

This point  $z_{1234}$  is one of the points of the curve determined by  $(z_1, z_2, z_3, z_4)$ . To get the remaining points of that curve, repeat the same construction on  $(z_1, z_{12}, z_{123}, z_{1234})$  and on  $(z_{1234}, z_{234}, z_{34}, z_4)$ , ad infinitum:



The process converges quickly, and the preliminary scaffolding (which appears above the limiting curve in our example) is ultimately discarded. The limiting curve has the following important properties:

- It begins at  $z_1$ , heading in the direction from  $z_1$  to  $z_2$ .
- It ends at  $z_4$ , heading in the direction from  $z_3$  to  $z_4$ .
- It stays entirely within the so-called convex hull of  $z_1$ ,  $z_2$ ,  $z_3$ , and  $z_4$ ; i.e., all points of the curve lie “between” the defining points.