

Final Project
Statistical Analysis on
Carbon Dioxide Uptake in Grass Plants Dataset
BANA 6043 Statistical Computing

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1. Describing the data: Part-A

The CO₂ uptake of six plants from Quebec and six plants from Mississippi was measured at different levels of ambient CO₂ Concentration. Half the plants of each type were chilled overnight before the experiment was conducted. It consists of 84 rows and 5 columns of data from an experiment on the cold tolerance of the grass species *Echinochloa crus-galli*.

First, 10 observations from the dataset are shown below Fig 1.1:

| | Plant | Type | Treatment | conc | uptake |
|----|-------|--------|------------|------|--------|
| 1 | Qn1 | Quebec | nonchilled | 95 | 16.0 |
| 2 | Qn1 | Quebec | nonchilled | 175 | 30.4 |
| 3 | Qn1 | Quebec | nonchilled | 250 | 34.8 |
| 4 | Qn1 | Quebec | nonchilled | 350 | 37.2 |
| 5 | Qn1 | Quebec | nonchilled | 500 | 35.3 |
| 6 | Qn1 | Quebec | nonchilled | 675 | 39.2 |
| 7 | Qn1 | Quebec | nonchilled | 1000 | 39.7 |
| 8 | Qn2 | Quebec | nonchilled | 95 | 13.6 |
| 9 | Qn2 | Quebec | nonchilled | 175 | 27.3 |
| 10 | Qn2 | Quebec | nonchilled | 250 | 37.1 |

Fig 1.1 First 10 Observations of the CO₂ data

| Obs | VAR1 | Plant | Type_new | Treatment_new | conc_new | uptake |
|-----|------|-------|----------|---------------|----------|--------|
| 1 | 1 | Qn1 | Q | NC | 1 | 16 |
| 2 | 2 | Qn1 | Q | NC | 2 | 30.4 |
| 3 | 3 | Qn1 | Q | NC | 3 | 34.8 |
| 4 | 4 | Qn1 | Q | NC | 4 | 37.2 |
| 5 | 5 | Qn1 | Q | NC | 5 | 35.3 |
| 6 | 6 | Qn1 | Q | NC | 6 | 39.2 |
| 7 | 7 | Qn1 | Q | NC | 7 | 39.7 |
| 8 | 8 | Qn2 | Q | NC | 1 | 13.6 |
| 9 | 9 | Qn2 | Q | NC | 2 | 27.3 |
| 10 | 10 | Qn2 | Q | NC | 3 | 37.1 |

Fig 1.2 First 10 Observations of the CO₂ data

Source: datasets in R

of Rows(observations): 84

of columns: 5

Names and type of Columns:

1. Plant: A categorical variable ordered with levels Qn1 < Qn2 < Qn3 < ... < Mc1 giving a unique identifier for each plant. This is also an Independent variable.
2. Type: This Independent variable represents the Origin of the Quebec or Mississippi and is a categorical variable.
3. Treatment: The plant is or not chilled before subject to different ambient concentration levels of CO₂ is provided by this categorical column. And, this is an Independent Variable.
4. Concentration: This provides the information of different levels of the ambient CO₂ concentration in (mL/L): 97, 175, 250, 350, 500, 675 and 1000. This is an Independent variable.
5. Uptake: This column will represent the CO₂ uptake of the plant in (umol/m² sec). And, this is a dependent variable.

A little data manipulation is done in R as follows:

Representing concentration levels as "1-7":

| conc | conc_new |
|------|----------|
| 95 | 1 |
| 175 | 2 |
| 250 | 3 |
| 350 | 4 |
| 500 | 5 |
| 675 | 6 |
| 1000 | 7 |

Representing treatment as:

| treatment | treatment_new |
|------------|---------------|
| Chilled | C |
| nonchilled | NC |

Representing type as:

| type | type_new |
|-------------|----------|
| Quebec | Q |
| Mississippi | M |

First, 10 observations from the dataset are shown in Fig 1.2 as SAS dataset after the above manipulations.

Part-B:

Hypothesis:

1. There exists significant difference between the plant's mean CO₂ uptake for the two origins (Quebec and Mississippi).
 $\mu_{\text{CO}_2 \text{ uptake of Quebec}} \neq \mu_{\text{CO}_2 \text{ uptake of Mississippi}}$
2. There exists significant difference between the plant's mean CO₂ uptake for the two treatments (Chilled and Non-chilled).
 $\mu_{\text{CO}_2 \text{ uptake of Chilled}} \neq \mu_{\text{CO}_2 \text{ uptake of Nonchilled}}$

3. There exists significant difference between the plant's mean CO₂ uptake for the 7 concentration levels (1-7).

$$\mu_{\text{CO}_2 \text{ uptake of L}_1} \neq \mu_{\text{CO}_2 \text{ uptake of L}_2} \neq \mu_{\text{CO}_2 \text{ uptake of L}_3} \neq \mu_{\text{CO}_2 \text{ uptake of L}_4} \neq \mu_{\text{CO}_2 \text{ uptake of L}_5} \neq \mu_{\text{CO}_2 \text{ uptake of L}_6} \neq \mu_{\text{CO}_2 \text{ uptake of L}_7}$$

4. There exists a relation between how the differences between the plant's mean CO₂ uptake against interaction between type and treatment.

2. Data Summary: Part-A:

The SAS dataset that is created with CO₂ uptake data consists of 12 unique identifiers for each plant $Qn1 < Qn2 < Qn3 < \dots < Mc1$, these labelled in such a way that it reflects whether the plant is chilled or non-chilled as well as its origin. For example: Qn1 denotes the plant sample is from Quebec and is non-chilled before the experiment. And, each plant is subject to 7 different concentration levels ($12 \times 7 = 84 \Rightarrow$ Total # of observations).

Part-B: Continuous variable (uptake)

The normal histogram plot of the uptake variable in Fig 2.1 (it is left skewed):

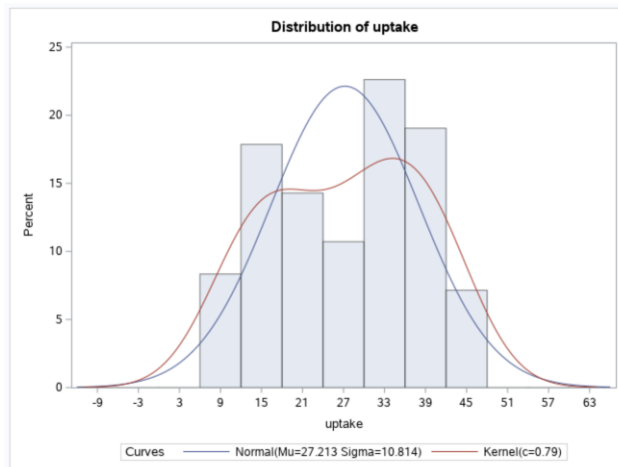


Fig 2.1 Normal Histogram plot of uptake variable

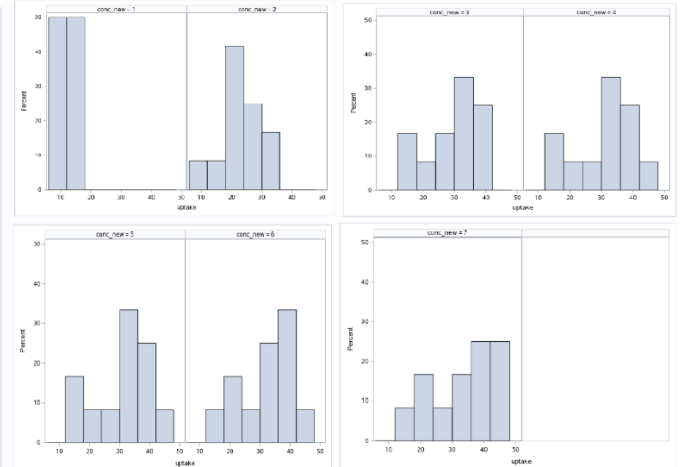


Fig 2.2 Histogram of uptake by conc_new level (1-7 -> L-R)

However, the individual plots of histograms of uptake by concentration level is little skewed as shown in the Fig 2.2. Additionally, the histogram plots for uptake by type and treatment are shown below in Fig 2.3 and Fig 2.4 respectively. From these plots it is observed that all histograms are skewed. Furthermore, by conducting the normality tests it is revealed that their skewness varied around -1 to 1 but not huge numbers as well as their probability plots are considerably close to the linear line.

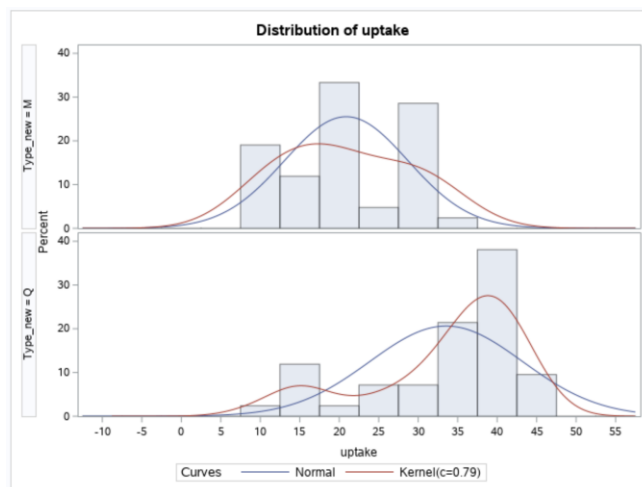


Fig 2.3 Histogram of uptake by type_new (M & Q)

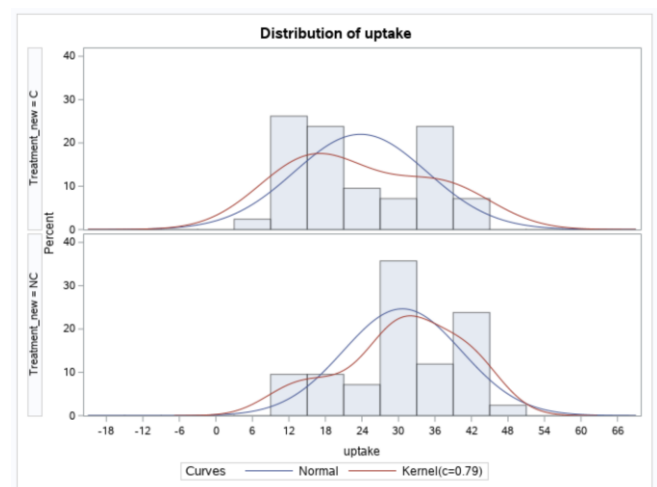


Fig 2.4 Histogram of uptake by treatment_new (C & NC)

Part-C: Categorical variable (type_new, treatment_new and conc_new)

The two-way tables are shown in the Fig 2.5 and Fig 2.6 for the categorical variables type_new, treatment_new and conc_new.

| Table of Treatment_new by conc_new | | | | | | | | |
|------------------------------------|----------|-------|-------|-------|-------|-------|-------|--------|
| Treatment_new | conc_new | | | | | | | Total |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | |
| C | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 42 |
| | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | |
| | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | |
| | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | |
| NC | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 42 |
| | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | 7.14 | |
| | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | |
| | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | 50.00 | |
| Total | 12 | 12 | 12 | 12 | 12 | 12 | 12 | 84 |
| | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 14.29 | 100.00 |

Fig 2.5 Two-way table between treatment_new and conc_new

| Table of Treatment_new by Type_new | | | |
|------------------------------------|----------|-------|--------|
| Treatment_new | Type_new | | Total |
| | M | Q | |
| C | 21 | 21 | 42 |
| | 25.00 | 25.00 | |
| | 50.00 | 50.00 | |
| | 50.00 | 50.00 | |
| NC | 21 | 21 | 42 |
| | 25.00 | 25.00 | |
| | 50.00 | 50.00 | |
| | 50.00 | 50.00 | |
| Total | 42 | 42 | 84 |
| | 50.00 | 50.00 | 100.00 |

Fig 2.6 Two-way table between type_new and conc_new

From treatment_new and conc_new two-way frequency table it shows that each treatment (chilled and non-chilled) observations are equal for every concentration (6). The same values show up with the type_new vs conc_new variable. And, for type_new and conc_new two-way frequency table it shows that each treatment (chilled and non-chilled) observations are equal for every type (21).

3. Analysis: Part-A

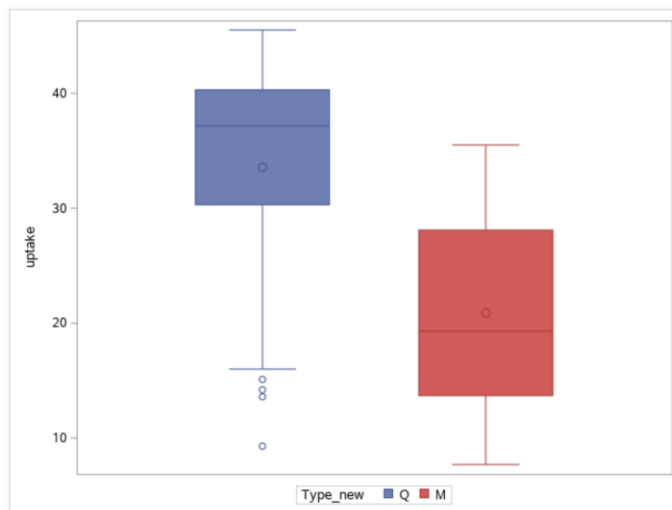


Fig 3.1 Box plots of uptake by type

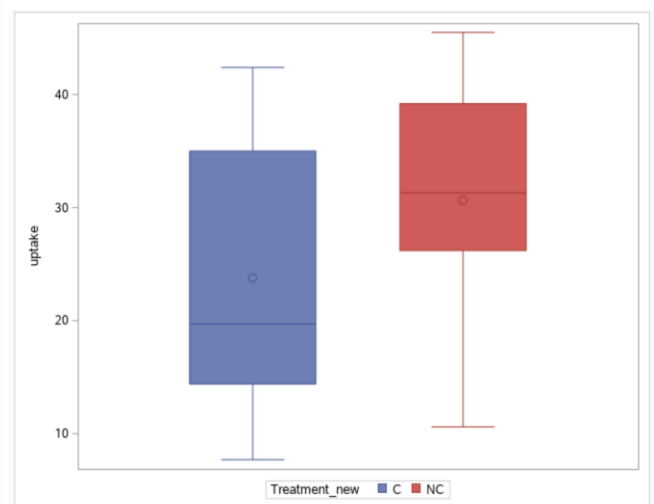


Fig 3.2 Box plots of uptake by treatment

Examining the Hypothesis 1:

There exists significant difference between the plant's mean CO₂ uptake for the two origins (Quebec and Mississippi).

$$\mu_{\text{CO}_2 \text{ uptake of Quebec}} \neq \mu_{\text{CO}_2 \text{ uptake of Mississippi}}$$

From the Fig 3.1 box plots of uptake by type, it is evident that mean CO₂ uptake of plants vary significantly with origin even though the four outliers are trying to pull the mean of type: Quebec(Q) down. So, the hypothesis seems to be valid. Furthermore, t-test will clarify the doubt.

Examining the Hypothesis 2:

There exists significant difference between the plant's mean CO₂ uptake for the two treatments (Chilled and Non-chilled).

$$\mu_{\text{CO}_2 \text{ uptake of Chilled}} \neq \mu_{\text{CO}_2 \text{ uptake of Nonchilled}}$$

From the Fig 3.2 box plots of uptake by treatment, it is not very sure of whether the mean CO₂ uptake of plants vary significantly whether chilled or non-chilled. So, the hypothesis claim is at question which should be resolved with the t-test results.

Examining the Hypothesis 3:

There exists significant difference between the plant's mean CO₂ uptake for the 7 concentration levels (1-7).

$$\mu_{\text{CO}_2 \text{ uptake of L}_1} \neq \mu_{\text{CO}_2 \text{ uptake of L}_2} \neq \mu_{\text{CO}_2 \text{ uptake of L}_3} \neq \mu_{\text{CO}_2 \text{ uptake of L}_4} \neq \mu_{\text{CO}_2 \text{ uptake of L}_5} \neq \mu_{\text{CO}_2 \text{ uptake of L}_6} \neq \mu_{\text{CO}_2 \text{ uptake of L}_7}$$

From the Fig 3.3 box plots of uptake by concentration levels, it is not certain that the mean CO₂ uptake of plants vary significantly with the ambient CO₂ concentration as you can see the level increases after 3 the plants seem to become saturated. So, the hypothesis is to be verified and concluded with the ANOVA test results.

Examining the Hypothesis 4:

There exists a relation between how the differences between the plant's mean CO₂ uptake and both type & treatment interaction. This claim is verified by ANOVA two-factor model test. Cannot infer interaction from the boxplots of Fig 3.4.

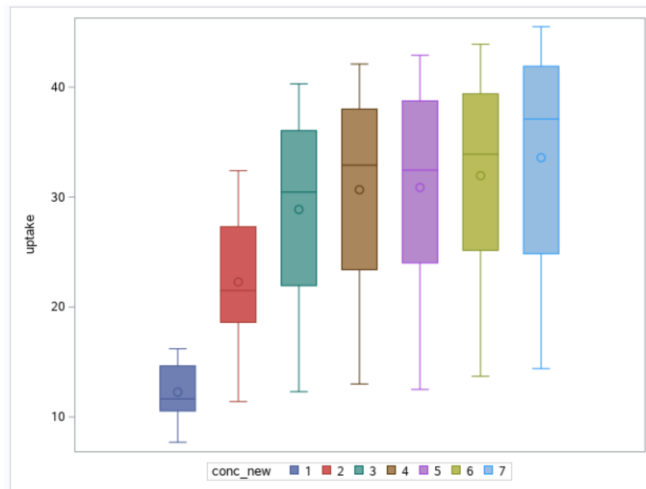


Fig 3.3 Box plots of uptake by concentration levels

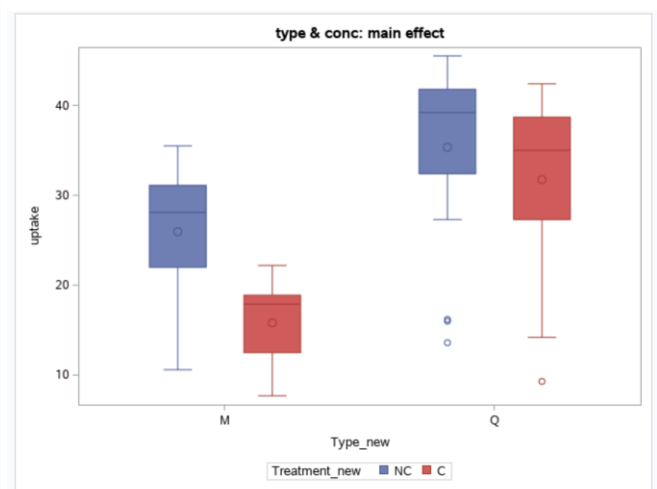


Fig 3.4 Box plots of uptake by type and treatment

Part-B: Test the Hypothesis claims

Testing the Hypothesis 1: t-test on uptake against type

$\alpha: 0.05$

corresponding critical value: 1.99* (for DF: 85)

Null Hypothesis:

$$\mu_{\text{CO}_2 \text{ uptake of Quebec}} = \mu_{\text{CO}_2 \text{ uptake of Mississippi}}$$

Alternate Hypothesis:

$$\mu_{\text{CO}_2 \text{ uptake of Quebec}} \neq \mu_{\text{CO}_2 \text{ uptake of Mississippi}}$$

Results of t-test on uptake against type:

The TTEST Procedure

Variable: uptake

| Type_new | Method | N | Mean | Std Dev | Std Err | Minimum | Maximum |
|------------|---------------|----|----------|---------|---------|---------|---------|
| M | | 42 | 20.8833 | 7.8158 | 1.2060 | 7.7000 | 35.5000 |
| Q | | 42 | 33.5429 | 9.6738 | 1.4927 | 9.3000 | 45.5000 |
| Diff (1-2) | Pooled | | -12.6595 | 8.7940 | 1.9190 | | |
| Diff (1-2) | Satterthwaite | | -12.6595 | | 1.9190 | | |

| Type_new | Method | Mean | 95% CL Mean | Std Dev | 95% CL Std Dev |
|------------|---------------|----------|------------------|---------|----------------|
| M | | 20.8833 | 18.4478 23.3189 | 7.8158 | 6.4309 9.9664 |
| Q | | 33.5429 | 30.5283 36.5574 | 9.6738 | 7.9597 12.3357 |
| Diff (1-2) | Pooled | -12.6595 | -16.4770 -8.8420 | 8.7940 | 7.6297 10.3810 |
| Diff (1-2) | Satterthwaite | -12.6595 | -16.4796 -8.8395 | | |

| Method | Variances | DF | t Value | Pr > t |
|---------------|-----------|--------|---------|---------|
| Pooled | Equal | 82 | -6.60 | <.0001 |
| Satterthwaite | Unequal | 78.533 | -6.60 | <.0001 |

| Equality of Variances | | | | |
|-----------------------|--------|--------|---------|--------|
| Method | Num DF | Den DF | F Value | Pr > F |
| Folded F | 41 | 41 | 1.53 | 0.1763 |

Fig 3.5 t-test results of uptake against type

From the above t-test results, the following can be inferred:

1. Since, the p-value is <0.0001 less α than for both methods (Pooled—assumes equal variances and Satterthwaite— assumes unequal variances), a statistically significant result that the **null hypothesis is rejected in favor of alternative hypothesis**.
2. Furthermore, the t-value -6.60 (Pooled) and -6.60 (Satterthwaite) which is <-1.99 (two-sided critical value), which also signifies that this difference in mean uptake is practically significant.
3. The mean difference is also given in the results as around -12.65 with 95% CL mean as -16.47 and -8.84. (NOTE: The negative sign signifies that mean uptake of Q type is more than M type).

Testing the Hypothesis 2: t-test on uptake against treatment

$\alpha: 0.05$

corresponding critical value: 1.99* (for DF: 85)

Null Hypothesis:

$$\mu_{\text{CO}_2 \text{ uptake of Chilled}} = \mu_{\text{CO}_2 \text{ uptake of Nonchilled}}$$

Alternate Hypothesis:

$$\mu_{\text{CO}_2 \text{ uptake of Chilled}} \neq \mu_{\text{CO}_2 \text{ uptake of Nonchilled}}$$

Results of t-test on uptake against treatment:

| The TTEST Procedure | | | | | | | |
|---------------------|---------------|----|---------|---------|---------|---------|---------|
| Variable: uptake | | | | | | | |
| Treatment_new | Method | N | Mean | Std Dev | Std Err | Minimum | Maximum |
| C | | 42 | 23.7833 | 10.8843 | 1.6795 | 7.7000 | 42.4000 |
| NC | | 42 | 30.6429 | 9.7050 | 1.4975 | 10.6000 | 45.5000 |
| Diff (1-2) | Pooled | | -6.8595 | 10.3115 | 2.2502 | | |
| Diff (1-2) | Satterthwaite | | -6.8595 | | 2.2502 | | |

| Treatment_new | Method | Mean | 95% CL Mean | Std Dev | 95% CL Std Dev |
|---------------|---------------|---------|------------------|---------|----------------|
| C | | 23.7833 | 20.3915 27.1751 | 10.8843 | 8.9557 13.8793 |
| NC | | 30.6429 | 27.6186 33.6671 | 9.7050 | 7.9853 12.3755 |
| Diff (1-2) | Pooled | -6.8595 | -11.3358 -2.3832 | 10.3115 | 8.9463 12.1724 |
| Diff (1-2) | Satterthwaite | -6.8595 | -11.3367 -2.3824 | | |

| Equality of Variances | | | | |
|-----------------------|--------|--------|---------|--------|
| Method | Num DF | Den DF | F Value | Pr > F |
| Folded F | 41 | 41 | 1.26 | 0.4660 |

Fig 3.6 t-test results of uptake against treatment

From the above t-test results, the following can be inferred:

1. Since, the p-value is 0.0031 less α than for both methods (Pooled—assumes equal variances and Satterthwaite— assumes unequal variances), a statistically significant result that the **null hypothesis is rejected in favor of alternative hypothesis**.
2. Furthermore, the t-value -3.05 (Pooled) and -3.05 (Satterthwaite) which is < -1.99 (two-sided critical value), which also signifies that this difference in mean uptake is practically significant.
3. The mean difference is also given in the results as around -6.85 with 95% CL mean as -11.33 and -2.38. (NOTE: The negative sign signifies that mean uptake of NC type is more than C type).

Testing the Hypothesis 3: ANOVA-test on uptake against concentration levels

α : 0.05

corresponding critical value: 2.22^{*(for DF: (6,77))}

Null Hypothesis:

$$\mu_{\text{CO2 uptake of L}_1} = \mu_{\text{CO2 uptake of L}_2} = \mu_{\text{CO2 uptake of L}_3} = \mu_{\text{CO2 uptake of L}_4} = \mu_{\text{CO2 uptake of L}_5} = \mu_{\text{CO2 uptake of L}_6} = \mu_{\text{CO2 uptake of L}_7}$$

Alternative Hypothesis:

$$\mu_{\text{CO2 uptake of L}_1} \neq \mu_{\text{CO2 uptake of L}_2} \neq \mu_{\text{CO2 uptake of L}_3} \neq \mu_{\text{CO2 uptake of L}_4} \neq \mu_{\text{CO2 uptake of L}_5} \neq \mu_{\text{CO2 uptake of L}_6} \neq \mu_{\text{CO2 uptake of L}_7}$$

Results of ANOVA-test on uptake against concentration levels:

| The ANOVA Procedure | | | | | |
|----------------------------|----|----------------|-------------|---------|--------|
| Dependent Variable: uptake | | | | | |
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 6 | 4068.771429 | 678.128571 | 9.26 | <.0001 |
| Error | 77 | 5638.204167 | 73.223431 | | |
| Corrected Total | 83 | 9706.975595 | | | |

| R-Square | Coeff Var | Root MSE | uptake Mean |
|----------|-----------|----------|-------------|
| 0.419160 | 31.44467 | 8.557069 | 27.21310 |

| Source | DF | Anova SS | Mean Square | F Value | Pr > F |
|----------|----|-------------|-------------|---------|--------|
| conc_new | 6 | 4068.771429 | 678.128571 | 9.26 | <.0001 |

Fig 3.7 ANOVA-test results of uptake against concentration levels 1-7

From the above ANOVA-test results, the following can be inferred:

1. Since, the p-value is < 0.0001 less α , a statistically significant result that the **null hypothesis is rejected in favor of alternative hypothesis**.
2. Furthermore, the f-value -9.26 which is > 2.22 , which also signifies that this difference is practically significant.
3. The R-Square, which is 0.4191, explains the variance about 41.91%.

NOTE: The above test only proves that at least one mean uptake is different from the other but not all are different from each other so, furthermore t-tests must be done by grouping two concentrations at once or from box plot it is evident that uptake reaches saturation after Level 3. So, conducting another ANOVA for the levels 3-7 will also serve the purpose.

Testing the Hypothesis 3: ANOVA-test on uptake against concentration levels 3-7

$\alpha: 0.05$

corresponding critical value: 2.54^{*(for DF: (4,55))}

Null Hypothesis:

$$\mu_{\text{CO2 uptake of L}_3} = \mu_{\text{CO2 uptake of L}_4} = \mu_{\text{CO2 uptake of L}_5} = \mu_{\text{CO2 uptake of L}_6} = \mu_{\text{CO2 uptake of L}_7}$$

Alternative Hypothesis:

$$\mu_{\text{CO2 uptake of L}_3} \neq \mu_{\text{CO2 uptake of L}_4} \neq \mu_{\text{CO2 uptake of L}_5} \neq \mu_{\text{CO2 uptake of L}_6} \neq \mu_{\text{CO2 uptake of L}_7}$$

Results of ANOVA-test on uptake against concentration levels:

| The ANOVA Procedure | | | | | |
|----------------------------|----|----------------|-------------|---------|--------|
| Dependent Variable: uptake | | | | | |
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 4 | 144.455667 | 36.113917 | 0.39 | 0.8165 |
| Error | 55 | 5123.198333 | 93.149061 | | |
| Corrected Total | 59 | 5267.654000 | | | |

| R-Square | Coeff Var | Root MSE | uptake Mean |
|----------|-----------|----------|-------------|
| 0.027423 | 30.94382 | 9.651376 | 31.19000 |

| Source | DF | Anova SS | Mean Square | F Value | Pr > F |
|----------|----|-------------|-------------|---------|--------|
| conc_new | 4 | 144.4556667 | 36.1139167 | 0.39 | 0.8165 |

Fig 3.8 ANOVA-test results of uptake against concentration levels 3-7

From the above ANOVA-test results, the following can be inferred:

1. Since, the p-value is >0.05 greater α , a statistically insignificant result that the **null hypothesis is failed to be rejected and needs more evidence**.
2. Furthermore, the f-value 0.39 which is <2.54 .
3. The R-Square, which is 0.4191, explains the variance about 2.74%.

Testing the Hypothesis 3: t-tests on uptake against concentration levels 1-2 and 2-3

$\alpha: 0.05$

corresponding critical value: 2.22^{*(for DF: (6,77))}

Null Hypothesis 1:

$$\mu_{\text{CO2 uptake of L}_1} = \mu_{\text{CO2 uptake of L}_2}$$

Null Hypothesis 2:

$$\mu_{\text{CO2 uptake of L}_2} = \mu_{\text{CO2 uptake of L}_3}$$

Alternative Hypothesis 1:

$$\mu_{\text{CO2 uptake of L}_1} \neq \mu_{\text{CO2 uptake of L}_2}$$

Alternative Hypothesis 2:

$$\mu_{\text{CO2 uptake of L}_2} \neq \mu_{\text{CO2 uptake of L}_3}$$

Results of t-test on uptake against concentration levels 1-2 and 2-3:

| Method | Variances | DF | t Value | Pr > t |
|---------------|-----------|--------|---------|---------|
| Pooled | Equal | 22 | -5.08 | <.0001 |
| Satterthwaite | Unequal | 15.038 | -5.08 | 0.0001 |

| Equality of Variances | | | | |
|-----------------------|--------|--------|---------|--------|
| Method | Num DF | Den DF | F Value | Pr > F |
| Folded F | 11 | 11 | 5.26 | 0.0105 |

Fig 3.9 t-tests results for Hypothesis 1

| Method | Variances | DF | t Value | Pr > t |
|---------------|-----------|--------|---------|---------|
| Pooled | Equal | 22 | -2.08 | 0.0491 |
| Satterthwaite | Unequal | 19.658 | -2.08 | 0.0505 |

| Equality of Variances | | | | |
|-----------------------|--------|--------|---------|--------|
| Method | Num DF | Den DF | F Value | Pr > F |
| Folded F | 11 | 11 | 2.05 | 0.2481 |

Fig 3.10 t-tests results for Hypothesis 2

From the above ANOVA-test results, the following can be inferred:

1. Since, the p-value is <0.05 greater α , that the **null hypothesis 1 is rejected in favor of alternative hypothesis**.
2. Since, the p-value is >0.05 greater α , that the **null hypothesis 2 is failed to be rejected and needs more evidence**.

Testing the Hypothesis 4: ANOVA-test on uptake against two-factor main effects model with interaction of type and treatment

$\alpha: 0.05$

corresponding critical value: 2.708*(for DF: (3,80))

Null Hypothesis:

$\mu_{\text{CO}_2 \text{ uptake of type and treatment interaction}} = \mu_{\text{CO}_2 \text{ uptake of type and treatment interaction}}$

Alternative Hypothesis:

$\mu_{\text{CO}_2 \text{ uptake of type and treatment interaction}} \neq \mu_{\text{CO}_2 \text{ uptake of type and treatment interaction}}$

Results of ANOVA-test:

| The ANOVA Procedure | | | | | |
|----------------------------|----|----------------|-------------|---------|--------|
| Dependent Variable: uptake | | | | | |
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 3 | 4579.378452 | 1526.459484 | 23.82 | <.0001 |
| Error | 80 | 5127.597143 | 64.094964 | | |
| Corrected Total | 83 | 9706.975595 | | | |

| R-Square | Coeff Var | Root MSE | uptake Mean |
|----------|-----------|----------|-------------|
| 0.471762 | 29.41941 | 8.005933 | 27.21310 |

| Source | DF | Anova SS | Mean Square | F Value | Pr > F |
|----------------------|----|-------------|-------------|---------|--------|
| Type_new | 1 | 3365.534405 | 3365.534405 | 52.51 | <.0001 |
| Treatment_new | 1 | 988.114405 | 988.114405 | 15.42 | 0.0002 |
| Type_new*Treatment_n | 1 | 225.729643 | 225.729643 | 3.52 | 0.0642 |

Fig 3.8 ANOVA-test results of uptake against

From the above ANOVA-test results, the following can be inferred:

1. Since, the p-value is 0.0642 little greater than α , a statistically insignificant result that the **null hypothesis is failed to be rejected and needs more evidence.**

4. Conclusion

Hypothesis:

1. There exists significant difference between the plant's mean CO₂ uptake for the two origins (Quebec and Mississippi).

$\mu_{\text{CO}_2 \text{ uptake of Quebec}} \neq \mu_{\text{CO}_2 \text{ uptake of Mississippi}}$

Conclusions:

Yes, the hypothesis is **true** which is verified with the t-test results.

2. There exists significant difference between the plant's mean CO₂ uptake for the two treatments (Chilled and Non-chilled).

$\mu_{\text{CO}_2 \text{ uptake of Chilled}} \neq \mu_{\text{CO}_2 \text{ uptake of Nonchilled}}$

Conclusions:

Yes, the hypothesis is **true** which is verified with the t-test results.

3. There exists significant difference between the plant's mean CO₂ uptake for the 7 concentration levels (1-7).

$\mu_{\text{CO}_2 \text{ uptake of L}_1} \neq \mu_{\text{CO}_2 \text{ uptake of L}_2} \neq \mu_{\text{CO}_2 \text{ uptake of L}_3} \neq \mu_{\text{CO}_2 \text{ uptake of L}_4} \neq \mu_{\text{CO}_2 \text{ uptake of L}_5} \neq \mu_{\text{CO}_2 \text{ uptake of L}_6} \neq \mu_{\text{CO}_2 \text{ uptake of L}_7}$

Conclusions:

Yes, the hypothesis is partially **true**, that is: $\mu_{\text{CO}_2 \text{ uptake of L}_2} \neq \mu_{\text{CO}_2 \text{ uptake of L}_3} \neq \mu_{\text{CO}_2 \text{ uptake of L}_4} \neq \mu_{\text{CO}_2 \text{ uptake of L}_5} \neq \mu_{\text{CO}_2 \text{ uptake of L}_6} \neq \mu_{\text{CO}_2 \text{ uptake of L}_7}$ is not supported by the test results, though the results support $\mu_{\text{CO}_2 \text{ uptake of L}_1} \neq \mu_{\text{CO}_2 \text{ uptake of L}_2}$.

4. There exists a relation between how the differences between the plant's mean CO₂ uptake against interaction between type and treatment.

Conclusions:

No, the hypothesis is **not true** which is verified with the ANOVA-test two-factor main effects model with interaction of type and treatment.

5. Appendix:

Rcode

```
# loading package
library(dplyr)

# Getting to data to df
df<-CO2

# Changing the concentration levels as described in 1. Part-A
df2 <- df %>% mutate (conc_new=case_when(conc==95 ~ "1", conc==175 ~ "2",conc==250 ~ "3",
conc==350 ~ "4",conc==500 ~ "5", conc==675 ~ "6",conc==1000 ~ "7"))

# Getting relevant data columns
df3<-df2[, c(1:3,6,5)]

# Changing the type and treatment as described in 1. Part-A
df4 <- df3 %>% mutate (Type_new=case_when(Type=="Quebec" ~ "Q", Type=="Mississippi" ~ "M"), Treament_new =
case_when(Treatment=="nonchilled"~"NC",Treatment=="chilled"~"C"))

# Getting relevant data columns
df5<-df4[, c(1,6,7,4,5)]

# Writing df to a file
write.csv (x=df5,file="C:/Users/Varun/Desktop/Spring 2019/Statistical Computing/co2_n.csv")
```

SASCode:

```
/*Contents of the SAS Dataset in library lproject.co2_n*/
proc contents data=lproject.co2_n;
run;

/*Printing the first 10 observations of the SAS Dataset in library lproject.co2_n*/
proc print data=lproject.co2_n(obs=10); run;

/*Creating type_new column Sorted SAS datasets */
proc sort data=lproject.co2_n out=lproject.co2_n_t;
by type_new;
run;

/*Creating treatment_new column Sorted SAS datasets */
proc sort data=lproject.co2_n out=lproject.co2_n_tr;
by Treatment_new;
run;

/*Creating conc_new column Sorted SAS datasets */
proc sort data=lproject.co2_n out=lproject.co2_n_conc;
by conc_new;
run;

/*Normal Histogram Plot of Uptake as well as normal test*/
```

```

ods graphics on;
proc univariate data=lproject.co2_n normaltest;
    histogram uptake /normal kernel;
run;
ods graphics off;

/*Histogram plot of uptake by treatment_new as well as normal test*/
ods graphics on;
proc univariate data=lproject.co2_n normaltest;
    histogram uptake /normal kernel;
    class treatment_new;
run;
ods graphics off;

/*Histogram plot of uptake by type_new as well as normal test*/
ods graphics on;
proc univariate data=lproject.co2_n normaltest;
    histogram uptake /normal kernel;
    class type_new;
run;
ods graphics off;

/*Histogram plot of uptake by conc_new in one panel*/
ods graphics on;
proc sgpanel data=lproject.co2_n;
    panelby conc_new;
    histogram uptake;
run;
ods graphics off;

/*Histogram plot of uptake by type_new in one panel*/
ods graphics on;
proc sgpanel data=lproject.co2_n;
    panelby type_new;
    histogram uptake;
run;
ods graphics off;

/*Histogram plot of uptake by treatment_new in one panel*/
ods graphics on;
proc sgpanel data=lproject.co2_n;
    panelby treatment_new;
    histogram uptake;
run;
ods graphics off;

/*Normality test of uptake var by type_new var with probplot*/
ods graphics on;
ods select Moments TestsForNormality ProbPlot;

```

```

proc univariate data=lproject.co2_n_t normaltest;
  var uptake;
  by type_new;
  probplot uptake / normal (mu=est sigma=est)
    square;
  label type_new = "type_new" uptake="Uptake";
  inset mean std / format=6.4;
run;

/*Normality test of uptake var by treatment_new var with probplot*/
ods graphics on;
ods select Moments TestsForNormality ProbPlot;
proc univariate data=lproject.co2_n_tr normaltest;
  var uptake;
  by treatment_new;
  probplot uptake / normal (mu=est sigma=est)
    square;
  label treatment_new = "treatment_new" uptake="Uptake";
  inset mean std / format=6.4;
run;

/*All relevant Frequency tables*/
proc freq data=lproject.co2_n;
  tables (treatment_new type_new)*(conc_new type_new);
run;

/* Examining the Hypotheses: type ~ uptake graphically*/

ods graphics on;
proc sgplot data=lproject.co2_n ;
  vbox uptake/group=type_new;
run;
ods graphics off;

/* Examining the Hypotheses: treatment ~ uptake graphically*/

ods graphics on;
proc sgplot data=lproject.co2_n_tr ;
  vbox uptake/group=treatment_new;
run;
ods graphics off;

/* Examining the Hypotheses: concentration ~ uptake graphically*/

ods graphics on;
proc sgplot data=lproject.co2_n ;
  vbox uptake/group=conc_new;
run;
ods graphics off;

```

```
/* Examining the Hypotheses: type*concentration ~ uptake graphically*/
```

```
ods graphics on;
```

```
proc sgplot data=lproject.co2_n;  
  vbox uptake / category=type_new  
    group=treatment_new  
    groupdisplay=clustered;  
  title "type & conc: main effect";  
run;
```

```
ods graphics off;
```

```
/* Testing the Hypotheses: type ~ uptake using t-test*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_t plots(only)=(histogram boxplot) alpha=0.05;  
  var uptake;  
  class type_new;  
run;
```

```
ods graphics off;
```

```
/* Testing the Hypotheses: treatment ~ uptake using t-test*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_tr plots(only)=(histogram boxplot) alpha=0.05;  
  var uptake;  
  class treatment_new;  
run;
```

```
ods graphics off;
```

```
/* simple ANOVA test: concentration ~ uptake*/
```

```
ods graphics on;
```

```
proc anova data=lproject.co2_n;  
  class conc_new;  
  model uptake = conc_new;  
  label conc_new = "Concentration";  
run;
```

```
ods graphics off;
```

```
/* From the above anova test we want to find if the difference in means of uptake of which concentrations matters most*/
```

```
/* 1 and 2 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(obs=24) plots(only)=(histogram boxplot) alpha=0.05;
```

```
var uptake;
```

```
class conc_new;
```

```
run;
```

```
ods graphics off;
```

```
/* 2 and 3 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(firstobs=13 obs=36) plots(only)=(histogram boxplot) alpha=0.05;
```

```
var uptake;
```

```
class conc_new;
```

```
run;
```

```
ods graphics off;
```

```
/* 3 and 4 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(firstobs=25 obs=48) plots(only)=(histogram boxplot) alpha=0.05;
```

```
var uptake;
```

```
class conc_new;
```

```
run;
```

```
ods graphics off;
```

```
/* 4 and 5 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(firstobs=37 obs=60) plots(only)=(histogram boxplot) alpha=0.05;
```

```
var uptake;
```

```
class conc_new;
```

```
run;
```

```
ods graphics off;
```

```
/* 5 and 6 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(firstobs=49 obs=72) plots(only)=(histogram boxplot) alpha=0.05;  
  var uptake;  
  class conc_new;  
run;
```

```
ods graphics off;
```

```
/* 6 and 7 conc levels*/
```

```
ods graphics on;
```

```
proc ttest data=lproject.co2_n_conc(firstobs=61 obs=84) plots(only)=(histogram boxplot) alpha=0.05;  
  var uptake;  
  class conc_new;  
run;
```

```
ods graphics off;
```

```
/* ANOVA to find is there any difference in means of 2-7 concentration levels*/
```

```
ods graphics on;
```

```
proc anova data=lproject.co2_n_conc(firstobs=13 obs=84);  
  class conc_new;  
  model uptake = conc_new;  
  label conc_new = "Concentration";  
run;
```

```
ods graphics off;
```

```
/* ANOVA test two-factor model: type+treatment ~ uptake*/
```

```
proc anova data=lproject.co2_n;  
  class type_new treatment_new;  
  model uptake = type_new|treatment_new;  
run;
```