

## Complex Plane or Argand Plane

The complex number  $x+iy$  which corresponds to the ordered pair  $(x,y)$  can be represented geometrically as the unique point  $P(x,y)$  in the  $XY$ -plane and vice-versa.

The plane having a complex number  $(0,0)$  assigned to each of its point is called the complex plane or Argand plane.

In the Argand plane, the modulus of the complex number  $x+iy$  is  $\sqrt{x^2+y^2}$  is the distance between the point  $P(x,y)$  and the origin  $O(0,0)$ .

The points on the  $x$ -axis corresponds to the complex numbers of the form  $a+io$  and the points on the  $y$ -axis corresponds to the complex numbers of the form  $0+ib$ . The  $x$ -axis and  $y$ -axis in the Argand plane are called, respectively, the real and the imaginary axes.

The representation of a complex number  $z = x+iy$  and its conjugate  $\bar{z} = x-iy$  in the Argand plane are, respectively, the points  $P(x,y)$  and  $Q(x,-y)$ . Geometrically, the point  $(x,-y)$  is the mirror image of the point  $(x,y)$  on the real axis.

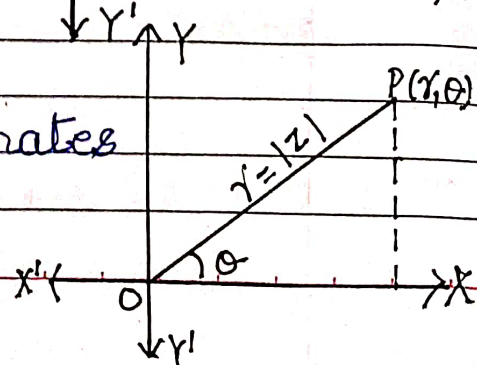
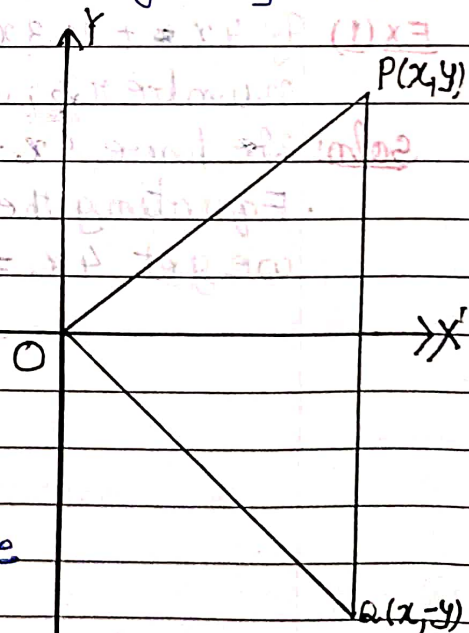
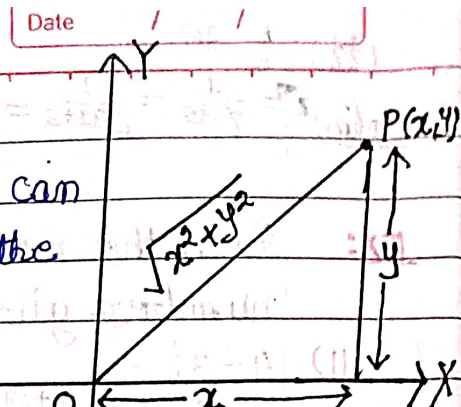
## Polar form of a complex number:

Let the complex number  $z = x+iy$  be represented by the point  $P(x,y)$  in the complex plane.

Let  $\angle XOP = \theta$  and  $|OP| = r > 0$ . Then,  $P(r, \theta)$  are called the polar coordinates of  $P$ . We call the origin  $O$  as Pole.

Clearly,  $x = r \cos \theta$ ,  $y = r \sin \theta$

(1)



$$\therefore Z = r(\cos \theta + i \sin \theta)$$

This is called the polar form or trigonometric form or modulus-amplitude form of  $Z$ .

The positive direction of the  $x$ -axis i.e.,  $OX$  is called as the initial line.

Here,  $r = \sqrt{x^2 + y^2} = |Z|$  is called the modulus of  $Z$ , and  $\theta$  is called the argument or amplitude of  $Z$  which is denoted by  $\arg(Z)$  or  $\text{amp}(Z)$ .

The value of  $\theta$  such that  $-\pi < \theta \leq \pi$  is called the principal argument of  $Z$ .