

37. given  $f(y; \theta) = \frac{3y^2}{\theta^3}$ , with  $\theta \in (0, \infty)$  and  $y \in [0, \theta]$ .

Let, we have a dataset of  $n$  points  $y_1, y_2, y_3, \dots, y_n$ .

The likelihood function for this is  $L(\theta)$ .

$$L(\theta) = \prod_{i=1}^n \frac{3y_i^2}{\theta^3} = \left( \frac{3^n}{\theta^{3n}} \right) \prod_{i=1}^n y_i^2$$

now to find maximum likelihood estimate for  $\theta$   
we need to find out  $\theta$  for which  $L(\theta)$  maximises

Also it is given  $y \in [0, \theta]$

So, we need small  $\theta$  such that above condition is satisfied, which is only possible for

$$[\theta = \max\{y_i\} : i = 1, 2, 3, \dots, n]$$