**CECS 328: Program #1**

For each of the tasks, I have included the algorithm in C# as well as a screenshot of the output. The source code for the project is available here: <https://github.com/Vardominator/CSULBProjects/tree/master/CECS328_DataStructuresAlgorithms>

1. Write a program to calculate S(n) by calculating the values of the Fibonacci sequence recursively.

**Source:**



**Sample run:**



1. Write a non-recursive program to calculate S(n).

**Source:**

**Sample run:** 

1. Algebraically verify that g(n) is a solution of Equ 1 by substituting g(n) in Equ 1.

(This portion is attached to the assignment packet)

1. Write a third iterative program by summing g(n) over n.

**Source:**



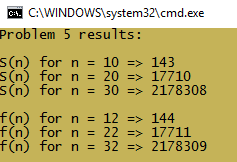
**Sample run:**



1. Calculate these values of S for n = 10, 20, 30. Calculates values of f for n = 12, 22, 32.

**Sample run:**





1. Prove the identity S(n) = f(n + 2) – 1 using induction.

(This portion is attached to the assignment packet)

1. Example run using the alternate sum from #6.

**Source:**

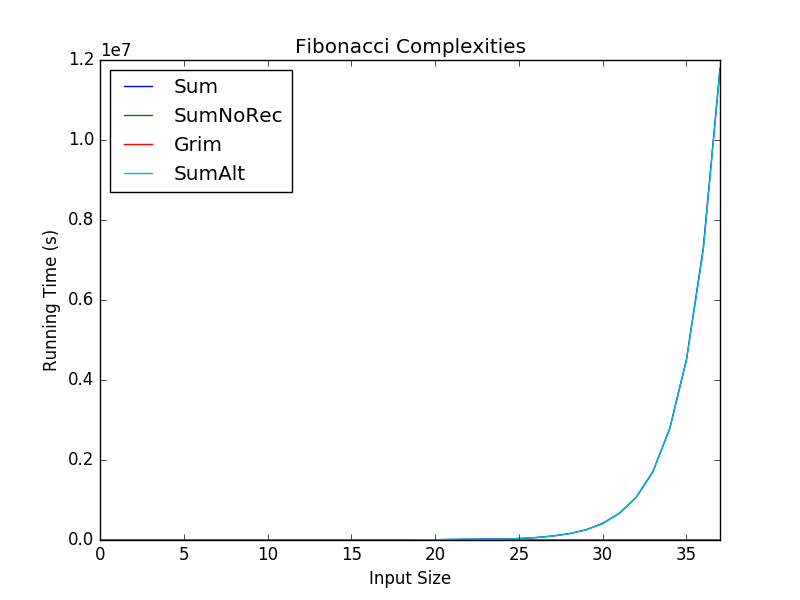
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**Sample run:**

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1. Since I am using Int64 (long in C#) to calculate the sums, the largest n that can be used is such that S(n) does not exceed 9,223,372,036,854,775,807. Another limitation would be the possibility of running out of stack space. Since the Fibonacci calls are recursive, a sufficiently large n would cause the program to crash.
2. Compare the running times of the 4 methods.

I computed the sum with each method for values of n starting at 1 and ending at 50. I recorded the running times for each. Finally, I ran a python script to plot the growth of the running times versus the input size.



1. Summary and conclusions.

We see in the plots above that the 4th method grows the fastest by a considerable amount. However, the difference is not much. The drawbacks of the recursive methods are that they have linear growth in space complexity: , as opposed to the non-recursive methods that have a constant space complexity.

Mathematically the recurrence relation for the Fibonacci sequence is . Using a recursion tree, we can prove that the time complexity is . This means that the recursive Fibonacci sequence grows relatively fast.

Finally, it is worth noting that a recursive solution to the sum is slower than the Grimaldi solution. I have shown this in the plots above. It is very clear that the recursive methods dominate in regards to computational time. Sum and SumAlt overlap because their computation times are nearly identical, but the non-recursive running times are so insignificant they are not even visible.