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Decimal to Binary (Convert Decimal to Binary):

Convert then show your work by using the expanded form to verify your answer. Also note how many binary digits are required to represent the decimal number.

Ex: 8 (dec) => 1000 (bin); verify:  $1*2^3 + 0*2^2 + 0*2^1 + 0*2^0 = 8 + 0 + 0 + 0 = 8$   
8 requires 4 binary digits.

1. Convert 14 to binary. => 1110:  $=> 1*2^3 + 1*2^2 + 1*2^1 + 0*2^0 = 8+4+2+0$   
=> 1110

2. Convert 25 to binary. =>  $1*2^4 + 1*2^3 + 0*2^2 + 0*2^1 + 1*2^0 = 16+8+0+0+1$   
=> 11001

3. Convert 39 to binary. =>  $1*2^5 + 0*2^4 + 0*2^3 + 1*2^2 + 1*2^1 + 1*2^0$   
 $= 32+0+0+4+2+1 = 39$  => 100111

4. Convert 56 to binary.  $=> 1*2^5 + 1*2^4 + 1*2^3 + 0*2^2 + 0*2^1 + 0*2^0$   
 $= 32+16+8+0+0+0 = 56$  => 111000

5. Convert 16 to binary.  $=> 1*2^4 + 0*2^3 + 0*2^2 + 0*2^1 + 0*2^0 = 16+0+0+0+0$   
=> 10000

Binary to Decimal (Convert Binary to Decimal):

You can just use the expanded form to convert binary to decimal.

1. Convert 1101 to decimal.  $= 1*2^3 + 1*2^2 + 0*2^1 + 1*2^0 = 8+4+0+1=13$

2. Convert 10101 to decimal.  $= 1*2^4 + 0*2^3 + 1*2^2 + 0*2^1 + 1*2^0$   
 $= 16+0+4+0+1=21$

3. Convert 111001 to decimal.  $= 1*2^5 + 1*2^4 + 1*2^3 + 0*2^2 + 0*2^1 + 1*2^0$   
 $= 32+16+8+0+0+1=57$

4. Convert 100110 to decimal.  $= 1*2^5 + 0*2^4 + 0*2^3 + 1*2^2 + 1*2^1 + 1*2^0 =$

$$32+0+0+4+2+0= 38$$

$$5. \text{ Convert } 1100101 \text{ to decimal. } = 1*2^6 + 1*2^5 + 0*2^4 + 0*2^3 + 1*2^2 + 0*2^1 + 1*2^0 = 64+32+0+0+4+0+1= 101$$

$$6. \text{ Convert } 101010 \text{ to decimal. } = 1*2^5 + 0*2^4 + 1*2^3 + 0*2^2 + 1*2^1 + 0*2^0 = 32+0+8+0+2+0 = 42$$

$$7. \text{ Convert } 1111 \text{ to decimal. } = 1*2^3 + 1*2^2 + 1*2^1 + 1*2^0 = 8+4+2+1 = 15$$

$$8. \text{ Convert } 1001 \text{ to decimal. } = 1*2^3 + 0*2^2 + 0*2^1 + 1*2^0 = 8+0+0+1 = 9$$

$$9. \text{ Convert } 1101101 \text{ to decimal. } = 1*2^6 + 1*2^5 + 0*2^4 + 1*2^3 + 1*2^2 + 0*2^1 + 1*2^0 = 64+32+0+8+4+0+1 = 109$$

$$10. \text{ Convert } 1000001 \text{ to decimal. } = 1*2^6 + 0*2^5 + 0*2^4 + 0*2^3 + 0*2^2 + 0*2^1 + 1*2^0 = 64+0+0+0+0+0+1 = 65$$

Range of number:

1. Given 4 binary digits, what is the number range I can represent with these digits?

A. The range is 0 to  $2^n - 1 = 2^4 - 1 = 16 - 1 = 15$ . so range is (0 to 15)

For Signed The range is from  $[-2^{(n-1)}, 2^{(n-1)} - 1] = [-2^{(4-1)}, 2^{(4-1)} - 1] = [-2^3, 2^3 - 1] = [-8, 7]$

2. Given 7 binary digits?

A. The range is 0 to  $2^n - 1 = 2^7 - 1 = 128 - 1 = 127$ . so range is (0 to 127)

For Signed The range is from  $[-2^{(n-1)}, 2^{(n-1)} - 1] = [-2^{(7-1)}, 2^{(7-1)} - 1] = [-2^6, 2^6 - 1] = [-64, 63]$

3. Given 8 binary digits? =>

A. The range is 0 to  $2^n - 1 = 2^8 - 1 = 256 - 1 = 255$ . So range is (0 to 255)

For Signed The range is from  $[-2^{(n-1)}, 2^{(n-1)} - 1] = [-2^{(8-1)}, 2^{(8-1)} - 1] = [-2^7, 2^7 - 1] = [-128, 127]$

$$[-2^7, 2^7 - 1] \Rightarrow [-128, 127]$$

4. Given 16 binary digits?

A. The range is 0 to  $2^n - 1 = 2^{16} - 1 \Rightarrow 65536 - 1 \Rightarrow 65535 \Rightarrow$  so range is (0 to 65535)

For Signed The range is from  $[-2^{(n-1)}, 2^{(n-1)} - 1] \Rightarrow [-2^{(16-1)}, 2^{(16-1)} - 1] \Rightarrow$   
 $[-2^{15}, 2^{15} - 1] \Rightarrow [-32768, 32767]$