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AI1103-Assignment-1

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Download all python codes from

https://github.com/VamsiPreetham-21/AI1103-Assignment---1/blog/main/Assignment1.py

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Ouestion - 5.5

If each element of a second order determinant is either zero or one , what is the probability that the value of the determinant is positive ? (Assume that the individual entries are chosen independently each value being assumed with probability 1/2)

Solution:

Total number of entries in the matrix are 4.Let the entries be $(a_{11}, a_{12}, a_{21}, a_{22})$ where the suffixes represent their row and column number respectively. Matrix

$$\begin{pmatrix} M \end{pmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}.$$
(0.0.1)

Let $X \in \{0,1\}$ be a random variable denoting the possible value for each entry.

$$\Pr(X=0) = \frac{1}{2} \tag{0.0.2}$$

$$\Pr(X=1) = \frac{1}{2} \tag{0.0.3}$$

For the determinant of the matrix to be positive:

$$a_{11}a_{22} - a_{12}a_{21} > 0 (0.0.4)$$

Then the entries a_{11} , a_{22} must be one and at least

one among a_{12} , a_{21} should be zero.

$$= \Pr(X = 1) \Pr(X = 1) (1 - (\Pr(X = 1) \Pr(X = 1)))$$

(0.0.5)

$$=\frac{1}{4} \times \left(1 - \frac{1}{4}\right) \tag{0.0.6}$$

$$=\frac{3}{16}\tag{0.0.7}$$