# Package 'markovchain'

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Type Package

Title Easy Handling Discrete Time Markov Chains

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**Author** Giorgio Alfredo Spedicato [aut,cre], Tae Seung Kang [aut], Sai Bhargav Yalamanchi [aut], Mildenberger Thoralf [ctb], Deepak Yadav [ctb], Nacho Cordón Castillo [ctb], Vandit Jain [ctb]

Maintainer Giorgio Alfredo Spedicato <spedicato\_giorgio@yahoo.it>

**Description** Functions and S4 methods to create and manage discrete time Markov chains more easily. In addition functions to perform statistical (fitting and drawing random variates) and probabilistic (analysis of their structural proprieties) analysis are provided.

License GPL-2

**Depends** R (>= 3.2.0), methods

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markovchain-package Easy Handling Discrete Time Markov Chains

### **Description**

The package contains classes and method to create and manage (plot, print, export for example) discrete time Markov chains (DTMC). In addition it provide functions to perform statistical (fitting and drawing random variates) and probabilistic (analysis of DTMC proprieties) analysis.

#### **Details**

Package: markovchain
Type: Package
Version: 0.6.5.2
Date: 2016-12-08
License: GPL-2

Depends: R (>= 3.2.0), methods, expm, matlab, igraph, Matrix

### Author(s)

Giorgio Alfredo Spedicato Maintainer: Giorgio Alfredo Spedicato <spedicato\_giorgio@yahoo.it>

# References

Discrete-Time Markov Models, Bremaud, Springer 1999

# Examples

4 absorbingStates

```
mcD<-new("markovchain", transitionMatrix=matrix(c(0,1,0,1), nrow=2,byrow=TRUE))

#operations with S4 methods

mcA^2
steadyStates(mcB)
absorbingStates(mcB)
markovchainSequence(n=20, markovchain=mcC, include=TRUE)</pre>
```

absorbingStates

Various function to perform structural analysis of DTMC

# **Description**

These functions return absorbing and transient states of the markovchain objects.

# Usage

```
absorbingStates(object)

transientStates(object)

## S4 method for signature 'markovchain'
transientStates(object)

canonicForm(object)

communicatingClasses(object)

recurrentClasses(object)

period(object)
```

# Arguments

object A markovchain object.

# Value

vector, matrix or list

# Author(s)

Giorgio Alfredo Spedicato

blanden 5

### References

Feres, Matlab listing for markov chain.

### See Also

markovchain

### **Examples**

```
statesNames <- c("a", "b", "c")
markovB <- new("markovchain", states = statesNames, transitionMatrix =</pre>
                                                                                      matrix(c(0.2, 0.5, 0.3,
                                                                                                                                       0, 1, 0,
                                                                                                                                0.1, 0.8, 0.1), nrow = 3, byrow = TRUE,
                                                                                                                                dimnames = list(statesNames, statesNames)
                                                               ))
communicatingClasses(markovB)
recurrentClasses(markovB)
absorbingStates(markovB)
transientStates(markovB)
canonicForm(markovB)
# periodicity analysis : 1
\label{eq:energy_energy} \texttt{E} < \texttt{-} \ \mathsf{matrix}(\texttt{c}(\texttt{0}, \ \texttt{1}, \ \texttt{0}, \ \texttt{0}, \ \texttt{0}.5, \ \texttt{0}
                                                       nrow = 4, ncol = 4, byrow = TRUE)
mcE <- new("markovchain", states = c("a", "b", "c", "d"),</pre>
                                             transitionMatrix = E,
                                             name = ^{"}E")
 is.irreducible(mcE) #true
period(mcE) #2
# periodicity analysis : 2
myMatr \leftarrow matrix(c(0, 0, 1/2, 1/4, 1/4, 0, 0,
                                                                                       0, 0, 1/3, 0, 2/3, 0, 0,
                                                                                       0, 0, 0, 0, 0, 1/3, 2/3,
                                                                                      0, 0, 0, 0, 0, 1/2, 1/2,
                                                                                      0, 0, 0, 0, 0, 3/4, 1/4,
                                                                                      1/2, 1/2, 0, 0, 0, 0, 0,
                                                                                       1/4, 3/4, 0, 0, 0, 0, 0), byrow = TRUE, ncol = 7)
myMc <- new("markovchain", transitionMatrix = myMatr)</pre>
period(myMc)
```

6 conditional Distribution

### **Description**

This table show mobility between income quartiles for father and sons for the 1970 cohort born

### Usage

```
data(blanden)
```

#### **Format**

An object of class table with 4 rows and 4 columns.

### **Details**

The rows represent fathers' income quartile when the son is aged 16, whilst the columns represent sons' income quartiles when he is aged 30 (in 2000).

#### Source

Personal reworking

#### References

Jo Blanden, Paul Gregg and Stephen Machin, Intergenerational Mobility in Europe and North America, Center for Economic Performances (2005)

# **Examples**

```
data(blanden)
mobilityMc<-as(blanden, "markovchain")</pre>
```

```
conditionalDistribution
```

 ${\tt conditionalDistribution}\ of\ a\ Markov\ Chain$ 

# **Description**

It extracts the conditional distribution of the subsequent state, given current state.

# Usage

```
conditionalDistribution(object, state)
```

# Arguments

object A markovchain object. state Subsequent state. craigsendi 7

# Value

A named probability vector

### Author(s)

Giorgio Spedicato, Deepak Yadav

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

markovchain

# **Examples**

craigsendi

CD4 cells counts on HIV Infects between zero and six month

# **Description**

This is the table shown in Craig and Sendi paper showing zero and six month CD4 cells count in six brakets

# Usage

```
data(craigsendi)
```

### **Format**

```
The format is: table [1:3, 1:3] 682 154 19 33 64 19 25 47 43 - attr(*, "dimnames")=List of 2 ..$: chr [1:3] "0-49" "50-74" "75-UP" ..$: chr [1:3] "0-49" "50-74" "75-UP"
```

# **Details**

Rows represent counts at the beginning, cols represent counts after six months.

### Source

Estimation of the transition matrix of a discrete time Markov chain, Bruce A. Craig and Peter P. Sendi, Health Economics 11, 2002.

### References

see source

### **Examples**

```
data(craigsendi)
csMc<-as(craigsendi, "markovchain")
steadyStates(csMc)</pre>
```

createSequenceMatrix Function to fit a discrete Markov chain

### Description

Given a sequence of states arising from a stationary state, it fits the underlying Markov chain distribution using either MLE (also using a Laplacian smoother), bootstrap or by MAP (Bayesian) inference.

### Usage

```
createSequenceMatrix(stringchar, toRowProbs = FALSE, sanitize = FALSE,
   possibleStates = character())

markovchainFit(data, method = "mle", byrow = TRUE, nboot = 10L,
   laplacian = 0, name = "", parallel = FALSE, confidencelevel = 0.95,
   confint = TRUE, hyperparam = matrix(), sanitize = FALSE,
   possibleStates = character())
```

### **Arguments**

stringchar

toRowProbs	converts a sequence matrix into a probability matrix
sanitize	put 1 in all rows having rowSum equal to zero
possibleStates	Possible states which are not present in the given sequence
data	A character list.
method	Method used to estimate the Markov chain. Either "mle", "map", "bootstrap" or "laplace"
byrow	it tells whether the output Markov chain should show the transition probabilities

Equivalent to data. It can be a nx2 matrix or a character vector or a list

by row.

nboot Number of bootstrap replicates in case "bootstrap" is used.

createSequenceMatrix 9

laplacian Laplacian smoothing parameter, default zero. It is only used when "laplace"

method is chosen.

name Optional character for name slot.

parallel Use parallel processing when performing Boostrap estimates.

confidencelevel

 $\alpha$ 

level for conficence intervals width. Used only when method equal to "mle".

confint a boolean to decide whether to compute Confidence Interval or not.

hyperparam Hyperparameter matrix for the a priori distribution. If none is provided, default

value of 1 is assigned to each parameter. This must be of size kxk where k is the number of states in the chain and the values should typically be non-negative

integers.

#### Details

Disabling confint would lower the computation time on large datasets. If data or stringchar contain NAs, the related NA containing transitions will be ignored.

#### Value

A list containing an estimate, log-likelihood, and, when "bootstrap" method is used, a matrix of standards deviations and the bootstrap samples. When the "mle", "bootstrap" or "map" method is used, the lower and upper confidence bounds are returned along with the standard error. The "map" method also returns the expected value of the parameters with respect to the posterior distribution.

#### Note

This function has been rewritten in Rcpp. Bootstrap algorithm has been defined "euristically". In addition, parallel facility is not complete, involving only a part of the bootstrap process. When data is either a data. frame or a matrix object, only MLE fit is currently available.

### Author(s)

Giorgio Spedicato, Tae Seung Kang, Sai Bhargav Yalamanchi

# References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

Inferring Markov Chains: Bayesian Estimation, Model Comparison, Entropy Rate, and Out-of-Class Modeling, Christopher C. Strelioff, James P. Crutchfield, Alfred Hubler, Santa Fe Institute

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

#### See Also

markovchainSequence, markovchainListFit

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### **Examples**

ctmc-class

Class "ctmc"

### **Description**

The S4 class that describes ctmc (continuous time Markov chain) objects.

### **Objects from the Class**

Objects can be created by calls of the form new("ctmc", states, byrow, generator, ...).

#### Slots

```
states: Name of the states. Must be the same of colnames and rownames of the generator matrix byrow: Binary flag.
generator: Square generator matrix
name: Optional character name of the Markov chain
```

# Methods

```
dim signature(x = "ctmc"): method to get the size
initialize signature(.Object = "ctmc"): initialize method
states signature(object = "ctmc"): states method.
steadyStates signature(object = "ctmc"): method to get the steady state vector.
```

### Warning

Validation method is used to assess whether either columns or rows totals to zero. Rounding is used up to 5th decimal. If state names are not properly defined for a generator matrix, coercing to ctmc object leads to overriding states name with artificial "s1", "s2", ... sequence

#### Note

ctmc objects are written using S4 Classes.

ctmcFit 11

### Author(s)

Sai Bhargav Yalamanchi, Giorgio Spedicato

#### References

Introduction to Stochastic Processes with Applications in the Biosciences (2013), David F. Anderson, University of Wisconsin at Madison

### See Also

generatorToTransitionMatrix,rctmc

### **Examples**

ctmcFit

Function to fit a CTMC

### **Description**

This function fits the underlying CTMC give the state transition data and the transition times using the maximum likelihood method (MLE)

### Usage

```
ctmcFit(data, byrow = TRUE, name = "", confidencelevel = 0.95)
```

### **Arguments**

states. The second is a numeric vector denoting the corresponding transition

times.

byrow Determines if the output transition probabilities of the underlying embedded

DTMC are by row.

name Optional name for the CTMC.

confidencelevel

Confidence level for the confidence interval construnction.

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# **Details**

Note that in data, there must exist an element wise corresponding between the two elements of the list and that data[[2]][1] is always 0.

### Value

It returns a list containing the CTMC object and the confidence intervals.

# Author(s)

Sai Bhargav Yalamanchi

### References

Continuous Time Markov Chains (vignette), Sai Bhargav Yalamanchi, Giorgio Alfredo Spedicato 2015

#### See Also

rctmc

# **Examples**

```
data <- list(c("a", "b", "c", "a", "b", "a", "c", "b", "c"), c(0, 0.8, 2.1, 2.4, 4, 5, 5.9, 8.2, 9))
ctmcFit(data)
```

firstPassage

First passage across states

# Description

This function compute the first passage probability in states

# Usage

```
firstPassage(object, state, n)
```

# Arguments

object A markovchain object

state Initial state

n Number of rows on which compute the distribution

# **Details**

Based on Feres' Matlab listings

fitHigherOrder 13

# Value

A matrix of size 1:n x number of states showing the probability of the first time of passage in states to be exactly the number in the row.

# Author(s)

Giorgio Spedicato

#### References

Renaldo Feres, Notes for Math 450 Matlab listings for Markov chains

# See Also

```
conditionalDistribution
```

# **Examples**

```
simpleMc <- new("markovchain", states = c("a", "b"), \\ transitionMatrix = matrix(c(0.4, 0.6, .3, .7), \\ nrow = 2, byrow = TRUE)) \\ firstPassage(simpleMc, "b", 20)
```

fitHigherOrder

Functions to fit a higher order Markov chain

# **Description**

Given a sequence of states arising from a stationary state, it fits the underlying Markov chain distribution with higher order.

# Usage

```
fitHigherOrder(sequence, order = 2)
seq2freqProb(sequence)
seq2matHigh(sequence, order)
```

# Arguments

sequence A character list.

order Markov chain order

# Value

A list containing lambda, Q, and X.

### Note

This function is written in Rcpp.

#### Author(s)

Giorgio Spedicato, Tae Seung Kang

#### References

Ching, W. K., Huang, X., Ng, M. K., & Siu, T. K. (2013). Higher-order markov chains. In Markov Chains (pp. 141-176). Springer US.

Ching, W. K., Ng, M. K., & Fung, E. S. (2008). Higher-order multivariate Markov chains and their applications. Linear Algebra and its Applications, 428(2), 492-507.

package version 0.2.5

#### See Also

markovchain

# **Examples**

fitHighOrderMultivarMC

Function to fit Higher Order Multivariate Markov chain

# Description

Given a matrix of categorical sequences it fits Higher Order Multivariate Markov chain.

### Usage

```
fitHighOrderMultivarMC(seqMat, order = 2, Norm = 2)
```

### **Arguments**

seqMat a matrix or a data frame where each column is a categorical sequence

order Multivariate Markov chain order. Default is 2.

Norm Norm to be used. Default is 2.

### Value

an homme object

### Author(s)

Giorgio Spedicato, Deepak Yadav

#### References

W.-K. Ching et al. / Linear Algebra and its Applications

# **Examples**

generatorToTransitionMatrix

Function to obtain the transition matrix from the generator.

# **Description**

The transition matrix of the embedded DTMC is inferred from the CTMC's generator.

# Usage

```
generatorToTransitionMatrix(gen, byrow = TRUE)
```

#### **Arguments**

gen The generator matrix.

byrow Flag to determine if rows (columns) sum to 0.

### Value

Returns the transition matrix.

# Author(s)

Sai Bhargav Yalamanchi

### References

Introduction to Stochastic Processes with Applications in the Biosciences (2013), David F. Anderson, University of Wisconsin at Madison

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### See Also

```
rctmc.ctmc-class
```

### **Examples**

HigherOrderMarkovChain-class

Class "HigherOrderMarkovChain"

# **Description**

The S4 class that describes HigherOrderMarkovChain objects.

holson

Holson data set

# Description

A data set containing 1000 life histories trajectories and a categorical status (1,2,3) observed on eleven evenly spaced steps.

# Usage

```
data(holson)
```

# **Format**

A data frame with 1000 observations on the following 12 variables.

```
id unique id
```

time1 observed status at i-th time

time2 observed status at i-th time

time3 observed status at i-th time

time4 observed status at i-th time

time5 observed status at i-th time

time6 observed status at i-th time

time7 observed status at i-th time

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```
time8 observed status at i-th time
time9 observed status at i-th time
time10 observed status at i-th time
time11 observed status at i-th time
```

#### **Details**

The example can be used to fit a markovchain or a markovchainList object.

#### **Source**

Private communications

#### References

Private communications

# **Examples**

data(holson)
head(holson)

hommc-class

An S4 class for representing High Order Multivariate Markovchain (HOMMC)

# Description

An S4 class for representing High Order Multivariate Markovchain (HOMMC)

# **Slots**

order an integer equal to order of Multivariate Markovchain states a vector of states present in the HOMMC model P array of transition matrices

Lambda a vector which stores the weightage of each transition matrices in P byrow if FALSE each column sum of transition matrix is 1 else row sum = 1 name a name given to hommc

# Author(s)

Giorgio Spedicato, Deepak Yadav

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### **Examples**

inferHyperparam

Function to infer the hyperparameters for Bayesian inference from an a priori matrix or a data set

### **Description**

Since the Bayesian inference approach implemented in the package is based on conjugate priors, hyperparameters must be provided to model the prior probability distribution of the chain parameters. The hyperparameters are inferred from a given a priori matrix under the assumption that the matrix provided corresponds to the mean (expected) values of the chain parameters. A scaling factor vector must be provided too. Alternatively, the hyperparameters can be inferred from a data set.

### Usage

```
inferHyperparam(transMatr = matrix(), scale = numeric(),
  data = character())
```

### **Arguments**

transMatr A valid transition matrix, with dimension names.

scale A vector of scaling factors, each element corresponds to the row names of the

provided transition matrix transMatr, in the same order.

data A data set from which the hyperparameters are inferred.

### **Details**

transMatr and scale need not be provided if data is provided.

# Value

Returns the hyperparameter matrix in a list.

is.accessible 19

### Note

The hyperparameter matrix returned is such that the row and column names are sorted alphanumerically, and the elements in the matrix are correspondingly permuted.

### Author(s)

Sai Bhargav Yalamanchi, Giorgio Spedicato

### References

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

### See Also

```
markovchainFit, predictiveDistribution
```

### **Examples**

is.accessible

*Verify if a state j is reachable from state i.* 

# Description

This function verifies if a state is reachable from another, i.e., if there exists a path that leads to state j leaving from state i with positive probability

# Usage

```
is.accessible(object, from, to)
```

#### **Arguments**

```
object A markovchain object.

from The name of state "i" (beginning state).

to The name of state "j" (ending state).
```

20 is.irreducible

# **Details**

It wraps an internal function named .commStatesFinder.

#### Value

A boolean value.

### Author(s)

Giorgio Spedicato

### References

James Montgomery, University of Madison

# See Also

is.irreducible

# **Examples**

is.irreducible

Function to check if a Markov chain is irreducible

# **Description**

This function verifies whether a markovchain object transition matrix is composed by only one communicating class.

# Usage

```
is.irreducible(object)
```

# Arguments

object

A markovchain object

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# **Details**

It is based on .communicatingClasses internal function.

### Value

A boolean values.

### Author(s)

Giorgio Spedicato

### References

Feres, Matlab listings for Markov Chains.

### See Also

summary

# **Examples**

kullback

Example from Kullback and Kupperman Tests for Contingency Tables

# **Description**

A list of two matrices representing raw transitions between two states

A list of two matrices representing raw transitions between two states

# Usage

```
kullback
data(kullback)
```

### **Format**

A list containing two 6x6 non - negative integer matrices

### **Source**

Kullback, Kupperman Tests for Contingency Tables Technometrics

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markovchain-class

Class "markovchain"

# **Description**

The S4 class that describes markovchain objects.

# **Objects from the Class**

Objects can be created by calls of the form new("markovchain", states, byrow, transitionMatrix, ...).

### **Slots**

```
states: Name of the states. Must be the same of colnames and rownames of the transition matrix byrow: Binary flag.

transitionMatrix: Square transition matrix

name: Optional character name of the Markov chain
```

#### Methods

```
* signature(e1 = "markovchain", e2 = "markovchain"): multiply two markovchain objects
* signature(e1 = "markovchain", e2 = "matrix"): markovchain by matrix multiplication
* signature(e1 = "markovchain", e2 = "numeric"): markovchain by numeric vector multi-
    plication
* signature(e1 = "matrix", e2 = "markovchain"): matrix by markov chain
* signature(e1 = "numeric", e2 = "markovchain"): numeric vector by markovchain mul-
     tiplication
[ signature(x = "markovchain", i = "ANY", j = "ANY", drop = "ANY"): ...
^ signature(e1 = "markovchain", e2 = "numeric"): power of a markovchain object
== signature(e1 = "markovchain", e2 = "markovchain"): equality of two markovchain
     object
!= signature(e1 = "markovchain", e2 = "markovchain"): non-equality of two markovchain
    object
absorbingStates signature(object = "markovchain"): method to get absorbing states
canonicForm signature(object = "markovchain"): return a markovchain object into canonic
    form
coerce signature(from = "markovchain", to = "data.frame"): coerce method from markovchain
    to data.frame
conditionalDistribution signature(object = "markovchain"): returns the conditional proba-
    bility of subsequent states given a state
coerce signature(from = "data.frame", to = "markovchain"): coerce method from data.frame
    to markovchain
```

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```
coerce signature(from = "table", to = "markovchain"): coerce method from table to
    markovchain
coerce signature(from = "msm", to = "markovchain"): coerce method from msm to markovchain
coerce signature(from = "msm.est", to = "markovchain"): coerce method from msm.est
    (but only from a Probability Matrix) to markovchain
coerce signature(from = "etm", to = "markovchain"): coerce method from etm to markovchain
coerce signature(from = "sparseMatrix", to = "markovchain"): coerce method from
    sparseMatrix to markovchain
coerce signature(from = "markovchain", to = "igraph"): coercing to igraph objects
coerce signature(from = "markovchain", to = "matrix"): coercing to matrix objects
coerce signature(from = "markovchain", to = "sparseMatrix"): coercing to sparseMatrix
    objects
coerce signature(from = "matrix", to = "markovchain"): coercing to markovchain objects
    from matrix one
dim signature(x = "markovchain"): method to get the size
names signature(x = "markovchain"): method to get the names of states
names<- signature(x = "markovchain", value = "character"): method to set the names
    of states
initialize signature(.Object = "markovchain"): initialize method
plot signature(x = "markovchain", y = "missing"): plot method for markovchain objects
predict signature(object = "markovchain"): predict method
print signature(x = "markovchain"): print method.
show signature(object = "markovchain"): show method.
sort signature(x = "markovchain", decreasing=FALSE): sorting the transition matrix.
states signature(object = "markovchain"): returns the names of states (as names.
steadyStates signature(object = "markovchain"): method to get the steady vector.
summary signature(object = "markovchain"): method to summarize structure of the markov
    chain
transientStates signature(object = "markovchain"): method to get the transient states.
t signature(x = "markovchain"): transpose matrix
transitionProbability signature(object = "markovchain"): transition probability
```

#### Warning

Validation method is used to assess whether either columns or rows totals to one. Rounding is used up to 5th decimal. If state names are not properly defined for a probability matrix, coercing to markovhcain object leads to overriding states name with artificial "s1", "s2", ... sequence. In addition, operator overloading has been applied for +, \*, \* ==, ! = operators.

#### Note

markovchain object are written in S4 Classes.

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### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

markovchainSequence,markovchainFit

### **Examples**

```
#show markovchain definition
showClass("markovchain")
#create a simple Markov chain
transMatr<-matrix(c(0.4,0.6,.3,.7),nrow=2,byrow=TRUE)</pre>
simpleMc<-new("markovchain", states=c("a","b"),</pre>
transitionMatrix=transMatr,
name="simpleMc")
#power
simpleMc^4
#some methods
steadyStates(simpleMc)
absorbingStates(simpleMc)
simpleMc[2,1]
t(simpleMc)
is.irreducible(simpleMc)
#conditional distributions
conditionalDistribution(simpleMc, "b")
#example for predict method
mcFit<-markovchainFit(data=sequence)</pre>
predict(mcFit$estimate, newdata="b",n.ahead=3)
#direct conversion
myMc<-as(transMatr, "markovchain")</pre>
#example of summary
summary(simpleMc)
## Not run: plot(simpleMc)
```

markovchainList-class Class "markovchainList"

# **Description**

A class to handle non - homogeneous Markov chains

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### **Objects from the Class**

A markovchainlist is a list of markovchain objects. They can be used to model non - homogeneous discrete time Markov Chains, when transition probabilities (and possible states) change by time.

#### **Slots**

```
markovchains: Object of class "list": a list of markovchains name: Object of class "character": optional name of the class
```

#### Methods

```
[[ signature(x = "markovchainList"): extract the i-th markovchain
dim signature(x = "markovchainList"): number of markovchain underlying the matrix
predict signature(object = "markovchainList"): predict from a markovchainList
print signature(x = "markovchainList"): prints the list of markovchains
show signature(object = "markovchainList"): same as print
```

#### Note

The class consists in a list of markovchain objects. It can help to deal with non - homogeneous Markov chains.

### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

#### See Also

markovchain

### **Examples**

```
showClass("markovchainList")
#define a markovchainList
statesNames=c("a","b")

mcA<-new("markovchain",name="MCA", transitionMatrix=matrix(c(0.7,0.3,0.1,0.9),
byrow=TRUE, nrow=2, dimnames=list(statesNames,statesNames)))

mcB<-new("markovchain", states=c("a","b","c"), name="MCB",
transitionMatrix=matrix(c(0.2,0.5,0.3,0,1,0,0.1,0.8,0.1),
nrow=3, byrow=TRUE))

mcC<-new("markovchain", states=c("a","b","c","d"), name="MCC",</pre>
```

26 markovchainListFit

```
transitionMatrix=matrix(c(0.25,0.75,0,0,0.4,0.6,
    0,0,0,0.1,0.9,0,0,0.7,0.3), nrow=4, byrow=TRUE)
)
mcList<-new("markovchainList",markovchains=list(mcA, mcB, mcC),
name="Non - homogeneous Markov Chain")</pre>
```

markovchainListFit

markovchainListFit

# **Description**

Given a data frame or a matrix (rows are observations, by cols the temporal sequence), it fits a non-homogeneous discrete time markov chain process (storing row). In particular a markovchainList of size = ncol - 1 is obtained estimating transitions from the n samples given by consecutive column pairs.

# Usage

```
markovchainListFit(data, byrow = TRUE, laplacian = 0, name)
```

### **Arguments**

data Either a matrix or a data.frame or a list object.

byrow Indicates whether distinc stochastic processes trajectiories are shown in distinct

rows.

laplacian Laplacian correction (default 0).

name Optional name.

#### **Details**

If data contains NAs then the transitions containing NA will be ignored.

### Value

A list containing two slots: estimate (the estimate) name

# **Examples**

```
# using holson dataset
data(holson)
# fitting a single markovchain
singleMc <- markovchainFit(data = holson[,2:12])
# fitting a markovchainList
mclistFit <- markovchainListFit(data = holson[, 2:12], name = "holsonMcList")</pre>
```

markovchainSequence 27

markovchainSequence	Function to generate a sequence of states from homogeneous Markov chains.

# **Description**

Provided any markovchain object, it returns a sequence of states coming from the underlying stationary distribution.

# Usage

```
markovchainSequence(n, markovchain, t0 = sample(markovchain@states, 1),
  include.t0 = FALSE, useRCpp = TRUE)
```

# Arguments

n Sample size

markovchain markovchain object

t0 The initial state

include.t0 Specify if the initial state shall be used

useRCpp Boolean. Should RCpp fast implementation being used? Default is yes.

### **Details**

A sequence of size n is sampled.

#### Value

A Character Vector

### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

markovchainFit

### **Examples**

```
# define the markovchain object
statesNames <- c("a", "b", "c")
mcB <- new("markovchain", states = statesNames,
    transitionMatrix = matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1),
    nrow = 3, byrow = TRUE, dimnames = list(statesNames, statesNames)))
# show the sequence
outs <- markovchainSequence(n = 100, markovchain = mcB, t0 = "a")</pre>
```

multinomialConfidenceIntervals

A function to compute multinomial confidence intervals of DTMC

# **Description**

These functions return multinomial confidence intervals of the markovchain objects.

# Usage

multinomialConfidenceIntervals(transitionMatrix, countsTransitionMatrix, confidencelevel)

### **Arguments**

```
transitionMatrix
Transition matrix.
countsTransitionMatrix
Counts transition matrix.
confidencelevel
Confidence level.
```

#### Value

A list with two matrices

### Author(s)

Tae Seung Kang, Giorgio Alfredo Spedicato

# References

Feres, Matlab listing for markov chain.

#### See Also

markovchain

name 29

### **Examples**

name

Method to retrieve name of markovchain object

# **Description**

This method returns the name of markovchain object

# Usage

```
name(object)
## S4 method for signature 'markovchain'
name(object)
```

# **Arguments**

object

A markovchain object

# Author(s)

Giorgio Spedicato, Deepak Yadav

# **Examples**

30 predictiveDistribution

name<-

Method to set name of markovchain object

# Description

This method modify the existing name of markovchain object

# Usage

```
name(object) <- value
## S4 replacement method for signature 'markovchain'
name(object) <- value</pre>
```

### Arguments

object A markovchain object

value New name of markovchain object

### Author(s)

Giorgio Spedicato, Deepak Yadav

# **Examples**

predictiveDistribution

Function to compute the probability of observing a new data set, given a data set

# **Description**

The function computes the probability of observing a new data set using information from a given data set. Additionally, hyperparameters can be provided.

#### **Usage**

```
predictiveDistribution(stringchar, newData, hyperparam = matrix())
```

predictiveDistribution 31

### Arguments

stringchar This is the data using which the Bayesian inference is performed.

newData This is the data whose predictive probability is computed.

hyperparam This determines the shape of the prior distribution of the parameters. If none is

provided, default value of 1 is assigned to each parameter. This must be of size kxk where k is the number of states in the chain and the values should typically

be non-negative integers.

#### **Details**

The underlying method is Bayesian inference. The probability is computed by averaging the likelihood of the new data with respect to the posterior. Since the method assumes conjugate priors, the result can be represented in a closed form (see the vignette for more details), which is what is returned.

#### Value

The log of the probability is returned.

### Author(s)

Sai Bhargav Yalamanchi

### References

Inferring Markov Chains: Bayesian Estimation, Model Comparison, Entropy Rate, and Out-of-Class Modeling, Christopher C. Strelioff, James P. Crutchfield, Alfred Hubler, Santa Fe Institute

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

### See Also

markovchainFit

### **Examples**

priorDistribution

preproglucacon

Preprogluccacon DNA protein bases sequences

# **Description**

Sequence of bases for preproglucacon DNA protein

# Usage

```
data(preproglucacon)
```

#### **Format**

A data frame with 1572 observations on the following 2 variables.

V1 a numeric vector, showing original coding

preproglucacon a character vector, showing initial of DNA bases (Adenine, Cytosine, Guanine, Thymine)

#### **Source**

Avery Henderson

### References

Averuy Henderson, Fitting markov chain models on discrete time series such as DNA sequences

# **Examples**

```
data(preproglucacon)
preproglucaconMc<-markovchainFit(data=preproglucacon$preproglucacon)</pre>
```

priorDistribution

Prior Distribution

# Description

Function to evaluate the prior probability of a transition matrix. It is based on conjugate priors and therefore a Dirichlet distribution is used to model the transitions of each state.

# Usage

```
priorDistribution(transMatr, hyperparam = matrix())
```

priorDistribution 33

### **Arguments**

transMatr The transition matrix whose probability is the parameter of interest.

hyperparam The hyperparam matrix (optional). If not provided, a default value of 1 is as-

sumed for each and therefore the resulting probability distribution is uniform.

### **Details**

The states (dimnames) of the transition matrix and the hyperparam may be in any order.

#### Value

The log of the probabilities for each state is returned in a numeric vector. Each number in the vector represents the probability (log) of having a probability transition vector as specified in corresponding the row of the transition matrix.

#### Note

This function can be used in conjunction with inferHyperparam. For example, if the user has a prior data set and a prior transition matrix, he can infer the hyperparameters using inferHyperparam and then compute the probability of their prior matrix using the inferred hyperparameters with priorDistribution.

### Author(s)

Sai Bhargav Yalamanchi, Giorgio Spedicato

### References

Yalamanchi SB, Spedicato GA (2015). Bayesian Inference of First Order Markov Chains. R package version 0.2.5

### See Also

predictiveDistribution, inferHyperparam

# **Examples**

```
\label{eq:priorDistribution} \begin{split} \text{priorDistribution}(\text{matrix}(c(0.5,\ 0.5,\ 0.5,\ 0.5),\\ & \text{nrow} = 2,\\ & \text{dimnames} = \text{list}(c("a",\ "b"),\ c("a",\ "b"))),\\ & \text{matrix}(c(2,\ 2,\ 2,\ 2),\\ & \text{nrow} = 2,\\ & \text{dimnames} = \text{list}(c("a",\ "b"),\ c("a",\ "b")))) \end{split}
```

34 retme

rain

Alofi island daily rainfall

# **Description**

Rainfall measured in Alofi Island

# Usage

```
data(rain)
```

### **Format**

A data frame with 1096 observations on the following 2 variables.

V1 a numeric vector, showing original coding rain a character vector, showing daily rainfall millilitres brackets

#### **Source**

Avery Henderson

### References

Avery Henderson, Fitting markov chain models on discrete time series such as DNA sequences

# **Examples**

```
data(rain)
rainMc<-markovchainFit(data=rain$rain)</pre>
```

rctmc

Function to generate a sequence of random CTMC transitions.

# Description

The function generates random CTMC transitions as per the provided generator matrix.

# Usage

```
rctmc(n, ctmc, initDist = numeric(), T = 0, include.T0 = TRUE, out.type = "list")
```

retme 35

### **Arguments**

n The number of samples to generate.

ctmc The CTMC S4 object.

initDist The initial distribution of states.

The time up to which the simulation runs (all transitions after time T are not

returned).

include. T0 Flag to determine if start state is to be included.

out.type "list" or "df"

### **Details**

In order to use the T0 argument, set n to Inf.

#### Value

Based on out.type, a list or a data frame is returned. The returned list has two elements - a character vector (states) and a numeric vector (indicating time of transitions). The data frame is similarly structured.

### Author(s)

Sai Bhargav Yalamanchi

#### References

Introduction to Stochastic Processes with Applications in the Biosciences (2013), David F. Anderson, University of Wisconsin at Madison

# See Also

generatorToTransitionMatrix,ctmc-class

# **Examples**

36 rmarkovchain

rmarkovchain	Function to generate a sequence of states from homogeneous or non-
	homogeneous Markov chains.

# Description

Provided any markovchain or markovchainList objects, it returns a sequence of states coming from the underlying stationary distribution.

# Usage

```
rmarkovchain(n, object, what = "data.frame", useRCpp = TRUE,
   parallel = FALSE, num.cores = NULL, ...)
```

# **Arguments**

n	Sample size
object	Either a markovchain or a markovchainList object
what	It specifies whether either a data.frame or a matrix (each rows represent a simulation) or a list is returned.
useRCpp	Boolean. Should RCpp fast implementation being used? Default is yes.
parallel	Boolean. Should parallel implementation being used? Default is yes.
num.cores	Number of Cores to be used
	additional parameters passed to the internal sampler

# **Details**

When a homogeneous process is assumed (markovchain object) a sequence is sampled of size n. When a non - homogeneous process is assumed, n samples are taken but the process is assumed to last from the begin to the end of the non-homogeneous markov process.

### Value

Character Vector, data.frame, list or matrix

# Note

Check the type of input

# Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

sales 37

#### See Also

markovchainFit, markovchainSequence

# **Examples**

```
# define the markovchain object
statesNames <- c("a", "b", "c")
mcB <- new("markovchain", states = statesNames,</pre>
   transitionMatrix = matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1),
   nrow = 3, byrow = TRUE, dimnames = list(statesNames, statesNames)))
# show the sequence
outs <- rmarkovchain(n = 100, object = mcB, what = "list")
#define markovchainList object
statesNames <- c("a", "b", "c")
mcA <- new("markovchain", states = statesNames, transitionMatrix =</pre>
   matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
   byrow = TRUE, dimnames = list(statesNames, statesNames)))
mcB <- new("markovchain", states = statesNames, transitionMatrix =</pre>
   matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
   byrow = TRUE, dimnames = list(statesNames, statesNames)))
mcC <- new("markovchain", states = statesNames, transitionMatrix =</pre>
   matrix(c(0.2, 0.5, 0.3, 0, 0.2, 0.8, 0.1, 0.8, 0.1), nrow = 3,
   byrow = TRUE, dimnames = list(statesNames, statesNames)))
mclist <- new("markovchainList", markovchains = list(mcA, mcB, mcC))</pre>
# show the list of sequence
rmarkovchain(100, mclist, "list")
```

sales

Sales Demand Sequences

### Description

Sales demand sequences of five products (A, B, C, D, E). Each row corresponds to a sequence. First row corresponds to Sequence A, Second row to Sequence B and so on.

#### Usage

```
data("sales")
```

# **Format**

An object of class matrix with 269 rows and 5 columns.

38 states

### **Details**

The example can be used to fit High order multivariate markov chain.

# **Examples**

```
data("sales")
# fitHighOrderMultivarMC(seqMat = sales, order = 2, Norm = 2)
```

show, hommc-method

Function to display the details of homme object

# **Description**

This is a convenience function to display the slots of homme object in proper format

# Usage

```
## S4 method for signature 'hommc'
show(object)
```

# **Arguments**

object

An object of class homme

states

Defined states of a transition matrix

# **Description**

This method returns the states of a transition matrix.

### Usage

```
states(object)
## S4 method for signature 'markovchain'
states(object)
```

# Arguments

object

A discrete markovchain object

### Value

The character vector corresponding to states slot.

steadyStates 39

### Author(s)

Giorgio Spedicato

#### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

markovchain

### **Examples**

steadyStates

Stationary states of a markovchain object

### Description

This method returns the stationary vector in matricial form of a markovchain object.

### Usage

```
steadyStates(object)
## S4 method for signature 'markovchain'
steadyStates(object)
```

### **Arguments**

object

A discrete markovchain object

# Value

A matrix corresponding to the stationary states

# Note

The steady states are identified starting from which eigenvectors correspond to identity eigenvalues and then normalizing them to sum up to unity. When negative values are found in the matrix, the eigenvalues extraction is performed on the recurrent classes submatrix.

40 transition2Generator

### Author(s)

Giorgio Spedicato

### References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

# See Also

markovchain

# **Examples**

transition2Generator Return the generator matrix for a corresponding transition matrix

### **Description**

Calculate the generator matrix for a corresponding transition matrix

# Usage

```
transition2Generator(P, t = 1, method = "logarithm")
```

# **Arguments**

P transition matrix between time 0 and t

t time of observation

method "logarithm" returns the Matrix logarithm of the transition matrix

### Value

A matrix that represent the generator of P

### See Also

rctmc

transitionProbability 41

### **Examples**

```
mymatr <- matrix(c(.4, .6, .1, .9), nrow = 2, byrow = TRUE)
Q <- transition2Generator(P = mymatr)
expm::expm(Q)</pre>
```

transitionProbability Function to get the transition probabilities from initial to subsequent states.

# Description

This is a convenience function to get transition probabilities.

# Usage

```
transitionProbability(object, t0, t1)
## S4 method for signature 'markovchain'
transitionProbability(object, t0, t1)
```

# Arguments

object A markovchain object.

t0 Initial state.

t1 Subsequent state.

### Value

Numeric Vector

### Author(s)

Giorgio Spedicato

# References

A First Course in Probability (8th Edition), Sheldon Ross, Prentice Hall 2010

### See Also

markovchain

### **Examples**

verifyMarkovProperty Various functions to perform statistical inference of DTMC

# Description

These functions verify the Markov property, assess the order and stationarity of the Markov chain.

This function tests whether an empirical transition matrix is statistically compatible with a theoretical one. It is a chi-square based test

Verifies that the s elements in the input list belongs to the same DTMC

# Usage

```
verifyMarkovProperty(sequence, verbose = TRUE)
assessOrder(sequence, verbose = TRUE)
assessStationarity(sequence, nblocks, verbose = TRUE)
verifyEmpiricalToTheoretical(data, object, verbose = TRUE)
verifyHomogeneity(inputList, verbose = TRUE)
```

# Arguments

sequence An empirical sequence.

verbose Should test results be printed out?

nblocks Number of blocks.

data matrix, character or list to be converted in a raw transition matrix

object a markovchain object

inputList A list of items that can coerced to transition matrices

### Value

Verification result

a list with following slots: statistic (the chi - square statistic), dof (degrees of freedom), and corresponding p-value

a list of transition matrices?

verifyMarkovProperty 43

### Author(s)

Tae Seung Kang, Giorgio Alfredo Spedicato

#### References

Anderson and Goodman.

#### See Also

markovchain

# **Examples**

```
sequence <- c("a", "b", "a", "a", "a", "a", "b", "a", "b", 
"a", "b", "a", "a", "b", "b", "b", "a")
mcFit <- markovchainFit(data = sequence, byrow = FALSE)</pre>
verifyMarkovProperty(sequence)
assessOrder(sequence)
assessStationarity(sequence, 1)
#Example taken from Kullback Kupperman Tests for Contingency Tables and Markov Chains
0,0,0,0,0,2,2,1,1,1,1,1,2,1,2,0,0,0,1,2,2,2,0,0,0,1,1)
mc=matrix(c(5/8,1/4,1/8,1/4,1/2,1/4,1/4,3/8,3/8),byrow=TRUE, nrow=3)
rownames(mc)<-colnames(mc)<-0:2; theoreticalMc<-as(mc, "markovchain")</pre>
verifyEmpiricalToTheoretical(data=sequence,object=theoreticalMc)
data(kullback)
verifyHomogeneity(inputList=kullback,verbose=TRUE)
```

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