

4) to find probability of passing midterm given the midterm performance was average and all assignments were submitted.

X_1 = 'average' midterm performance

X_2 = all assignments were submitted

Y = passing midterm.

$X = \{x_1, x_2\}$

assuming conditional independence of features

$$P(Y|X) = \frac{P(X|Y) P(Y)}{P(X)}$$

$$P(Y|X) = \frac{P(x_1|Y) P(x_2|Y) P(Y)}{\sum_{i=1}^2 P(x_1|Y_i) P(x_2|Y_i) P(Y_i)}$$

$$P(Y|x_1, x_2) = \frac{\left(\frac{3}{6}\right) \left(\frac{5}{6}\right) \left(\frac{6}{11}\right)}{\left(\frac{12}{5}\right) \left(\frac{1}{5}\right) \left(\frac{5}{11}\right) + \left(\frac{3}{6}\right) \left(\frac{5}{6}\right) \left(\frac{6}{11}\right)}$$

$$P(Y|x_1, x_2) = \frac{\frac{15}{6}}{\frac{2}{5} + \frac{15}{6}} = \frac{25}{29}$$