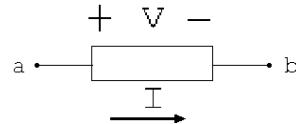


## Lecture 21, February 23, 2022

- Average absorbed power
  - If  $v$  and  $i$  are time-varying, then the instantaneous power is

$$p(t) = v(t)i(t)$$



- For periodic signals with period  $T$ , the *average absorbed power* is

$$P = \frac{1}{T} \int_T p(t)dt = \frac{1}{T} \int_T v(t)i(t)dt$$

- For cosinusoidal  $v(t) = \text{Re}\{Ve^{j\omega t}\}$  and  $i(t) = \text{Re}\{Ie^{j\omega t}\}$

$$P = \frac{1}{2} \text{Re}\{VI^*\} = \frac{1}{2} \text{Re}\{V^*I\}$$

- Resistor

$$P = \frac{1}{2} \text{Re}\{VI^*\} = \frac{1}{2} \text{Re} \left\{ V \left( \frac{V}{R} \right)^* \right\} = \frac{|V|^2}{2R} = \frac{R|I|^2}{2}$$

*Important:* take the magnitude before squaring, and remember dividing by 2.

- Inductor

$$P = \frac{1}{2} \text{Re}\{VI^*\} = \frac{1}{2} \text{Re} \{(j\omega LI)I^*\} = 0 \text{ W}$$

- Capacitor

$$P = \frac{1}{2} \text{Re}\{VI^*\} = \frac{1}{2} \text{Re} \left\{ \left( \frac{I}{j\omega C} \right) I^* \right\} = 0 \text{ W}$$