
Attitude Control of a Quadcopter Using Adaptive Control Technique

Ramiro Ibarra Pérez, Gerardo Romero Galvan,
Aldo Jonathan Muñoz Vázquez,
Silvia Florida Melo and David Lara Alabazares

Additional information is available at the end of the chapter

<http://dx.doi.org/10.5772/intechopen.71382>

Abstract

This chapter presents an adaptive control technique to stabilize the attitude dynamics of unmanned aerial vehicle (UAV) type quadrotor in the presence of disturbances and/or uncertainties in the parameters due to changes in the payload, nonlinear actuators, and change in environmental conditions. To address the above problem, MRAC (model reference adaptive control) strategy is used. In this schema, a cost function is defined as a function of the error between the output of the system and a desired response from a reference model. Based on this error, the controller parameters are updated. To guarantee the global asymptotic stability of the system, Lyapunov's theory is applied. Simulation results using MATLAB-Simulink platform are presented to demonstrate the convergence of the controller parameters.

Keywords: Quadrotor UAV, adaptive control, Lyapunov's method, aircraft, attitude control

1. Introduction

Unmanned aerial vehicles (UAVs) are aircrafts that do not require a pilot on board to be controlled. In the beginning, they were solely used for military purposes. One of the first applications of these vehicles was aerial photography. In the 1883, an Englishman named Douglas Archibald provided one of the world's first reconnaissance UAVs. However, it was not until the World War I that UAVs became recognized systems. Since then, they are being widely used in military missions such as surveillance of enemy activity, airfield base security, airfield damage assessment, elimination of unexploded bombs, etc.

In the last decades, advances in technology and costs reduction permitted to adopt this technology in civil applications such as aerial photography, video and mapping, pollution and land monitoring, powerline inspection, fire detection, agriculture, and among other applications [1].

Quadrotors are a kind of mini-UAV's with vertical take-off and landing, controlled completed through four rotors mounted on each end of the crossed axes, which provide lift forces for the quadrotor move, this vehicle is very popular in the research community due to their special features like strong coupling subsystems, unknown physical parameters, and nonparametric uncertainties in inputs and external disturbances. Therefore, a suitable control system for stabilizing the closed loop control system is required; to do this, various control techniques, linear and nonlinear, have been implemented such as control PD [2, 3], control PID [4, 5], control of position and orientation by vision [6], sliding mode control [1, 7], fuzzy logic [8, 9], and adaptive control in [10].

The dynamic behavior of quadrotor has been published in varying complexity [11, 12]; particularly, the model we used is based on [13], where an extended mathematical description by the full consideration of nonlinear coupling between the axes is presented. We assume elastic deformations sufficient stiffness and realistic flight maneuvers were omitted, mass distributions of the quadrotor are symmetrical in the x-y plane, drag factor and thrust factor of the quadrotor are constant, and air density around the quadrotor is constant.

In this work, we develop an adaptive control strategy to stabilize the attitude dynamics of a quadrotor UAV. The adaptive control permit deals with modeling errors and disturbance uncertainty, variations of the mass, inertia, actuators faults, nonlinear aerodynamics, etc.

This chapter is organized as follows: Section 2 presents the mathematical model of the quadrotor obtained using Newton-Euler equations. Section 3 provides brief introduction about the adaptive control theory and the methodology used is based to obtain the adaptive law equations. In Section 4, simulations and analysis are presented to verify the performance of MRAC schema, and finally in Section 5, conclusions of this work are presented.

2. Mathematical model

2.1. ESC + motor + propeller

The rotors of quadrotor are modeled by

$$T_i = K \frac{\omega_M}{s + \omega_M} u_i \quad (1)$$

$$v_i = \frac{\omega_M}{s + \omega_M} u_i \quad (2)$$

For $i=(1,2,...,4)$, where u_i represents the PWM input, the gain $K>0$ and ω_M are the rotor bandwidth, v_i is the actuator dynamics. We assume K and ω_M are the same for all rotors [5].

2.2. Description of Quadrotor system

The configurations of quadrotor are described in **Figure 1** and consist of a body-fixed frame denoted by $F_b = \{F_{bx}, F_{by}, F_{bz}\}$, the center mass that coincident with the body-frame origin denoted

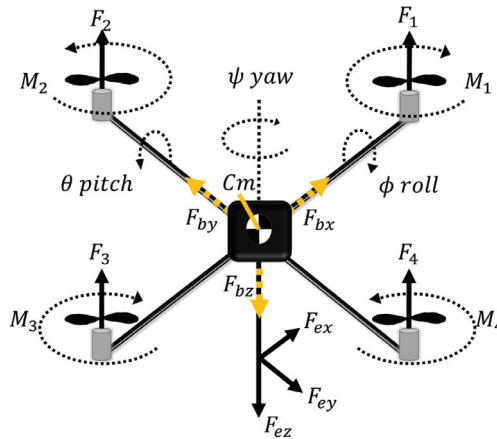


Figure 1. Quadrotor configuration.

by C_m , the earth-fixed inertial frame is denoted by $F_e = \{F_{ex}, F_{ey}, F_{ez}\}$, the position in earth-fixed inertial frame is given by a vector $r_I = (x, y, z)^T$, four rotors denoted each one as M_i with $i = (1, 2, \dots, 4)$.

To obtain the position of CM in the NED (North-East-Down) coordinate system with respect to the inertial frame F_e , we use the Euler angles (roll ϕ , pitch θ , yaw ψ) combined in a vector $\Omega = (\phi, \theta, \psi)^T$, where roll angle is generated by differential thrust between M_2 and M_4 , pitch angle is generated by differential thrust between M_1 and M_3 , and yaw angle is generated by differential torque between clock wise and anticlock wise rotors, i.e., $(M_1 - M_2 + M_3 - M_4)$. This kind of device is considered an underactuated system with six degree of freedom (DOF). Rotation matrix R is used to map from F_b to F_e applying three consecutive rotations denoted by

$$\begin{aligned}
 R_z &= \begin{pmatrix} C_\psi & -S_\psi & 0 \\ S_\psi & C_\psi & 0 \\ 0 & 0 & 1 \end{pmatrix} \\
 R_y &= \begin{pmatrix} C_\theta & 0 & S_\theta \\ 0 & 1 & 0 \\ -S_\theta & 0 & C_\theta \end{pmatrix} \\
 R_x &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & C_\phi & -S_\phi \\ 0 & S_\phi & C_\phi \end{pmatrix} \\
 R &= (R_z, R_y, R_x) = \begin{pmatrix} C_\psi C_\theta & C_\psi S_\theta S_\phi - S_\psi C_\phi & C_\psi S_\theta C_\phi + S_\psi S_\phi \\ S_\psi C_\theta & S_\psi S_\theta S_\phi + C_\psi C_\phi & S_\psi S_\theta C_\phi - C_\psi S_\phi \\ -S_\theta & C_\theta S_\phi & C_\theta C_\phi \end{pmatrix}
 \end{aligned} \tag{3}$$

where S and C refer to sin and cos function, respectively.

2.3. Rigid body dynamics

The dynamics of a rigid body under external forces and moments in the f_b can be formulated as follows [14]

$$m\dot{v} = \sum F_i \quad (4)$$

$$J\dot{W} + W \times JW = \sum M_i \quad (5)$$

where $i=(1, 2, \dots, 4)$, $\sum F_i \in \mathbb{R}^3$ represent the sum of thrust forces from each rotor, $\sum M_i \in \mathbb{R}^3$ represent the sum of moments acting on the vehicle, v is the velocity in the F_b , m is the quadrotor mass, $W=(wx, wy, wz)^T$ determines the angular velocity vector which has its origin in at the center of mass of the rigid body, and J is the inertial tensor of the symmetric rigid body around its center of mass.

To obtain the thrust force contribution of each rotor applied to F_b , we use the following formula

$$F_i = f_{xi} + f_{yi} + f_{zi} = -k \omega_i^2 \quad (6)$$

with f_{xi} force from rotor i applied in F_b respect x axes, f_{yi} force from rotor i applied in F_b respect y axes and f_{zi} force from rotor i applied in F_b respect z axes, ω_i as rotor's angle speed, k as proportional gain related with air density, the geometry of the rotor blade and its pitch angles. As f_{xi} and f_{yi} is zero, since they form an angle of 90 degrees respect to the rotor thrust, rewriting Eq. (6), we have

$$F_i = -k\omega_i^2 [0 \ 0 \ 1]^T \quad (7)$$

By transforming F_i to F_e and making use of the principle of linear momentum, the following equations can be introduced for a quadrotor of mass m under gravity g :

$$\ddot{r} = [0 \ 0 \ g]^T + R \sum_1^4 \left(\frac{F_i}{m} \right) \quad (8)$$

The rotatory moment of the body is described by Eq. (4) can be rewrite as

$$J\dot{W} + W \times JW = M_B - M_G \quad (9)$$

where M_B is the vector of external torques and is composed of the thrust differences and drag moments of the individual rotors and under considerations of the rotatory directions and can be calculated by

$$M_B = \begin{pmatrix} Lb(\omega_2^2 - \omega_4^2) \\ Lb(\omega_1^2 - \omega_3^2) \\ d(\omega_1^2 - \omega_2^2 + \omega_3^2 - \omega_4^2) \end{pmatrix} \quad (10)$$

where d is called drag factor and it is related with the air resistance, L is a parameter which represents the length of the lever between center of mass and the four rotors. M_G is the vector of gyroscopic torques generated due to the propellers rotational movements and can be calculated by the follow formula

$$M_G = J_R \left(W \times \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \right) (\omega_1 - \omega_2 + \omega_3 - \omega_4) \quad (11)$$

where J_R represents the inertia of rotating rotors. The follow equations permit us to determine the rate of change of the Euler angles in the inertial frame F_e

$$\dot{\Omega} = H(\Phi)W = \begin{bmatrix} 1 & \tan \theta \sin \phi & \tan \theta \cos \phi \\ 0 & \cos \phi & \sin \phi \\ 0 & \frac{\sin \phi}{\cos \theta} & \frac{\cos \phi}{\cos \theta} \end{bmatrix} W \quad (12)$$

The relationship that maps rotor angular velocities to forces and moments on the vehicle is

$$u = \begin{pmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \end{pmatrix} = \begin{pmatrix} b & b & b & b \\ 0 & b & 0 & -b \\ b & 0 & -b & 0 \\ d & -d & d & -d \end{pmatrix} \begin{pmatrix} \omega_1^2 \\ \omega_2^2 \\ \omega_3^2 \\ \omega_4^2 \end{pmatrix} \quad (13)$$

where the variable $u_1 = F_1 + F_2 + F_3 + F_4$. The variables u_2 and u_3 correspond the forces from rotors necessary to generate the pitch and roll moments, and u_4 represents the yaw moment.

The translation motion is obtained combining Eqs. (3), (7), (8), and (13), as a result, we have the follow equations

$$\ddot{r} = \begin{bmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} \end{bmatrix} = \begin{pmatrix} -(C_\psi S_\theta C_\phi + S_\psi S_\phi) \frac{u_1}{m} \\ -(S_\psi S_\theta C_\phi - C_\psi S_\phi) \frac{u_1}{m} \\ g - (C_\theta C_\phi) \frac{u_1}{m} \end{pmatrix} \quad (14)$$

On the other hand, if we assume small perturbations in hover flight, $\dot{\Omega} \approx W$ and combining Eqs. (9), (11), and (13), we obtain the follow equations

$$\begin{aligned}
\ddot{\phi} &= \dot{\theta}\dot{\psi}\left(\frac{J_y - J_z}{J_x}\right) - \left(\frac{J_r}{J_x}\right)\dot{\theta}h(u) + \frac{L}{J_x}u_2 \\
\ddot{\theta} &= \dot{\phi}\dot{\psi}\left(\frac{J_z - J_x}{J_y}\right) + \left(\frac{J_r}{J_y}\right)\dot{\phi}h(u) + \frac{L}{J_y}u_3 \\
\ddot{\psi} &= \dot{\phi}\dot{\theta}\left(\frac{J_x - J_y}{J_z}\right) - \frac{1}{J_z}u_4
\end{aligned} \tag{15}$$

2.4. Linearization of quadrotor dynamics

To simplify the earlier equations, we have linearized the rotatory system around hover state assuming small change in Euler angles, $u_1 \approx mg$ in x and y directions, $\cos(\alpha) = 1$, $\sin(\alpha) = \alpha$ and neglected the gyroscopic torques; therefore,

$$\begin{aligned}
\ddot{x} &= -\theta g \\
\ddot{y} &= \phi g \\
\ddot{z} &= u_1 - mg \\
\ddot{\phi} &= \frac{L}{J_x}u_2 \\
\ddot{\theta} &= \frac{L}{J_y}u_3 \\
\ddot{\psi} &= \frac{1}{J_z}u_4
\end{aligned} \tag{16}$$

This work only considers the angular momentum corresponding to the orientation of the vehicle, so that the displacement in (x, y, z) axes will not be used for mathematical analysis.

Therefore, the transfer function for dynamic correspondence of orientation is expressed as

$$\begin{aligned}
\phi(s) &= \frac{L}{s^2 J_x}u_2 \\
\theta(s) &= \frac{L}{s^2 J_y}u_3 \\
\psi(s) &= \frac{1}{s^2 J_z}u_4
\end{aligned} \tag{17}$$

and adding rotor's model, we have

$$G(s, e^{-\tau s}) = \begin{pmatrix} \frac{K_{p1}}{s^2(s + a_\phi)} & 0 & 0 \\ 0 & \frac{K_{p2}}{s^2(s + a_\theta)} & 0 \\ 0 & 0 & \frac{K_{p3}}{s^2(s + a_\psi)} \end{pmatrix} \tag{18}$$

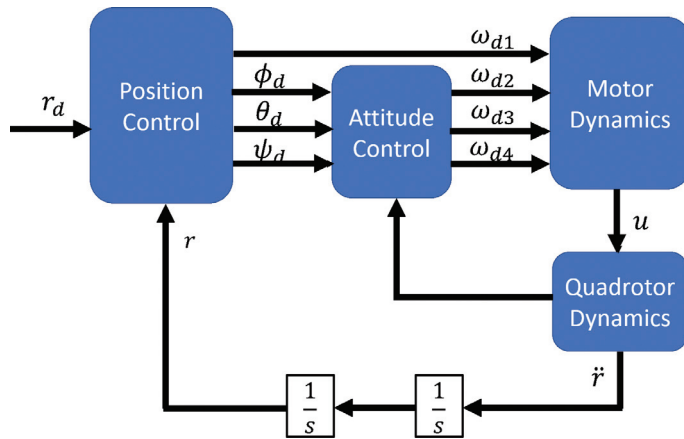


Figure 2. Overall control system.

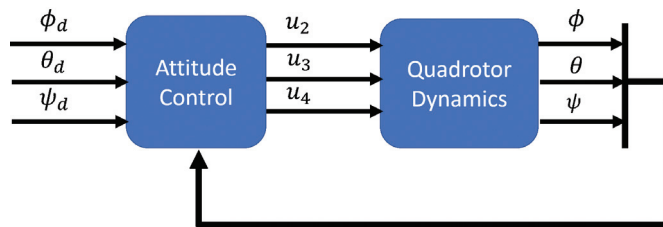


Figure 3. Attitude control system of a quadrotor.

where $K_{p1}=Lk_{\phi}/J_x$, $K_{p2}=Lk_{\theta}/J_y$, $K_{p3}=Lk_{\psi}/J_z$. These parameters were computed for a X4-flyer and have the following values: $K_{p1}=K_{p2}=33.23$, $K_{p3}=16.95$, $a_{\phi}=a_{\theta}=a_{\psi}=4.1$ and $\tau=0.017$. This mathematical model will be used to synthesize the control law to stabilize the closed-loop system [15].

The overall control schema is showed in **Figure 2**, where position and attitude control are presented. This schema consist in two loops, first one is used to perform the quadrotor tracking of desired trajectory r_d , while the second one is used to achieve the desired Euler $(\phi_d, \theta_d, \psi_d)$. Due that we are only interested in attitude control, the above schema is redrawn as is showed in **Figure 3**.

3. Adaptive controller design

The adaptive control is an advance control technique which provides a systematic approach for automatic adjustment of controllers in real time, in order to achieve or to maintain a desired level of control system performance, when the parameters of the plant dynamic model are unknown and/or change in time [16]. Two different approaches can be distinguished: indirect and direct approaches. In the first approach, the plant parameters are estimate online and used

to calculate the controller parameters. In the second, the plant model is parameterized in terms of the controller parameters that are estimated directly without intermediate calculations involving plant parameter estimates [17].

The model reference adaptive control or MRAC is a direct adaptive strategy which consists of some adjustable controller parameters and an adjusting mechanism to adjust them. The goal of the MRAC approach is adjusting the controller parameters so that the output of the plant tracks the output of the reference model having the same reference input. The MRAC schema is combine two loops: the inner or primary loop where controller and plant are feedback as in normal loop and outer loop or also called adjustment loop where some adaptive mechanisms and a model reference are used to obtain the some performance [18]. In **Figure 4**, an overall MRAC schema is presented.

This section presents the design of an adaptive controller MRAC using the Lyapunov's stability theory. This allows us to ensure the tracking trajectory of an X4 to our reference model and makes the system insensitive to parameter variation and external disturbances, leading the state error to zero. Based on this, the process model can be represented by state space as follows:

$$\dot{x} = A_p x + B_p u \quad (19)$$

$$y = Cx \quad (20)$$

where A_p and B_p represent the matrix and the vector of unknown constant parameters of the system, u is the output signal of the controller, and x is the state vector.

The reference model is defined as follows:

$$\dot{x}_m = A_m x_m + B_m u_c \quad (21)$$

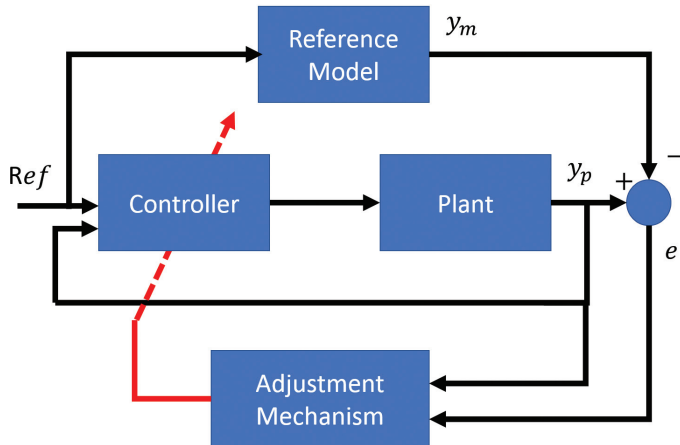


Figure 4. MRAC control schema.

$$y = C_m x_m \quad (22)$$

Then, the control law is selected as:

$$u = L_r u_c - Lx = \theta_4 u_c - \theta_1 x_1 - \theta_2 x_2 - \theta_3 x_3 \quad (23)$$

where L_r and L are the matrix containing the parameters of the controller, which can be freely selected, and u_c is the reference signal.

Substituting (Eq. (22)) in (Eq. (18)), the closed loop system is expressed as follows:

$$\dot{x} = (A_p - B_p L)x + B_p L_r u_c = A(\theta)x + B(\theta)u_c \quad (24)$$

Now we introduce the error equation as follows

$$e = x - x_m \quad (25)$$

Differentiating the error with respect to time, we obtain:

$$\frac{de}{dt} = \frac{dx}{dt} - \frac{dx_m}{dt} = Ax + Bu - A_m x_m - B_m u_c \quad (26)$$

and adding $A_m x$ and subtracting to the left side of the equation

$$\frac{de}{dt} = A_m e + (A - A_m)x + (B - B_m)u_c \quad (27)$$

The error goes to zero if A_m is stable and

$$A(\theta) - A_m = 0 \quad (28)$$

$$B(\theta) - B_m = 0 \quad (29)$$

If we assume that the closed-loop system can be described by (Eq. (14)), where the matrices A and B depend on the parameter θ , and it is some combination of L_r and L , then we can define the following Lyapunov function for the parameter adaptation law:

$$V = e^T P e + \text{tr}(A(\theta) - A_m)^T Q_a (A(\theta) - A_m) + \text{tr}(B(\theta) - B_m)^T Q_b (B(\theta) - B_m) \quad (30)$$

where $P \in \mathbb{R}^{3 \times 3}$ is a positive definite matrix and V is a positive definite function. If its first derivative to time V is not positive definite, then V is Lyapunov function. Now we can solve the derivative of V to time t .

$$\frac{dV}{dt} = e^T P A_m e + e^T A_m^T P e + 2\text{tr}(A - A_m)^T (Q_a \dot{A} + P e x^T) + 2\text{tr}(B - B_m)^T (Q_b \dot{B} + P e u_c^T) \quad (31)$$

where Q is a positive definite matrix such that meet the follow equation:

$$A_m^T P + P A_m = -Q \quad (32)$$

Therefore, if we choose a stable A_m matrix, we will get always a P and Q positive definite matrix.

Accordingly, the derivative to time of function V is

$$\frac{dV}{dt} = -e^T Q e \quad (33)$$

Where the function V is a Lyapunov function negative semi-definite ensures the output error between the real system and the reference model will tend to be zero, and the system is asymptotically stable.

Thus, we obtain the following parameter adaptation laws

$$\frac{d\theta_1}{dt} = p_{11}e_1x_1 + p_{12}e_2x_1 + p_{13}e_3x_1 \quad (34)$$

$$\frac{d\theta_2}{dt} = p_{11}e_1x_2 + p_{12}e_2x_2 + p_{13}e_3x_2 \quad (35)$$

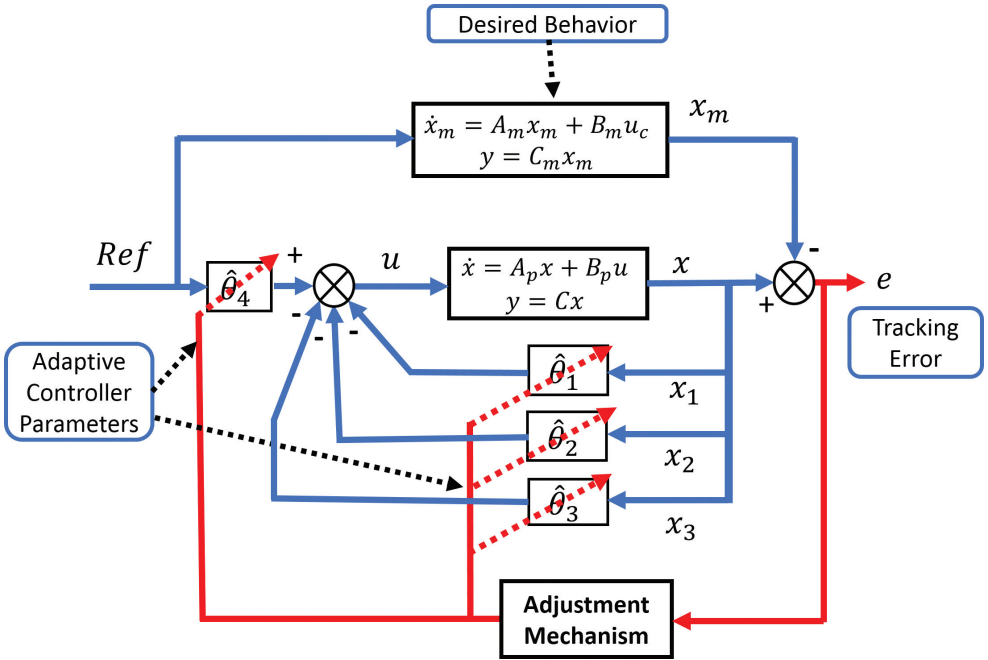


Figure 5. MRAC control of quadrotor: block diagram.

$$\frac{d\theta_3}{dt} = p_{11}e_1x_3 + p_{12}e_2x_3 + p_{13}e_3x_3 \quad (36)$$

$$\frac{d\theta_4}{dt} = -(p_{11}e_1r + p_{12}e_2r + p_{13}e_3r) \quad (37)$$

Then, the resulting control diagram is shown in **Figure 5**.

4. Simulation and analysis

This section presents several simulations test made to prove the performance of MRAC controller to stabilize a mini-UAV quadrotor. As mentioned before, only orientation dynamic (angle position, angular velocity and acceleration) are considered. Analyzing Eq. (18), it is easy to see that roll, pitch, and yaw dynamics are very similar; for this reason, only roll moment is used as example in simulation.

The test begins considering controller parameters are unknown and by using an online adaptive mechanism to determine the values that permit the convergence of plant response to reference model response. It is important to note that the MRAC approach seeks to keep the tracking error $(x - x_m)$ equal to zero by an adjustment of the controller parameters and do not to seek to identify the real parameters of the plant.

Figures 6–8 shows a comparative between the states response of the plant and the state response of the model reference, where can be observer than all states of the plant converge asymptotical to the reference model states. To verify this, the **Figures 9–11** are presented; these figures show the tracking error of states goes to zero. Additionally, in **Figure 12**, the reference input is compared to the plant and model reference output.

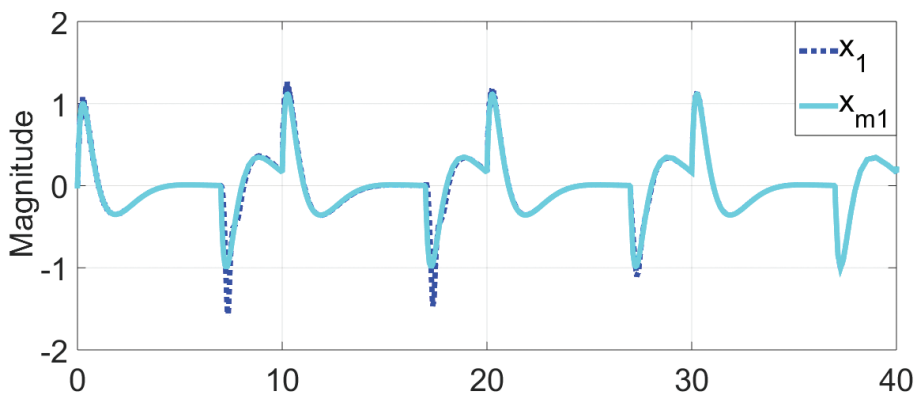


Figure 6. Comparison between x_1 and x_{m1} .

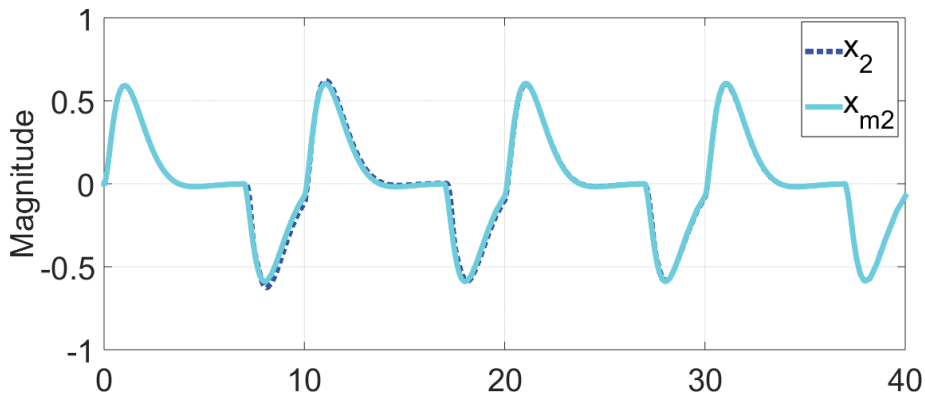


Figure 7. Comparison between x_2 and x_{m2} .

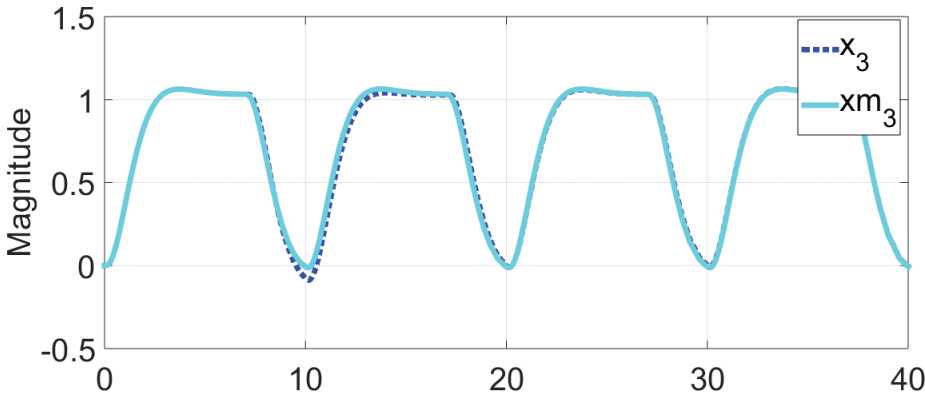


Figure 8. Comparison between x_3 and x_{m3} .

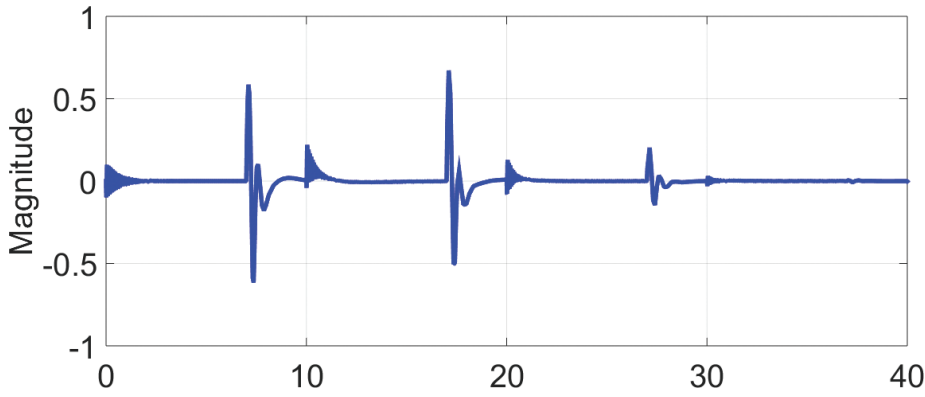


Figure 9. Error between x_1 to x_{m1} .

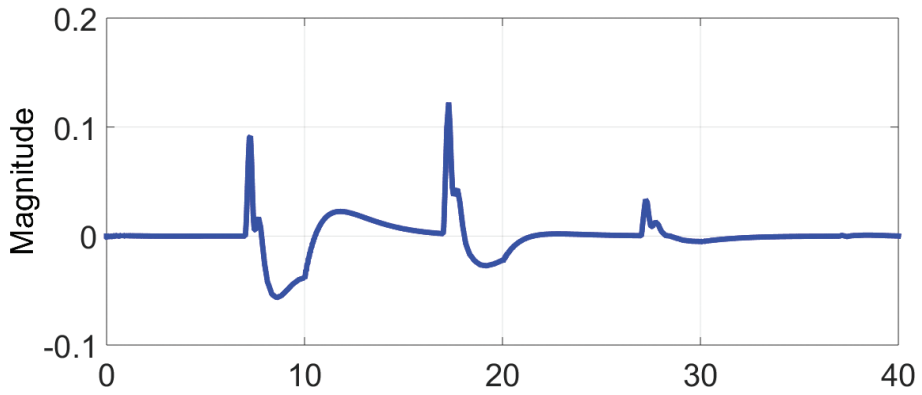


Figure 10. Error between x_2 to x_{m2} .

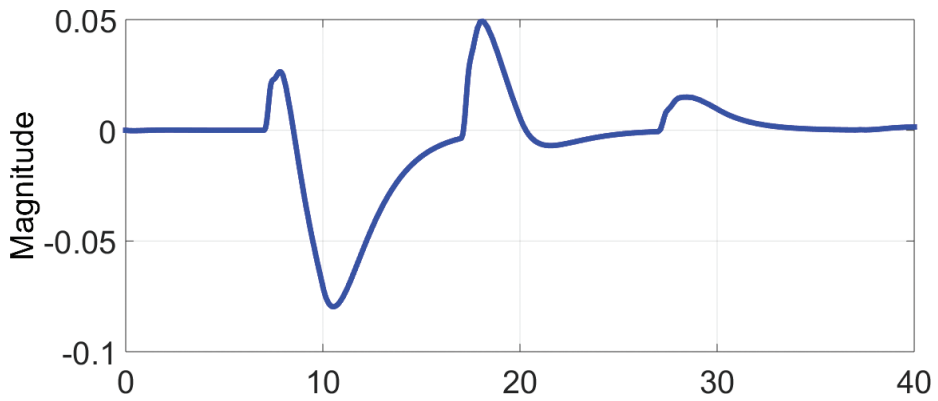


Figure 11. Error between x_3 to x_{m3} .

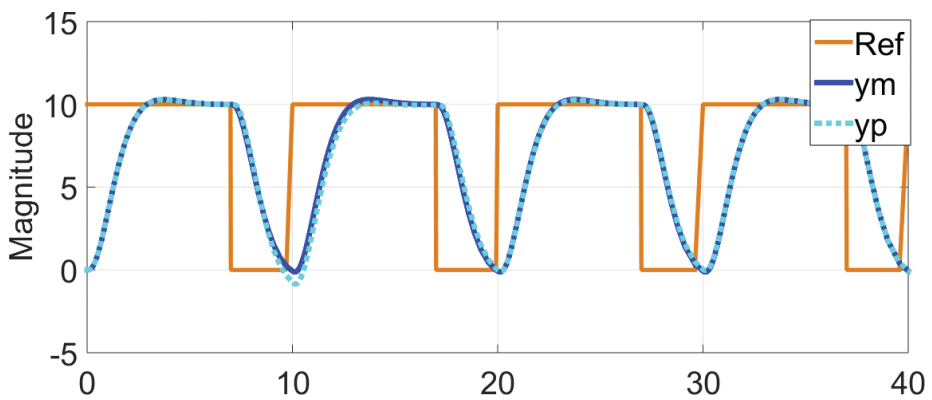


Figure 12. Roll response.

Figure 13 shows the variations of the controller parameters during the adjustment process. This mechanism started many times is necessary to assure the perfect tracking of the plant to the desire response. Finally, in **Figure 14**, the simulation diagram is presented.

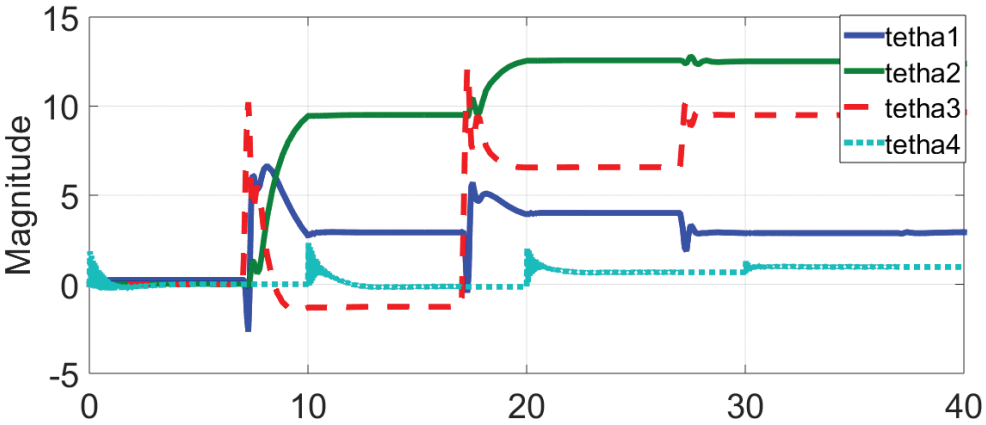


Figure 13. Tuning of controller parameters.

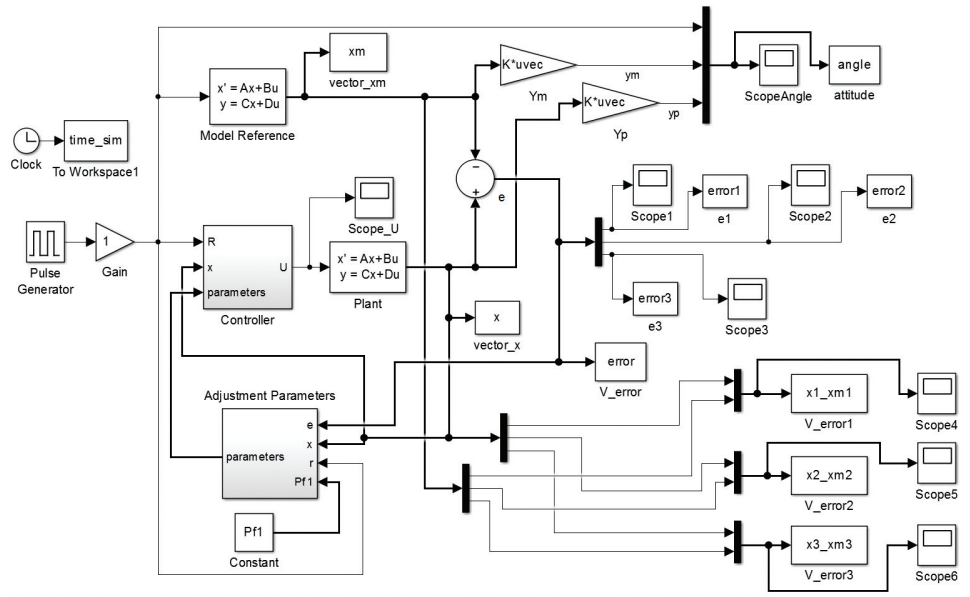


Figure 14. Simulink diagram.

5. Conclusions

This work presents an adaptive control technique to stabilize the attitude of a quadrotor UAV using MRAC schema, which requires no information of the plant model. The asymptotic stability was demonstrated using the well-known Lyapunov's theory, obtaining in this way the adaptation law of the controller parameters. Simulations results demonstrate that the adaptive control approach proposed have a good performance to perform the asymptotic tracking of model reference output. It is important to note that the adaptive mechanism is started only when it is needed.

Author details

Ramiro Ibarra Pérez*, Gerardo Romero Galvan, Aldo Jonathan Muñoz Vázquez,
Silvia Florida Melo and David Lara Alabazares

*Address all correspondence to: rm_ibarra@live.com

UAM Reynosa Rodhe, Autonomous University of Tamaulipas, Tamaulipas, México

References

- [1] Austin R. Unmanned Aircraft Systems: UAVS Design, Development and Deployment. John Wiley & Sons. United Kingdom; 2010. p. 372 DOI: 10.1002/9780470664797
- [2] Jeong S et al. Position Control of a Quad-Rotor System. In: Kim J-H, Matson ET, Myung H, Xu P, editors. Robot Intelligence Technology and Applications. Berlin Heidelberg: Springer-Verlag; 2013; 2012. p. 971-981. DOI: [doi.org/10.1007/978-3-642-37374-9_94](http://dx.doi.org/10.1007/978-3-642-37374-9_94)
- [3] Bouabdallah S, editor. Design and control of quadrotor with application to autonomous flying [dissertation]. École Polytechnique Fédérale de Lausanne; 2007
- [4] Jithu G, Jayasree PR. Quadrotor modelling and control. International Conference on Electrical, Electronics, and Optimization Techniques (ICEEOT)—2016
- [5] Jun L, Yuntang Li. Dynamic analysis and PID control for a quadrotor. In: Proceedings of the 2011 IEEE. 2011
- [6] Changlong L, Jian P, Chang Y. PID and LQR trajectory tracking control for an unmanned quadrotor helicopter: Experimental studies. In: Proceedings of the 35th Chinese Control Conference. 2016; DOI: 10.1109/ChiCC.2016.7555074
- [7] Salazar S, Romero H, et al. Real-time stereo visual serving control of an UAV having eight rotors, In: 6th International Conference on Electrical engineering, computing science and automatic control, CCE 2009. DOI: 10.1109/ICEEE.2009.5393423

- [8] Bouabdallah S, Siegwart R. Backstepping and sliding-mode techniques applied to an indoor micro quadrotor. In: Proceedings of the 2005 IEEE International Conference on Robotics and Automation, ICRA 2005. DOI: 10.1109/ROBOT.2005.1570447
- [9] Abeywardena DMW, Amaratunga LAK, Shakoor SAA, Munasinghe SR. A velocity feedback fuzzy logic controller for stable hovering of a quadrotor UAV. In: International Conference on Industrial and Information Systems (ICIIS), 2009. DOI: 10.1109/ICIINF.2009.5429800
- [10] Theerasak S, Pined L, Wonlop C, et al. Path tracking of UAV using self-tuning PID controller based on fuzzy logic, In: Proceedings of SICE Annual Conference 2010
- [11] M Imran R, Akhtar S. Adaptive control of a quadrotor with unknown model parameters In: 9th International Bhurban Conference on Applied Sciences and Technology (IBCAST) 2012. DOI: 10.1109/IBCAST.2012.6177518
- [12] Bouabdallah S, Murrieri P, Siegwart R. Design and control of an indoor micro quadrotor. Proceedings of IEEE International Conference on Robotics and Automation, ICRA '04. 2004. DOI: 10.1109/ROBOT.2004.1302409
- [13] Sanca AS, Alsina PJ, Cerqueira JJ. Dynamic modelling of a quadrotor aerial vehicle with nonlinear inputs. In: IEEE Latin American Robotic Symposium, 2008. LARS '08. 2009. DOI: 10.1109/LARS.2008.17
- [14] Schreier M. Modeling and adaptive control of a quadrotor. International Conference on Mechatronics and Automation (ICMA), 2012. 2012; DOI: 10.1109/ICMA.2012.6282874
- [15] Tao G, Selfridge Justin M. A multivariable adaptive controller for a Quadrotor with guaranteed matching conditions. In: American Control Conference (ACC) Portland, Oregon, USA. 2014. DOI: 10.1109/ACC.2014.6859355
- [16] Lara D, Romero G. Onboard system for flight control of a small UAV. In: World Automation Congress (WAC), 2012. 04 October 2012. Puerto Vallarta, Mexico. Mexico: IEEE. 2012.
- [17] Landau ID, Lozano R, M'Saad M, Karimi A. Introduction to adaptive control. In: Adaptive Control: Algorithms, Analysis and Applications. London: Springer; 2011. p. 1-33. DOI: 10.1007/978-0-85729-664-1
- [18] Ioannou P, Sun J. Robust Adaptive Control. Mineola, New York: Dover Publications; 2013. p. 848