

Q1 Team Name

0 Points

Lazarus

Q2 Commands

10 Points

List the commands used in the game to reach the ciphertext

go
enter
pick
c
back
give
back
back
thrnxtzy
read

Q3 Analysis

50 Points

Give a detailed analysis of how you figured out the password? (Explain in less than 500 words)

A group theory problem was given to us to clear this level. This problem mentioned that password for the level is a member of the multiplicative group of modulo p where $p = 455470209427676832372575348833$ is a prime number.

We were given 3 pairs of the form $(a, password * g^a)$.

We formed equations using the above pairs as

$$\begin{aligned}(password * g^{429}) \pmod{p} &= 431955503618234519808008749742 \dots (i) \\(password * g^{1973}) \pmod{p} &= 176325509039323911968355873643 \dots (ii) \\(password * g^{7596}) \pmod{p} &= 98486971404861992487294722613 \dots (iii)\end{aligned}$$

Let,

$$x_1 = 431955503618234519808008749742$$

$$x_2 = 176325509039323911968355873643$$

$$x_3 = 98486971404861992487294722613$$

To get equations in only variable g we eliminate password from above equations :

Dividing iii by ii

$$\frac{g^{7596}}{g^{1973}} \equiv \frac{x_3}{x_2} \pmod{p}$$

As division operation is not defined in modulo arithmetic we take mod inverse instead

$$g^{7596} * g^{-1973} \equiv x_3 * (x_2^{-1}) \pmod{p}$$

$$g^{7596-1973} \equiv x_3 * x_2^{-1} \pmod{p}$$

$$g^{5623} \equiv x_3 * x_2^{-1} \pmod{p} \dots (iv)$$

Note - x^{-1} denotes the inverse of x in group Z_p^*

Similarly by dividing ii by i and iii by i

$$g^{1544} \equiv x_2 * x_1^{-1} \pmod{p} \dots (v)$$

$$g^{7167} \equiv x_3 * x_1^{-1} \pmod{p} \dots (vi)$$

As p is prime, inverse of all elements exists. If y is inverse of x then $x * y \equiv 1 \pmod{p}$.

Using Fermat's little theorem

$$a^{p-1} \equiv 1 \pmod{p}$$

Multiplying by a^{-1} on both sides

$$a^{-1} \equiv a^{p-2} \pmod{p}$$

Using above formula we calculate inverse :

$$x_1^{-1} = 70749996790223471732904681640$$

$$x_2^{-1} = 228947149478752602606353685125$$

Substituting the value of x_2^{-1} and x_1^{-1} in equations iv, v, vi

$$g^{5623} \equiv 420413074251022028027270785553 \pmod{p} \dots$$

$$g^{1544} \equiv 111590994894663139264552154672 \pmod{p} \dots$$

$$g^{7167} \equiv 110411376670918912626907526185 \pmod{p} \dots$$

Multiplying both sides of equation vii by inverse of $(g^{1544})^3$

$$g^{5623} * ((g^{1544})^3)^{-1} \equiv 42041307425102202802727078555$$

$$g^{991} \equiv 161798558270556961732424822635$$

We iteratively reduce the power of g to 1

$$g^{7167} * ((g^{991})^7)^{-1} \equiv 110411376670918912626907526185$$

$$g^{230} \equiv 263509268584013168241508095725$$

$$(g^{230})^7 * (g^{1544})^{-1} \equiv (26350926858401316824150809572$$

$$g^{66} \equiv 81667014892317214151967824518$$

$$(g^{66})^4 * (g^{230})^{-1} \equiv (81667014892317214151967824518)^4$$

$$g^{34} \equiv 454838375047265263248274620636$$

$$(g^{34})^2 * (g^{66})^{-1} \equiv (454838375047265263248274620636)^2$$

$$g^2 \equiv 108044907665466013935627786069$$

$$g^{991} * ((g^2)^{495})^{-1} \equiv 161798558270556961732424822635$$

$$g \equiv 52565085417963311027694339$$

Value of g computed above matches the hint

(5__50__4____31____94__9) given for the value of g in

problem so we move ahead with this.

$$g = 52565085417963311027694339$$

Substituting value of g in equation (i), we get:

$$(password * (52565085417963311027694339)^{429}) \pmod{p}$$

Multiplying both sides by inverse of g^{429}

$$password \equiv 43195550361823451980800874974 * 442956 \pmod{p}$$

$$password = 1913376364007938238997164320978558878 \pmod{p}$$

Taking \pmod{p}

$$password = 134721542097659029845273957$$

Q4 Password

10 Points

What was the final command used to clear this level?

134721542097659029845273957

Q5 Codes

0 Points

Upload any code that you have used to solve this level

▼ Assign3.ipynb

Download

In [1]: `import gmpy2`

In [2]:

```
x1 = 431955503618234519808008749742
x2 = 176325509039323911968355873643
x3 = 98486971404861992487294722613
p = 455470209427676832372575348833
```

In [3]:

```
invx1 = gmpy2.invert(x1,p)
invx1
```

Out [3]:

```
mpz(70749996790223471732904681640)
```

In [4]:

```
invx2 = gmpy2.invert(x2,p)
invx2
```

Out [4]:

```
mpz(228947149478752602606353685125)
```

In [5]:

```
g5623 = (x3 * invx2)%p
g5623
```

Out [5]:

```
mpz(420413074251022028027270785553)
```

In [6]:

```
g1544 = (x2 * invx1)%p
g1544
```

Out [6]:

```
mpz(111590994894663139264552154672)
```

In [7]:

```
g7167 = (x3* invx1)%p
g7167
```

Out [7]:

```
mpz(110411376670918912626907526185)
```

In [8]:

```
g991 = (g5623 *
gmpy2.invert(pow(g1544,3,p),p))%p
g991
```

Out [8]:

```
mpz(161798558270556961732424822635)
```

In [9]:

```
g230 =
(g7167*gmpy2.invert(pow(g991,7,p),p))%p
g230
```

Out [9]:

```
mpz(263509268584013168241508095725)
```

In [10]:

```
g66 =  
(pow(g230,7,p)*gmpy2.invert(g1544,p))%p  
g66
```

Out [10]:

```
mpz(81667014892317214151967824518)
```

In [11]:

```
g34 =  
(pow(g66,4,p)*gmpy2.invert(g230,p))%p  
g34
```

Out [11]:

```
mpz(454838375047265263248274620636)
```

In [12]:

```
g2 = (pow(g34,2,p)*gmpy2.invert(g66,p))%p  
g2
```

Out [12]:

```
mpz(108044907665466013935627786069)
```

In [13]:

```
g = (g991*gmpy2.invert(pow(g2,495,p),p))%p  
g
```

Out [13]:

```
mpz(52565085417963311027694339)
```

In [14]:

```
inv429 = gmpy2.invert(pow(g,429,p),p)  
inv429
```

Out [14]:

```
mpz(442956820316148690889301696615)
```

In [15]:

```
password = (inv429*x1)%p  
password
```

Out [15]:

```
mpz(134721542097659029845273957)
```


Assignment 3

GRADED**GROUP**

Varun Vankudre

Aditya Loth

Harsh Agarwal

 [View or edit group](#)**TOTAL POINTS****70 / 70 pts****QUESTION 1**[Team Name](#)**0 / 0 pts****QUESTION 2**[Commands](#)**10 / 10 pts****QUESTION 3**[Analysis](#)**50 / 50 pts** **+ 15 pts** Finding at least two distinct powers of g . **+ 25 pts** Finding the values of g by repeated division or Extended Euclid's algorithm or any other method. **+ 5 pts** The value of g is 52565085417963311027694339 **+ 5 pts** Finding *password* using the information of g
Password: 134721542097659029845273957**+ 0 pts** Wrong**+ 50 pts** Solving the assignment using an entirely different approach.**QUESTION 4**[Password](#)**10 / 10 pts****QUESTION 5**[Codes](#)**0 / 0 pts**