

Machine Learning

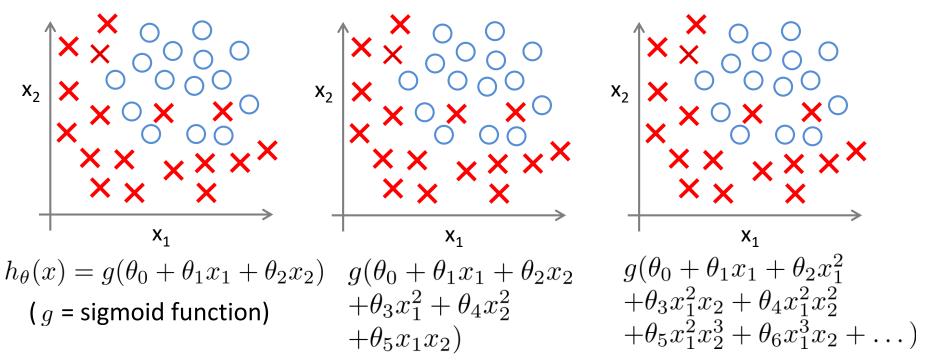
Regularization

The problem of overfitting

Example: Linear regression (housing prices)

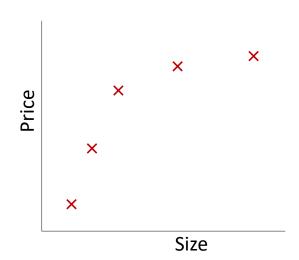
Overfitting: If we have too many features, the learned hypothesis may fit the training set very well $(J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 \approx 0)$, but fail to generalize to new examples (predict prices on new examples).

Example: Logistic regression



Addressing overfitting:

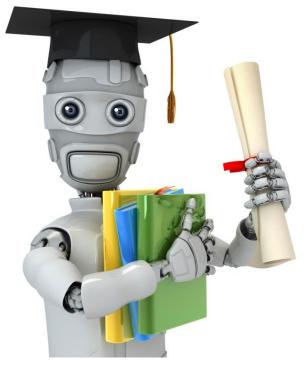
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x_1 = \text{size of house}
x_2 = \text{ no. of bedrooms}
x_3 = \text{ no. of floors}
x_4 = age of house
x_5 = average income in neighborhood
x_6 = \text{kitchen size}
x_{100}
```



Addressing overfitting:

Options:

- 1. Reduce number of features.
 - Manually select which features to keep.
 - Model selection algorithm (later in course).
- 2. Regularization.
 - Keep all the features, but reduce magnitude/values of parameters θ_i .
 - Works well when we have a lot of features, each of which contributes a bit to predicting y.

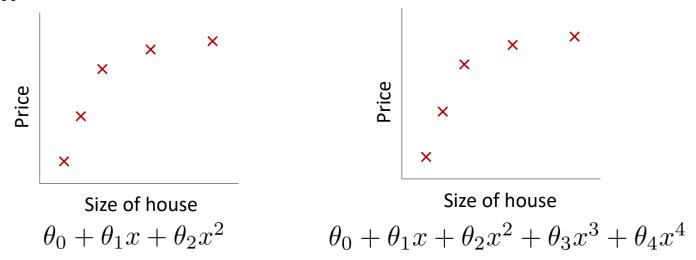


Machine Learning

Regularization

Cost function

Intuition



Suppose we penalize and make θ_3 , θ_4 really small.

$$\min_{\theta} \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Regularization.

Small values for parameters $\theta_0, \theta_1, \dots, \theta_n$

- "Simpler" hypothesis
- Less prone to overfitting

Housing:

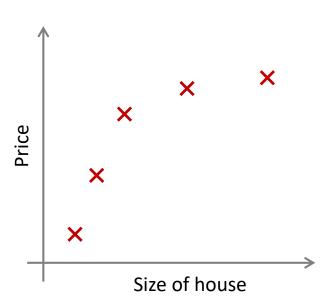
- Features: $x_1, x_2, \ldots, x_{100}$
- Parameters: $\theta_0, \theta_1, \theta_2, \dots, \theta_{100}$

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^{2}$$

Regularization.

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{n} \theta_j^2 \right]$$

$$\min_{\theta} J(\theta)$$



In regularized linear regression, we choose θ to minimize

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{n} \theta_j^2 \right]$$

What if λ is set to an extremely large value (perhaps for too large for our problem, say $\lambda=10^{10}$)?



$$\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$