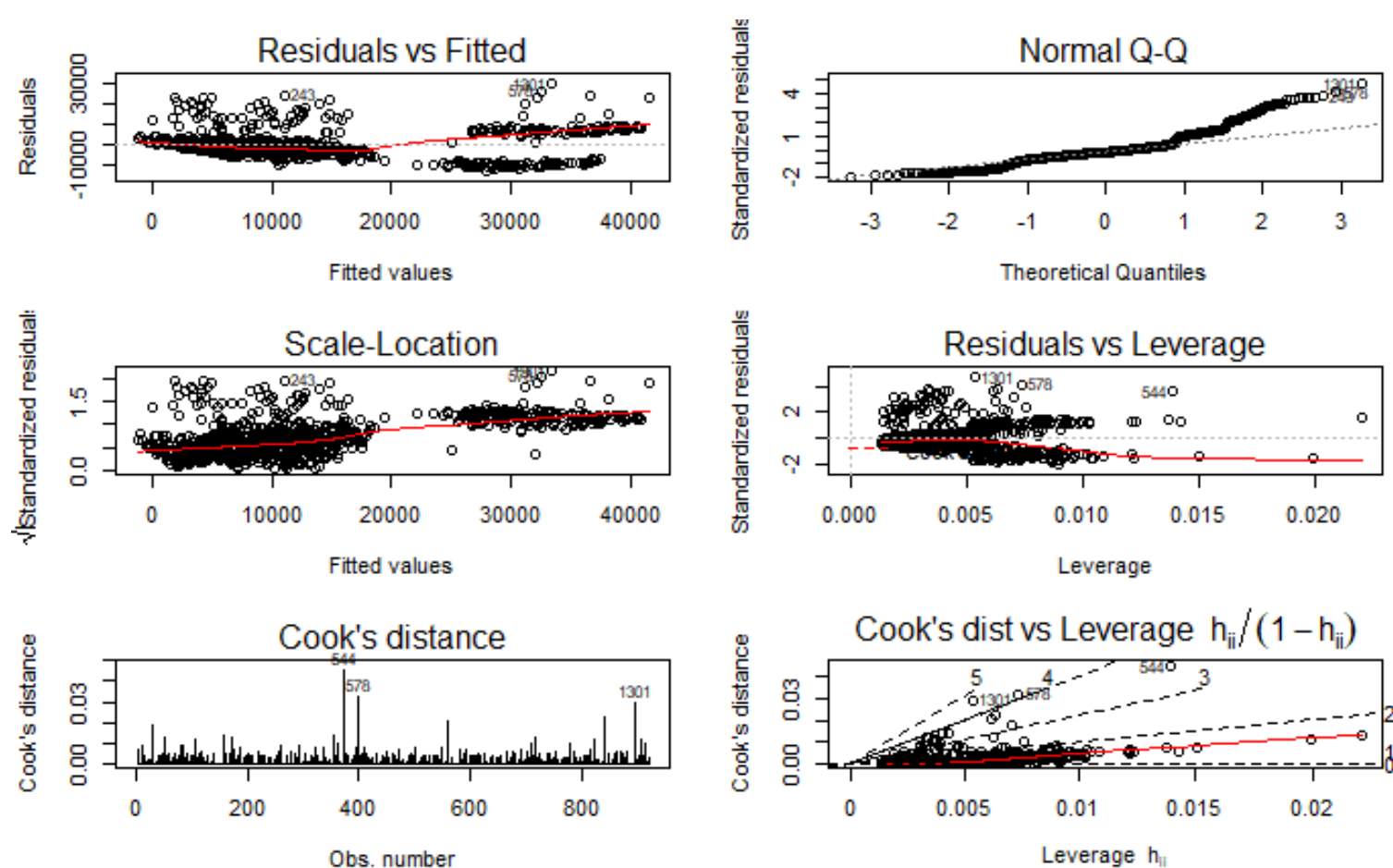
Hide



```
plot(bestmodel_anova, which=3) #Plotted Scale-Location graph
plot(bestmodel_anova, which=5) #Plotted Residuals v/s Leverage graph
```

Hide

```
plot(bestmodel_anova, which=4) #Graph for determining Cook's Distance
plot(bestmodel_anova, which=6) #Plotted Cook's Distance-Leverage graph
```



Hide

```
# Non-constant variance score test
car::ncvTest(bestmodel_anova)
```

```
Non-constant Variance Score Test
Variance formula: ~ fitted.values
Chisquare = 151.619, Df = 1, p = < 2.22e-16
```

Hide

```
# Testing for Autocorrelated errors
durbinWatsonTest(bestmodel_anova)
```

```
lag Autocorrelation D-W Statistic p-value
1 0.006906446 1.98215 0.778
Alternative hypothesis: rho != 0
```

Hide

```
#Test for normal distribution
shapiro.test(bestmodel_anova$residuals)
```

```
Shapiro-Wilk normality test
```

```
data: bestmodel_anova$residuals
W = 0.89898, p-value < 2.2e-16
```

## Predictions for annova based fit model

Hide

```
predict_Abest <- predict(bestmodel_anova, test_health, type = "response")
residual_Abest <- test_health$charges - predict_Abest
predict_Aregbest <- data.frame("Predicted"= predict_Abest, "Actual" =test_health$charges, "Residuals" = residual_Abest)
accuracy(predict_Abest, test_health$charges)
```

	ME	RMSE	MAE	MPE	MAPE
Test set	60.4786	5667.741	4005.492	-19.5216	45.08702

# BEST MODEL ACCORDING TO STEPWISE AND BACKWARD

Hide

```
bestmodel_StepBack <- lm(train_health$charges~ age + bmi + smoker +children, data =train_health)
summary(bestmodel_StepBack)
```

Call:  
lm(formula = train\_health\$charges ~ age + bmi + smoker + children,  
data = train\_health)

Residuals:

Min	1Q	Median	3Q	Max
-11588	-3122	-1026	1491	29616

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-12565.34	1180.38	-10.645	<2e-16 ***
age	255.28	14.76	17.292	<2e-16 ***
bmi	341.87	33.98	10.062	<2e-16 ***
smokeryes	23675.65	507.69	46.634	<2e-16 ***
children	421.95	170.06	2.481	0.0133 *

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6259 on 917 degrees of freedom  
Multiple R-squared: 0.7406, Adjusted R-squared: 0.7395  
F-statistic: 654.6 on 4 and 917 DF, p-value: < 2.2e-16

- From the above summary(), the equation came out to be:
- $y = -12565.34 + (255.28age) + (341.87bmi) + (23675.65smokeryes) + (421.95children)$

# Model Diagnostic Tests for stepwise and backward based fit model

Hide

```
# Checking the Multicollinearity
car::vif(bestmodel_StepBack)
```

age	bmi	smoker	children
1.013816	1.014245	1.000070	1.002078

Hide

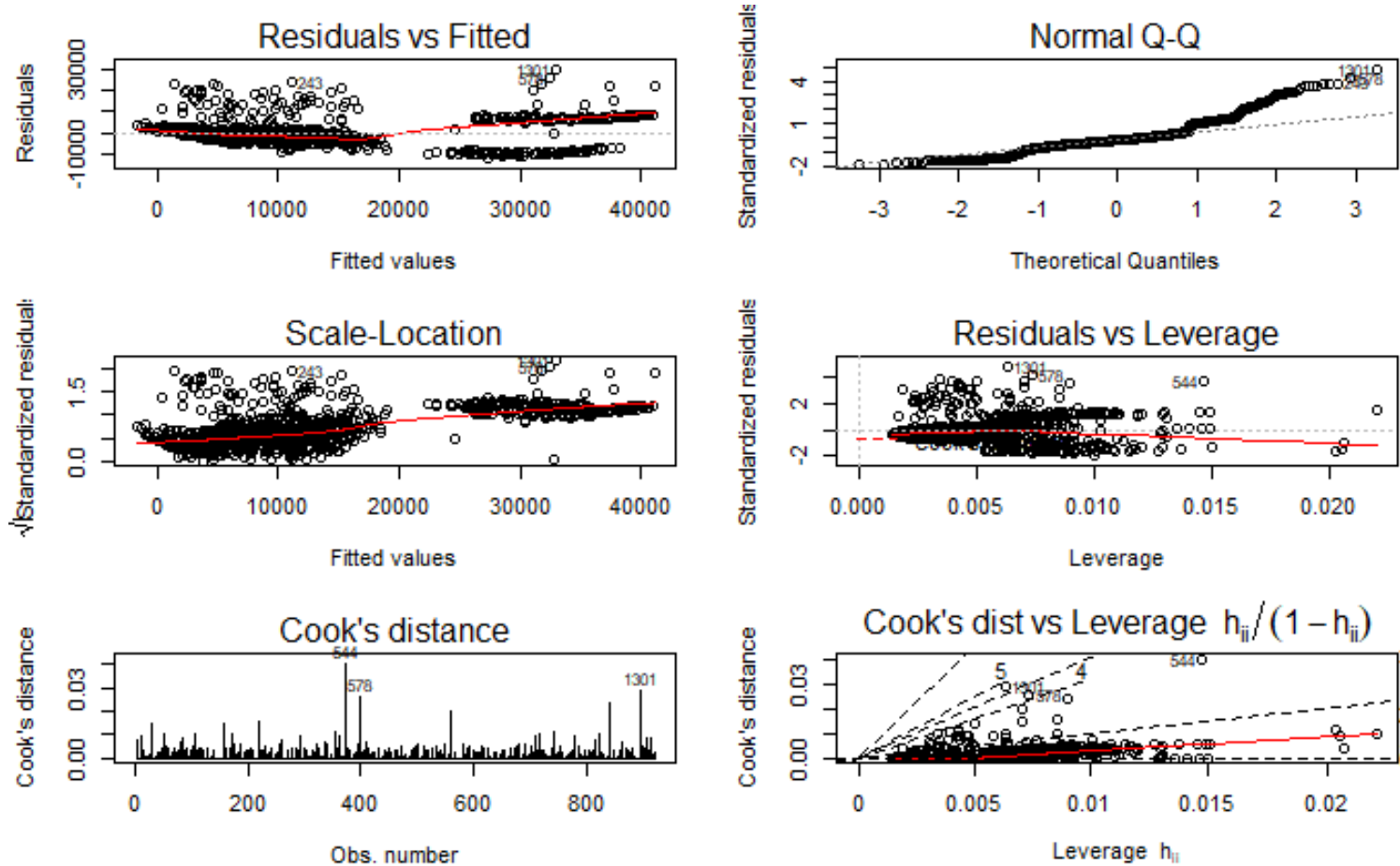
```
par(mfrow = c(3, 2))
plot(bestmodel_StepBack, which=1) #Plotted Residuals v/s fitted graph
plot(bestmodel_StepBack, which=2) # Normality plot for residuals
```

Hide

```
plot(bestmodel_StepBack, which=3) #Plotted Scale-Location graph
plot(bestmodel_StepBack, which=5) #Plotted Residuals v/s Leverage graph
```

Hide

```
plot(bestmodel_StepBack, which=4) #Graph for determining Cook's Distance
plot(bestmodel_StepBack, which=6)
```



Hide

```
# Non-constant variance score test
car::ncvTest(bestmodel_StepBack)
```

Non-constant Variance Score Test  
Variance formula: ~ fitted.values  
Chisquare = 156.9308, Df = 1, p = < 2.22e-16

Hide

```
# Testing for Autocorrelated errors
durbinWatsonTest(bestmodel_StepBack)
```

lag Autocorrelation D-W Statistic p-value  
1 0.002167906 1.992042 0.884  
Alternative hypothesis: rho != 0

Hide

```
#Test for normal distribution
shapiro.test(bestmodel_StepBack$residuals)
```

Shapiro-Wilk normality test  
  
data: bestmodel\_StepBack\$residuals  
W = 0.89561, p-value < 2.2e-16

# Prediction for stepwise and backward based fit model

Hide

```
predict_SBbest <- predict(bestmodel_StepBack, test_health, type = "response")
residual_SBbest <- test_health$charges - predict_SBbest
predict_SBregbest <- data.frame("Predicted"= predict_SBbest, "Actual" =test_health$charges, "Residuals" = residual_SBbest)
accuracy(predict_SBbest, test_health$charges)
```

	ME	RMSE	MAE	MPE	MAPE
Test set	107.7915	5628.947	3972.476	-16.4929	43.83209

# BEST MODEL ACCORDING TO FORWARD AND ALL POSSIBLE SUBSET REGRESSION

Hide

```
bestmodel_fwd <- lm(train_health$charges~ age + bmi + smoker +children + region, data =train_health)
summary(bestmodel_fwd)
```

```
Call:
lm(formula = train_health$charges ~ age + bmi + smoker + children +
    region, data = train_health)

Residuals:
    Min       1Q   Median       3Q      Max
-11165.7  -3111.7   -979.4   1507.6  30377.4

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  -12546.15    1211.88  -10.353  < 2e-16 ***
age             254.74      14.73   17.294  < 2e-16 ***
bmi             369.25      35.32   10.454  < 2e-16 ***
smokeryes      23756.57     507.70   46.793  < 2e-16 ***
children        428.42     169.84    2.522  0.01182 *
regionnorthwest  -638.41     592.12   -1.078  0.28124
regionsoutheast -1668.87     589.10   -2.833  0.00471 **
regionsouthwest -1030.88     598.17   -1.723  0.08516 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6241 on 914 degrees of freedom
Multiple R-squared:  0.743, Adjusted R-squared:  0.741
F-statistic: 377.4 on 7 and 914 DF,  p-value: < 2.2e-16
```

- From the above summary(), the equation came out to be:
- $y = -12546.15 + (254.74age) + (369.25bmi) + (23756.57smokeryes) + (428.42children) - (638.41regionnorthwest) - (1668.87regionsoutheast) - (1030.88regionsouthwest)$

# Model Diagnostic Tests for forward and all possible subset based fit model

Hide

```
# Checking the Multicollinearity
car::vif(bestmodel_fwd)
```

```
          GVIF Df GVIF^(1/(2*Df))
age       1.015301 1       1.007622
bmi       1.102430 1       1.049967
smoker    1.005959 1       1.002975
children  1.005435 1       1.002714
region    1.097810 3       1.015674
```

Hide

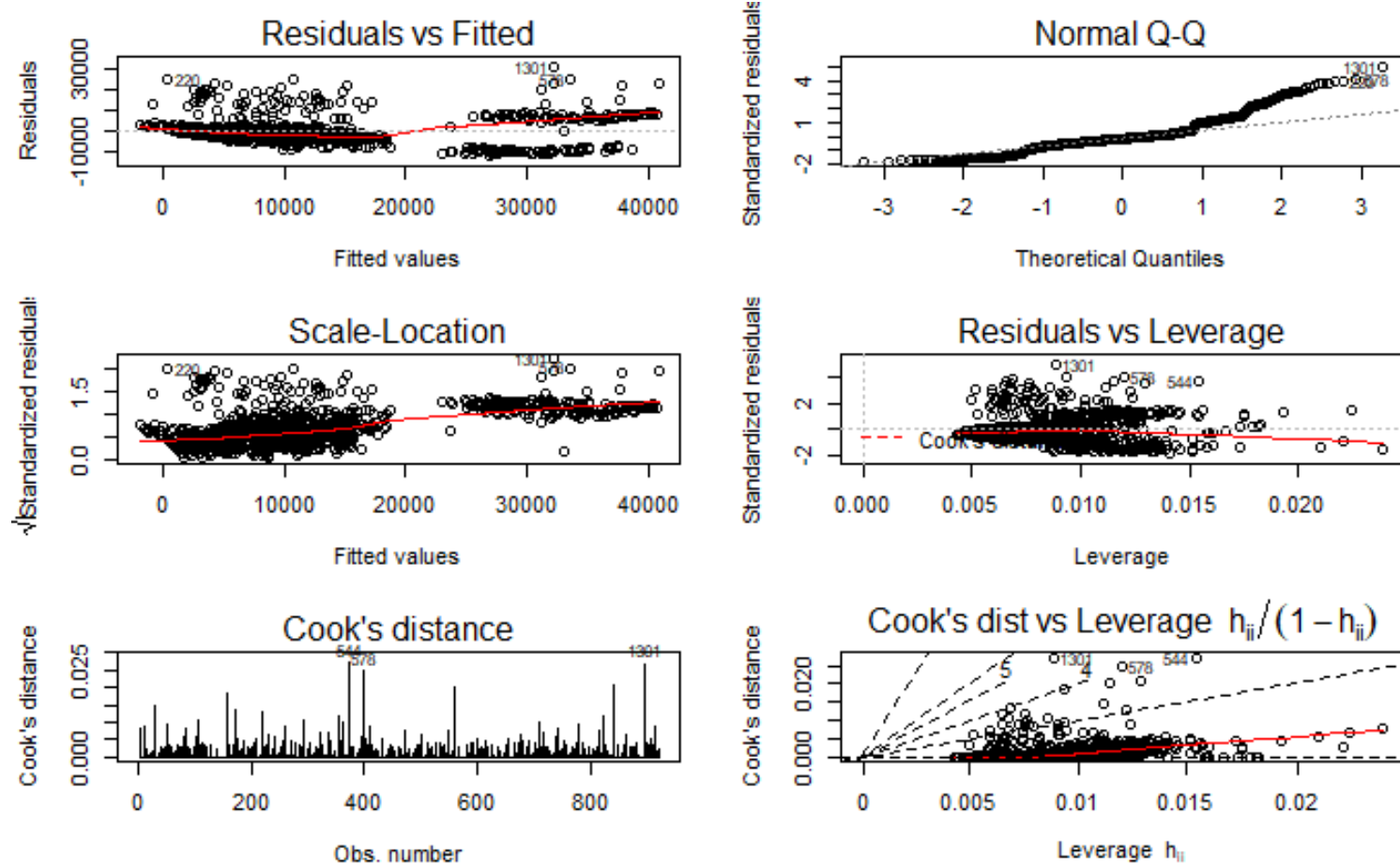
```
par(mfrow = c(3, 2))
plot(bestmodel_fwd, which=1) #Plotted Residuals v/s fitted graph
plot(bestmodel_fwd, which=2) # Normality plot for residuals
```

Hide

```
plot(bestmodel_fwd, which=3) #Plotted Scale-Location graph
plot(bestmodel_fwd, which=5) #Plotted Residuals v/s Leverage graph
```

Hide

```
plot(bestmodel_fwd, which=4) #Graph for determining Cook's Distance
plot(bestmodel_fwd, which=6)
```



Hide

```
# Non-constant variance score test
car::ncvTest(bestmodel_fwd)
```

Non-constant Variance Score Test  
 Variance formula: ~ fitted.values  
 Chisquare = 153.8316, Df = 1, p = < 2.22e-16

Hide

```
# Testing for Autocorrelated errors
durbinWatsonTest(bestmodel_fwd)
```

```
lag Autocorrelation D-W Statistic p-value
1 -0.0008177996 1.997969 0.952
Alternative hypothesis: rho != 0
```

Hide

```
#Test for normal distribution
shapiro.test(bestmodel_fwd$residuals)
```

Shapiro-Wilk normality test

```
data: bestmodel_fwd$residuals
W = 0.89578, p-value < 2.2e-16
```

## Prediction for forward and all possible subset based fit model

Hide

```
predict_fwdbest <- predict(bestmodel_fwd, test_health, type = "response")
residual_fwdbest <- test_health$charges - predict_fwdbest
predict_linregbest2 <- data.frame("Predicted"= predict_fwdbest, "Actual" =test_health$charges, "Residuals" = residual_fwdbest)
accuracy(predict_fwdbest, test_health$charges)
```

	ME	RMSE	MAE	MPE	MAPE
Test set	102.2186	5665.428	4017.834	-14.77523	43.3282