

$$T(x, y) = \left(\frac{5x+y}{2}, \frac{-x-4y}{2} \right)$$

Program:-

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1. Import numpy as np
   from numpy import linalg as la
   def T(x, y, z):
       return (x-y+z, 2*x+3*y-(1/2)*z, x+y-2*z)
   B1 = np.array([[ -1, 1, 0], [ 5, -1, 2], [ 1, 2, 1]])
   print("The specified basis for the domain space is \n", B1)
   B2 = np.array([[ 1, 1, 0], [ 0, 0, 1], [ 1, 5, 2]])
   print("The specified basis for the codomain space is \n", B2)
   u1 = T(-1, 1, 0)
   u2 = T(5, -1, 2)
   u3 = T(1, 2, 1)
   print("Evaluating T at the vectors of basis B1: ", u1, u2, u3)
   v1 = la.solve(B2, T, u1)
   v2 = la.solve(B2, T, u2)
   v3 = la.solve(B2, T, u3)
   M = np.array([v1, v2, v3])
   print("The matrix of the linear transformation is: \n", M.T)

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2. from sympy import *
import numpy as np
x, y, c1, c2 = symbols('x y c1 c2')
A = Matrix([ [2, 3], [4, -5] ])
u1 = np.array([1, -1])
u2 = np.array([1, 1])
v1 = np.array([1, 0])
v2 = np.array([0, 1])
Tu1 = A[0,0]*v1 + A[1,0]*v2
Tu2 = A[0,1]*v1 + A[1,1]*v2
print("The images of the ordered basis vectors in B1 under the transformation T expressed using the basis vectors of B2 are, Tu1, Tu2")
eq = (c1*u1 + c2*u2 - [x,y])
sol = solve(eq, (c1, c2), dict=True)
c1 = sol[0][c1]
c2 = sol[0][c2]
print("The co-ordinates of any arbitrary vectors (x,y) w.r.t the basis B1 are, c1 and, c2")
T = (c1*Tu1 + c2*Tu2)
print("The linear transformation T on any arbitrary vector (x,y) is T(x,y) = ", tuple(T))

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S. N.
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