

6.1 Kinetics of a Particle (KNP) - Class Work Questions

6.1.1 KNP-Force and Acceleration (D'Alembert and Newton Principles)

1. An elevator has a downward acceleration of 1 m/s^2 . What pressure will be transmitted to the floor of the elevator by a man weighing 500 N travelling in the lift?
[449 N]
2. A 50 kg block is kept on the top of a 15° sloping surface is pushed down the plane with an initial velocity of 20 m/s . If $\mu_k = 0.4$, determine the acceleration of the block. *also determine the distance travelled by the block and the time it will take to come to rest*
[$a = -1.25 \text{ m/s}^2$]
3. Two blocks A and B are separated by 10 m as shown in Figure 6.1-1 on a 20° incline plane. If the blocks start moving, find the time t when the blocks collide and distance travelled by each block. Assume $\mu_k = 0.3$ for block A and plane and $\mu_k = 0.10$ for block B and plane.
[$t = 3.29 \text{ sec}$, $S_A = 3.18 \text{ m}$, $S_B = 13.18 \text{ m}$]

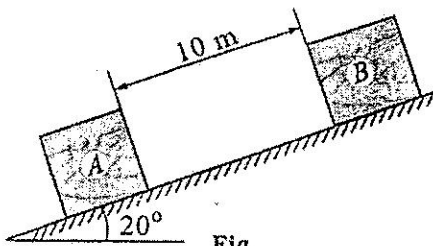


Fig.
Figure 6.1-1

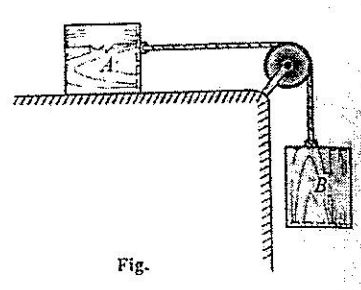


Fig.

Figure 6.1-2

4. Two blocks A and B of masses $M_A = 280 \text{ Kg}$ and $M_B = 420 \text{ Kg}$ are joined by an inextensible cable as shown in Figure 6.1-2. Assume that the pulley is frictionless and $\mu = 0.3$ between block A and the surface. The system is initially at rest. Determine (a) acceleration of block A, (b) Velocity after it has moved 3.5 m and (c) velocity after 1.5 sec .
[$a = 4.71 \text{ m/s}^2$, V after $3.5 \text{ m} = 5.74 \text{ m/s}$, V after $1.5 \text{ sec} = 7.06 \text{ m/s}$]
5. A horizontal force $P = 600 \text{ N}$ is exerted on block A of mass 120 kg as shown in Figure 6.1-3. The μ between block A and the horizontal plane is 0.25 . Block B has a mass of 30 kg and μ between it and the plane is 0.4 . The wire between the two blocks makes 30° with horizontal. Calculate the tension in the wire.
[$T = 147.78 \text{ N}$]
6. The 550 N box rest on a horizontal plane for which the coefficient of kinetic friction $\mu_k = 0.32$. If the box is subjected to a 400 N towing force as shown Figure 6.1-4, find the velocity of the box in 4 seconds starting from the rest.
[$v = 16.724 \text{ m/s}$]

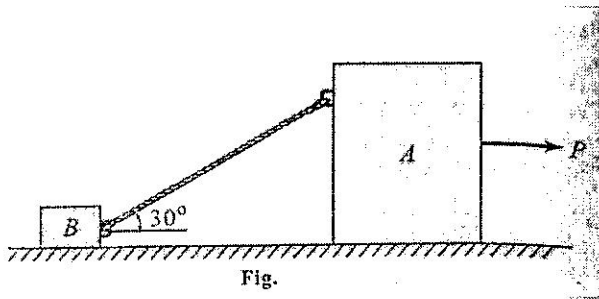


Figure 6.1-3

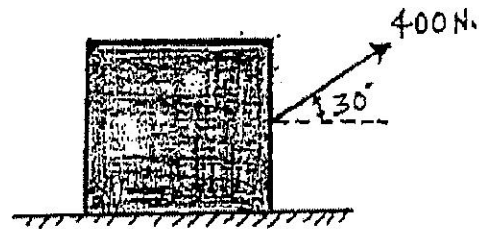


Figure 6.1-4

6.1.2 KNP - Work Energy Principle

1. A 3000N block shown in Figure 6.1-5 slide down a 50° incline. It starts from rest. After moving 2m it strikes a spring whose modulus is 20N/mm. If the coefficient of friction between block and incline is 0.2, Determine the maximum deformation of the spring. [0.72m]

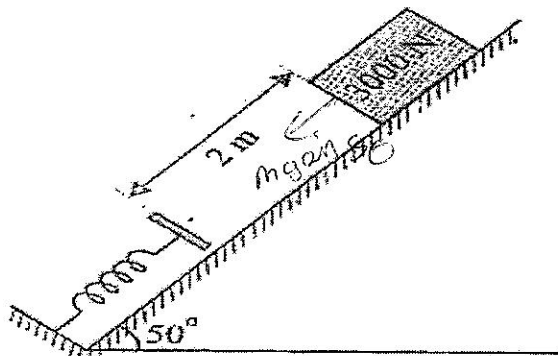


Figure 6.1-5

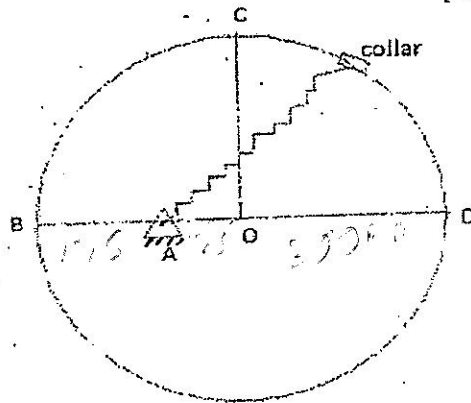


Figure 6.1-6

2. A 1 Kg collar is attached to a spring and slides without friction along a circular rod which lies in a horizontal plane as shown in Figure 6.1-6. The spring has a constant $K=250\text{N/m}$ and is undeformed when collar is at B. knowing the collar passes through point D with a speed of 1.6 m/s, determine the speed of the collar when it passes through point C and point B. Radius of circular path=300mm and distance $OA=125\text{ mm}$. [$V_B=4.343\text{ m/s}$, $V_C=3.638\text{ m/s}$]
3. Figure 6.1-7 shows a collar of mass 20kg which is supported on the smooth rod. The attached springs are undeformed when $d=0.5\text{m}$. Determine the speed of the collar after the applied force of 1000N causes it to displace so that $d=0.3\text{m}$. The collar is at rest when $d=0.5\text{m}$. [4.6m/s] {MU, May 2018, 6 Marks}

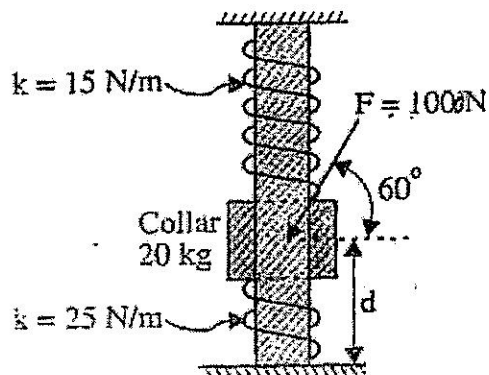


Figure 6.1-7

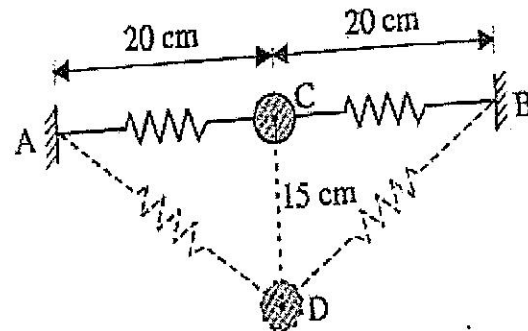


Figure 6.1-8

4. Two springs each having stiffness of 0.5 N/cm are connected a ball B having a mass of 5 kg in horizontal position producing initial tension of 1.5 N in each spring. If the ball is allowed to fall from rest. What will be its velocity after it has fallen through a height of 15 cm . Refer Figure 6.1-8. [1.683 m/s]
5. A 2 kg collar M is attached to a spring and slides without friction in a vertical plane along the curved rod ABC as shown in Figure 6.1-9. The spring has an undeformed length of 100 mm and its constant is 800 N/m . If the collar is released from rest at A. Determine its velocity (i) as it passes through B (ii) as it reaches C. ✗ [$2.3332, 1.414 \text{ m/s}$]

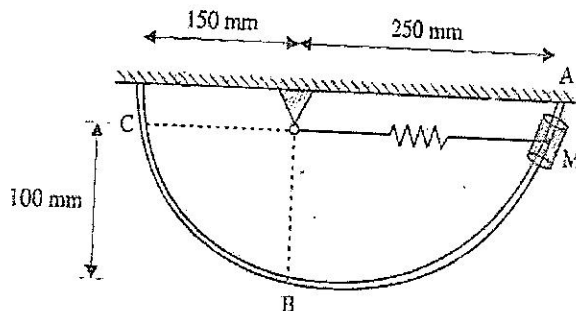


Figure 6.1-9

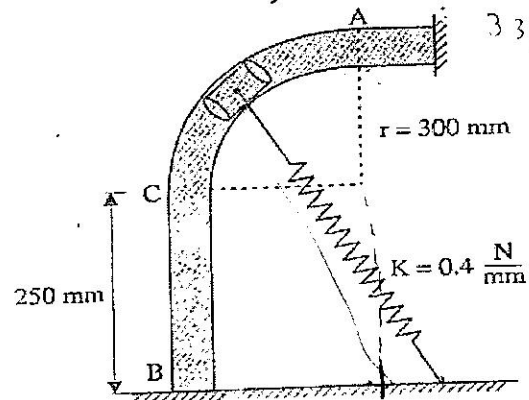


Figure 6.1-10

6. The 25 N collar is released from rest at A and travels along the smooth guide. Determine its speed when its centre reaches point 'C'. The spring has an unstretched length of 300 mm , and point 'C' is located just before the end of the curved portion of the rod. Refer Figure 6.1-10. [3.796 m/s]

6.1.3 KNP - Impulse Momentum Principle and Impact

1. A 2 kg sphere is moving towards left with velocity of 1.8 m/s . It strikes the vertical face of stationary block B of mass 4 kg . A spring $K = 5000 \text{ N/m}$ is attached to the other face of the block. If $e = 0.75$. Determine the maximum compression of the spring. Refer Figure 6.1-11. [26.69 mm]

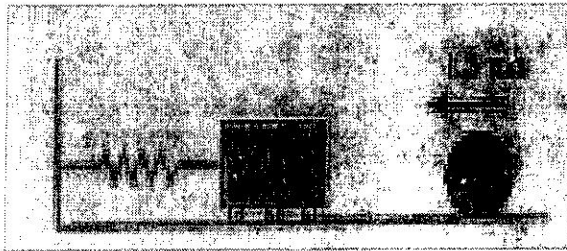


Figure 6.1-11

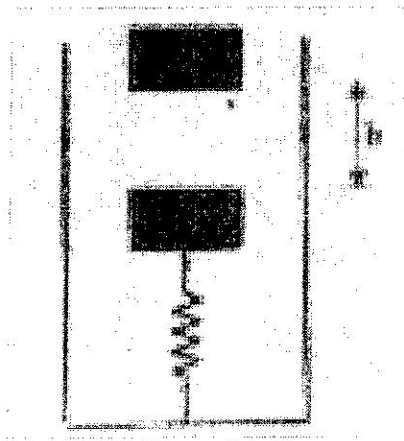


Figure 6.1-12

2. Block A falls through height H onto block B supported on spring of stiffness K . Assuming the impact to be plastic, calculate maximum compression of the spring over and above that due to static action of block A. $W_A = W_B = 20\text{N}$, $K = 20\text{ N/mm}$, $h = 100\text{mm}$. Refer . Figure 6.1-12
[10mm]
3. A bullet of mass 20 gm and moving horizontally with 800 m/s strikes a block of wood of mass 5 kg suspended by a wire 2m long. To what angle with vertical will the block and embedded bullet swing. Refer Figure 6.1-13.
[42.18°]

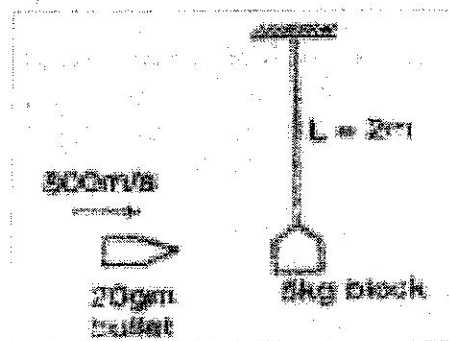


Figure 6.1-13

4. A smooth spherical ball A of mass 120 gms is moving from left to right, with a velocity of 2 m/s in a horizontal plane. Another identical ball B travelling in perpendicular direction with a velocity of 6 m/s collides with ball A as shown in Figure 6.1-14. Determine velocities of A and B after impact. Assume $e = 0.8$.
[$V_A = 0.2\text{ m/s} (\rightarrow)$ and $V_B = 6.26\text{ m/s} (\theta^\circ)$]