

Lecture 33, Wednesday, March 23, 2022

- The energy content of $f(t)$ is given by

$$W = \int_{-\infty}^{\infty} |f(t)|^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty} |F(\omega)|^2 d\omega$$

- $|F(\omega)|^2$ is called the *energy spectrum* of $f(t)$
- Energy bandwidth
 - Lowpass signals
 - * 3dB bandwidth (Ω_{3dB}): smallest $\omega > 0$ such that

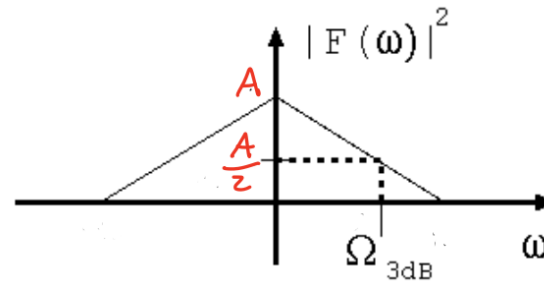
$$10 \log_{10} \left(\frac{|F(\omega)|^2}{|F(0)|^2} \right) = -3$$

or equivalently

$$\frac{|F(\omega)|^2}{|F(0)|^2} = \frac{1}{2}$$

or equivalently

$$\frac{|F(\omega)|}{|F(0)|} = \frac{1}{\sqrt{2}}$$



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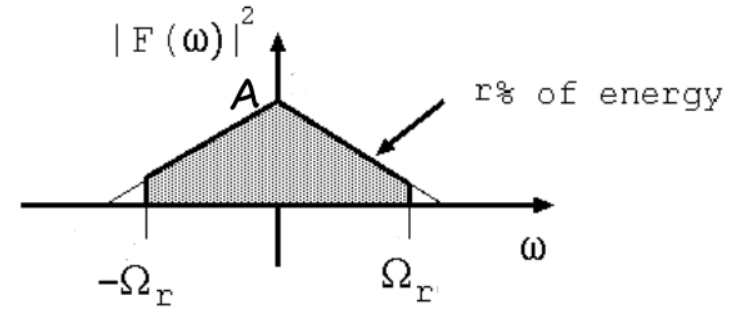
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* $r\%$ bandwidth: $\Omega_r > 0$ such that

$$\frac{1}{2\pi} \int_{-\Omega_r}^{\Omega_r} |F(\omega)|^2 d\omega = \frac{r}{100} W$$

or

$$\frac{1}{2\pi} \int_0^{\Omega_r} |F(\omega)|^2 d\omega = \frac{r}{100} \frac{W}{2}$$



• Energy bandwidth

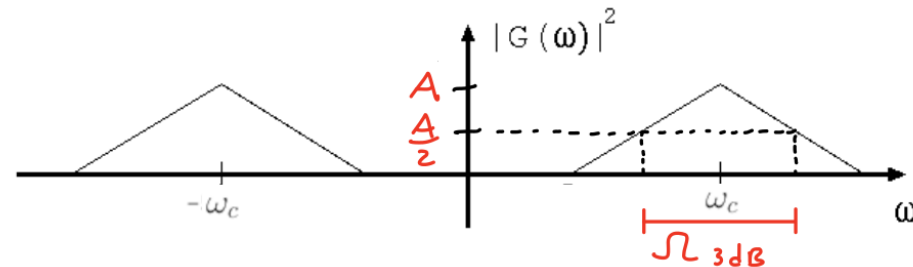
– Bandpass signals

* Assume the energy spectrum, $|F(\omega)|^2$, is symmetric around a center frequency ω_c

* 3dB bandwidth (Ω_{3dB}):

· First find smallest $\hat{\omega} > 0$ such that

$$\frac{|F(\omega_c + \hat{\omega})|^2}{|F(\omega_c)|^2} = \frac{1}{2}$$



· Then $\Omega_{3dB} = 2\hat{\omega}$