

Lecture 2, Wednesday, January 19, 2022

- *Node voltage*: energy gain per Coulomb moved from a reference node to a specific node.

It changes if the reference changes. Element voltages do no change.

- *Kirchhoff's voltage law (KVL)*: Around any closed loop

$$\sum V_{\text{rise}} = \sum V_{\text{drop}} \Rightarrow \sum V_{\text{drop}} - \sum V_{\text{rise}} = 0$$

– don't loose or gain energy when you return to the same node

- *Kirchhoff's current law (KCL)*: At any node

$$\sum I_{\text{in}} = \sum I_{\text{out}}$$

– don't create/loose current at any node

- *Resistor*:

– Resistance, $R \in [0, \infty)$

* If $R = 0$ it acts as a short

* If $R = \infty$ it acts as an open circuit

– Units: Ohms: $\Omega = \frac{V}{A}$

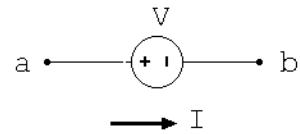
– *Ohm's law*: $V = RI$

* assumes SRS: current enters the \oplus terminal

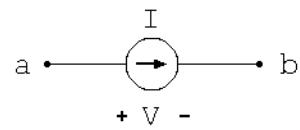
continued on next page....

Lecture 2, continued from previous page...

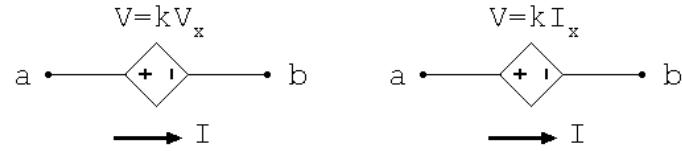
- *Independent voltage source*: voltage and polarity are fixed



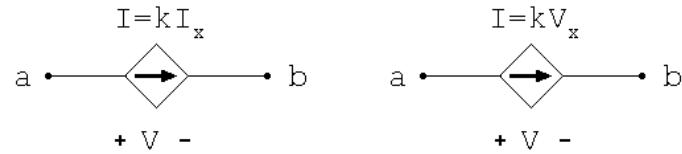
- *Independent current source*: current and its direction are fixed



- *Dependent voltage source*: voltage depends on voltage or current somewhere else in circuit



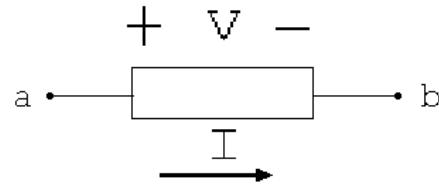
- *Dependent current source*: current depends on voltage or current somewhere else in circuit



continued on next page....

Lecture 2, continued from previous page...

- *Absorbed power*: total energy loss of charge carriers per unit time from terminal \oplus to \ominus .



$$P = \frac{dW}{dt} = \frac{dW}{dq} \frac{dq}{dt} = VI \quad \left\{ \begin{array}{l} > 0 \text{ absorbs} \\ = 0 \\ < 0 \text{ injects} \end{array} \right.$$

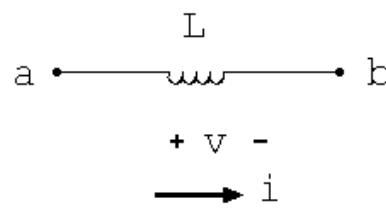
– assume SRS: current enters the \oplus terminal

– Units: Watts: $W = \frac{J}{s}$

– Resistor:

$$P = VI = (RI)I = RI^2 \geq 0 \quad P = VI = V \left(\frac{V}{R} \right) = \frac{V^2}{R} \geq 0$$

– *Inductor*:



* Inductance $L \in [0, \infty)$

* Units: Henries (H)

$$* v(t) = L \frac{di}{dt}$$

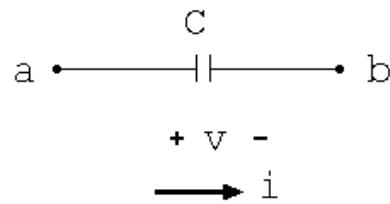
· if current, i , is constant then inductor acts as a short

$$* P = vi = \left(L \frac{di}{dt} \right) i = \frac{d}{dt} \underbrace{\left(\frac{1}{2} Li^2 \right)}_{\text{energy stored}} \quad \left\{ \begin{array}{l} > 0 \text{ absorbs} \\ = 0 \\ < 0 \text{ injects} \end{array} \right.$$

continued on next page....

Lecture 2, continued from previous page...

– Capacitor:



* Capacitance $C \in [0, \infty)$

* Units: Farads (F)

$$* i(t) = C \frac{dv}{dt}$$

• if voltage, v , is constant then capacitor acts as an open circuit

$$* P = vi = v \left(C \frac{dv}{dt} \right) = \frac{d}{dt} \underbrace{\left(\frac{1}{2} Cv^2 \right)}_{\text{energy stored}} \quad \begin{cases} > 0 \text{ absorbs} \\ = 0 \\ < 0 \text{ injects} \end{cases}$$