

## **Team 58 : Homework 4**

### **Team members**

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### **PART 1:**

1.  $R = ABCDEGH$  and  $F = \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$ 
  - a. ABC
    - i. The set of dependencies that hold over ABC is  $\{AB \rightarrow C, AC \rightarrow B, BC \rightarrow A\}$ . This is already a minimal cover.
    - ii. This is in BCNF as AB, AC, and BC are all candidate keys of the set ABC.
    - iii. It is already in BCNF form.
  - b. ABCD
    - i. The set of dependencies that hold over ABCD is  $\{AB \rightarrow C, AC \rightarrow B, B \rightarrow D, BC \rightarrow A\}$ . This is already a minimal cover.
    - ii. The keys are AB, AC, and BC. The FD  $B \rightarrow D$  violates 2NF as B is a proper subset of the key AB. So, this set is in 1NF form.
    - iii. Decompose the set into ABC, BD and it's now in BCNF form.
  - c. ABCEG
    - i. The set of dependencies that hold over ABCEG is  $\{AB \rightarrow C, AC \rightarrow B, BC \rightarrow A, E \rightarrow G\}$ . This is already in minimal cover.
    - ii. The keys are ABE, ACE, and BCE. The FD  $E \rightarrow G$  violates 2NF form as E is a proper subset of a key. So, this set is in 1NF form.

iii. Decompose the set into ABC, ABE, EG and it's now in BCNF form.

d. DCEGH

- i. The set of dependencies that hold over DCEGH is  $\{E \rightarrow G\}$ . This is already in minimal cover.
- ii. The key is DCEH. The FD  $E \rightarrow G$  violates 2NF form as E is a proper subset of the key DCEH. So, this set is in 1NF form.
- iii. Decompose the set into DCEH, EG and it's now in BCNF form.

e. ACEH

- i. The set of dependencies that hold over the set ACEH is  $\{\}$ . No FDs exist. This is already in minimal cover.
- ii. The key is ACEH. It is in BCNF form.
- iii. It is already in BCNF form.

2.  $R = ABCDEG$ ,  $F = \{AB \rightarrow C, AC \rightarrow B, AD \rightarrow E, B \rightarrow D, BC \rightarrow A, E \rightarrow G\}$ .

a.  $\{AB, BC, ABDE, EG\}$ .

Consider the following instance of R:

$\{(a1, b, c1, d1, e1, g1), (a2, b, c2, d2, e2, g2)\}$

Because of the FDs  $BC \rightarrow A$  and  $AB \rightarrow C$ ,  $a1 = a2$  only when  $c1 = c2$ .

So, if we do AB join BC, we get

$\{(a1, b, c1), (a1, b, c2), (a2, b, c1), (a2, b, c2)\}$

So the join on AB, BE, ABDE, EG will contain at least 4 tuples.

Thus, we have a lossy join.

Also, the FDs  $AB \rightarrow C$  and  $AC \rightarrow B$  are not preserved.

Thus, this decomposition is not dependency preserving either.

b. {ABC, ACDE, ADG}

First, join ABC and ACDE.

This is lossless because their intersection AC is a key for ABCDEG.

Now, join (ABC join ACDE) with ADG.

This is also lossless because their intersection is AD and  $AD \rightarrow ADG$ .

Thus, this decomposition is lossless.

The projection of FDs of R onto ABC gives-

$AB \rightarrow C$ ,  $AC \rightarrow B$ ,  $BC \rightarrow A$

The projection of FDs of R into ACDE gives-

$AD \rightarrow E$

The projection of FDs of R onto ADG gives-

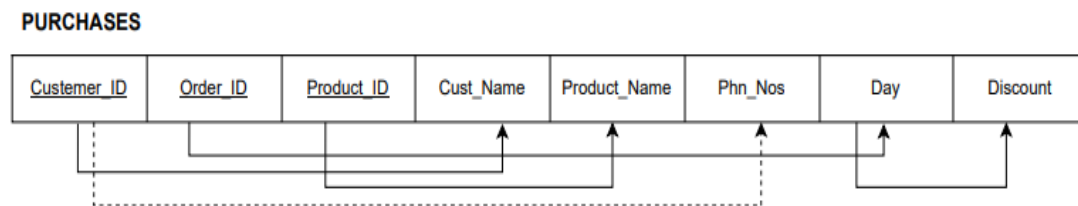
$AD \rightarrow G$  by transitivity

The closure of this set of dependencies doesn't contain  $E \rightarrow G$  and  $B \rightarrow D$ .

Thus, this decomposition is not dependency preserving.

## Part 2:

ASSUMING ONLY 2 PH\_NO IN MULTIVALUED ATTRIBUTE Phn\_no which can be extended for n



a) 1 NF

**PURCHASES**

<u>Customer_ID</u>	<u>Order_ID</u>	<u>Product_ID</u>	Cust_Name	Product_Name	Day	Discount	
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**PURCHASE\_CONTACTS**

<u>Customer_ID</u>	<u>Phn_Nos1</u>	Phn_No2
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b) 2 NF

**PURCHASES**

<u>Customer_ID</u>	<u>Order_ID</u>	<u>Product_ID</u>
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**CUSTOMERS**

<u>Customer_ID</u>	Cust_Name
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**PRODUCTS**

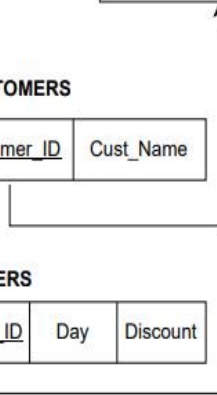
<u>Product_ID</u>	Product_Name
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**ORDERS**

<u>Order_ID</u>	Day	Discount
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**PURCHASE\_CONTACTS**

<u>Customer_ID</u>	<u>Phn_Nos1</u>	<u>Phn_No2</u>
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c) 3NF

