

# Vectors

1. Unit vector along  $\mathbf{PQ}$ , where coordinates of  $\mathbf{P}$  and  $\mathbf{Q}$  respectively are (2,1,-1) and (4,4,-7), is

- (a)  $2\hat{i} + 3\hat{j} - 6\hat{k}$
- (b)  $-2\hat{i} - 3\hat{j} + 6\hat{k}$
- (c)  $-\frac{2\hat{i}}{7} - \frac{3\hat{j}}{7} + \frac{6\hat{k}}{7}$
- (d)  $\frac{2\hat{i}}{7} + \frac{3\hat{j}}{7} - \frac{6\hat{k}}{7}$

2. If in  $\triangle ABC$ ,  $\overrightarrow{BA} = 2\vec{a}$  and  $\overrightarrow{BC} = 3\vec{b}$ , then  $\overrightarrow{AC}$  is

- (a)  $2\vec{a} + 3\vec{b}$
- (b)  $2\vec{a} - 3\vec{b}$
- (c)  $3\vec{b} - 2\vec{a}$
- (d)  $-2\vec{a} - 3\vec{b}$

3. Equation of line passing through origin and making  $30^\circ$ ,  $60^\circ$  and  $90^\circ$  with x, y, z axes respectively is

- (a)  $\frac{2x}{\sqrt{3}} = \frac{y}{2} = \frac{z}{0}$
- (b)  $\frac{2x}{\sqrt{3}} = \frac{2y}{1} = \frac{z}{0}$
- (c)  $2x = \frac{2y}{\sqrt{3}} = \frac{z}{1}$
- (d)  $\frac{2x}{\sqrt{3}} = \frac{2y}{1} = \frac{z}{1}$

4. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are three non-zero unequal vectors such that  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$ , then find the angle between  $\vec{a}$  and  $\vec{b} - \vec{c}$ .

5. If the equation of a line is

$$x = ay + b, z = cy + d, \quad (1)$$

then find the direction ratios of the line and a point on the line.

6. Using Integration, find the area of triangle whose vertices are (-1, 1), (0, 5) and (3, 2).

# Probability

7. If A and B are two events such that

$$\Pr(A|B) = 2 \times \Pr(B|A) \Pr(A) + \Pr(B) = \frac{2}{3} \quad (2)$$

then  $\Pr(B)$  is equal to

- (a)  $\frac{2}{9}$
  - (b)  $\frac{7}{9}$
  - (c)  $\frac{4}{9}$
  - (d)  $\frac{5}{9}$
8. (a) Two balls are drawn at random one by one with replacement from an urn containing equal number of red balls and green balls. Find the probability distribution of number of red balls. Also, find the mean of the random variable.
- (b) A and B throw a die alternately till one of them gets '6' and wins the game. Find their respective probabilities of winning, if A starts the game first.
9. Recent studies suggest that roughly 12% of the world population is left handed.
- Depending upon the parents, the chances of having a left handed child are as follows :
- (a) When both father and mother are left handed : Chances of left handed child is 24%.
  - (b) When father is right handed and mother is left handed : Chances of left handed child is 22%.
  - (c) when father is left handed and mother is right handed : Chances of left handed child is 17%.

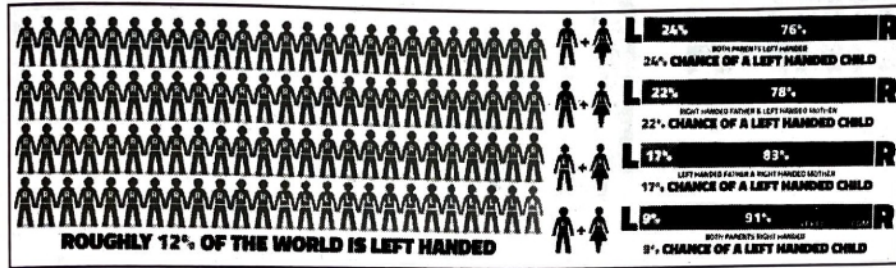


Figure 1: chance of left hand, depending upon parents

- (d) When both father and mother are right handed : Chances of left handed child is 9%.

Assuming that  $\Pr(A) = \Pr(B) = \Pr(C) = \Pr(D) = \frac{1}{4}$  and  $L$  denotes the event that child is left handed. Based on the above information, answer the following questions :

- Find  $\Pr(L|C)$
- Find  $\Pr(\bar{L}|A)$
- Find  $\Pr(A|L)$
- Find the probability that a randomly selected child is left handed given that exactly one of the parent is left handed.