

```
In [1]: from keras.datasets import mnist;
        (train_images, train_labels), (test_images, test_labels) = mnist.load_data()
        print( train_images.shape )
        print( len(train_labels) )
        print( train_labels )
        print( train_images[0])
```

Downloading data from <https://storage.googleapis.com/tensorflow/tf-keras-datasets/mnist.npz>

11490434/11490434  **0s** 0us/step

(60000, 28, 28)

60000

[5 0 4 ... 5 6 8]

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[ [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0]
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  0 0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
  0 0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 3 18 18 18 126 136
 175 26 166 255 247 127 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 30 36 94 154 170 253 253 253 253 253
 225 172 253 242 195 64 0 0 0 0]
 [ 0 0 0 0 0 0 49 238 253 253 253 253 253 253 253 253 253 251
 93 82 82 56 39 0 0 0 0]
 [ 0 0 0 0 0 0 18 219 253 253 253 253 253 198 182 247 241
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 80 156 107 253 253 205 11 0 43 154
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 14 1 154 253 90 0 0 0 0
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 139 253 190 2 0 0 0
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 11 190 253 70 0 0 0
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 35 241 225 160 108 1
 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 81 240 253 253 119
 25 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 45 186 253 253
 150 27 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 16 93 252
 253 187 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 249
 253 249 64 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 46 130 183 253
 253 207 2 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 39 148 229 253 253 253
 250 182 0 0 0 0 0 0 0]
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 78 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 23 66 213 253 253 253 253 198 81 2
 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 18 171 219 253 253 253 253 195 80 9 0 0
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 [ 0 0 0 55 172 226 253 253 253 253 244 133 11 0 0 0 0
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 [ 0 0 0 136 253 253 253 212 135 132 16 0 0 0 0 0 0
 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
 0 0 0 0 0 0 0 0]
```

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[ 0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0
  0  0  0  0  0  0  0  0  0  0]]
```

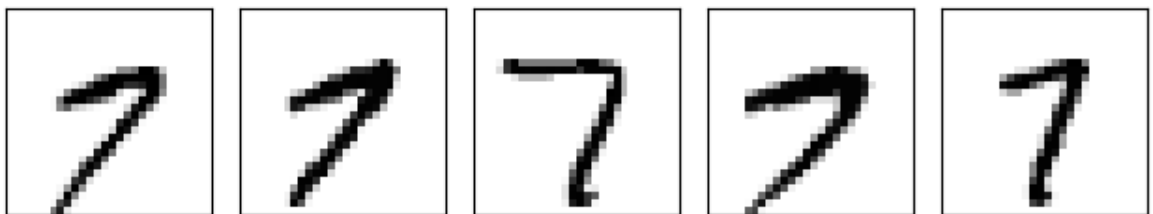
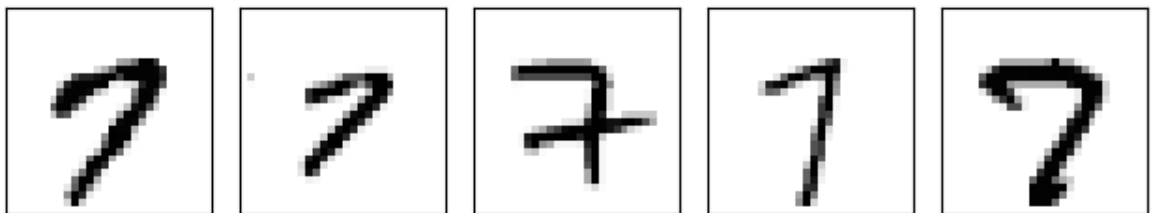
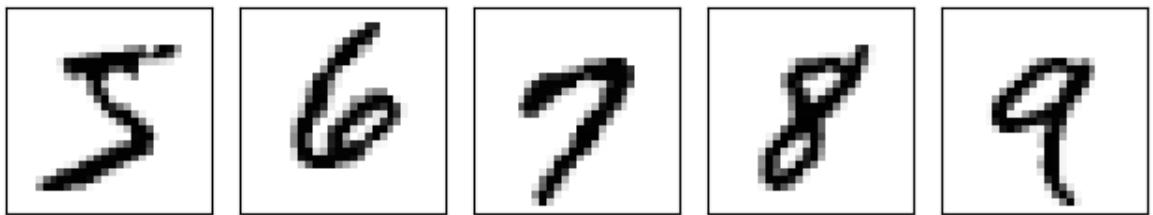
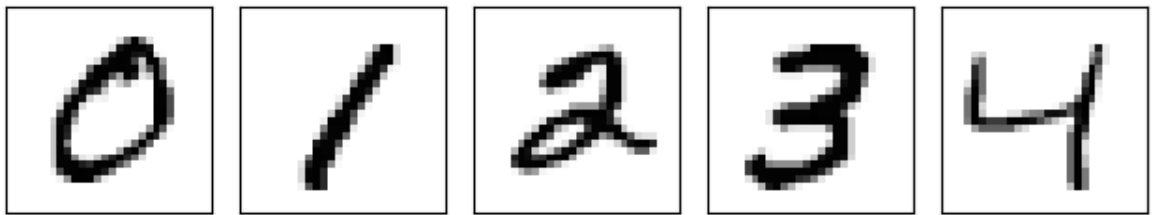
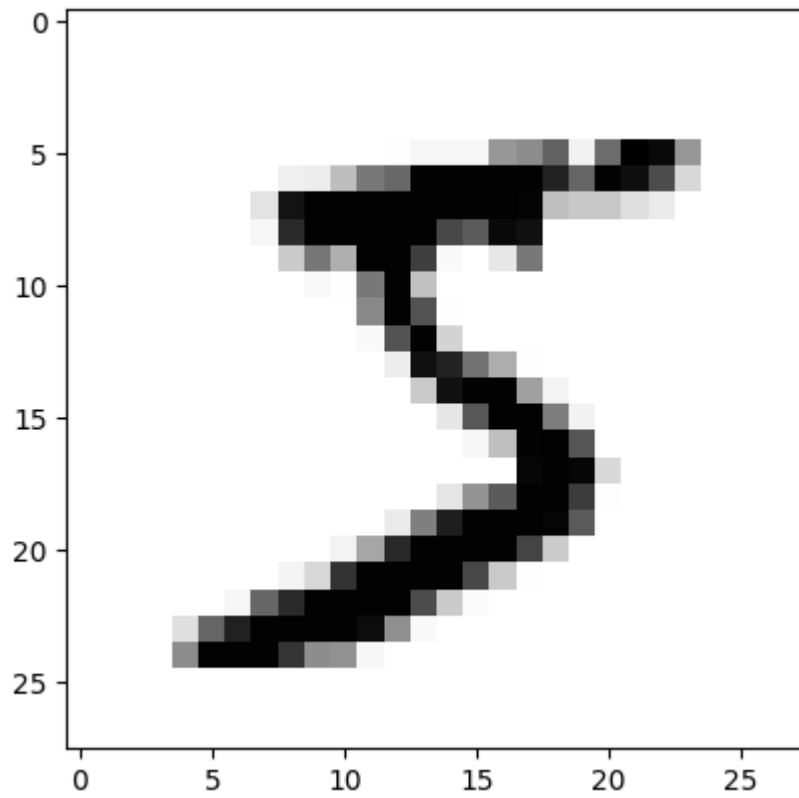
```
In [2]: import matplotlib.pyplot as plt
img = train_images[0].reshape(28,28)
plt.imshow( img, cmap='Greys')
print("Liczba ", train_labels[0])

fig, ax = plt.subplots(nrows=2, ncols=5, sharex=True, sharey=True)
ax = ax.flatten()
for i in range(10):
    img = train_images[ train_labels==i ][0].reshape(28,28)
    ax[i].imshow( img, cmap='Greys')
ax[0].set_xticks([])
ax[0].set_yticks([])
plt.tight_layout()
plt.show()

fig, ax = plt.subplots(nrows=2, ncols=5, sharex=True, sharey=True)
ax = ax.flatten()
for i in range(10):
    img = train_images[ train_labels==7 ][i].reshape(28,28)
    ax[i].imshow( img, cmap='Greys')
ax[0].set_xticks([])
ax[0].set_yticks([])
plt.tight_layout()
plt.show()

x_train = train_images.reshape((60000, 28*28))
x_train = x_train.astype('float32') / 256
x_test = test_images.reshape((10000, 28*28))
x_test = x_test.astype('float32') / 256
print( train_images[0])
print( x_train[0])
```

Liczba 5



```

[[ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
   0 0 0 0 0 0 0 0 0 0]
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   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 3 18 18 18 126 136
  175 26 166 255 247 127 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 30 36 94 154 170 253 253 253 253 253
  225 172 253 242 195 64 0 0 0 0]
 [ 0 0 0 0 0 0 0 49 238 253 253 253 253 253 253 253 253 251
  93 82 82 56 39 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 18 219 253 253 253 253 253 198 182 247 241
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 80 156 107 253 253 205 11 0 43 154
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 14 1 154 253 90 0 0 0 0
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 139 253 190 2 0 0 0
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 11 190 253 70 0 0
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 35 241 225 160 108 1
   0 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 81 240 253 253 119
  25 0 0 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 45 186 253 253
  150 27 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 16 93 252
  253 187 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 249
  253 249 64 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 46 130 183 253
  253 207 2 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 0 0 39 148 229 253 253 253
  250 182 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 0 0 0 24 114 221 253 253 253 253 201
  78 0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 0 0 23 66 213 253 253 253 253 198 81 2
   0 0 0 0 0 0 0]
 [ 0 0 0 0 0 0 18 171 219 253 253 253 253 195 80 9 0 0
   0 0 0 0 0 0 0]
 [ 0 0 0 0 55 172 226 253 253 253 253 244 133 11 0 0 0 0
   0 0 0 0 0 0 0]
 [ 0 0 0 0 136 253 253 253 212 135 132 16 0 0 0 0 0 0
   0 0 0 0 0 0 0]
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[0. 0. 0. 0. 0. 0.
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[illegible]

0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.31640625	0.9375	0.98828125
0.98828125	0.46484375	0.09765625	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.17578125	0.7265625	0.98828125	0.98828125
0.5859375	0.10546875	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.0625	0.36328125	0.984375	0.98828125	0.73046875
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.97265625	0.98828125	0.97265625	0.25	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.1796875	0.5078125	0.71484375	0.98828125
0.98828125	0.80859375	0.0078125	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.15234375	0.578125
0.89453125	0.98828125	0.98828125	0.98828125	0.9765625	0.7109375
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.09375	0.4453125	0.86328125	0.98828125	0.98828125	0.98828125
0.98828125	0.78515625	0.3046875	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.08984375	0.2578125	0.83203125	0.98828125
0.98828125	0.98828125	0.98828125	0.7734375	0.31640625	0.0078125
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.0703125	0.66796875
0.85546875	0.98828125	0.98828125	0.98828125	0.98828125	0.76171875
0.3125	0.03515625	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.21484375	0.671875	0.8828125	0.98828125	0.98828125	0.98828125
0.98828125	0.953125	0.51953125	0.04296875	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.53125	0.98828125
0.98828125	0.98828125	0.828125	0.52734375	0.515625	0.0625
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
0.	0.	0.	0.	0.	0.
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```

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0.      0.      0.      0.      0.      0.
0.      0.      0.      0.      0.      0.
0.      0.      0.      0.      0.      0.
0.      0.      0.      0.      0.      0.

```

```

In [3]: from keras.utils import to_categorical
y_train = to_categorical(train_labels)
y_test = to_categorical(test_labels)

print( train_labels[0] )
print( y_train[0] )

```

```

5
[0. 0. 0. 0. 0. 1. 0. 0. 0. 0.]

```

Zadanie nr 1:

```

In [4]: from keras import models
from keras import layers
network = models.Sequential()
network.add(layers.Input(shape=(28*28,)))
#kolejne warstwy sieci Dense
#...
network.add(layers.Dense(10, activation="relu"))
network.add(layers.Dense(10, activation='softmax'))
network.compile(optimizer='rmsprop', loss='categorical_crossentropy',
metrics=['accuracy'])

```

Zadanie nr 2:

```

In [5]: import copy
from sklearn.metrics import accuracy_score
def getIndexOfMax(arr):
    index = 0;
    for i in range(len(arr)):
        if arr[i] > arr[index]:
            index = i
        #elif (i != index) and (arr[i] == arr[index]):
        #raise Exception("Cannot get max element. Elements aren't unique.")
    return index
def maxtolresttto0(_mat):
    mat = copy.deepcopy(_mat)
    for arr in mat:
        index = getIndexOfMax(arr)
        for i in range(len(arr)):
            if i == index:
                arr[i] = 1.0;
            else:
                arr[i] = 0.0;
    return mat

history = network.fit(x_train, y_train, epochs=500, batch_size=32, verbose

```



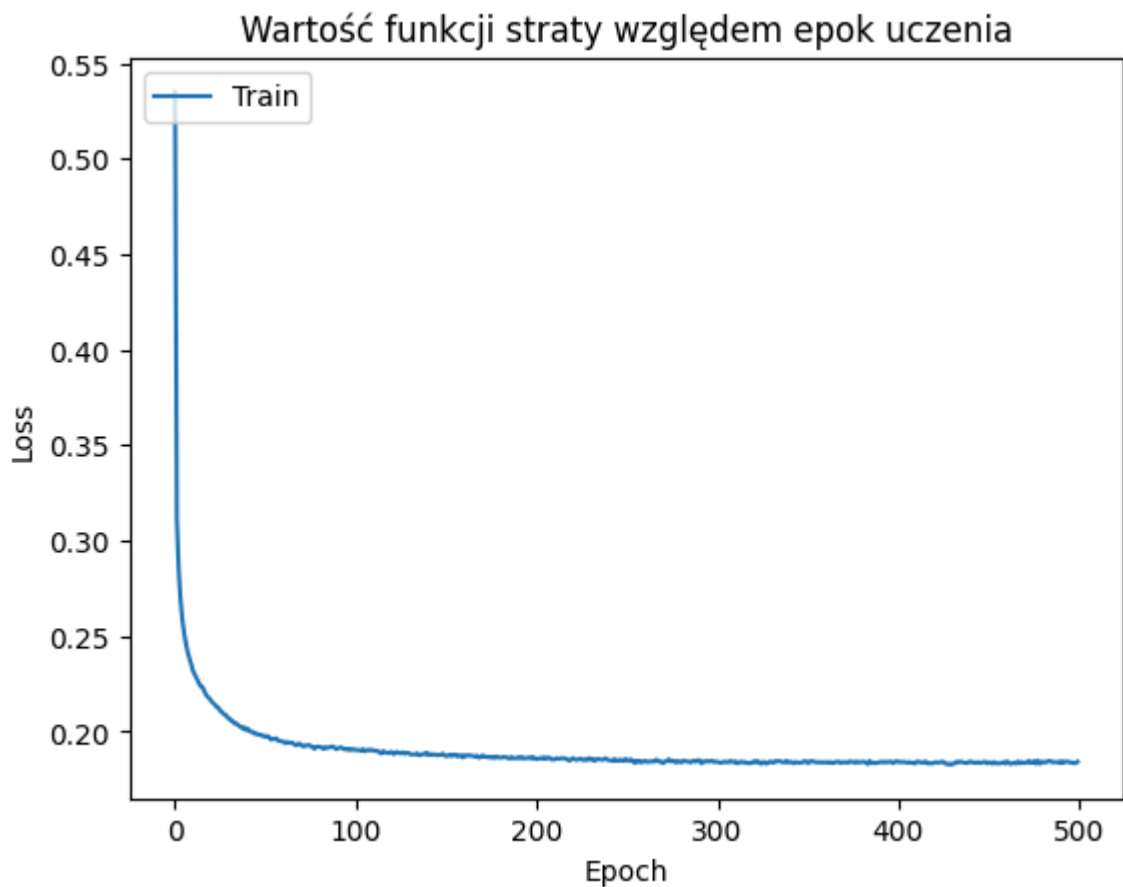
```

print("Ostatni błąd:", history.history['loss'][-1])
plt.plot(history.history['loss'])
plt.title('Wartość funkcji straty względem epok uczenia')
plt.ylabel('Loss')
plt.xlabel('Epoch')
plt.legend(['Train'], loc='upper left')
plt.show()

#treniowe
y_result_train = network.predict(x_train)
y_result_train_rounded = maxtolrestto0(y_result_train)
accuracy = accuracy_score(y_train, y_result_train_rounded)
print("Accuracy:", accuracy)
print("Wyniki obliczeń:\n", y_result_train[0], "\nZaokrąglone:\n", y_result

```

Ostatni błąd: 0.18411201238632202



1875/1875 ————— 2s 1ms/step

Accuracy: 0.9544666666666667

Wyniki obliczeń:

```

[1.1338093e-09 1.7666850e-12 4.8749328e-08 1.4026439e-02 5.2114424e-29
 9.8597360e-01 3.3910630e-12 1.3519860e-08 2.1042602e-10 1.2197202e-12]

```

Zaokrąglone:

```

[[0. 0. 0. ... 0. 0. 0.]
 [1. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 ...
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 0. 0.]
 [0. 0. 0. ... 0. 1. 0.]]

```

Zadanie nr 3

```
In [20]: import numpy as np
def hitPercentage(_x, _y, model, label):
    predict_x = model.predict(_x)
    y_result = np.argmax(predict_x,axis=1)
    count = 0
    goodCount = 0
    for i in range(len(_y)):
        if(y_result[i] == _y[i]):
            goodCount += 1
        count += 1
    print(label,(goodCount/count)*100,"%")
hitPercentage(x_train, train_labels, network, "Zbiór treningowy:")
hitPercentage(x_test, test_labels, network, "Zbiór testowy:")
```

1875/1875 ————— 2s 1ms/step

Zbiór treningowy: 95.44666666666667 %

313/313 ————— 1s 2ms/step

Zbiór testowy: 92.88 %

Zadanie nr 4

```
In [34]: from sklearn.metrics import accuracy_score, precision_score, recall_score
import numpy as np
def metrics(_x, _y, model,label):
    # Przewidywanie wyników
    y_pred = model.predict(_x)
    # Zaokrąglenie wyników przewidywań
    y_pred_rounded = np.argmax(y_pred, axis=1)
    # Obliczenie metryk
    accuracy = accuracy_score(_y, y_pred_rounded)
    precision = precision_score(_y, y_pred_rounded, average="macro")
    recall = recall_score(_y, y_pred_rounded, average="macro")
    # Uzyskanie macierzy pomyłek
    conf_matrix = confusion_matrix(_y, y_pred_rounded)
    # Wyświetlanie wyników
    print(label)
    print("Accuracy:", accuracy)
    print("Precision:", precision)
    print("Recall:", precision)
    print("Confusion Matrix:\n", conf_matrix)

metrics(x_train, train_labels, network, "Metriki i macierz pomyłek dla zb
metrics(x_test, test_labels, network, "Metrik i macierz pomyłek dla zbior
```

1875/1875 ————— **2s** 1ms/step

Metriki i macierz pomyłek dla zbioru treningowego:

Accuracy: 0.9544666666666667

Precision: 0.9542385739932907

Recall: 0.9542385739932907

Confusion Matrix:

```
[[5812   1  12   4   1  13  31   5  41   3]
 [  1 6643  22   8   3   7   3  10  37   8]
 [ 28  30 5632  64  28   8  50  31  79   8]
 [ 20  23  87 5683   2 116  16  27 127  30]
 [ 10  17  33   8 5553   6  67   8  39 101]
 [ 31  31  15 102  13 5046  85   3  81  14]
 [ 15   9   6   3  15  43 5805   3  18   1]
 [ 21  19  20  23  30   5   5 6022  35  85]
 [ 20  67  21  69  17  53  33   8 5549  14]
 [ 22  11   6  55 108  35   7  96  86 5523]]
```

313/313 ————— **1s** 2ms/step

Metrik i macierz pomyłek dla zbioru testowego:

Accuracy: 0.9288

Precision: 0.9282213884893157

Recall: 0.9282213884893157

Confusion Matrix:

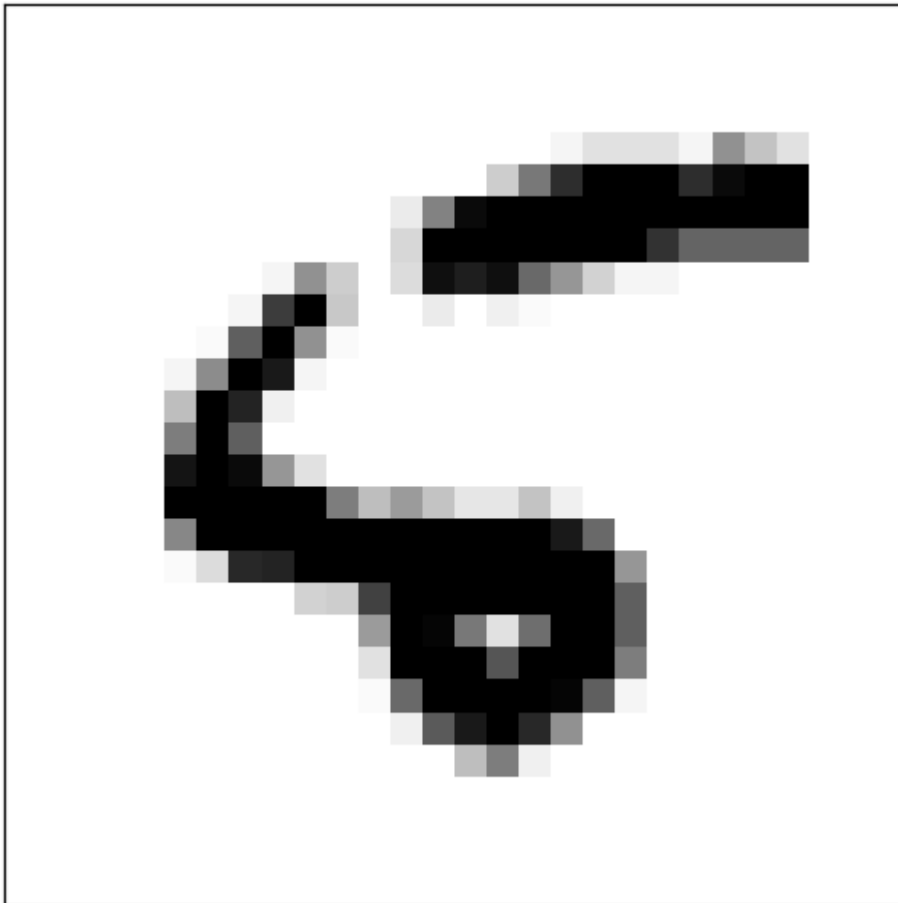
```
[[ 960   0   2   2   0   2   8   2   4   0]
 [  0 1110   4   2   2   2   5   0   9   1]
 [  9   9  930  15  12   7  16   8  26   0]
 [  2   4  16  920   2  26   3  10  24   3]
 [  1   2   9   7  898   4  17   7   3  34]
 [  5   3   2  24   5  810  17   1  18   7]
 [  9   4   7   1   3  10  918   2   4   0]
 [  2   9  14  14   5   2   0  947   8  27]
 [  5  13   7  14   9  14  10   9  888   5]
 [  8   6   0  11  26   8   0  25  18  907]]
```

Zadanie nr 5

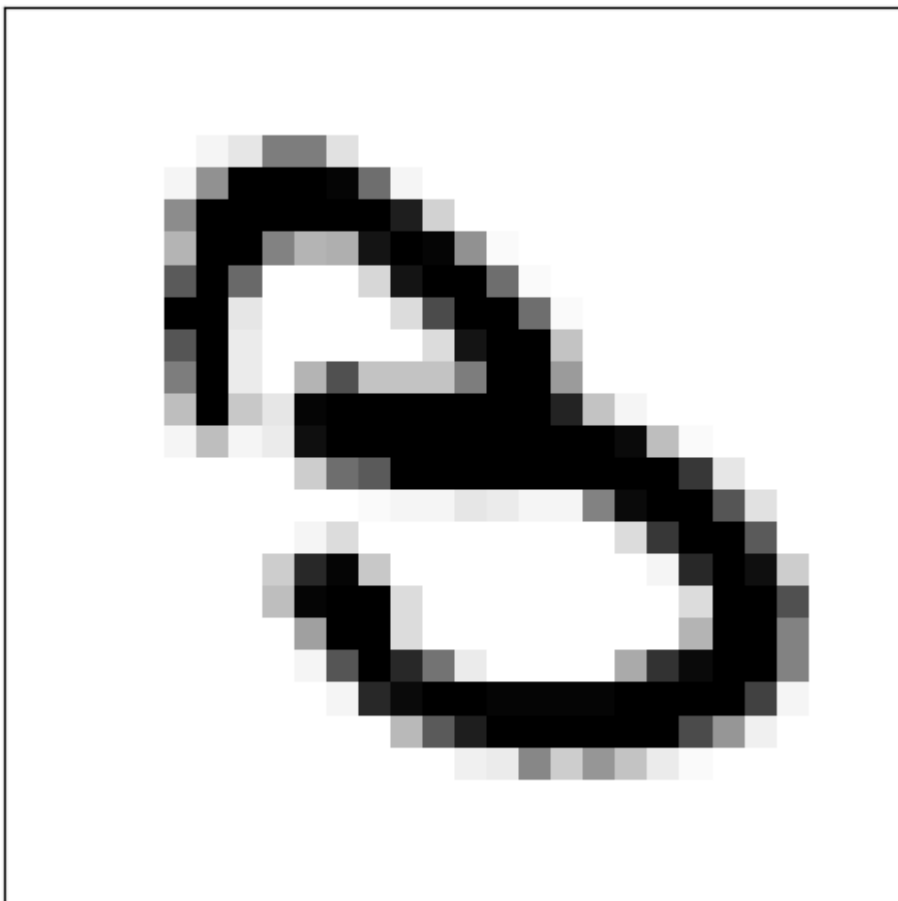
```
In [47]: badIndexes = []
y_pred = network.predict(x_test)
y_pred_rounded = np.argmax(y_pred, axis=1)
for i in range(len(y_pred_rounded)):
    if(y_pred_rounded[i] != test_labels[i]):
        badIndexes.append(i)
#otrzymaliśmy tablicę zawierającą indexy błędnie sklasyfikowanych cyfr
#wyświetlenie błędnych 4 cyfr
len_badIndexes = len(badIndexes)
for i in range(4):
    if i < len_badIndexes:

        fig, ax = plt.subplots(nrows=1, ncols=1, sharex=True, sharey=True)
        img = test_images[badIndexes[i]].reshape(28,28)
        ax.imshow( img, cmap='Greys')
        ax.set_xticks([])
        ax.set_yticks([])
        plt.tight_layout()
        plt.show()
        print("Cyfra sklasyfikowana jako:",y_pred_rounded[badIndexes[i]])
        print("Poprawna klasyfikacja:", test_labels[badIndexes[i]])
```

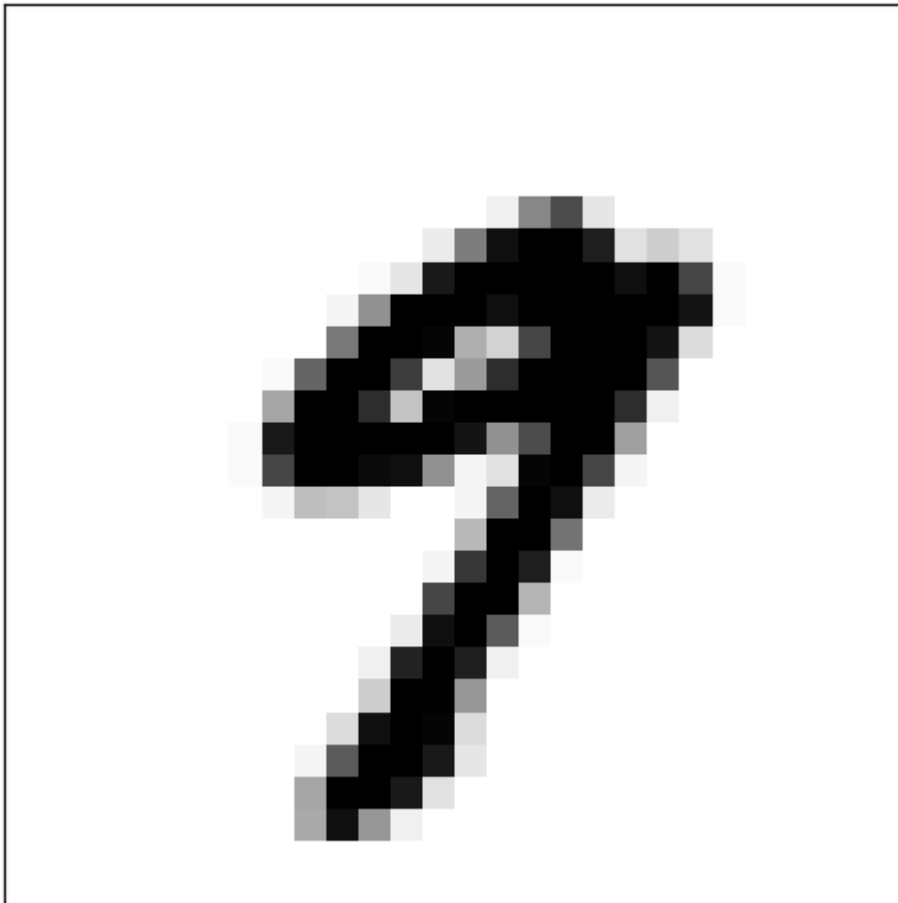
313/313 ————— **1s** 2ms/step



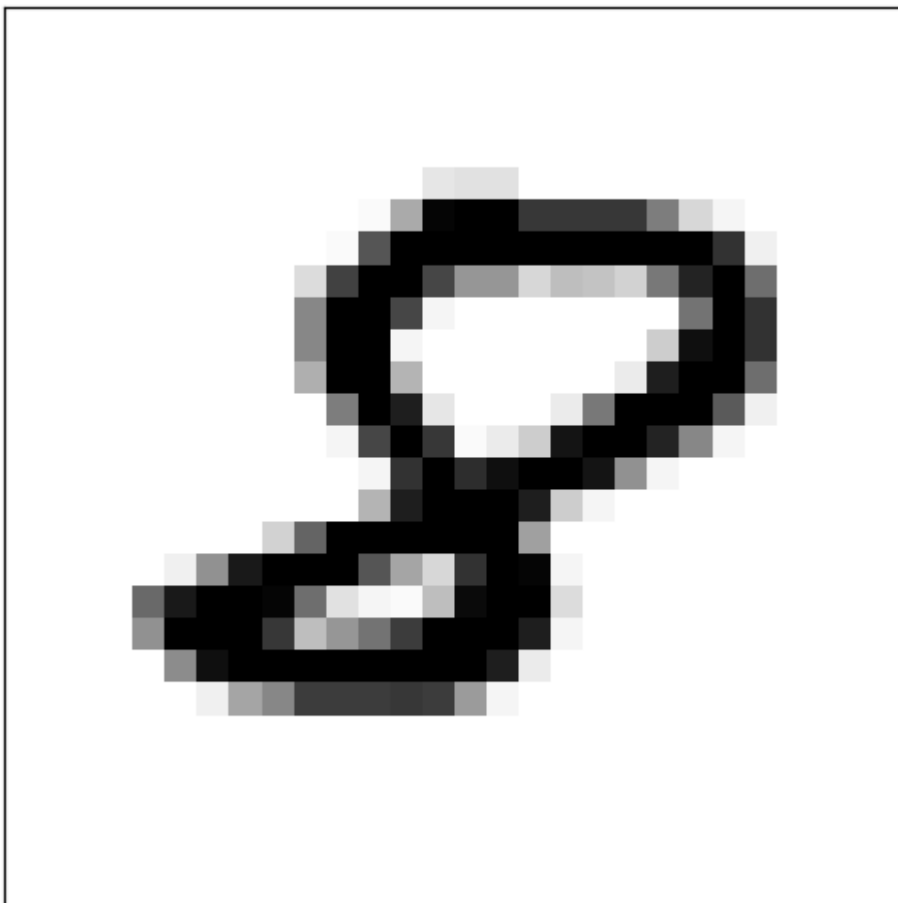
Cyfra sklasyfikowana jako: 6
Poprawna klasyfikacja: 5



Cyfra sklasyfikowana jako: 8
Poprawna klasyfikacja: 3



Cyfra sklasyfikowana jako: 7
Poprawna klasyfikacja: 9



Cyfra sklasyfikowana jako: 2
Poprawna klasyfikacja: 8

In []: