

\* Newton Raphson method to find the roots.

let us consider an eqn  $f(x) = x^4 - x - 10 \rightarrow ①$

step ① find  $f'(x) = 4x^3 - 1 \rightarrow ②$

By putting 0, 1, 2, 3, ... in eq ①

$$f(0) = 0 - 0 - 10 = -10$$

$$f(1) = 1 - 1 - 10 = -10 \quad \rightarrow \text{Neg} \quad \text{so } f(1) = -10$$

$$f(2) = 16 - 2 - 10 = 4 \quad \rightarrow \text{pos} \quad f(2) = 4$$

roots lie b/w  $f(1)$  &  $f(2)$

$$\text{let } x_0 = 2$$

By Newton Raphson method

$$x_{i+1} = \frac{x_i - \frac{f(x_i)}{f'(x_i)}}{f'(x_i)}$$

$$x_{i+1} = \frac{x_i - \frac{x_i^4 - x_i - 10}{4x_i^3 - 1}}{4x_i^3 - 1}$$

$$= \frac{x_i(4x_i^3 - 1) - (x_i^4 - x_i - 10)}{4x_i^3 - 1}$$

$$x_{i+1} = \frac{3x_i^4 + 10}{4x_i^3 - 1} \quad @ \ i=0$$

$$x_{i+1} \rightarrow x_1 = \frac{3x_0^4 + 10}{4x_0^3 - 1}$$

$$= \frac{3 \times 16 + 10}{4(2)^3 - 1} = 1.871$$

@  $i=1$

$$x_2 = \frac{3x_1^4 + 10}{4x_1^3 - 1} = 1.856$$

@ i=2

$$x_{i+1} = x_3 = \frac{3x_2^4 + 10}{4x_2^3 - 1} = 1.856$$

so as  $x_2 = x_3 = 1.856$  → This is the root

$$\frac{(x) + \dots}{(x) + \dots}$$

$$\frac{x^4 - x - 10}{4x^3 - 1}$$