

Support Tensor Machines for Classification of Hyperspectral Remote Sensing Imagery

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Abstract—In recent years, the support vector machines (SVMs) have been very successful in remote sensing image classification, particularly when dealing with high-dimensional data and limited training samples. Nevertheless, the vector-based feature alignment of the SVM can lead to an information loss in representation of hyperspectral images, which intrinsically have a tensor-based data structure. In this paper, a new multiclass support tensor machine (STM) is specifically developed for hyperspectral image classification. Our newly proposed STM processes the hyperspectral image as a data cube and then identifies the information classes in tensor space. The multiclass STM is developed from a set of binary STM classifiers using the *one-against-one* parallel strategy. As a part of our tensor-based processing chain, a multilinear principal component analysis (MPCA) is used for preprocessing, in order to reduce the tensorial data redundancy and, at the same time, preserve the tensorial structure information in sparse and high-order subspaces. As a result, the contributions of this work are twofold: a new multiclass STM model for hyperspectral image classification is developed, and a tensorial image interpretation framework is constructed, which provides a system consisting of tensor-based feature representation, feature extraction, and classification. Experiments with four hyperspectral data sets, covering agricultural and urban areas, are conducted to validate the effectiveness of the proposed framework. Our experimental results show that the proposed STM and MPCA-STM can achieve better results than traditional SVM-based classifiers.

Index Terms—Classification, dimensionality reduction, feature extraction, hyperspectral, support tensor machine (STM), support vector machine (SVM), tensor.

I. INTRODUCTION

IN THE past decades, hyperspectral imaging has attracted extensive research efforts since such data provide continuous bands throughout the electromagnetic spectrum, as well as exhibit the potential to precisely discriminate between different land cover types using a wealth of spectral information [1], [2]. Supervised hyperspectral image classification where pixels are labeled to one of the predefined classes, is among the most active research areas in hyperspectral analysis [3]. Many supervised classification methods have been developed for hyperspectral imagery [4]–[8], including random forest [9], [10], spectral unmixing [11], [12], subpixel mapping [13], neural networks [14], decision trees [15], and several others [16]–[18]. As a supervised machine learning technique, support vector machine (SVM) has achieved great success in various applications, including military problems [19], biological analysis [20], and pattern recognition [21]. It aims to acquire a classification hyperplane that maximizes the margin between the samples [22]. Taking advantage from its ability in dealing with high-dimensional data sets and limited training samples, SVM has been shown to be successful for hyperspectral image classification [23]–[25].

However, when the ratio between the number of spectral bands and the number of available training samples is unbalanced, hyperspectral image classification becomes an ill-posed problem that can reduce the interpretation accuracy [26], [27]. To alleviate the problem of information redundancy in hyperspectral spaces, SVM is often implemented together with the dimensionality reduction preprocessing [28]. Meanwhile, semisupervised SVMs have been also developed for solving the problem of limited training samples in high-dimensional feature spaces [29]. In addition, variations of the SVM-based algorithms include postprocessing based on decision rules [30], consideration of spatial information [31], [32], composite kernels [33], and active learning [34], [35].

It should be noted that the vector-based processing mode and feature alignment traditionally used by the SVM can lead to the loss of structural information for hyperspectral imagery, which has an intrinsic tensor-based data structure. Specifically, the spatial relationship between pixels cannot be effectively exploited in a vector-based approach for feature representation and interpretation. Inspired by the tensor learning methods

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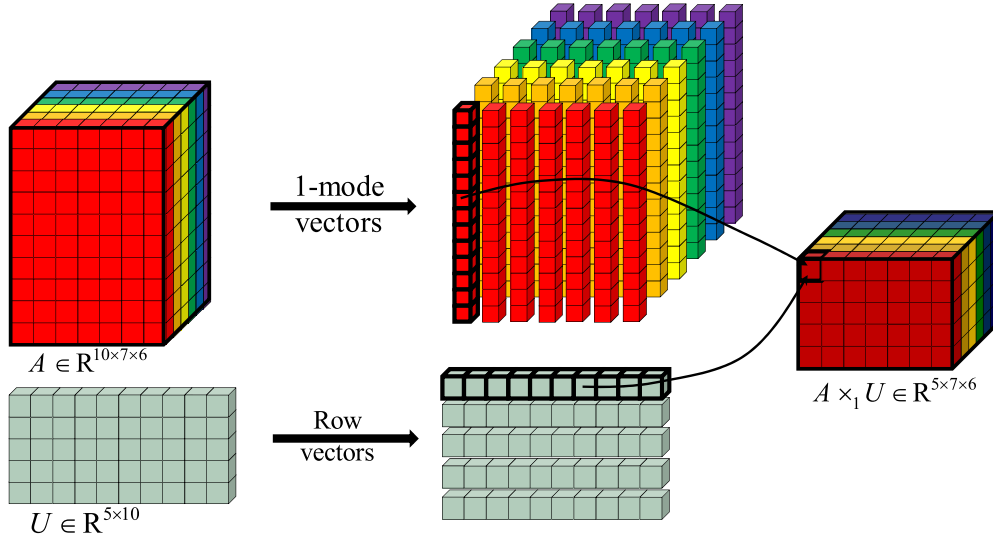


Fig. 1. Visual illustration of the mode- d tensor product operation.

developed in the area of signal processing, a support tensor machine (STM) [36] can be achieved by generalizing the SVM to its tensorial version based on multilinear algebra principles. The goal is to keep the robust performance of the classic SVM formulation while, at the same time, preserving the manifold data structure in sparse and high-dimensional feature spaces. STM has been applied to multiple applications, such as data retrieval [37], face recognition [38], and gait recognition [39]. However, in the existing literature, few studies have been reported for applying STM to remote sensing problems in general and hyperspectral image classification problems in particular. In this context, here, we develop a new multiclass STM and a tensor-based hyperspectral image processing chain to solve the multiclass classification for remote sensing imagery. Our systematic framework includes tensor-based feature extraction, dimensionality reduction, and classification. Specifically, in this paper, a multilinear principal component analysis (MPCA) [40] is used to reduce data redundancy due to the sparse and redundant high-dimensional tensor feature space for the hyperspectral data. The main contribution of this work is to introduce and adapt STM into hyperspectral remote sensing image classification. The effectiveness of the proposed method is validated by a set of experiments conducted on four hyperspectral data sets covering various land cover types. In addition, the parameters (e.g., window size, number of training samples, penalty coefficient, and feature dimensionality) are analyzed in detail in experiments.

The remainder of this paper is organized as follows. A brief review of multilinear algebra is given in Section II. The proposed STM and its multiclass version are described in Section III, followed by the tensor-based dimensionality reduction framework, which is described in Section IV. Experimental results and a comparison with state-of-the-art methods for hyperspectral image classification are provided in Section V. Section VI analyzes the impact of parameters in the developed processing chain. The last section concludes this paper with some remarks and hints at plausible future research lines.

II. TENSOR AND MULTILINEAR ALGEBRA

The proposed STM classification framework was based on multilinear algebra theory [41], [42] and processes the tensorial input data in a multidimensional manner. In the related literature, a multidimensional array is defined as a tensor, which is represented as $A \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$. The order of the tensor A is N , and each order is called the i th mode. An arbitrary element of A is a scalar, which is denoted by $a_{l_1, l_2, \dots, l_i, \dots, l_N}$, where $1 \leq l_i \leq L_i$, and $1 \leq i \leq N$, with l_i being the location of this element in the i th mode. According to this definition, a tensor is the higher order equivalent of a vector (one-order tensor) and a matrix (two-order tensor). In this context, a hyperspectral data cube can be regarded as a three-order tensor $A \in \mathbb{R}^{L_1 \times L_2 \times L_3}$, in which orders 1 and 2 represent the spatial domain and order 3 represents the spectral domain. Some definitions related to basic tensor algebra [43] are given as follows.

Definition 2.1 (Mode- d Matricizing): Also known as mode- d matrix unfolding, the mode- d matricizing of an N -order tensor $A \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$ is denoted by $\text{mat}_d A \in \mathbb{R}^{L_d \times (L_1 L_2 \dots L_{d-1} L_{d+1} \dots L_N)}$, which represents an ensemble of vectors in the d th mode obtained by keeping index L_d fixed and varying the other indices.

Definition 2.2 (Mode- d Product): The mode- d product is an operation between a tensor $A \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$ and a matrix $U \in \mathbb{R}^{L_d \times L_{d'}}$, which is defined as

$$(A \times_d U^T)_{l_1 \times l_2 \times \dots \times l_{d-1} \times l_{d'} \times l_{d+1} \times \dots \times l_N} = \sum_{l_d} (A_{l_1 \times l_2 \times \dots \times l_{d-1} \times l_d \times l_{d+1} \times \dots \times l_N} U_{l_d' \times l_d}) \quad (1)$$

where l_1, l_2, \dots, l_N represent the indices of each mode. It should be emphasized that the d th mode size of tensor A is equal to the second mode size of matrix U . The mode- d product can be regarded as incorporating the information of the input tensor and matrix. Meanwhile, as the first mode size of U varies, dimensionality reduction and data filtering can be implemented via this operation. A visual illustration of mode-1 product between a three-order tensor and a matrix is presented in Fig. 1.

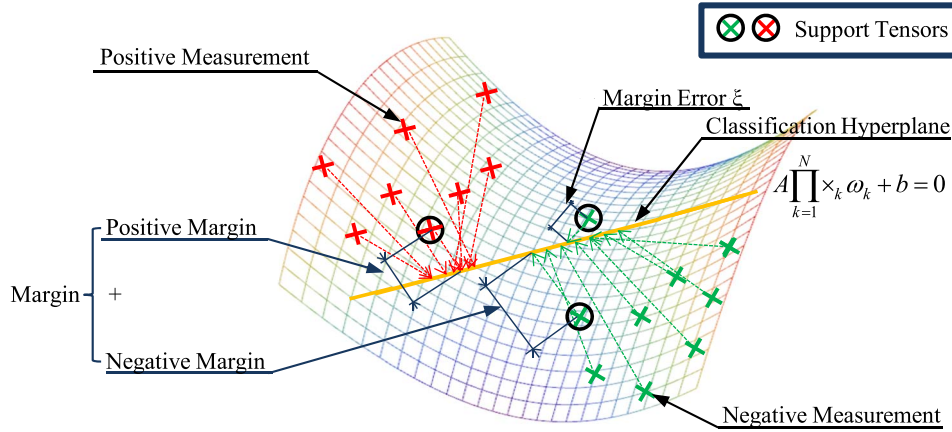


Fig. 2. Two-class problem in a high-dimensional input space solved with STMs.

Definition 2.3 (Outer Product): Operator “ \circ ” refers to outer product. $\mathbf{a}_1 \circ \dots \circ \mathbf{a}_N = \mathbf{A}$ constructs a new tensor $\mathbf{A} \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$, with each element being the product of the corresponding vector elements [44], i.e.,

$$\mathbf{a}_{l_1, l_2, \dots, l_N} = \mathbf{a}_1(l_1) \cdot \mathbf{a}_2(l_2) \cdot \dots \cdot \mathbf{a}_N(l_N) \quad (2)$$

where $\mathbf{a}_N(l_N)$ denotes the l_N ($1 \leq l_N \leq L_N$) element from \mathbf{a}_N .

III. STM

A. Binary STM

As aforementioned, SVM employs optimization algorithms to find the optimal separation boundaries between classes [45]. These optimal boundaries are calculated by minimizing the errors among all possible boundaries estimated by the available samples for each class. The decision function of the classic SVM is $y(\mathbf{a}) = \text{sign}(\boldsymbol{\omega}^T \mathbf{a} + b)$, where $\mathbf{a} \in \mathbb{R}^{L \times 1}$ is the unlabeled vector input, $y \in \{-1, +1\}$ refers to the predicted label, b is the bias term, and $\boldsymbol{\omega} \in \mathbb{R}^{L \times 1}$ is the projection matrix. The model parameters can be calculated by solving the following optimization problem:

$$\left[\begin{array}{ll} \min_{\boldsymbol{\omega}, b, \xi} & f(\boldsymbol{\omega}, b, \xi) = \frac{1}{2} \|\boldsymbol{\omega}\|^2 + c \sum_{i=1}^N \xi_i \\ \text{s.t.} & y_i [\boldsymbol{\omega}^T \mathbf{a}_i + b] \geq 1 - \xi_i, \quad 1 \leq i \leq N \\ & \xi_i \geq 0 \end{array} \right] \quad (3)$$

As a tensorial generalization of SVM, STM aims at finding a series of hyperplanes that separate the tensorial data set into a set of predefined classes in a way that is consistent with the training samples. The multilinear decision function for STM is modeled to classify the unlabeled tensorial input $\mathbf{A} \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$ in the following high-order form:

$$y(\mathbf{A}) = \text{sgn} \left(\mathbf{A} \prod_{k=1}^N \times_k \boldsymbol{\omega}_k + b \right) \quad (4)$$

where $y \in \{-1, +1\}$, b is the bias term, and $\boldsymbol{\omega}_k \in \mathbb{R}^{L_k \times 1}$ is the weight calculated by

$$\left[\begin{array}{ll} \min_{\boldsymbol{\omega}_k |_{k=1}^N, b, \xi} & f(\boldsymbol{\omega}_k |_{k=1}^N, b, \xi) = \frac{1}{2} \|\boldsymbol{\omega}_1 \circ \dots \circ \boldsymbol{\omega}_N\|^2 + c \sum_{i=1}^N \xi_i \\ \text{s.t.} & y_i \left[\mathbf{A}_i \prod_{k=1}^N \times_k \boldsymbol{\omega}_k + b \right] \geq 1 - \xi_i, \quad 1 \leq i \leq M \\ & \xi_i \geq 0 \end{array} \right] \quad (5)$$

where $\boldsymbol{\omega}_k |_{k=1}^N$ represents $\boldsymbol{\omega}_k$ ($k = 1, 2, \dots, N$) for short, and $\boldsymbol{\omega}_k$ corresponds to the weight matrix on the k th mode. In the equation, ξ is the slack variable vector used to deal with the linearly nonseparable cases, and c is a regularization coefficient for penalizing misclassification errors. M is the number of total training samples, and \mathbf{A}_i ($1 \leq i \leq M$) corresponds to the i th training tensor.

Based on the objective function defined in (5), the Lagrangian for STM is given by

$$L(\boldsymbol{\omega}_k |_{k=1}^N, b, \xi, \alpha) = f(\boldsymbol{\omega}_k |_{k=1}^N, b, \xi) - \sum_{i=1}^M \alpha_i \left(y_i c_i \left(\mathbf{A}_i \prod_{k=1}^N \times_k \boldsymbol{\omega}_k + b \right) - \xi_i \right) \quad (6)$$

where $\alpha_i \geq 0$ ($i = 1, 2, \dots, M$) are the Lagrangian multipliers. The derivations of $L(\boldsymbol{\omega}_k |_{k=1}^N, b, \xi, \alpha)$ with respect to variables $\boldsymbol{\omega}_k$ ($k = 1, 2, \dots, N$) and b should be set to 0 in the optimization process, which can be solved by

$$\partial_{\boldsymbol{\omega}_j} f = \sum_{i=1}^M \alpha_i y_i \frac{d c_i}{d z} (\mathbf{A}_i \times_j \boldsymbol{\omega}_j) \quad (7)$$

$$\partial_b f = \sum_{i=1}^M \alpha_i y_i \frac{d c_i}{d z} \quad (8)$$

with $z = \mathbf{A}_i \prod_{k=1}^N \times_k \boldsymbol{\omega}_k + b$. However, the weight matrix $\boldsymbol{\omega}_j$ in (7) depends on matrix $\boldsymbol{\omega}_i$ ($1 \leq i \leq N, i \neq j$) and hence cannot be solved independently. An alternating projection optimization [46] is therefore adopted to obtain the local optimal solution. Specifically, the parameters associated with $\boldsymbol{\omega}_i$ are iteratively solved while keeping the other parameters fixed. After achieving convergence, with the parameters $\boldsymbol{\omega}$ and b resolved, the classification hyperplane obtained is given by

$$\mathbf{A} \prod_{k=1}^N \times_k \boldsymbol{\omega}_k + b = 0. \quad (9)$$

A graphical illustration of the scenario corresponding to a two-class problem in a high-dimensional input space solved with STMs is given in Fig. 2.

B. Multiclass STM

The STM is intrinsically a binary classifier. It can be adapted to multiclass classification problems, however, with a

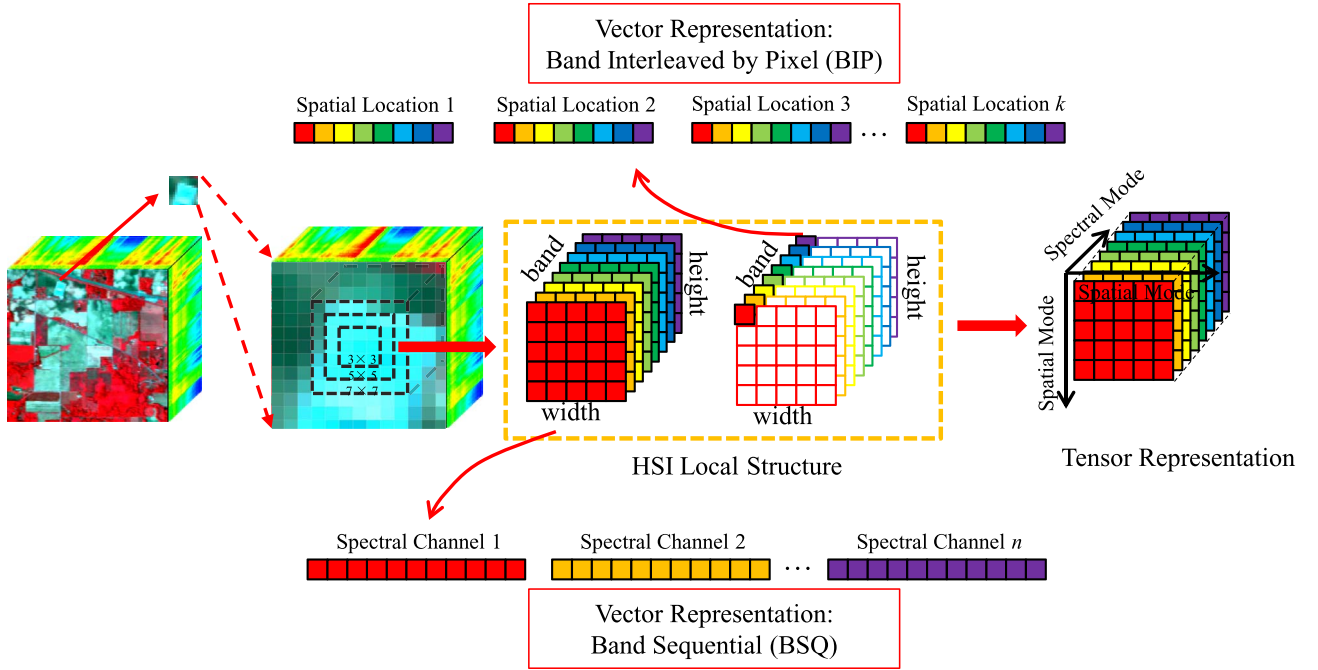


Fig. 3. Comparison between vector and tensor representations for a hyperspectral image (HSI).

one-against-one (OAO) parallel strategy [47]. Similarly, the multiclass STM can be extended from the binary STM by finding a series of hyperplanes which pairwise maximize the margin between positive and negative samples from different classes, as well as predict the class label by majority voting. This way, the outputs of all binary classifiers are taken into account for constructing the multiclass STM.

Let us consider a multiclass problem defined by a set $\Omega = \{C_1, C_2, \dots, C_S\}$ consisting of S information classes; the decision function $y_{i,j}(A)$ between each possible pair of classes C_i and C_j ($i \neq j$) can be obtained. The OAO strategy constructs $S(S-1)/2$ binary STMs to model all the possible pairwise classifications. Subsequently, an unlabeled sample A is classified by applying each pairwise classifier and computing the score function which sums the number that this sample is assigned to that class label as follows:

$$\text{Score}_i = \sum_{j=1, j \neq i}^S y_{i,j}(A). \quad (10)$$

The class with the highest score is then considered as the predicted label for the unlabeled sample A .

C. STM-Based Classification

To obtain the tensorial inputs corresponding to the labeled and unlabeled samples, a local neighborhood around the central pixel is extracted to represent a spatial-spectral tensor. For example, the tensor representation with a series of window sizes is graphically illustrated in Fig. 3 considering two types of vector representation: **band interleaved by pixel (BIP)** and **band sequential (BSQ)**. After the tensor feature representation is obtained, the labeled training tensors are used for generating the classification hyperplanes, which can be used to interpret the unlabeled ones.

It should be noted that the conventional vector-based analysis approach needs to unfold the cubic features into vectors for feature description and classification since traditional classifiers can only process vector inputs. However, the proposed STM is able to directly model the spectral-spatial tensor, which is naturally aligned as a cube for image interpretation. Compared with the traditional SVM, this characteristic presents a main methodological advantage of STM.

IV. REDUNDANCY REDUCTION FOR STM

Although the tensor-based processing approach described in the previous section can fully exploit the image spectral-spatial data structure and preserve the data manifold, the tensor-based data representation will necessarily lead to information redundancy due to the fact that a sparse hyperspectral feature space is derived from hundreds of continuous spectral channels. Moreover, due to the spatial similarity, the spectral signals of neighboring pixels are likely to be quite correlated, which is also a source of redundancy. **The sparse and high-dimensional feature space exists in both spectral and spatial domains, particularly when the neighboring pixels (in a moving window) in a hyperspectral image are simultaneously taken into consideration for classification.** Therefore, the direct use of tensor inputs will lead to a large amount of data redundancy, which poses problems to computational storage and efficiency, particularly for hyperspectral data with limited training samples. In this regard, **reducing the redundancy is a crucial step for the proposed tensor processing and classification framework.**

To deal with this problem, dimensionality reduction and feature extraction methods have been commonly applied. Here, we consider a tensor dimensionality reduction method and adapt it to the proposed tensor-based processing framework. Specifically, we use the MPCA [40], [48] as preprocessing for the STM classifier. This way, a novel tensor-based image interpretation framework is proposed by effectively

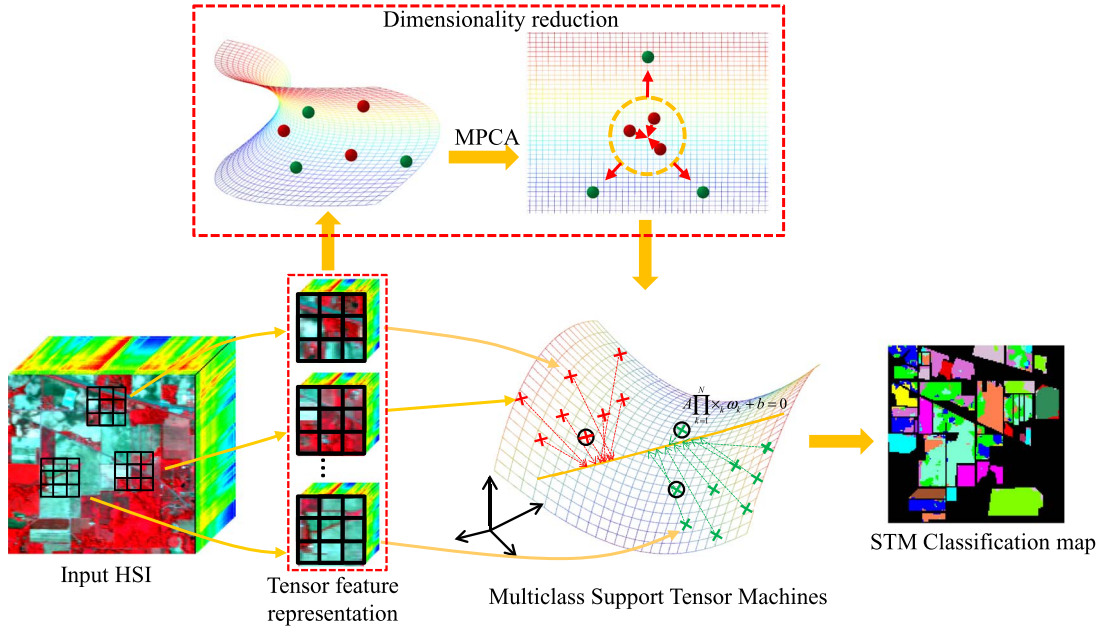


Fig. 4. Flowchart of the proposed tensor-based classification framework.

integrating tensor-based dimensionality reduction and classification. Please note that, in the proposed framework, MPCA can be replaced by other tensor-based dimensionality reduction methods, e.g., higher order singular value decomposition (HOSVD) [49]–[51].

A. MPCA

The basic idea of the MPCA is to extract the most significant signal components for all the tensor modes, while retaining as much as possible the data variation in the original data set. The potential of the MPCA-based tensor feature extraction has been shown in high-order computer vision and pattern recognition applications, such as face [52], handwriting [53], and gait recognition [54], [55]. However, few studies have been devoted to the use of MPCA for hyperspectral image feature extraction in the existing literature.

MPCA formulation involves the acquisition of projection matrices and low-dimensional tensors. Given a set of N -mode tensors $\{A_m \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}\}$, $m = 1, 2, \dots, M$, we attempt to derive the projection matrices $U_d \in \mathbb{R}^{L_d \times D_d}$, $d = 1, 2, \dots, N$, with which the low-dimensional representation of input tensor $B \in \mathbb{R}^{L_1 \times L_2 \times \dots \times L_N}$ can be obtained by $B' = B \times_1 U_1^T \times \dots \times_d U_d^T \times \dots \times_N U_N^T$, with $B \in \mathbb{R}^{D_1 \times D_2 \times \dots \times D_N}$. However, it is an NP-hard problem to obtain all N projection matrices simultaneously. For this purpose, the alternating least square (ALS) algorithm can be used to solve the optimization of projection matrices approximately [56]. The procedure of MPCA can be summarized by the following steps:

- 1) Data centralization: $\tilde{A}_m = A_m - \bar{A}$, $\bar{A} = (1/M) \sum_{m=1}^M A_m$.
- 2) At d th mode, unfold tensor \tilde{A}_m into matrix $\text{mat}_d \tilde{A}_m$ and perform eigendecomposition using $\phi_d = \sum_{m=1}^M (\text{mat}_d \tilde{A}_m) \cdot (\text{mat}_d \tilde{A}_m)^T$. The projection matrix U_d is initialized as the eigenvectors associated with the most significant D_d eigenvalues.
- 3) Optimization of the projection matrices with ALS. The initial projection is formed by calculating $\tilde{P}_m =$

$\tilde{A}_m \times_1 U_1^T \times \dots \times_d U_d^T \times \dots \times_N U_N^T$ and the scatter matrix $\psi_0 = \sum_{m=1}^M \|\tilde{P}_m\|_F^2$. Perform eigendecomposition for the covariance matrix $\phi_d = \sum_{m=1}^M (\text{mat}_d \tilde{P}_m) \cdot (\text{mat}_d \tilde{P}_m)^T$ and define U_d as the eigenvectors corresponding to the most significant D_d eigenvalues, $d = 1, 2, \dots, N$. In an iterative way, the projection $\tilde{P}_m = \tilde{A}_m \times_1 U_1^T \times \dots \times_d U_d^T \times \dots \times_N U_N^T$ and the corresponding scatter ψ_k can be updated. If the difference of the scatter matrix $\psi_k - \psi_{k-1}$ is smaller than a predefined threshold, the optimization of projection matrices is completed.

- 4) The low-dimensional tensor can be obtained by applying the mode- d product between the input tensor and the optimized projection matrix: $B' = B \times_1 U_1^T \times \dots \times_d U_d^T \times \dots \times_N U_N^T$.

B. MPCA-STM

The traditional vector-based image processing framework unfolds high-order features into vectors, which are subsequently fed into a vector-based classifier. This vector-based image processing strategy cannot sufficiently exploit the intrinsic tensor-based data structure. However, the tensor-based data representation is necessarily subject to the problem of data redundancy. As aforementioned, the redundancy is caused by the sparse hyperspectral feature space in both spectral (hundreds of continuous spectral channels) and spatial (similar pixels in the neighborhood) domains. In this context, in order to guarantee the efficiency and successful application of the STM to hyperspectral image classification, redundancy reduction is needed for preprocessing. In this paper, a tensor-based dimensionality reduction method (e.g., MPCA) is used for preprocessing of the STM classification. The whole procedure of the proposed tensor-based classification framework is therefore summarized in Fig. 4. Here, the tensor-based redundancy reduction refers to both the spectral and spatial dimensions. In the following,

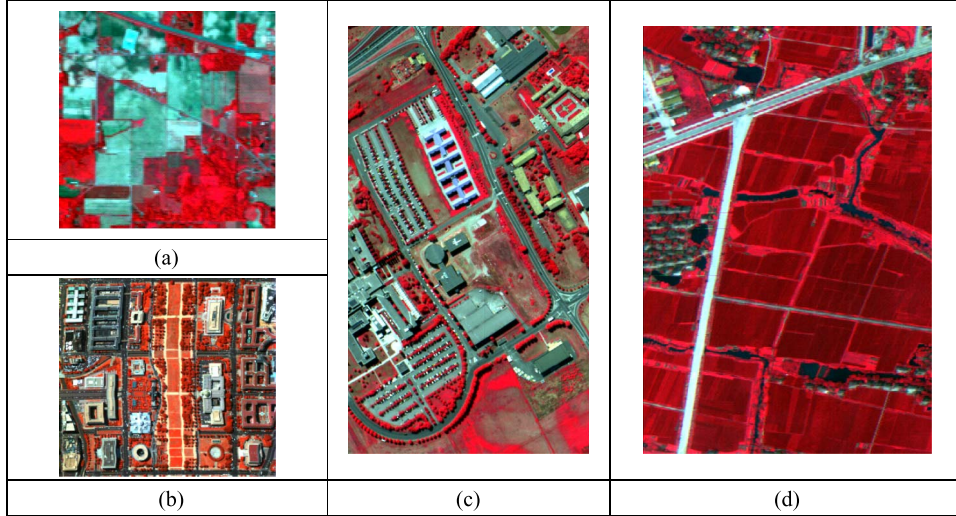


Fig. 5. False-color compositions of the four hyperspectral images used in our experiments. (a) AVIRIS Indian Pines. (b) HYDICE Washington DC Mall. (c) ROSIS-03 Pavia University. (d) PHI Xiaqiao.

$\{D_{\text{spa}}, D_{\text{spa}}, D_{\text{spe}}\}$ are used to denote the reduced dimensions for a hyperspectral image, where D_{spa} and D_{spe} are the spatial and spectral dimensions after reduction, respectively. The same value of dimensionality (i.e., D_{spa}) is defined for the x (horizontal) and y (vertical) directions in the spatial domain, since no prior information is available to determine which direction is the most relevant. In the following, we provide a set of experimental results to evaluate the classification accuracy of the framework presented in Fig. 4.

V. EXPERIMENTS

The proposed classification framework has been validated using four real hyperspectral images acquired from the instruments: Airborne Visible/Infrared Imaging Spectrometer (AVIRIS), Reflective Optics System Imaging Spectrometer (ROSIS-03), Hyperspectral Digital Imagery Collection Experiment (HYDICE), and Pushbroom Hyperspectral Imager (PHI). The considered images are presented in Fig. 5.

To verify the effectiveness of the proposed tensor-based classification framework, the proposed STM and MPCA-STM are compared with SVM with various kernel functions (e.g., the linear kernel and the Radial Basis Function (RBF) kernel). Furthermore, in this study, PCA-SVM is also carried out to consider dimensionality reduction in the SVM classification for comparison with MPCA-STM. Specifically, analogous to MPCA-STM, the pixels in a window are stacked as a long feature vector, and PCA is then used to reduce the information redundancy in the vector. The reduced features are then input to an SVM for classification. The model parameters (i.e., penalty coefficient c and bandwidth γ for the RBF kernel) of the SVM are selected based on fivefold cross validation. The classification accuracy is assessed by using the overall accuracy (OA) and the κ coefficient based on a confusion matrix. Each classification scenario is repeated ten times with different randomly selected training sets, and the mean and standard deviation of the classification results are reported for the assessment of classification performance.

A. Experiments With the AVIRIS Indian Pines Data Set

The Indian Pines data were collected by the AVIRIS sensor in 1992 over an agricultural area in northern Indiana, USA. This hyperspectral image contains 16 classes with 145×145 pixels and 220 spectral bands between 0.4 and $2.5 \mu\text{m}$. The classes and the corresponding numbers of training and test samples are listed in Table I. For each class, we randomly select a very limited number of 15 pixels for each class for training and use the remaining samples for accuracy assessment. The window size for the STM classification is set empirically to 9×9 , and the reduced dimensionality in MPCA-STM is set as $\{1, 1, 40\}$ according to our cross-validation experiments. Please note that the first principal component in the spatial domain is sufficient to represent the local image cube, as will be discussed in Section VI-D.

The classification maps and accuracy assessment for the AVIRIS Indian Pines are shown in Fig. 6 and Table I. By analyzing the classification accuracies, it is observed that the SVM with the RBF kernel (RBF-SVM) outperforms the linear SVM (Lin-SVM) since the former can effectively discriminate samples that are not linearly separable. It can be seen that the proposed STM outperforms the SVM in terms of accuracies, as the SVM neglects the local correlation of neighboring pixels, which also leads to salt and pepper noise. Compared with SVM with linear and RBF kernel, the proposed multiclass STM increases the accuracy of OA by 11.8% and 5.0%, respectively. It can be also seen that the highest accuracy, i.e., $\text{OA} = 80.6\%$, is achieved by MPCA-STM, which significantly outperforms STM. This demonstrates that large amount of redundancy exists in the tensor-based hyperspectral image representation, and a spectral-spatial dimensionality reduction approach is necessary for the tensor-based image interpretation. As shown in Table I, the proposed STM and MPCA-STM methods outperform PCA-SVM in terms of improvements of OA (0.2% and 18.2%, respectively). The better performance of the STM methods can be attributed to the fact that they process an image as a cube, but the PCA-SVM realigns the cube into a

TABLE I
ACCURACY COMPARISON FOR THE AVIRIS INDIAN PINES DATA SET (MEAN AND STANDARD DEVIATIONS OF TEN DIFFERENT EXPERIMENTS ARE GIVEN)

class	Test	Lin-SVM	RBF-SVM	PCA-SVM	STM	MPCA-STM
Alfalfa	54	81.4±4.8	95.3±8.2	100±0	94.8±6.1	98.7±2.3
Corn-notill	1434	41.2±8.0	51.3±7.3	49.4±4.9	49.7±9.4	71.9±3.5
Corn-min	834	41.1±6.3	45.6±4.2	47.3±4.5	43.1±6.8	78.2±7.5
Corn	234	65.6±7.3	65.2±8.3	86.9±7.0	82.1±4.4	93.2±4.7
Grass/Pasture	497	65.7±4.4	75.4±6.9	87.2±9.1	83.9±2.7	89.7±4.0
Grass/Trees	747	71.1±4.4	82.4±8.6	80.3±2.9	89.2±3.4	93.5±3.0
Grass/pasture-mowed	26	92.3±6.6	94.6±4.3	100±0	100±0	100±0
Hay-windrowed	489	75.8±3.5	92.0±5.5	94.6±1.7	94.8±8.6	98.4±3.4
Oats	20	86.0±7.3	97.0±3.1	100±0	100±0	100±0
Soybeans-notill	968	48.0±8.2	55.9±7.6	54.0±5.4	61.3±11.5	75.9±6.1
Soybeans-min	2468	36.1±8.0	39.4±6.5	53.6±3.0	42.0±11.6	66.9±7.1
Soybeans-clean	614	38.8±7.5	42.8±7.6	59.2±3.6	44.8±10.4	76.9±9.7
Wheat	212	90.8±2.9	95.7±4.0	97.6±4.0	96.8±2.4	99.3±0.8
Woods	1294	71.2±6.2	78.6±7.8	61.5±5.8	87.8±3.8	94.4±3.1
Bldg-Grass-Tree-Drives	380	41.4±5.4	49.7±5.8	79.2±4.6	74.0±7.5	94.5±3.7
Stone-steel towers	95	93.1±4.3	92.4±4.5	100±0	99.0±0.5	99.6±0.6
OA(%)		50.8±1.9	57.6±2.1	62.4±1.2	62.6±2.6	80.6±1.9
κ		0.45±0.02	0.53±0.02	0.58±0.01	0.58±0.03	0.78±0.02

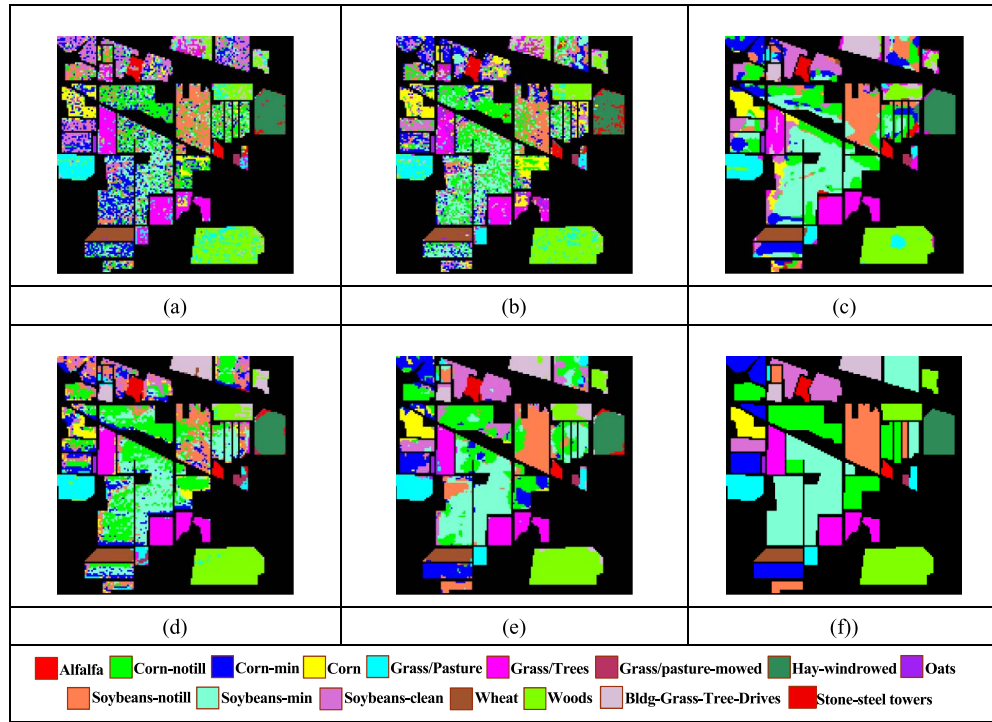


Fig. 6. Classification results obtained by different methods for the AVIRIS Indian Pines data. (a) SVM (linear kernel). (b) SVM (RBF kernel). (c) PCA-SVM. (d) STM. (e) MPCA-STM. (f) Ground-truth reference.

vector, which does not sufficiently exploit the spatial correlation between pixels.

B. ROSIS-03 Pavia University Data Set

The data set considered in this experiment is a high-resolution hyperspectral image (610×340 pixels) acquired by the ROSIS-03 sensor on the campus of the University of Pavia,

Italy. A total of 115 spectral bands was acquired in the range $0.43\text{--}0.86\ \mu\text{m}$ of the visible and infrared spectrum with a 1.3-m spatial resolution. The geospatial objects in this image refer to nine thematic classes, consisting of urban, soil, and vegetation features. In total, 42 776 labeled pixels are used for validation, as listed in Table II. The window size of the proposed tensor-based classifier and PCA-SVM is set empirically to 7×7 , and a limited number of 20 pixels per class are randomly selected as

TABLE II
ACCURACY COMPARISON FOR THE ROSIS PAVIA UNIVERSITY DATA (MEAN AND STANDARD DEVIATIONS OF TEN DIFFERENT EXPERIMENTS ARE GIVEN)

Class	Test	Lin-SVM	RBF-SVM	PCA-SVM	STM	MPCA-STM
Asphalt	6631	69.7±3.2	73.6±2.8	73.4±6.1	72.6±4.7	88.5±1.9
Meadows	18649	76.1±4.6	76.3±5.9	91.6±8.9	88.0±2.5	90.1±3.1
Gravel	2099	80.4±3.3	77.5±3.3	70.2±6.3	65.6±4.2	80.6±3.8
Trees	3064	87.3±1.3	84.7±3.1	92.5±2.8	86.5±3.6	88.9±2.9
Metal_sheets	1345	99.3±0.4	99.0±0.3	100±0	98.2±0.9	99.0±0.7
Bare_soil	5029	74.0±4.9	73.7±4.3	39.1±9.6	75.2±9.3	93.7±2.3
Bitumen	1330	90.4±3.6	86.9±5.3	83.1±4.2	84.4±4.6	96.2±4.1
Bricks	3682	73.3±11.2	76.6±5.2	58.8±8.8	70.8±10.8	78.8±6.8
Shadows	947	99.8±0.2	99.9±0.1	98.7±1.1	96.7±1.0	98.4±0.5
OA(%)		77.3±2.9	77.8±1.9	79.0±3.2	79.5±1.4	89.4±0.5
κ		0.71±0.03	0.72±0.02	0.72±0.03	0.76±0.02	0.86±0.01

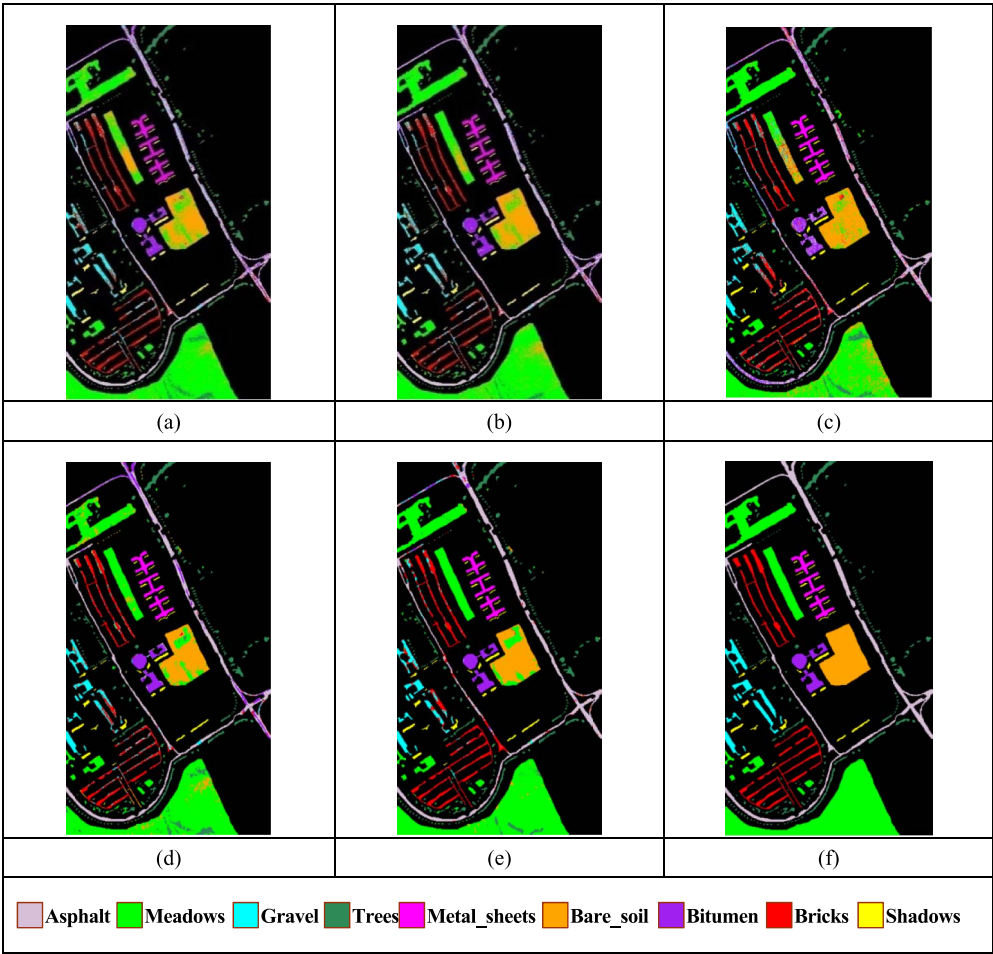


Fig. 7. Classification maps obtained by different methods for the ROSIS Pavia University data. (a) SVM (linear kernel). (b) SVM (RBF kernel). (c) PCA-SVM. (d) STM. (e) MPCA-STM. (f) Ground-truth reference.

training samples. The reduced dimensionality for MPCA-STM is chosen as {1,1,20}. This aspect is discussed in detail in Section VI-D.

The classification maps obtained by the considered algorithms are shown in Fig. 7, and the corresponding accuracy scores are presented in Table II. Misclassifications in this case lie in spectrally similar objects such as meadows–bare soil, gravel–bricks, which implies that spectral information alone is

inadequate for classification purposes. The accuracies can be improved using the proposed STM, which actually considers the intrinsic spectral–spatial data structure. For instance, the classification accuracies of bare soil and meadows classes are increased by 2% and 12%, respectively, compared with RBF-SVM. Furthermore, when redundancy reduction is considered, MPCA-STM yields 12.1% and 11.6% improvements in terms of OA, compared with Lin-SVM and RBF-SVM,

TABLE III
ACCURACY COMPARISON FOR THE HYDICE WASHINGTON DC DATA (MEAN AND STANDARD DEVIATIONS OF TEN DIFFERENT EXPERIMENTS ARE GIVEN)

class	test	Lin-SVM	RBF-SVM	PCA-SVM	STM	MPCA-STM
Roof	8806	69.7±5.2	78.3±4.0	74.8±7.1	84.6±5.3	89.9±2.6
Road	1402	93.3±3.4	84.8±5.9	89.0±2.0	90.8±2.6	92.1±0.6
Trails	1446	96.1±3.0	92.4±5.1	85.4±5.2	91.7±3.6	95.6±1.9
Grass	1790	98.1±4.0	91.0±3.1	95.6±1.2	96.0±1.2	95.8±2.7
Shadow	2423	96.6±1.0	97.2±0.6	91.1±3.9	84.5±4.8	91.3±3.7
Tree	1194	97.0±0.9	94.4±1.9	96.1±0.9	95.6±2.0	98.0±0.4
OA(%)		81.2±2.4	84.4±6.8	82.0±3.8	87.6±2.7	91.7±1.6
κ		0.74±0.03	0.78±0.08	0.74±0.05	0.83±0.04	0.87±0.02

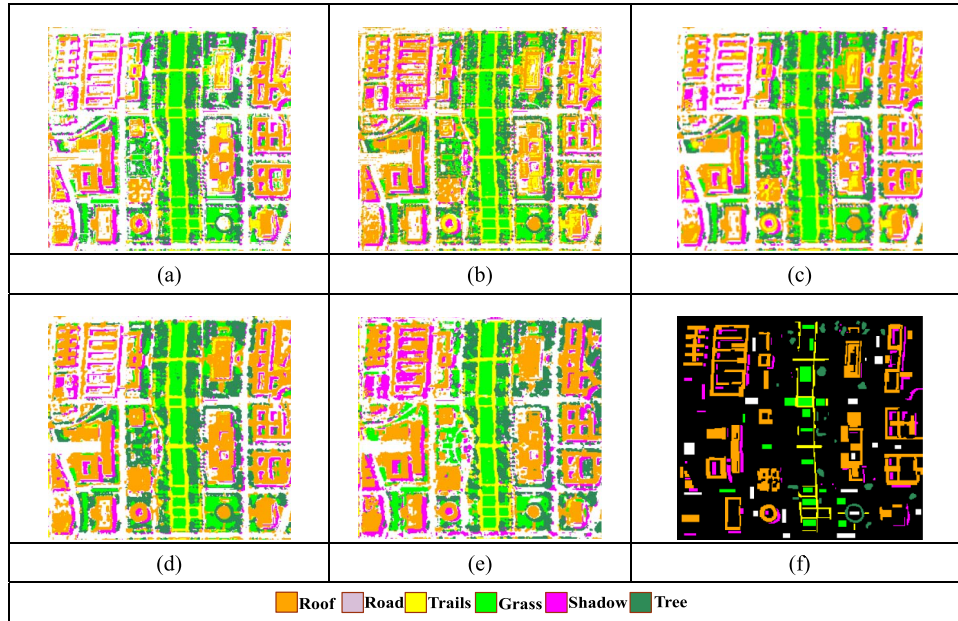


Fig. 8. Classification maps obtained by different methods for the HYDICE Washington DC data. (a) SVM (linear kernel). (b) SVM (RBF kernel). (c) PCA-SVM. (d) STM. (e) MPCA-STM. (f) Ground-truth reference.

respectively. Compared with PCA-SVM, STM and MPCA-STM achieve an accuracy increase of 0.5% and 10.4%, respectively, benefitting from the tensor-based data processing. In this experiment, it can be also observed that the proposed MPCA-STM not only exploits the implicit spectral-spatial information of hyperspectral data via tensor representation but also overcomes the issues caused by redundancy by incorporating STM with MPCA.

C. HYDICE Data Set

The HYDICE airborne hyperspectral data flight over the Washington DC Mall has been also considered in experiments. These data consist of 210 spectral bands from 0.4 to 2.4 μm , among which 19 bands were discarded due to water absorption. The test image contains 280×307 pixels with a 5-m spatial resolution. The reference data consist of 19 332 test samples, as listed in Table III, from which a limited number of 20 pixels per class are randomly selected as training samples. The classification results using Lin-SVM, RBF-SVM, STM, and MPCA-STM are given in Table III. The corresponding classifi-

cation maps are shown in Fig. 8. In this experiment, the window size is chosen as 3×3 for PCA-SVM, STM, and MPCA-STM. The reduced dimensionality for MPCA-STM is set to $\{1, 1, 20\}$.

As shown in Table III, the proposed tensor-based classifiers can give substantially more accurate results than vector-based approaches. Compared with Lin-SVM and RBF-SVM, the improvements of OA achieved by STM are 6.4% and 3.2%, respectively, whereas the increments obtained by MPCA-STM are 10.6% and 7.3%, respectively. It can be also observed from Fig. 8 that Lin-SVM is not very effective for discrimination between bare soil, roads, and buildings due to their similar spectral reflectance. The classification of these similar classes is slightly improved with RBF-SVM. In the case of STM, where tensors are considered as the basic processing unit and, hence, the contextual spectral spatial relationship can be considered adequately, the classification accuracy for the roof is improved by 14.8% and 6.3%, respectively, compared with Lin-SVM and RBF-SVM. In this experiment, the proposed MPCA-STM achieves an increment of 5.3% compared with STM, by reducing the redundancy in the tensor-based spectral-spatial domain.

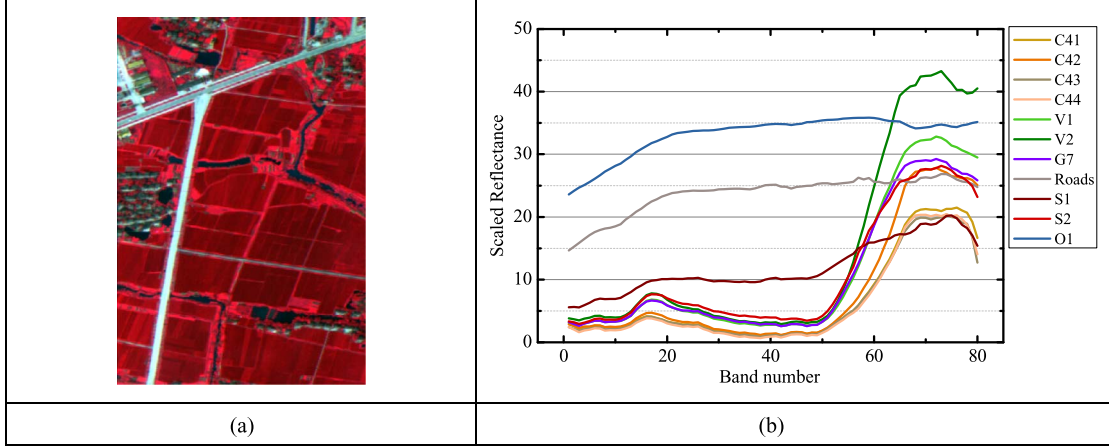


Fig. 9. (a) PHI Xiaqiao image RGB (70,40,10). (b) Reflectance curves for the classes: C, V, S, G, and O refer to corn, vegetation, soil, grass, and other classes (including lime and rocks).

TABLE IV
ACCURACY COMPARISON FOR THE PHI DATA SET (MEAN AND STANDARD DEVIATIONS OF TEN DIFFERENT EXPERIMENTS ARE GIVEN)

class	test	Lin-SVM	RBF-SVM	PCA-SVM	STM	MPCA-STM
C41	345	83.2±1.2	88.0±4.4	91.8±4.4	97.2±2.8	98.9±1.9
C42	150	96.4±3.6	99.2±0.9	99.0±1.3	99.5±1.0	100±0
C43	262	66.0±4.2	64.9±0.2	88.7±8.3	96.5±2.6	98.5±1.3
C44	155	86.7±5.9	83.7±5.9	98.4±4.2	99.3±1.1	99.5±0.9
V1	218	79.3±2.8	75.2±4.2	91.2±10.0	92.4±7.9	95.1±3.9
V2	253	85.4±10.1	94.4±9.9	90.5±5.7	90.1±4.1	97.4±1.9
G	229	67.0±5.5	62.7±12.1	86.4±6.7	90.1±3.8	99.8±0.3
Roads	221	90.0±0.5	90.0±0.3	91.0±7.1	91.1±5.7	87.1±5.5
S1	112	97.5±1.3	97.8±2.5	100±0	100±0	100±0
S2	280	88.6±3.8	93.8±7.4	85.6±6.3	90.5±9.1	98.1±1.0
O	147	74.5±5.6	84.2±2.1	99.6±1.0	83.5±9.0	98.4±2.7
OA(%)		81.9±2.2	83.9±1.6	91.6±1.5	93.4±2.2	97.4±2.8
κ		0.80±0.02	0.82±0.02	0.91±0.02	0.93±0.02	0.97±0.04

D. PHI Data Set

The PHI is a Chinese hyperspectral sensor based on push-broom imaging technique with a focal plane detector, which has a field of view of 21° and a spatial resolution of 1.5 mrad. The data set used here (346×512 pixels) was acquired by the PHI sensor over a mixed agricultural area of Xiaqiao in Jiangsu Province, China. The wavelength range for the data set is from 0.417 to $0.854 \mu\text{m}$, and 80 spectral bands are available. Eleven land cover classes are labeled with 2372 pixels used as reference based on a field survey. The challenge for this data set is to discriminate multiple crop types, which have very similar spectral properties, as shown in Fig. 9. The figure presents the spectral reflectance curves, where C, V, S, G, and O refer to corn, vegetation, soil, grass, and other classes (including lime and rocks), respectively. The classes C41, C42, C43, and C44 represent different types of corn. In experiments, a limited number of 20 pixels are randomly selected from each class as training samples.

In this experiment, STM and MPCA-STM are implemented with a 9×9 window, and the reduced dimensionality for the

MPCA is $\{1, 1, 30\}$. From the classification results in Table IV, it can be seen that (compared with Lin-SVM and RBF-SVM) the improvements of OA achieved by STM are 11.4% and 9.4%, respectively, when the local contextual information is included in the classification. Similarly, in this experiment, MPCA-STM further improves the classification accuracy of the original STM by removing the data redundancy in the sparse and hyperspectral tensor space, resulting in the highest accuracy (OA = 97.35%).

VI. DISCUSSION

The experimental results in the previous section show that the proposed STM and MPCA-STM can achieve a satisfactory performance for hyperspectral remote sensing image classification. Moreover, they provide more accurate results than the traditional SVM by constructing a new tensor-based image feature representation and interpretation framework, which is particularly appropriate for the intrinsic tensor data structure of hyperspectral data.

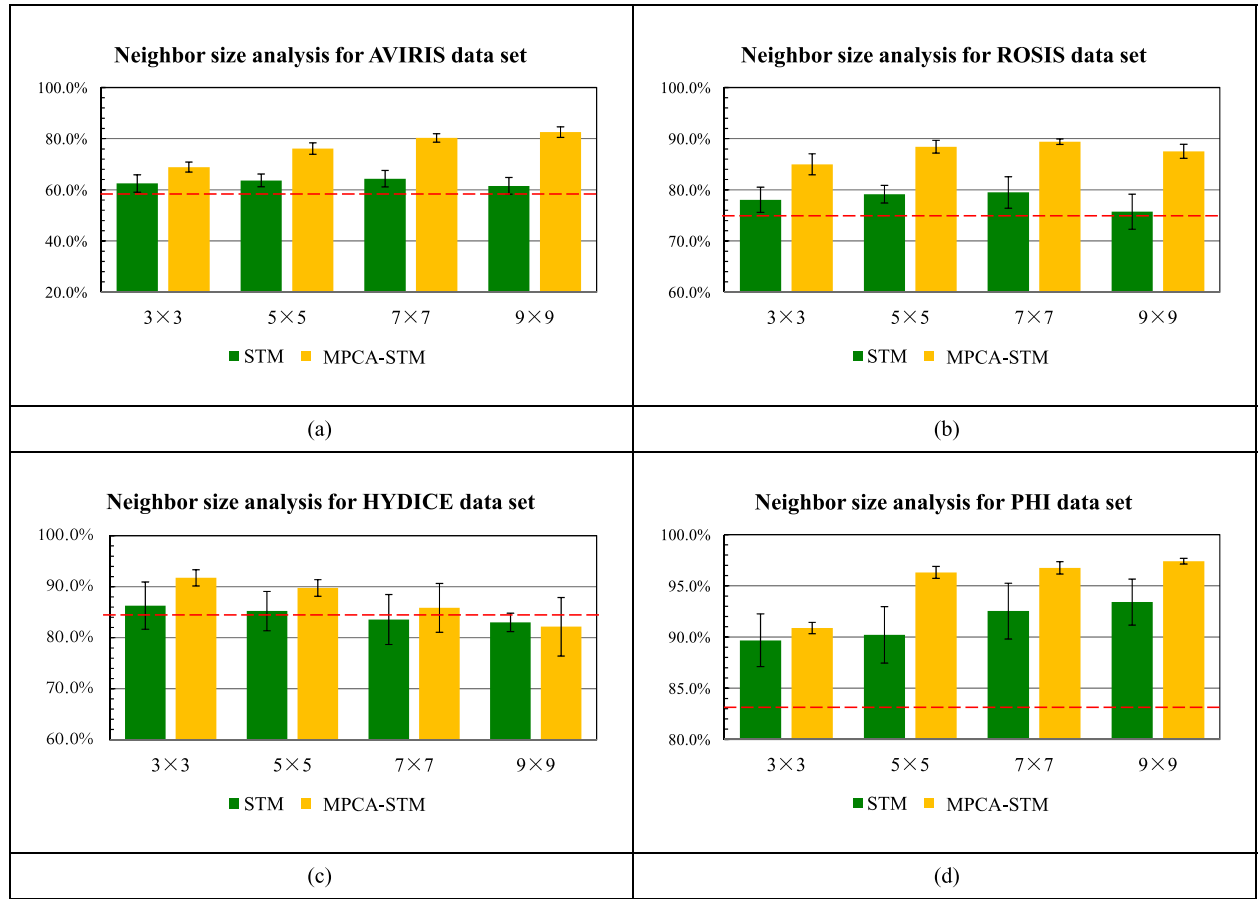


Fig. 10. Overall classification accuracy (in percentage) of STM and MPCA-STM with different window sizes for tensor representation for (a) AVIRIS, (b) ROSIS-03, (c) HYDICE, and (d) PHI data sets.

Here, the parameters for the proposed STM and MPCA-STM, namely, the window size, training samples, penalty coefficient, and tensor dimensionality, are discussed in detail in order to better understand the tensor-based image processing system.

A. Window Size for the Tensorial Feature Representation

Fig. 10 shows the classification accuracies of STM and MPCA-STM with different window sizes for the four considered experimental data sets. STM and MPCA-STM are implemented using window sizes varying from 3×3 to 9×9 by randomly choosing 20 pixels (15 pixels for AVIRIS data set) from each class for training. In the figure, the dash lines represent the accuracies obtained by RBF-SVM with the same training samples. The reduced dimensionality for MPCA is set to $\{1, 1, 40\}$ (AVIRIS), $\{1, 1, 20\}$ (ROSIS-03), $\{1, 1, 20\}$ (HYDICE), and $\{1, 1, 30\}$ (PHI), respectively.

From the perspective of image classification, small windows may not contain sufficient spatial information, whereas large windows can complicate the analysis with the possibility that multiple objects or classes are included in the window. In our experiments, it was found that the window size does not show a significant influence on the results obtained, demonstrating the robustness of the tensor image processing system. In addition,

it can be seen that the tensor-based classifiers obtain a better performance than SVM for different window sizes. Meanwhile, it can be also seen that MPCA-STM significantly outperforms the original STM in nearly all the cases since redundancy reduction is very important for the tensor-based processing.

B. Influence of the Number of Training Samples

To investigate the impact of the number of training samples on the proposed tensor-based classification framework, different numbers of training samples are used in this experiment. Specifically, for each data set, training samples are randomly generated from the reference data using a number of training samples per class that ranges from 5 to 95 pixels and using the remaining ones for testing. As shown in Fig. 11, the OA values increase rapidly with the increment of the number of training samples, and then, the accuracy curves become stable when 20–40 samples per class are used. In addition, it can be observed that the proposed tensor-based classifiers outperform the classic SVM and contextual SVM (i.e., PCA-SVM) in all cases, particularly for small numbers of training samples. This reveals that the proposed tensor feature presentation has a potential for addressing the classification uncertainty with small numbers of training samples, since tensor-based classifiers yield much better results than vector-based methods when

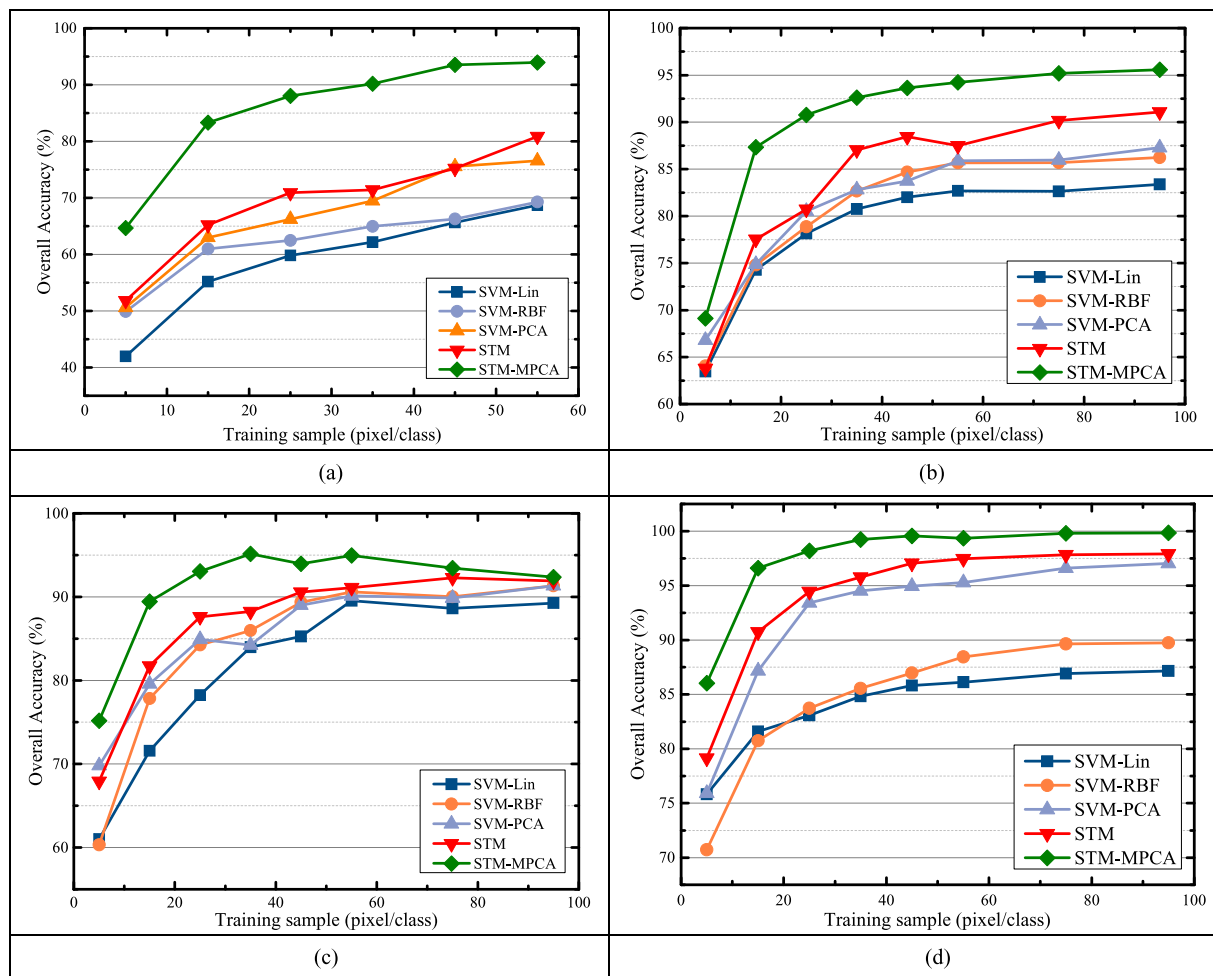


Fig. 11. Impact of numbers of training samples for different classifiers in (a) AVIRIS, (b) ROSIS-03, (c) HYDICE, and (d) PHI data sets.

5–10 samples/class are used. In this experiment, it can be also seen that MPCA-STM outperforms STM no matter how many training samples are used for training.

C. Penalty Coefficient of the STM

The penalty coefficient c determines the degree by means of which the classifier penalizes the negative samples in the training. It is an important parameter for STM since it controls the generalization of the classifier. Here, a series of experiments are conducted to investigate how the penalty coefficient c affects the performance of STM and MPCA-STM. Fig. 12 shows the obtained classification accuracies as a function of the coefficient $c \in [2^{-16}, 2^{16}]$. From the figure, it can be seen that the accuracy curves are parabolic. This phenomenon can be attributed to the fact that a small value means giving less penalty to misclassified samples, which can mix up margin support tensors and nonmargin support tensors (i.e., fall on the “wrong” side of this margin) in a problem that is not linearly separable. On the other hand, a large value can shrink the classification margin and result in performance degradation. The optimal value of the penalty parameter can be determined by cross validation.

D. Reduced Dimensionality for MPCA-STM

Here, the impact of using reduced spatial and spectral dimensions (i.e., D_{spa} and D_{spe}) for the proposed MPCA-STM is analyzed. The overall accuracies of MPCA-STM for different numbers of dimensions (in both spectral and spatial directions) are shown in Fig. 13, where the x - and y -axes refer to the spatial and spectral dimensions after reduction, respectively; and the z -axis denotes the OA (%). The highest accuracy achieved by the original STM with the optimal parameters is also indicated with a dot dashed line. Fig. 13 shows that reduced dimensionality is an important parameter, which significantly influences the performance of MPCA-STM. Specifically, we have found that the 1-D or 2-D principal components are adequate for the tensor feature representation in the spatial domain. In particular, when the first spatial principal component is considered, the performances of the MPCA-STM are much better than the original STM regardless of the spectral dimensionality. An exception is the HYDICE DC mall experiment, where the high classification accuracy (between 80% and 90%) corresponds to wide spatial dimension (between 1 and 5), but relatively narrow spectral dimension (between 1 and 50). This suggests that the spatial redundancy is relatively smaller in this study area.

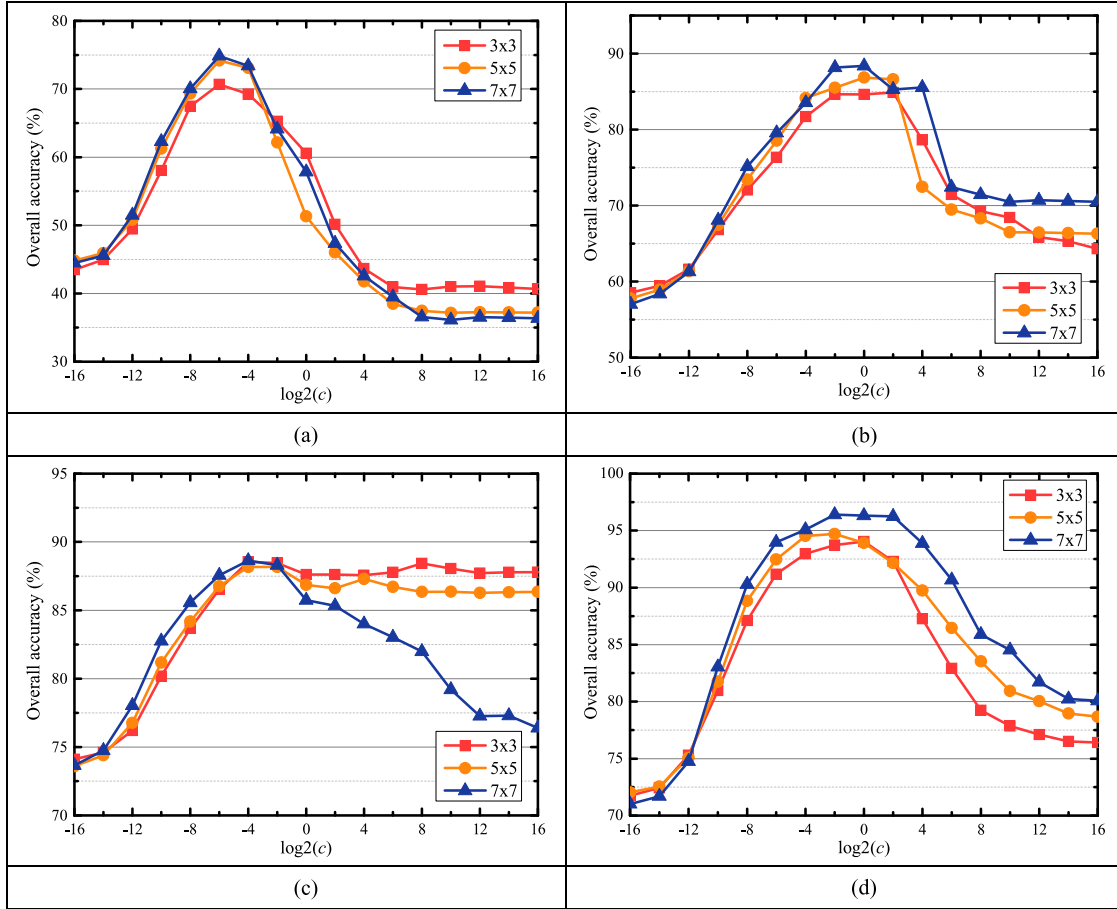


Fig. 12. Analysis of the sensitivity of the penalizing parameter c for the STM on four considered data sets. (a) AVIRIS. (b) ROSIS. (c) HYDICE. (d) PHI.

E. Computational Load

Here, the computational cost for different methods is compared in Table V. From the table, we can conclude that the moving-window-based classifiers are subject to more processing time than the traditional vector-based ones. It should be noted that PCA-SVM leads to large computational burden due to the pixel-by-pixel alignment of the local window. Additionally, the use of MPCA can remarkably alleviate the computational burden of STM.

VII. CONCLUSION AND FUTURE LINES

In this paper, we have presented a new tensor-based framework for classification of hyperspectral remote sensing imagery. Specifically, we have developed a new multiclass STM, which extends the traditional vector-based feature representation and classification strategy such as the SVM to a tensor-based version. In particular, tensor-based processing is naturally appropriate for hyperspectral remote sensing imagery, which has an intrinsic tensor data structure. Furthermore, our work reveals that information redundancy exists in the sparse and high-dimensional feature space for hyperspectral data. As a result, redundancy reduction becomes a crucial issue, particularly when the tensor data representation is considered, since redundancy can exist in both spectral and spatial directions.

Accordingly, we introduced an MPCA, which is a tensor-based dimensionality reduction algorithm, and then constructed a novel MPCA-STM classifier. MPCA-STM takes advantage of tensor feature extraction and at the same time solves the problem of information redundancy.

In order to validate the effectiveness of the newly developed STM and MPCA-STM, a series of experiments were conducted using four representative hyperspectral data sets, covering various land cover types (e.g., rural, urban, and agriculture). In all the experiments, the proposed STM outperformed the SVM in terms of both quantitative accuracy scores and visual inspection. Moreover, the interpretation accuracy can be further improved when MPCA-STM is carried out, since data redundancy is reduced simultaneously in both the spectral and spatial domains. These results demonstrate that our proposed methods exhibit potential for hyperspectral classification.

Hyperspectral data play an important part in quantitative remote sensing, precision agriculture, detailed land cover mapping, and military applications. The tensor-based system presented in this paper represents a novel method for processing and understanding hyperspectral imagery, by fully considering its intrinsic tensor data structure. In the future, we will conduct further experiments to fully substantiate the potential of the proposed tensor-based system for replacing the traditional vector-based data representation, providing more accurate analysis

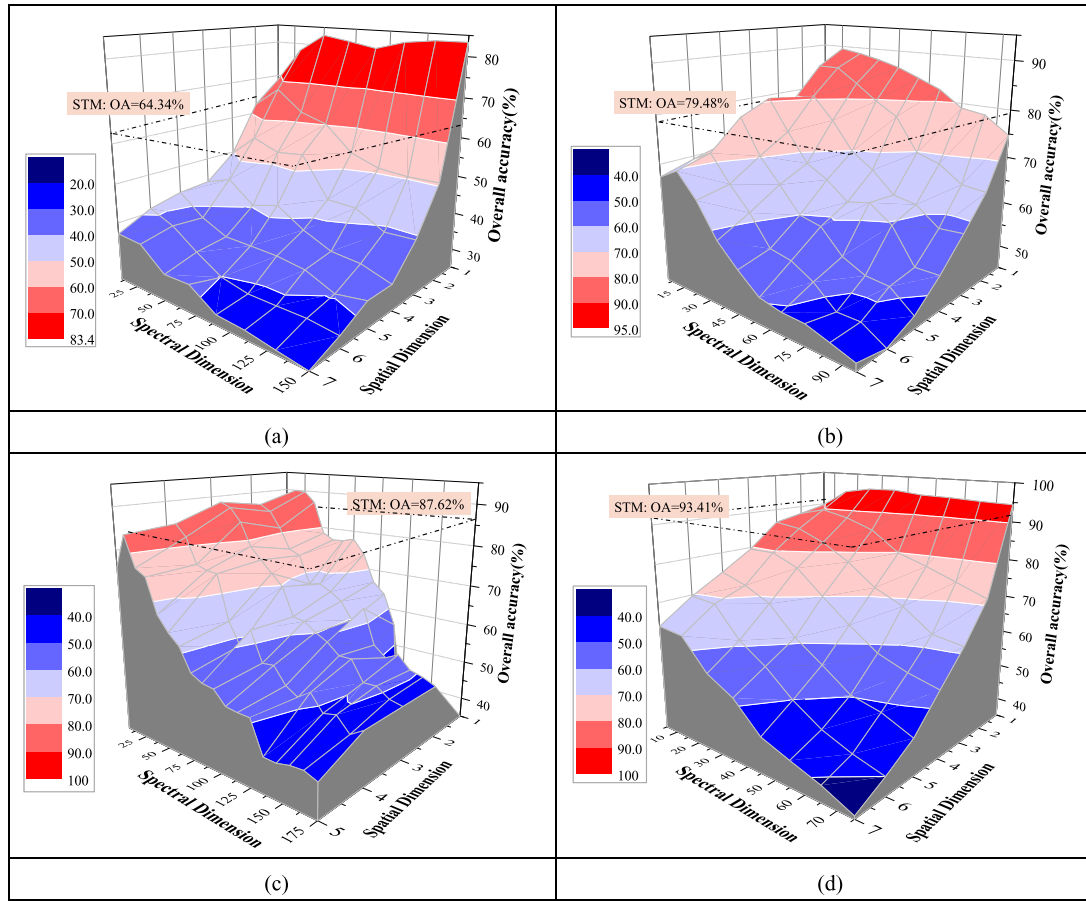


Fig. 13. Effect of using reduced spatial and spectral dimensionality for MPCA-STM. (a) AVIRIS Indian Pines. (b) ROSIS-03 Pavia University. (c) HYDICE Washington DC Mall. (d) PHI Xiaqiao.

TABLE V
COMPUTATIONAL TIME (IN SECONDS) FOR VARIOUS METHODS

Computational time(s)	SVM-Linear	SVM-RBF	PCA-SVM	STM	MPCA-STM
AVIRIS	3.10	7.20	43.42	350.52	45.93
ROSIS	1.38	3.37	150.52	143.27	43.79
HYDICE	0.63	3.31	9.28	28.67	13.55
PHI	1.95	2.13	104.78	58.12	26.91

for remote sensing applications such as classification, target detection, regression, and change detection. In addition, the spatial or structural features [57], [58] can be also represented in a tensor framework.

ACKNOWLEDGMENT

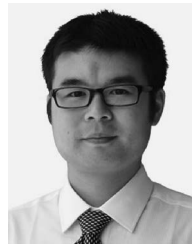
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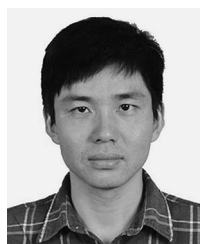
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