

Functional Programming

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Introduction: the functional way of problem solving

Lecture 1

Outline

- Organization
- Literature
- Motivation
- What's it all about?

Organisation

- **Lecture (Hybrid, Monday – 10:30-12:15):**
 - introduction and explanation of concepts
 - lecture slides available immediately on Brightspace after lecture
- **Assignments:**
 - Exercise sets (Brightspace)
 - assignment available immediately after lecture (on Brightspace)
 - deadline Monday 12:30
- **Tutorial (Online Wednesday – First quarter: 13:30-15:15, second quarter: ?):**
 - discuss any questions you have about lecture / assignments
- **Lab (Friday – 8:30-12:15):**
 - work on assignments, student assistants are available

Organisation

- **Preparatory assignments:**

- exercises intended to familiarize yourself with the concepts
- do them before the tutorial to see how well you understand the new stuff

- **Mandatory assignments:**

- upload before deadline: only last upload is stored on Brightspace!
- exercises intended to apply your skills with new concepts

- **Regulation**

- at most 1 Fail for the mandatory assignments (Btw, Fail \neq Insufficient)
- Fail if
 - Program syntactically incorrect: cannot be loaded into GHCi.
 - Essential parts are missing
- the course is concluded with a written (digital) exam. If you do not meet the above requirement, you may take the written exam, but your final result for the course will be a maximum of 5.

Exam

- **Exam:** closed book, digital with Cirrus

Literature

- Miran Lipovaca, *Learn You a Haskell for Great Good!: A Beginner's Guide*, No Starch Press, 2011.
- Richard Bird, *Thinking Functionally with Haskell*, Cambridge University Press, 2015.
- Will Kurt, *Get Programming with Haskell*, Manning Publications, 2018.
- Graham Hutton, *Programming in Haskell (2nd Edition)*, Cambridge University Press, 2016.
- Bryan O'Sullivan, John Goerzen, Don Stewart, *Real World Haskell*, O'Reilly Media, 2008.
- Simon Thompson, *Haskell: The Craft of Functional Programming (3rd Edition)*, Addison-Wesley Professional, 2011.

square $x = x * x$

Motivation

“LISP is worth learning for a different reason — the profound enlightenment experience you will have when you finally get it. That experience will make you a better programmer for the rest of your days, even if you never actually use LISP itself a lot.”

Eric Steven Raymond, How To Become A Hacker
<http://www.catb.org/~esr/faqs/hacker-howto.html>

“You can never understand one language until you understand at least two.”

Ronald Searle, British artist (1920--2011)

FP and OOP

Imperative

- assignment
 - iteration
 - arrays
 - eager evaluation
 - Von Neumann architecture
-

Object oriented programming

- classes, interfaces, inheritance
 - generic classes
-

Functional

- pure, no side-effects
 - recursion
 - (infinite) lists
 - lazy evaluation
 - reduction
-
- higher order functions

Expressions vs statements

- in ordinary programming languages the world is divided into a world of *statements* and a world of *expressions*

- statements:

- $x := e, \quad s1 ; s2, \text{ while } e \text{ do } s$

- execution order is important

- $i := i + 1 ; a := a * i \neq a := a * i ; i := i + 1$

- expressions:

- $a + b * c, \quad a \text{ and not } b$

- evaluation order is unimportant (*referential transparency*): in

- $(2 * a * y + b) * (2 * a * y + c)$

- evaluate either parenthesis first (or both simultaneously!)

- assumes no side-effects: order matters in $++x + x--$

Comparison with 'ordinary' programming

- insertion sort
- quicksort
- (binary search trees)

Insertion sort: Modula-2

```
PROCEDURE InsertionSort ( VAR a : ArrayT ) ;  
  VAR i , j : CARDINAL ;  
      t : ElementT ;  
BEGIN  
  FOR i := 2 TO Size DO  
    (* a[1..i-1] already sorted *)  
    t := a [ i ] ;  
    j := i ;  
    WHILE ( j > 1 ) AND ( a [ j-1 ] > t ) DO  
      a [ j ] := a [ j-1 ] ; j := j-1  
    END ;  
    a [ j ] := t  
  END  
END InsertionSort ;
```

Insertion sort: Haskell

```
insertionSort [ ]      = [ ]
insertionSort (x : xs) = insert x (insertionSort xs)

insert a [ ]          = [a]
insert a (b : xs)
  | a ≤ b              = a : b : xs
  | otherwise          = b : insert a xs
```

q: C

```
void    q    ( int a [ ] , int l , int r ) {  
    if ( r > l ) {  
        int i = l ; int j = r ;  
        int p = a [ ( l + r ) / 2 ] ;  
        for ( ; ; ) {  
            while ( a [ i ] < p ) i++;  
            while ( a [ j ] > p ) j--;  
            if ( i > j ) break ;  
            swap(&a[i++] , &a[j--]);  
        } ;  
        q    ( a , l , j ) ;  
        q    ( a , i , r ) ;  
    }  
}
```

Quicksort: Haskell

```
quicksort [ ] = [ ]
quicksort (x : xs) = quicksort littles ++ [x] ++ quicksort bigs
  where littles = [a | a ← xs, a < x]
        bigs    = [a | a ← xs, x ≤ a]
```

Editors, IDEs, Interpreters, Compilers, Scripts and sessions

- *Haskell Platform*
 - Compiler + interpreter, no editor/IDE
 - Available on the PCs in the computer labs (not on Windows)
 - Install on our own PC/laptop
- we will use *GHCI*, an interactive version of the *Glasgow Haskell Compiler*, a popular implementation of *Haskell*
- a program is a collection of *modules*
- a module is a collection of (functions and data) *definitions* (aka a *script*)
- a standalone program includes a 'main' expression

My First Haskell Script

- When developing a Haskell script, it is useful to keep two windows open, one running an editor for the script, and the other running GHCi.
- Start an editor, type in the following two function definitions, and save the script as `mfhs.hs`:

```
double x = x + x
```

```
quadruple x = double (double x)
```

My Second Haskell Script

- Define a function that adds the numbers 1 to 10
 - You cannot use loops because there are none in Haskell
 - You also cannot use variables

```
sum1to10 = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10
```

- And now more general: Define a function that adds the numbers n to m.
- Use recursion (think recursively)
 - Base case (no more numbers left): result is 0
 - Recursive case (still numbers left): result is the current number added to the result of the recursive call for the remaining numbers.

```
sumNtoM n m = if n > m then 0 else n + sumNtoM (n+1) m
```

Evaluation

- interpreter evaluates expression by reducing to simplest possible form
- *reduction* is rewriting using meaning-preserving simplifications: *replacing equals by equals*

square (3 + 4)

\Rightarrow { definition of + }

square 7

\Rightarrow { definition of *square* }

7 * 7

\Rightarrow { definition of * }

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square x = x * x

- expression 49 cannot be reduced any further: *normal form*
- *applicative order* evaluation: reduce arguments before expanding function definition (call by value, eager evaluation)

Alternative evaluation orders

- other evaluation orders are possible:

square (3 + 4)

⇒ { definition of *square* }

(3 + 4) * (3 + 4)

⇒ { definition of + }

7 * (3 + 4)

⇒ { definition of + }

7 * 7

⇒ { definition of * }

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- final result is the same: if two evaluation orders terminate, both yield the same result (*confluence*)
- *normal order* evaluation: expand function definition before reducing arguments (call by need, lazy evaluation)

square x = x * x

Values

- in FP, as in maths, the sole purpose of an expression is to denote a value
- other characteristics (time to evaluate, number of characters, etc) are irrelevant
- values may be of various kinds: numbers, truth values, characters, tuples, lists, functions, etc
- important to distinguish *abstract value* (the number 42) from *concrete representation* (the characters '4' and '2', the string "XLII", the bit-sequence 0000000000101010)
- evaluator prints *canonical representation* of a value
- some values have no canonical representation (e.g. functions), some have only infinite ones (e.g. π)

Functions

- naturally, FP is a matter of functions
- script defines *functions* (*square*, *insert*)
- function transforms (one or more) arguments into result
- *deterministic*: same arguments always give same result
- may be *partial*: result may sometimes be undefined
- e.g. cosine, square root; distance between two cities; compiler; text formatter; process controller

Function types

- *type declaration* in a script specifies the type of function
- e.g. `square :: Integer → Integer`
- in general, `f :: A → B` indicates that function `f` takes arguments of type `A` and returns results of type `B`
- *apply* function to argument: `f x`
- sometimes parentheses are necessary: `square (3 + 4)` (function application is an operator, binding more tightly than the operator `+`)

Operators

- functions with alphabetic names are *prefix*: `f 3 4`
- functions with symbolic names are *infix*: `3 + 4`
- make an alphabetic name infix by enclosing in back-quotes: `17 `mod` 10`
- make symbolic operator prefix by enclosing it in parentheses: `(+) 3 4`

Definitions

- we've seen some simple definitions of functions so far
- can also define other kinds of values:

`name :: String`

`name = "Sjaak"`

- all definitions so far have had an identifier (and perhaps formal parameters) on the left, and an expression on the right
- other forms possible: conditional, pattern-matching, and local definitions
- also recursive definitions (later)

Conditional definitions

- definition of *smallest* using a *conditional expression*:

```
smallest :: Integer → Integer → Integer
```

```
smallest x y = if x ≤ y then x else y
```

- could also use *guarded equations*:

```
smallest :: Integer → Integer → Integer
```

```
smallest x y
```

```
    | x ≤ y      = x
```

```
    | otherwise = y
```

- each *clause* has a *guard* and an *expression* separated by =
- last guard can be *otherwise* (synonym for *True*)
- especially convenient with three or more clauses

Declaration vs expression style

- Haskell supports two different programming styles
- *declaration style*: using (guarded) equations, patterns and expressions

```
smallest :: Integer → Integer → Integer
```

```
smallest x y
```

```
    | x ≤ y      = x
```

```
    | otherwise = y
```

- *expression style*: emphasizing the use of expressions

```
smallest :: Integer → Integer → Integer
```

```
smallest x y = if x ≤ y then x else y
```

- expression style is often more flexible
- experienced programmers use both simultaneously

Pattern matching

- define function by several equations
- arguments on lhs not just variables, but *patterns*
- patterns may be *variables* or *constants* (or *constructors*, later)
- e.g.

```
day :: Integer → String
day 1 = "Saturday"
day 2 = "Sunday"
day _ = "Weekday"
```

- also *wild-card pattern* `_`
- evaluate by reducing argument to normal form, then applying first matching equation
- result is undefined if argument has no normal form, or no equation matches

Local definitions

- repeated sub-expressions can be captured in a *local definition*

```
sqroots :: (Float, Float, Float) → (Float, Float)
sqroots (a, b, c) = ((-b-sd)/(2*a), (-b+sd)/(2*a))
  where sd = sqrt (b*b - 4*a*c)
```

- scope of **where** clause extends over whole right-hand side
- multiple local definitions can be made:

```
demo :: Integer → Integer → Integer
demo x y = (a + 1) * (b + 2)
  where a = x - y
        b = x + y
```

- in conjunction with guarded equations, the scope of a **where** clause covers all guard clauses

Layout

- structure obtained by layout, not punctuation
 - all definitions in same scope must start in the same column
 - indentation from start of definition implies continuation

demo :: Integer → Integer → Integer

demo x y = (a + 1) * (b + 2) where

a = x - y

b = x + y

- use spaces, not tabs!

let-expressions

- **where** clause is syntactically attached to an equation
- also: definitions local to an expression

`demo :: Integer → Integer → Integer`

`demo x y = let a = x - y`

`b = x + y`

`in (a + 1) * (b + 2)`

- *declaration style*: **where**; *expression style*: **let ... in ...**
- **let**-expressions are more flexible than **where** clauses

Programming example: a pyramid of strings

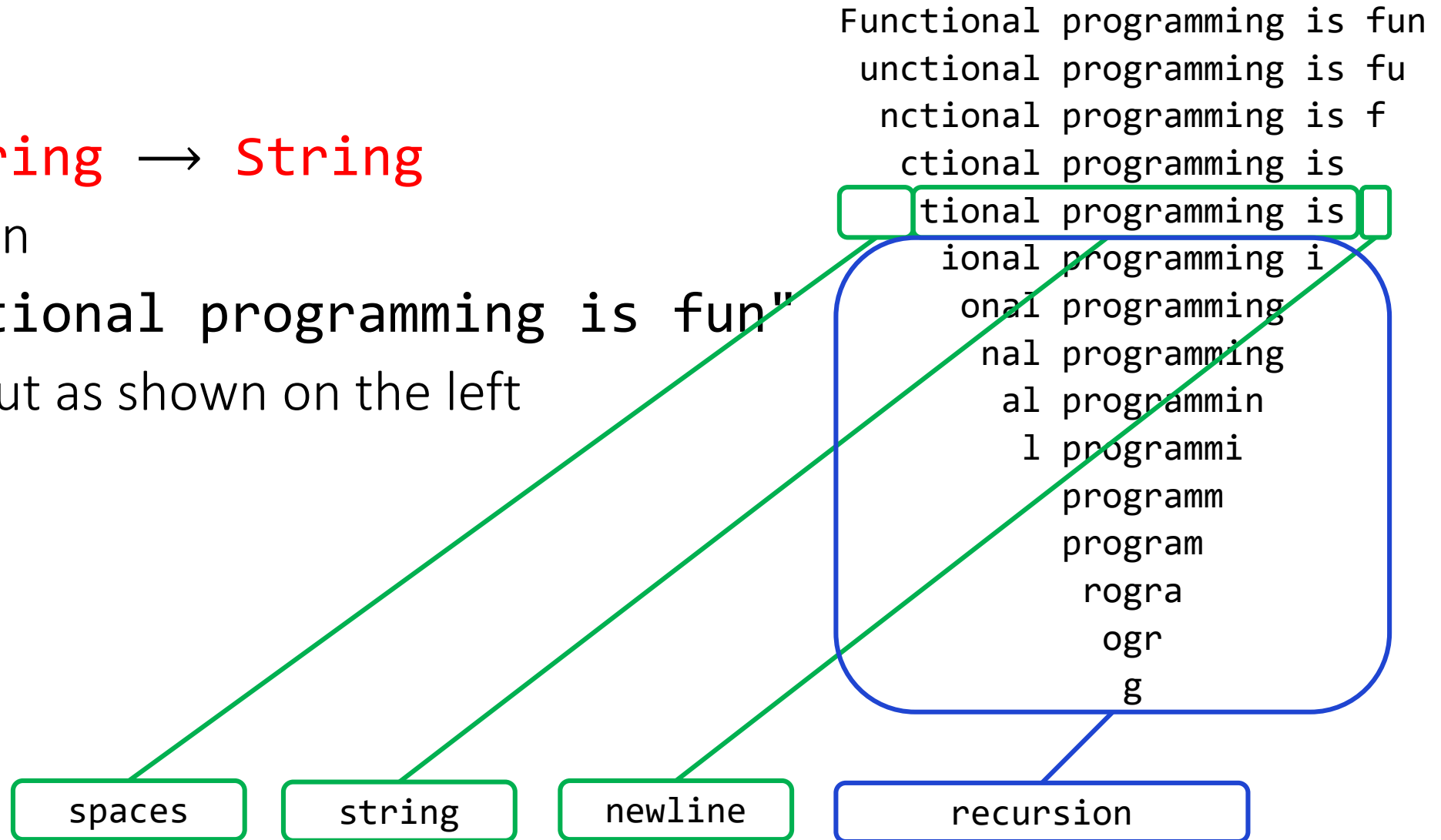
write a function

```
pyramid :: String → String
```

such the application

```
pyramid "Functional programming is fun"
```

produces the output as shown on the left



Pyramid: Java

```
public class Main {  
  
    public static void main(String[] args) {  
        System.out.print( pyramid("Functional Programming is fun") );  
    }  
  
    private static String pyramid(String str) {  
        StringBuilder sb = new StringBuilder();  
        for (int n = 0; n < (str.length() + 1) / 2; n++) {  
            sb.append(" ".repeat(n));  
            sb.append(str.substring(n, str.length() - n));  
            sb.append("\n");  
        }  
        return sb.toString();  
    }  
}
```

Pyramid: Haskell

```
module Pyramid where

pyramid :: String -> String
pyramid str = pyram 0 str where
    pyram :: Int -> String -> String
    pyram n str
        | length str <= 2 = spaces ++ str ++ newline
        | otherwise       = spaces ++ str ++ newline ++ pyram (n+1) substr

    where spaces  = replicate n ' '
          newline = "\n"
          substr  = tail (init str)

main = putStr (pyramid "Functional programming is fun")
```

The art of functional programming



- a problem is given by an expression
- a solution is a value
- a solution is obtained by evaluating an expression to a value
- a program introduces vocabulary to express problems and specifies rules for evaluating expressions
- the art of functional programming: finding rules
- Haskell has a very simple computational model
- . . . as in primary school: replacing equals by equals
- we can calculate not only with numbers, but also with lists, trees, grammars, pictures, music . . .