Diffrencial Equations

* Differential Equations *
Egn = 24/=2 diff. egn = dy x44=2
$\Rightarrow 2 = 1 + 2 = 1 $ solf $\Rightarrow 2 = f(3)$
Differential eqn
ordinary diff. egn partial diff. egn
single variable $\frac{d^2y}{dx^2} + \left(\frac{d^2y}{dx}\right)^3 + 37 = 0$
order = highest derivative degree = highest power of highest degree degree = 3 degree = highest power of highest degree from radicals degree = highest power of highest degree degree degree = 3
order = 1; degree = 1 + traction. Order - The highest derivative involved in diff. egn.
Radicali - (dy) fraction - derivative chaud not in denomenator
$O\left(\frac{d^{2q}}{dn^{2}}\right)^{2} = \left(\frac{x+dy}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{2} = \left(\frac{x+dy}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} = \left(\frac{x+dy}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} = \left(\frac{x+dy}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} = \left(\frac{x+dy}{dx}\right)^{3/2} \qquad O\left(\frac{d^{2q}}{dx}\right)^{3/2} = \left(\frac{x+dy}{dx}\right)^{3/2} = \left(\frac{x+dy}$
$\left(\frac{d^2y}{dx^2}\right)^4 = \left(\frac{n+d+1}{dx}\right)^3 \qquad \left(\frac{d+1}{dx}\right)^2 = xd+\frac{e^7}{dx}$ $0 = 1$ $0 = 2$ $0 = 1$

**		Differential	Equations	*	2
	2: 1 1:	5°01"	diff egn	dy x +1	
	Ordinory di	allerent ff. eqn	icl en	partial o	liff egn
d21 d22	$\frac{\text{single var}}{\left(\frac{dr}{dx}\right)^3 + 37}$			more the $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}$	an one val
degre	er = highest e = highe 2 ; degree	It power of	highest deg etire should fractions.	urpp deo	er=2 ree=3 tadicali
rder -	The highes	t denivative	involved	in diff, e	egn.
Radico	$xh = \begin{pmatrix} dy \\ dy \end{pmatrix}$	2,3,4)	fraction -	derivative rot in den	chaud
$\int \left(\frac{d^2q}{dn^2}\right)^2$	= (x+dy)	9/2 0	di = 2 d	et dy	
i (di	$\frac{2y}{x^2} = \left(\frac{x}{x} + \frac{y}{x} \right)$	D=4.	$\frac{di^2}{dx} = x di$ $\frac{d}{dx}$	4 e ⁷ 4 = 2	



)
$$\left(\frac{d^{3}Y}{dx^{3}}\right)^{2} + \left(\frac{d^{2}y}{dx^{2}}\right)^{3} + 3Y = 0$$
 (7) $dY = (t + sin t) dt$

$$0 = 3, \quad 0 = 2$$

$$\frac{dy}{dx} = t + sin t$$

$$\frac{\partial^{2}u}{\partial x^{2}} = \frac{\partial^{2}u}{\partial x^{3}} = \frac{\partial^{2}u}{\partial x^{3}} = \frac{\partial^{2}u}{\partial x^{3}}$$

$$0 = 3, \quad 0 = 2$$
Formation of differential and

Formation of differential equal
$$F(x,y,a,b) = 0$$

$$F_2(x,y, \frac{dy}{dx}, \frac{d^2y}{dx^2}, a, b) = 0$$
 = 3

lote:

The no of drbitrary constants eliminated should be equal to the order of resulting ordinary diff. egns

P(N, 4, 27 d24)=0

A ANTONIA A	anyly of the the many
through origin is	
(3) xdx + ydiin	
The state of the s	
AT 1111 MARIE AND	
$y = \frac{d_1}{d_1} x$	
dyx = dx -1	
- May- Jakes	and the second s
	The second secon
(5) Find the diff egn	of family of circle centred
@ Find the diff eqn	of family of ande centred where his are arbitrary
(2) Find the diff. eqn out (h, k) of radius of constants	of family of circle centred where hik are arbitrary
at (h, k) fradius o	of family of circle centred (where hik are arbitrary
constants $(2-h)^2 + (y-k)^2 = q^2$ $diff $	where high are
constants $(2-h)^2 + (y-k)^2 = q^2$	where high are
constants $(2-h)^2 + (y-k)^2 = q^2$ $diff $	where high are
constants $(2-h)^2 + (y-k)^2 = q^2$ $2(x-h) + 2(y-k) + 3$	where high are

Put (2) in (1)

$$\frac{(1+y^{1})^{2}y^{12}}{y^{112}} + \frac{(1+y^{12})^{2}}{y^{112}} = q^{2}$$

$$(1+1/2)^{2}(y^{2}+1) = a^{2}y^{2}$$

(3)
$$Y = C(x - C)^2 - 0$$

Diff. w.r.t.x

$$y' = ac(x-c) - 0$$

(2)
$$\frac{y}{y'} = \frac{c(x-0)^2}{2c(x-c)} = \frac{x-c}{2}$$
 $\frac{z-c}{y'}$

$$y = \frac{2y'-2y}{y'} \left(\frac{1}{y'} - \frac{2y'-2y}{y'} \right)^2 = \frac{2y'-2y}{y'} \frac{4y^2}{y'^2}$$

the given egn is of the form y=getg + get +... Note: -Then DE 15 (D-9)(D-b)(D-c)y =0 y=qe+ cze+ cze+ czet (D+1)(D-3) (D-2) y=0 $(D^3 - 4D^2 + D + 6)Y = 0$ $\frac{d^{3}Y - 4 d^{2}y}{dx^{3}} + \frac{dy}{dx^{2}} + \frac{6y}{dx} = 0$ i=get + ge4t 2 (D-2) (D+4) V = 0 (D2+2D1=0 8 d21 + adi - 81 =0

Vote:

If the given egn is of the form

Y = Paf(M) + Bg(x) Then the D.E. is obtained by simplifying the following determinant.

 $\frac{1}{4}$ f(x) g(x) = 0 $\frac{1}{4}$ f''' f''' g''

e.g. 1 y=Ae + Bx

· 4" (1-2x) + 4xy-47=0.

(3) y=e (Acos1 + B sinx) -0

Y' = ex (1 cosx + B sinx) + ex (-A sinx + B cosx) -0

 $y' = y + e^{x} (-A sinn + B coin)$

Y" = Y' + ex (-Asinx + Bcosx) + ex (-Acosx - Brinn)

Y" = Y' + (Y'-Y) - Y

·· 11 - 241 + 24 = 0

131 = 9 dre 9	1 (6) 20
de de la	
General sol	1 - 0 + (2 · N) - 0 + 1 1 5 1 1 5 1 1 1 1
dey = 9 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Ge+Co
B 4-7963	Gt3+62
~ y= +9t2+	-GE+C
(d) None	
first order first degree	diff. egmi.
Notation de F(x,1) or	[Mda+Ndy=0 M(n,y) fN10,
1) Variable separable me	Hod
dy ECNY)	
fonda = gord	
$\int F(n) dn = \int 940 d7$	+ (

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$$0 \quad \log(dy) = 21 - y$$

$$\frac{3}{4} \quad \frac{2}{4} = e^{-2y} + e^{2} \cdot y$$

$$\frac{dy}{dx} = \frac{21-y}{e^2} = \frac{21}{e^2} = \frac{1}{e^2} =$$

$$\int e^{y} dy = \int e^{2x} dx \qquad \qquad = e^{x} = \frac{e^{2x}}{-2} + \frac{x^{2}}{2} + C$$

$$e' = \frac{22}{2} + C$$
 (5) $\frac{dy}{dx} = 1 + \frac{y^2}{2}$

$$\frac{3}{dx} = \frac{4^2}{1-x^4} = \int \frac{dy}{1+y^2} = \int \frac{dy}{1+y$$

$$= \frac{1}{2} \left(\frac{1}{2} dx + \frac{1}{2} dx \right) \qquad \frac{1}{2} \frac{$$

$$\frac{dy}{dy} = \int \frac{d(xy)}{dx}$$

$$\int \frac{dy}{dy} = \int \frac{d(xy)}{dx}$$

$$\int \frac{dy}{dx} = \int \frac{d(xy)}{dx}$$

$$\frac{7}{3} = -1 = 20$$

$$\frac{3}{209} = \frac{1}{109} + \frac{1}{100} + \frac{1}{100} = \frac{200}{100} = \frac{$$

$$\begin{array}{c|c}
\hline
 & C = 2 \\
\hline
 & X^2 + y^2 = 4
\end{array}$$

6) Find the curve passing throughout and satisfing sin (di) - b	gh the privat (0,1)
sin (dr.) -b	
di sin'h) di - (1) (1)=1
$\int dy = \int 310 b dx$ $y = \chi \sin^2 b + c$	then find y' when x=-1
CEIL	Seldy-Selda
$\frac{1}{y} = \pi \sin b + 1$	-e'= e'+c
(a) $x = 3e^{3E}$ (b) $x = 3t^3$	$\frac{-1}{e} = e = c$ $\frac{-1}{e} = c$
(a) $x = 2e^{2t}$ (b) $x = 3e^{3t}$ (c) $x = 2e^{2t}$ (d) $x = 3e^{3t}$	e e e e e e e
$\frac{dx}{dx} = 3dx$	
800/2 = -3t -109°C	e = 7 7 - e
$\frac{2 - ce^{3t}}{\left[n - 3e^{3t} \right]}$	e ! = e

<)
	1

(9)
$$\frac{dy}{dx} = 3x^2 - 2x$$
 at $x = 1, y = 1$ (0) $\frac{dy}{dx} = y^2 \sin x$ with $\frac{y}{x} = 1$
Then find $\frac{y}{x} = 2$

$$y = \chi^3 - \chi^2 + c$$

$$(c-1)$$

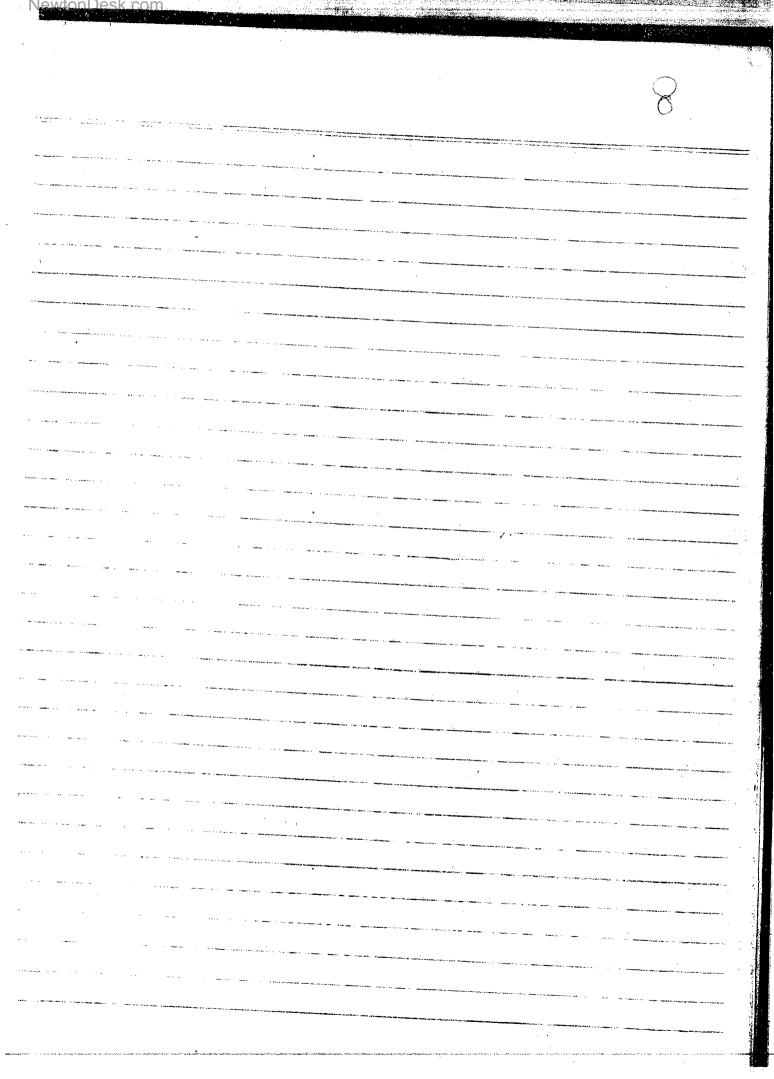
If the equation contains the terms like cos(ny), sin(n+y), Cantby+()², etc. can be reduced to variable separable form with a substitution
$$xy = v$$
, $x+y=v$, antbyte= v resp.

(1)
$$\frac{dY}{dn} = \frac{(4n+4+1)^2}{dn} = \frac{dV}{dn} = \frac{V^2}{(4+V^2)}$$

$$\frac{dV}{(4+v^2)} = \int dx$$

$$\frac{1}{2} = \frac{4\pi}{2} + C$$

Homogeneous diff method -	
$\frac{dV}{dx} = E(X, V)$	
dy = F(N,1) is said to be homogeneous difference of equal of F(N,1) should be a homogeneous function of degree zero.	 14
Note - En Mont. Noty = 0 is said to homogeneous diff. egn if all the terms of M FN should be of same degree.	
Substitution $y = vx$ or $x = vy$ reduces homogeneous ean to variable separation form.	parameter and the second
$\frac{dy}{dx} = \frac{x^2 y - y^3}{ay^2} = \frac{x^8 (y_a - (y_a)^3)}{x^6 (y_b)^2}.$	»-e
Every homogeneous for of degree zero can be written as for of You or ally foundstitution reduction it to variable separation form.	ول



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xd4 = 4flogy - loga + 1)		
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Ju y Flogry 3 + 17	e de servicio de la companione de la compa	
$\frac{dy}{dx} = \frac{y}{x} \left[\frac{\log(y)}{2} + 1 \right]$	en e	
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log v=t.		
+ dv = dt		and the second second second second second
	and the second seco	and the second second
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the second secon		and the second second second second
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The same	-	

$$\frac{dy}{dx} = \frac{a_1x + b_1y + c_1}{a_2x + b_2y + c_2}$$

case 1:-
$$\frac{a_1-b_1}{a_2-b_2}$$

case II:
$$\begin{bmatrix} a_1 + b_1 \\ a_2 \end{bmatrix}$$

$$\frac{dy}{dx} = \frac{a_1(x+h) + b_1(y+k) + q}{a_2(x+h) + b_2(y+k) + q}$$

				·
0	(22+24	-1)dx =	= (x+°	1+1) d7
	Ja. 9	Ind)		. and

$$\frac{dy}{dx} = \frac{2x+2y-1}{2x+y+1} \qquad \left(\begin{array}{c} a_1 - b_1 \\ a_2 - b_2 \end{array}\right)$$

$$\frac{dy}{dx} = \frac{dv}{dx} - 1$$

$$\frac{dV-1}{da} = \frac{2V-1}{V+1}$$

$$\frac{dv}{dx} = \frac{2V - 1 + V + 1}{V + 1} = \frac{0}{V} \frac{3V}{V + 1}$$

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	dy		4+11-2		A_	1		, V-S	CAIL	7

$$\chi = \chi - 1$$
, $\chi = \chi + 3$

(8) (9) 2=x+h, y=x+k reduces
$$\frac{dy}{dx} = \frac{1+x-2}{y-x-4}$$

to homo form then find h, k.

Ans.
$$h = -1$$
, $16 = 3$

(b)
$$\frac{d^2y}{dx^2} + (h+3)\frac{dy}{dx} + (K+1)\frac{y}{50}$$

Exact differential earl	
Mdx + Ndy = 0	
an even litterential egn Mdx + Ndy = 0 is soud to be	
different en maria ser	
e-g. 12 da + 22/d1=0	
d[x12]= 42d4+221dj	
The DE Month Not =0 is exact => am = and	
Mar Notice Fraul in (am - on)	
[man + [Reterms of N without 2) dy	
Eate 4'	
D Property Property of the Pro	
3M - Q (67X - 51)) //	

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pohr-(1+ sin2y+cos2x)d1=0 is exact then find p

- 3) (302 12 + by cosx) dn + (20inn 4973) dy 50 is exact then
 - a Exactness depends on both a and b
 - @ Enacthers depends only on a
- © Exactness depends only on b
- @ Exactness not depends on both at b

$$\frac{\partial \lambda}{\partial w} = -2i \frac{\partial \lambda}{\partial w} + \left(1+\frac{1}{2}\right) \qquad \frac{\partial w}{\partial w} = 1+\frac{1}{2} - 2i \frac{\omega}{2}$$

$$\int (y + \frac{y}{x} + \cos y) dx + \int o dx = c$$

$$\frac{3N}{9N} = 1$$
 $\frac{3N}{9N} = -1$

Integrating factor.

A non exact eqn is converted to the exact by multiplying it with a function f(x,y). Then f(x,y) is called integrating factor.

$$ydx - xdy = 0$$

| I.F.

| 1
| 1
| 1
| 2
| x^2 | x

A constant multiple of an integrating factor is calso an integrating factor.

Mda + Ndy=0

Non exact eqn (i.e. $\frac{\partial M}{\partial y} \neq \frac{\partial W}{\partial x}$)

il All terms of in and N should be of same degree

$$IF = \frac{1}{Mx + Ny} \qquad (Mx + Ny \neq 0)$$

ii) The egn is of the ferm

	3M 3M : 180 AND 1900	
	$\int \int \int (\mathbf{d}) dx$	
¥.;	DA DE AND MADE AND THE CONTROL OF TH	er e
	IF = e	
<i>I.</i>)	Inspection method.	and the second s
Mole	A non-exact homogeneous differential converted to exact by multiply	egn mdxindy
Q	Find integrated factor of	The second secon
no se manualle	(472 27182 + (243 + 274 - 42) de o	
	$\frac{\partial M}{\partial y} = 443 + 2 \qquad \frac{\partial N}{\partial x} - 4^3 - 4$	
Annual metallic state of the st		-3(49+2) = -3

		, .	93
	7(M)	SFCNIda e	
	2	. χ	
1.	2	22	
	3	1 3	
	- <u>1</u>	x = 1/2	
And the second s	-2/2	$\chi^{-2} = 1/\chi^2$	
O y(1- (xy) da - 2 M2-N4 =	31- x212+ 2c1+x212	The second secon
	IF =	o with 1/14	
<u> 4</u>	(1-24) dn	x(1+x4) d7 20	
	(- y) dn -	$-\int \frac{1}{4} d7 = c$	
	Jog x/4	_	

er dy e	7 - NE	<u>146</u> 28		
			A Section of the sect	u
<i>y</i>	$TF = \frac{1}{x^2 + dx}$ $\frac{x^2 + dx}{1 + x^3 + y^3}$ $\frac{x^3 + y^3}{2}$)dj = 0	7	
	$\frac{x^2}{4n+\frac{x^3}{4n+x^$			
	$\frac{-14}{\sqrt{3}}$	to the second		
		94 - C		

$$\frac{4dx-xdy}{x^2} + \frac{(1+x)}{x^2} \frac{dx}{dx} + \frac{2c^2\cos y}{2c^2} \frac{dy}{dx} = 0$$

$$\int \frac{d\left[-\frac{y}{x}\right]}{x^2} + \int \left(\frac{1}{x^2} + \frac{1}{x}\right) dx + \int \cos y \, dy = 0$$

$$-\frac{1}{x} - \frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^2} + \sin y = C$$

multiply with
$$\frac{1}{4}$$

$$\frac{y dx - x dy}{xy} + \frac{(y^2 + y) x dy}{xy} + \frac{x + e^{1} dy}{xy} = 0$$

Ne	wto	nDes	k	CO	m
1 10	4417		11 \ .	$\mathcal{U}\mathcal{U}$	-

* Yde ad 12 Add c	
multiply with /ay	
ydnindi nyedn = o	
$\int d(\log(ny)) + \int d^{n}dn = 0$	المنافقة الم
log (24) + e (2-1) = c	
	and the second s
· Linear differential ears -	and the second s
The differential eqn is soud to if it satisfies the following two conditions: i) The dependent variable and all it's derivation be of 1st degree only it. (4') (dy) (d ² y)!	di
ii) There is no product of the dependent varia	uble and
(1d1) dy glad dn) da dn2 /	
and the second of the second	, in a second second of the constant

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$$\frac{*}{dx^2} + \frac{3d^4}{dx} + \frac{xy}{x} = \frac{x^3}{2}$$

-> Linear

The ear containing for of dependent variable is not linear in that variable.

-e-g.

$$\frac{d^2y}{dx^2} + \frac{3dy}{dx} + xe^{\frac{1}{2}} = x^3$$

Non-linear

* Linear in y -

 $\frac{dy}{dx} + py = q$ $sol \int P \text{ and } Q \text{ are } f^{n} \text{ of } \lambda' \text{ or constaint}.$

* Lines in X -

$$\frac{dx}{dy} + px = 0$$

$$\frac{dy}{dy} \cdot p \text{ and } cy \text{ are } f^{n} \circ f^{n} = 0$$

$$\frac{dy}{dy} \cdot p = 0$$

$$\frac{dY}{dx} + \frac{y}{x} = \frac{x^3}{x^3} \cdot x \cdot dx + c = \int \frac{x^3}{x^3} \cdot dx + c$$

$$y_{1} = \frac{x_{5}}{6} + c$$
of $y(1) = 6/6$



16

*
$$\frac{dy}{dx}$$
 + $\frac{dy}{dx}$ + $\frac{dy}{dx}$

$$\frac{d\gamma}{dx} \approx \frac{1}{x} \left(\frac{x \sin x + \cos x}{x \cos x} \right) \frac{y}{x} = 1$$

$$\frac{dy}{dx} + \left(\frac{\tan x + \frac{1}{4}}{2\cos x}\right) = \frac{1}{2\cos x}$$

$$x$$
 $\frac{d!}{dx} + \frac{2xy}{2} = \frac{2 + \log x}{2}$ with $y(1) = 0$ then find $y(2) = 0$ then $y(3) = 0$

$$\frac{dt}{dx} + \frac{24}{2} - \frac{21094}{x^3}$$

$$\int \frac{dx}{dx} = \frac{12}{x^2} \frac{dx}{dx}$$

$$= \frac{12}{x^2} \frac{dx}{dx}$$

	···	
	2 logn=t => ydn=dt	er e agai
	2º1= 12tdr +c	
	A.K.	remarkas skilling
	ney = et +c	- '
	224 = (-109x)2+C	
	→ C=0	
		Comment of the same
e meninin a ada	$x^{2}y = (\log x)^{2}$	Marie de partira de la companya
	when x=e then	
	e ² y= 1	White continues to the continues of the
a ta	$\frac{1}{1-y} = e^{2y}$	min attraction and an action of the second
*	(x+2y3) dy = 1 with $a(1)=0$	
	$\frac{1-dq}{dx} + \frac{2q^3dy}{dx} = \frac{q}{2}$ $\frac{1}{2} \frac{1}{2} \frac{1}$	
The second	1 dr 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	

$$\frac{x}{y} = \frac{y^2 + c}{y}$$

$$ye^2 = \frac{2q}{2} + c$$

$$y(0) = 1$$

+ Ber	noullis diff	erential	egn:			
	dy p	j=qy	(O) + 1	inear if	Meo.	
	82° 1)	P and	a are	fnof	ж (ar) С	ionstanti
	yi-n e f((-n)	र्वेष	(1-n) Q 6	J(1-n)p	dx +c	
	£		11-n V]. St	ubstitution)
1	substitu!	yFh	=V re	duces	Bernoulli	s egn to
GATE P eqn	45		$\frac{y^{1-n}}{y} = v$ to c $\frac{to}{req}$			non-linear
	dy Iv	£300				
	de 2 e ftdt		29 x tro	120		
g garagag untergraphings and the second	and the second s	and the second of the second o	anga matau and di dada kana kana manada anga si Anga ya wanawa sangiya k	ia uma ya iya iyayungan na na niyunaga gaari madaada 🍾		And the common substantial section 2000 and the common of

$$\frac{1}{1-n} \frac{dv}{dn} + PV = 0$$

$$\frac{dv}{dx} + \frac{(1-n)pv}{} = \frac{(1-n)q}{}$$

9. Which of the following substitution reduces the non-linear egn
$$x dy$$
 $x^2y^2 = x^3y^3$ to linear dy form?

$$\frac{dx}{dy} + \frac{xy^2 - x^2y^3}{}$$

$$\frac{dy - y + anx = -y^2 secx}{dx}$$
 with $y(0) = 1$

$$\int (1-2) (-\tan x) dx \qquad \log \sec x$$

$$= e \qquad = \sec x$$

$$Y^{-2} = \int (1-2) (-seca) (seca) da + c$$

$$\frac{x}{y}\frac{dy}{dx} + \log y = xe^x$$

$$\chi \frac{dv}{dx} + v = \chi e^{\eta}$$

$$\frac{dv}{dn} + \frac{1}{2}V = e^{2}$$

$$\int \frac{1}{x} dx = x$$

$$V \cdot \chi = \int e^{x} x dx + c$$

$$N(09y = e^{x}(x+1) + c$$

*	Clairauts eg
	$\frac{y-x}{dx}+\frac{f}{dx}$
. .	y = px + f(p) where $p = dy$
e e	Directly replace dy by c'
علق المناسب بي المناسب المناسب	Y = Cx + f(c)
*	$\left(y-\alpha\frac{dy}{dx}\right)\left(\frac{dy}{dx}\right) = \frac{dy}{dx}$
	1-ny' = y' y'-1
	y = y' + xy'
	y = cx + c

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*
$$p = \sin(y - \pi p)$$
 where $p = dy$

$$\frac{d^n y}{dx^n} + k_1 \frac{d^{n-1} y}{dx^{n-1}} + \cdots + k_{n-1} \frac{d^1}{dx} + k_n y = x$$

$$D = \frac{d}{dx}$$

$$D^{2} = \frac{d^{2}}{dx^{2}}$$

$$D^{3} = \frac{d^{3}}{dx^{3}}$$

$$\Rightarrow e \cdot g \cdot D \cdot e^{\frac{2M}{2}} = 2e^{\frac{2M}{2}}$$

$$\downarrow \qquad \qquad \downarrow \qquad$$

$$(D^{n} + KD^{n-1} + \cdots + BD + Kn + D + Kn) y = X$$

$$F(D) Y = X \qquad F(D) = \int_{1}^{h} k_{1}D + \cdots + k_{n}D + k_{n}$$

$$f^{h} \circ f \circ differential}$$
operator

Tie	complete				ege ox		
(****)		omple	Mentay	7 + 1		integro	Ą)

- O If X=0 then F(D) c = relied homogeneous invent differential eggs
- (3) If x \pm 0 the FCD y= x is radied nonhomogeneous a differential eq.?
- (9) The solution of homogeneous linear differential eqn F(D) y=0 is called complementary for.

The no of arbitrary constants in the complementary for should be equal to the order of given differential egn.

- 1) The particular integral of FLDY= X is
 - PI = [| PI will not contain)

 F(D) | X any arbitrary constants
- @ If x=0 then complete som of the given eqn is only complementary function.
- (7) By assuming D' as an algebric an quantity

 E(D)=0 becomes an algebric egns

 And is called Awillian eggs

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roots based on nature of this roots we write the CF as follows:

Nature of roots	CF
Real and distinant D=11,112,113	$CF = Ge + C_2e^2 + C_3e^3$
) Real f repeated D= m, M,	$CF = (C_1 + C_2 x) e^{iM_1 x}$
3 Complex & distinct D = Atib	$CF = e^{qn} [q cosba + c_2 sinba]$
D=atib, atib	$CF = e^{\alpha N} \left[(C_4 + C_2 N) \cos b N + (C_8 + C_4 N) \sin b N \right]$
3) Surds (Real no.) at Jb	$CF = QR \qquad (q-Jb)M$ $CR \qquad$

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Roots CF= Ge + Ge + Cze D=1,-1/2,2 CF = GEM + (G+Gx)=2M D=2/-2/-2 CF = e [q cossx + 6 sin3x] + c, e 13 D=2131, } CF = Ge + C2e + [C3 COS2N+ C4 SIN2N] D= ±21, ±4 $\frac{d^2y}{dx^2} = \frac{5}{dx} + \frac{6y}{4x}$ D4-168)4=0 $D^2 - 5D + 6 = 0$ D4- 160 =0 D = +3 D = +2CF=q=+ Cg=21x. 000= 36 $(\mathfrak{D}^2-4)(\mathfrak{D}^2+4)=0$ D=2,-2, 121 CF = Ge + Ge + [G CORM+ GSin

$$\frac{1}{2} \frac{d^2y}{dx^2} + \frac{2pdy}{dx} + \frac{(p^2+q^2)y}{dx} = 0$$

$$D^2 + 2PD + (p^2 + q^2) = 0$$

$$D_{1}, D_{2} = -2P \pm \sqrt{4P^{2} - 4P^{2} - 4Q^{2}} = -2P \pm \sqrt{-49^{2}}$$

$$= -29 \pm 291$$

$$\mathcal{D}_{1,1}\mathcal{D}_{2} = -P \pm qi$$

Note!

If $y=qy_1+c_2y_2+c_3t_3+---$ is the complete solution of homogeneous differential ear Faby = e then each one of $d_1, d_2, d_3, ---$ is linearly independent solution of the homogeneous of linear differential ear Faby = 0.

que y, y2 are linearly independent solut of the corresponding linearly independent solut of the corresponding linearly independent solution of FCD7=x then y, is a solution of the following eggs

$$G F(9)y=X V G F(9)y=0$$

CH = Qunisin Sasanai

Similar cossis are linearly independent with

18t = C

 $= \sum_{i=1}^{n} \hat{j}_{i} \left[\hat{j}_{i} \right] = 0$

... (N' <u>19)1 30</u>

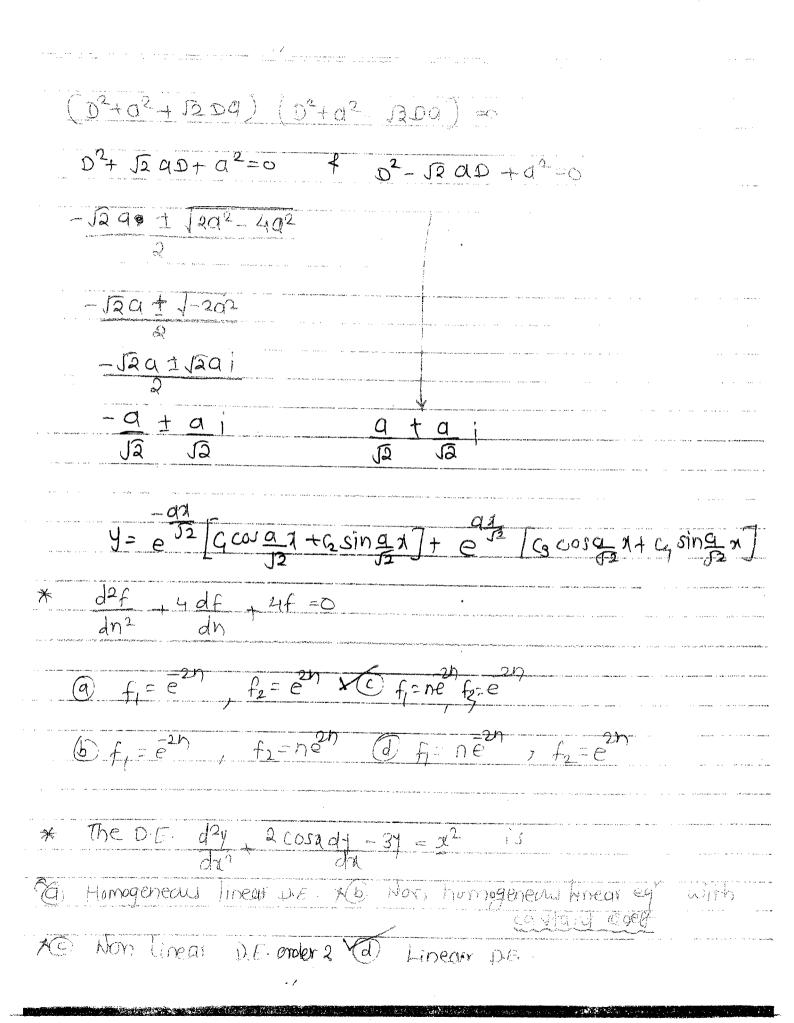
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$$D_3 + D_5 + D + 1 = 0$$

$$D_{\overline{D}} = 0 \quad \text{if } D_{\overline{D}} = -1 \quad \text{if } D_{\overline{D}} = -1$$

$$(D^2 + \alpha^2)^2 - 2D^2\alpha^2 = 0$$



The solv of
$$\frac{d^2i}{dt^2} + \frac{R}{L} \frac{di}{dt} + \frac{i}{Lc} = 0$$
 where $R^2c = 4L$

$$D^{2} + RD + 1 = 0$$

$$R + R^{2} + 4$$

$$D_{1}, P_{2} = \frac{-\frac{P}{L} \pm \sqrt{\frac{P^{2}}{L^{2}} + \frac{4}{L^{2}}}}{Q}$$

$$= -\frac{R}{L} + \int \frac{R^2C - 4L}{L^2C}$$

$$= -\frac{R}{L} + 0$$

$$P_{1}, P_{2} = \frac{-R}{2L}, \frac{-R}{2L}$$

$$\frac{-Pt}{1-y} = \frac{-Pt}{1-y} + \frac{-Pt}{1-y}$$

$$d^{2}y + ddy + 13y = 0$$
 $dx^{2} + dx$
with $y(0) = 0 + 4$

$$D_{1}, D_{2} = \frac{4 \pm 61}{2}$$

$$y = e^{-2\pi} [q \cos 3x + c_2 \sin 3x]$$

at
$$x=0$$
, $y=0 \Rightarrow q=0$

$$y = c_0 e^{-2x}$$
 sin3x

$$\frac{7}{3} = \frac{21}{3} \sin 31$$

$$\frac{1}{2}$$
 $\frac{9 d^2 4}{dx^2}$ $\frac{6 d4}{dx}$ $\frac{4}{3}$ $\frac{4}{3}$ $\frac{9 d^2 4}{dx^2}$ $\frac{6 d4}{dx}$ $\frac{4}{3}$ $\frac{1}{3}$ $\frac{1}{3}$

-->

$$y(0) = 3 \implies 3 = q$$

$$y' = C_1 \left[\frac{3}{3} e^3 + e^{3/3} \right]$$

$$\lambda = (3 + 0x) = 3$$

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* d/	9				<u> </u>					
(á s				3)[12]			
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Linked

1)* The complete som of the differential egn
$$\frac{d^2y}{dx^2} + \frac{pdf}{dx} + \frac{qy}{dx} = 0$$
 is $y = \frac{e^2f}{6} + \frac{e^{3d}}{6} +$

Particular	r integral				an and the second
	FCD)d=	X	The second secon	e Table of the second of the	.=
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constant	cospx	poly.ir) 7	singn, cosbx,	The same of the sa
Case 1 -	X=e	or conste	int		
	$PT = \begin{bmatrix} 1 \\ F(D) \end{bmatrix}$] da =	1 e F(a)	(where	F(a) \$0)
	Replace 'D'	by a' in fn	f(D)		The second secon
1 f	f(a) =0	then	gara yangganganakan ke sasah, memperahangan kepada sinak barasa berasa d		
	PI = X	J K COCCE	<u>΄</u> γ'(D)] e'	1 1	
	Replace	D' 67 'C'	in f'(<u>D)</u>	
	PI =	$2\left[\frac{1}{F'(a)}\right]$	1e (F(a) + 0)	

if
$$F'(\alpha)=0 \Rightarrow PI = x^2 \left(\frac{1}{F''(\alpha)}\right) e^{dx} \left(\frac{F''(\alpha) \neq 0}{F''(\alpha)}\right)$$

The p.1. of dey rady
$$\frac{1}{2}$$
 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

$$PI = \frac{1}{0^{2} + 2D + 7} = \frac{1}{0^{2} + 2(-2) + 7} = \frac{1}{0^{2} + 2D + 7} = \frac{1$$

$$PI = \frac{e^{2\pi}}{7}$$

* PI of
$$\frac{d^2y}{dt^2} - \frac{9}{9} = \frac{8}{3} + \frac{3}{4}$$

$$PI = \frac{1}{D^2 - g} \left(e^{3t} + 3e^{3t} \right) = \frac{1}{D^2 - g}$$

$$= x \left(\frac{1}{2D}\right) e^{3x} + 3 \frac{1}{6} e^{-9}$$

$$=\frac{\chi e^{34}}{6}+\frac{3}{-9}$$

$$PI = \frac{\chi e^{31} - 1}{6}$$

$$P2 - \left[\frac{1}{0^2 + 4D + 4}\right]^{\frac{2}{6}} = 2\left(\frac{1}{2D + 4}\right)^{\frac{2}{6}} = 2^{\frac{2}{6}} \left(\frac{1}{2}\right)^{\frac{2}{6}}$$

$$\chi = singn(a) cosba (sin(ax+b) or cos(ax+d)$$

$$PI = \begin{bmatrix} 1 \\ F(D) \end{bmatrix} singx = \begin{bmatrix} 1 \\ F(-a^2) \end{bmatrix} singx (F(-a^2))$$

$$PT = a \left[\int Slnqn = x Sinqn \right]$$

$$Explace y^{2} by -a^{2} in F'(0)$$

$$PI = \frac{1}{D^4 + D^2 + 3} = \frac{1}{(-q)^2 + (-q) + 3} = \frac{1}{(-q)^2 + (-q) + 3}$$

* FI of
$$\frac{d^{2}1}{dx^{2}} + 4y = \cos(2x+4) + e^{x}$$

$$PI = \frac{1}{D^2 + 4} \left(\cos(2u + 4) + e^{24} \right)$$

$$= \chi \left(\frac{1}{20'}\right) \cos(2x+44) + \frac{1}{(-2)^2+24} = \frac{-2x^2}{(-2)^2+24}$$

$$= \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{8}$$

$$PL = \frac{x \sin(2x) + 4}{4} + \frac{e^{-24}}{8}$$

* PI of
$$\frac{d^{3}y}{dx^{3}} + \frac{d^{2}y}{dx^{2}} + \frac{2}{2}\frac{d^{2}y}{dx} + \frac{2}{2}y = \sin x$$

$$PI = 1 \qquad Sinx$$

$$D^3 + D^2 + 2D + 2$$

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$$= \frac{1}{2} \left[1 - \left(\frac{D^2 + 2D}{2} \right) + \left(\frac{D^2 + 2D}{2} \right)^2 - \right] (N^2 + 2)$$

$$= \frac{1}{2} \left[x^2 + 2 - 1 - 2x + 2 \right]$$

$$\frac{1}{2} + \frac{1}{2} = \frac{1^2 - 2x + 3}{2}$$

* PI of
$$\frac{d3y}{dx^3} + \frac{3d^2y}{dx^2} = \frac{x^3+3x}{x^3+3x}$$

$$PI = \frac{1}{D^3 + 3D^2} \left(\dot{\chi}^3 + 3\chi \right) = \frac{1}{3D^2 \left[1 + \frac{D^3}{3D^2} \right]}$$
 (1³+3 χ)

$$= \frac{1}{3D^2} \left[1 + \frac{D}{3} \right] - (x^3 + 31)$$

$$= \frac{1}{30^2} \frac{[1-\frac{D}{3} + \frac{D^2}{9} - \frac{D^3}{9} - -](u^3 + 3u)}{3}$$

$$= \frac{1}{30^2} \left[\chi^3 + 3\chi^2 - 1 + \frac{6\chi}{9} - \frac{6}{87} \right]$$

$$= \frac{1}{3D^2} \left[\frac{\chi^3 - \chi^2 + 33\chi - 33}{9} - \frac{1}{3D^2} \left[\frac{\chi^3 - \chi^2 + 11\chi - 11}{3} \right] \right]$$

$$\frac{1}{3} \begin{bmatrix} \frac{1}{10} & \frac{1}{10} & \frac{1}{10} \\ \frac{1}{10} & \frac{1}{10} & \frac{1}{10} \end{bmatrix}$$

* Code
$$D$$
 : $X = e^{-V}$

PI = $\begin{bmatrix} 1 \\ e^{-V} \end{bmatrix} = e^{A} \begin{bmatrix} 1 \\ e^{-V} \end{bmatrix} V$

Replace D' by ' $D+Q'$ in $F(D)$

The if $V = sinble or codes by the sinble of the sinble of$