

Lecture 21, February 23, 2022

- Average absorbed power

- If v and i are time-varying, then the instantaneous power is

$$p(t) = v(t)i(t)$$


- For periodic signals with period \mathbf{T} , the *average absorbed power* is

$$P = \frac{1}{T} \int_T p(t) dt = \frac{1}{T} \int_T v(t)i(t) dt$$

- For cosinusoidals $v(t) = \text{Re}\{V e^{j\omega t}\}$ and $i(t) = \text{Re}\{I e^{j\omega t}\}$

$$P = \frac{1}{2} \text{Re}\{V I^*\} = \frac{1}{2} \text{Re}\{V^* I\}$$

- Resistor

$$P = \frac{1}{2} \text{Re}\{V I^*\} = \frac{1}{2} \text{Re} \left\{ V \left(\frac{V}{R} \right)^* \right\} = \frac{|V|^2}{2R} = \frac{R|I|^2}{2}$$

Important: take the magnitude before squaring, and remember dividing by 2.

- Inductor

$$P = \frac{1}{2} \text{Re}\{V I^*\} = \frac{1}{2} \text{Re} \{ (j\omega L I) I^* \} = 0 \text{ W}$$

- Capacitor

$$P = \frac{1}{2} \text{Re}\{V I^*\} = \frac{1}{2} \text{Re} \left\{ \left(\frac{I}{j\omega C} \right) I^* \right\} = 0 \text{ W}$$