

• LTIC systems - Example # 5-cont

- For each of the following systems, determine if they are linear, time-invariant, BIBO stable and/or causal:

3. $y(t) = f^2(t)$

is linear: \uparrow as a function of f , this is not a line $\Rightarrow X$

T.I.: $y(t) = f^2(t)$
 \swarrow same time \Rightarrow T.I. \checkmark

BIBO stable: $y(t) = f^2(t)$

$$|f(t)| \leq C \Rightarrow |f^2(t)| \leq C^2 \Rightarrow \checkmark$$

Causal: $y(t) = f^2(t)$
 \swarrow same t , present \Rightarrow causal \checkmark

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- For each of the following systems, determine if they are linear, time-invariant, BIBO stable and/or causal:

4. $y(t) = f(t) * u(t-1)$

$\underbrace{u(t-1)}_{h(t)}$

\Rightarrow Linear + T.I. \checkmark

$f^2(t)$

\uparrow it breaks linearity

$f(t^2)$

\uparrow it breaks T.I.

$$f(t) \rightarrow \boxed{\text{LTI}} \rightarrow y(t) = f(t) * h(t)$$

$h(t)$

BIBO stable: if LTI

$$\text{BIBO} \Leftrightarrow \int_{-\infty}^{\infty} |h(t)| dt < \infty$$

$$h(t) = u(t-1) \quad \text{--- A.I.}$$



causal: if LTI:

$$\text{causal} \Leftrightarrow h(t) = 0 \quad t < 0 \quad \checkmark$$

Chapter objectives

- Understand the meaning of an LTI system's impulse response and its relation to the frequency response
- Understand and test for BIBO stability
- Understand and test for causality of systems and signals