Numerical Optimization Practical File

Ques list:-

- 1. WAP for finding optimal solution using Line Search method.
- 2. WAP to solve a LPP graphically.
- 3. WAP to compute the gradient and Hessian of the function $f(x) = 100(x^2 x^1)$ 2 + $(1 x^1)$ 2
- 4. WAP to find Global Optimal Solution of a function $f(x) = -10Cos(\pi x 2.2) + (x + 1.5)x$ algebraically
- 5. WAP to find Global Optimal Solution of a function $f(x) = -10Cos(\pi x 2.2) + (x + 1.5)x$ graphically
- 6. WAP to solve constraint optimization problem.
- 7. WAP to implement Newton Method
- 8. WAP to implement gradient descent method
- 9. WAP to implement steepest descent method

10.WAP to implement Taylor polynomial

Ques 1

```
#Ques 1
import numpy as np
from scipy.optimize import minimize_scalar

def objective_function(x):
    return -(x**2 + 2*x + 1)

print()

min_result = minimize_scalar(objective_function, method='golden', bracket=(0, 1))
max_result = minimize_scalar(objective_function, method='golden', bracket=(0, 1))

optimal_max_solution = max_result.x
optimal_min_solution = min_result.x

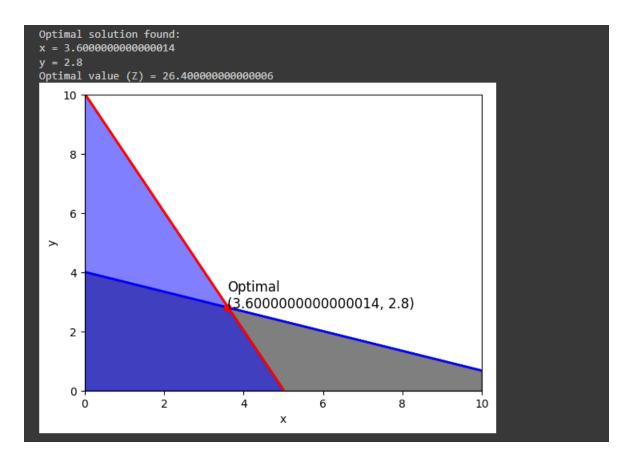
print("Maximization Result - Optimal Solution :", optimal_max_solution)
print("Minimization Result - Optimal Solution :", optimal_min_solution)
```

output

```
Maximization Result - Optimal Solution : 1.340780795141782e+154
Minimization Result - Optimal Solution : 1.340780795141782e+154
```

```
print("x =", result.x[0])
    print("y =", result.x[1])
    print("Optimal value (Z) =", -result.fun)
    x = result.x[0]
    y = result.x[1]
    print("No optimal solution found.")
x range = np.linspace(0, 10, 400)
y range = np.linspace(0, 10, 400)
X, Y = np.meshgrid(x range, y range)
constraint1 = 2 * X + Y
constraint2 = X + 3 * Y
plt.figure()
plt.contour(X, Y, (constraint1 <= 10) , colors='red', levels=[0], linewidths=2)</pre>
plt.contour(X, Y, (constraint2 <= 12), colors='blue', levels=[0], linewidths=2)</pre>
plt.fill between(x range, 0, (12 - x range) / 3, where=(12 - x range) / 3 >= 0,
color='black', alpha=0.5)
plt.fill between(y range, 0, (10-2*x range), where=(10 - 2 * y range) >= 0,
color='blue', alpha=0.5)
plt.plot(x, y, 'ro')
plt.text(x, y, f'Optimal\n(\{x\}, \{y\})', fontsize=12, ha='left')
plt.xlabel('x')
plt.ylabel('y')
plt.xlim(0, 10)
plt.ylim(0, 10)
plt.show()
```

output



Ques 3

```
#Ques 3
import sympy as sp

x1, x2 = sp.symbols('x1 x2')

f = 100 * (x2**2 - x1**2)**2 + (1 - x1)**2

gradient = [sp.diff(f, x1), sp.diff(f, x2)]

hessian = sp.hessian(f, (x1, x2))

print("Function:")

print(f)

print("\nGradient:")

print(gradient)

print(gradient)

print("\nHessian:")

print(hessian)
```

Output

```
Function:
(1 - x1)**2 + 100*(-x1**2 + x2**2)**2

Gradient:
[-400*x1*(-x1**2 + x2**2) + 2*x1 - 2, 400*x2*(-x1**2 + x2**2)]

Hessian:
Matrix([[1200*x1**2 - 400*x2**2 + 2, -800*x1*x2], [-800*x1*x2, -400*x1**2 + 1200*x2**2]])
```

Ques 4

```
#QUES 4
import numpy as np
from scipy.optimize import minimize

# Define the function to be minimized

def objective_function(x):
    return -10 * np.cos(np.pi * x - 2.2) + (x + 1.5) * x

# Initial guess for the minimum
initial_guess = [0.0]

# Use the minimize function from SciPy to find the minimum
result = minimize(objective_function, initial_guess, method='Nelder-Mead')

# Extract the optimal solution
optimal_solution = result.x[0]
optimal_value = result.fun

print("Optimal Solution:", optimal_solution)
print("Optimal Value:", optimal_value)
```

Output

Optimal Solution: 0.6714375000000008 Optimal Value: -8.500986423547845

```
#Ques 5
import numpy as np
import matplotlib.pyplot as plt

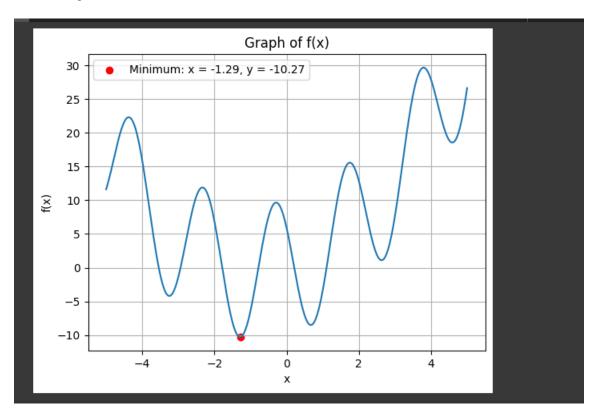
# Define the function
def f(x):
    return -10 * np.cos(np.pi * x - 2.2) + (x + 1.5) * x

# Generate x values
x = np.linspace(-5, 5, 1000)

# Calculate corresponding y values
y = f(x)

# Find the x value where the function is minimized
optimal_x = x[np.argmin(y)]
optimal_y = min(y)

# Plot the function
```



```
#Ques 6
from scipy.optimize import minimize

def objective_function(x):
    return x[0]**2 + x[1]**2

def constraint_function(x):
    return x[0] + x[1] - 1

initial_guess = [0.0, 0.0]

constraints = ({'type': 'ineq', 'fun': constraint_function})

result = minimize(objective_function, initial_guess, constraints=constraints)

print("Optimal solution:", result.x)
```

```
print("Optimal value:", result.fun)
```

```
Optimal solution: [0.5 0.5]
Optimal value: 0.500000000000000000
```

Ques 7

```
#Ques 7
def f(x):
    return x**2 - 4*x + 4

def f_prime(x):
    return 2*x - 4

def f_double_prime(x):
    return 2

x0 = 3

tolerance = 1e-6

max_iterations = 100

for i in range(max_iterations):
    x1 = x0 - f_prime(x0) / f_double_prime(x0)

    if abs(x1 - x0) < tolerance:
        break

    x0 = x1

print()
print(f"Minimum Value: {f(x0)}")
print(f"Location: {x0}")</pre>
```

Output

```
Minimum Value: 0.0
Location: 2.0
```

```
#Ques 8
import sympy as sp

def gradient_descent(initial_x, learning_rate, num_iterations):
```

```
x = sp.symbols('x')

f = x**2 + 5*x + 6

df = sp.diff(f, x)

f_prime = sp.lambdify(x, df, 'numpy')

for _ in range(num_iterations):
    gradient = f_prime(initial_x)
    initial_x = initial_x - learning_rate * gradient

return initial_x, f.subs(x, initial_x)

initial_x = 0

learning_rate = 0.1

num_iterations = 1000

min_x, min_value = gradient_descent(initial_x, learning_rate, num_iterations)

print(f"Minimum value is {min_value} at x = {min_x}")
```

```
#Ques 8
import sympy as sp

def gradient_descent(initial_x, learning_rate, num_iterations):
    x = sp.symbols('x')

    f = x**2 + 5*x + 6

    df = sp.diff(f, x)

    f_prime = sp.lambdify(x, df, 'numpy')

    for _ in range(num_iterations):
        gradient = f_prime(initial_x)
        initial_x = initial_x - learning_rate * gradient

    return initial_x, f.subs(x, initial_x)

initial_x = 0
learning_rate = 0.1
num_iterations = 1000

min_x, min_value = gradient_descent(initial_x, learning_rate, num_iterations)

print(f"Minimum value is {min_value} at x = {min_x}")
```

OUTPUT

Ques 9

```
import numpy as np
def objective function(x):
def gradient(x):
    return 2*x + 4
def steepest descent(initial guess, learning rate, tolerance):
   x = initial guess
   while True:
        grad value = gradient(x)
        if np.linalg.norm(grad value) < tolerance:</pre>
        x = x - learning_rate * grad_value
    return x, objective function(x)
initial guess = np.array([0.0])
learning rate = 0.1
tolerance = 1e-6
result = steepest descent(initial guess, learning rate, tolerance)
print("Optimal solution: x =", result[0])
```

Output

```
Optimal solution: x = [-1.99999959]
```

```
import math

def factorial(n):
    if n == 0:
```

```
return 1
return n * factorial(n - 1)

def taylor_coefficient(func, point, degree, derivative_order):
    return func(point) / factorial(derivative_order)

def taylor_polynomial(func, degree, point, var='x'):
    x = point
    taylor_poly = sum(taylor_coefficient(func, point, i, i) * (x - point)**i for i
in range(degree + 1))
    return taylor_poly

def sin_function(x):
    return math.cos(x)

degree_of_polynomial = 3
center_point = 0

taylor_poly = taylor_polynomial(sin_function, degree_of_polynomial, center_point)
print("Taylor Polynomial:", taylor_poly)
```

Taylor Polynomial: 1.0