

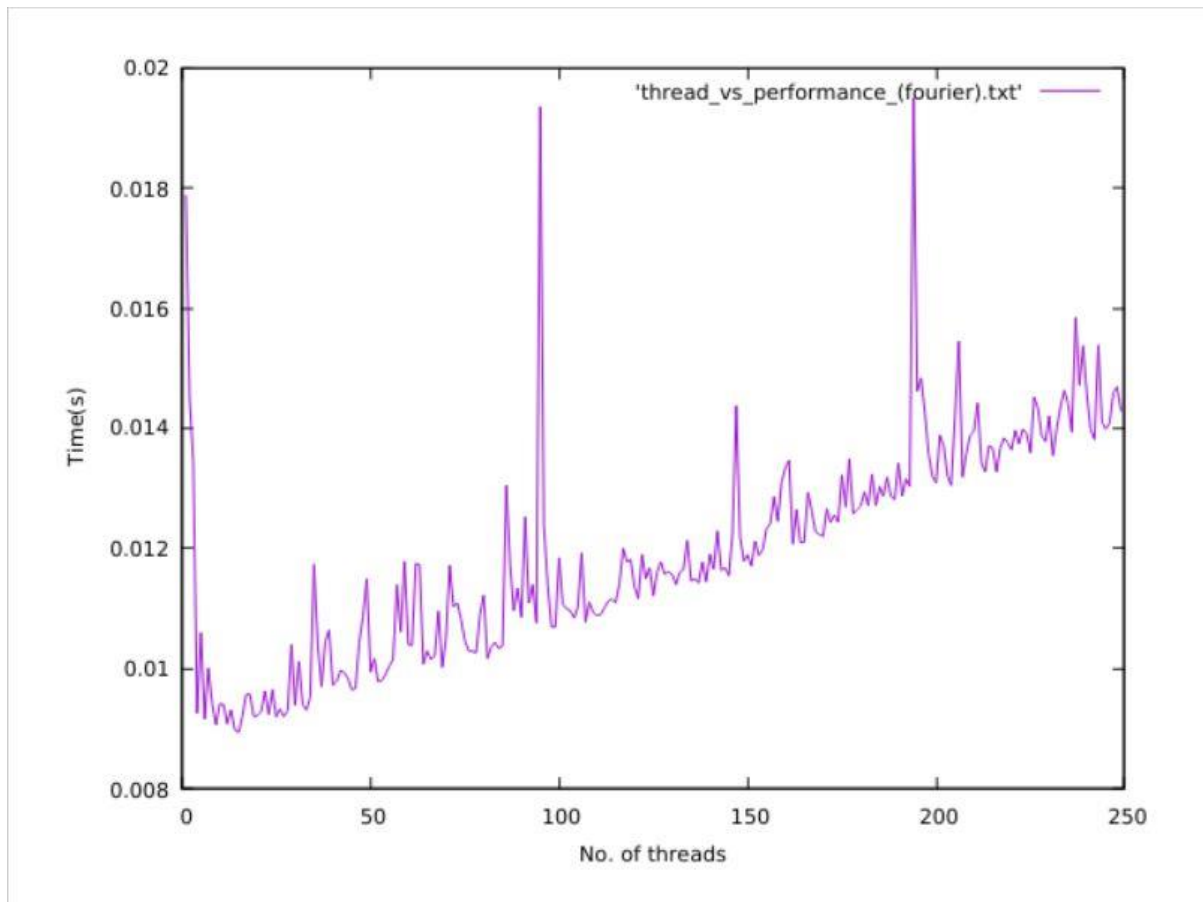
Assignment 2

- Methods implemented to calculate the value of pi
 - **Fourier Series Method**
 - **Wallis' Method**
- **Fourier Series Method**
 - This is a slow converging series and for experimental purposes it can show clear change in value of pi at high number of iterations because a fast converging series at high iterations would be almost stagnant.
 - Fourier Series could be used to implement value
 - $f(x) = a/2 + \text{Summation (A)}\cos(nx) + \text{Summation (B)}\sin(nx)$
 - Here we use $f(x) = |x|$ for $-\pi < x < \pi$
 - Hence we get:
 - $f(x) = \pi/2 - 4\pi(\cos x + 1/3^2 \cos 3x + 1/5^2 \cos 5x + \dots), -\pi < x < \pi$
 - Substituting $x=0$
 - We get

$$\pi/8 = 1 + 1/3^2 + 1/5^2 + \dots = \sum_{n=1}^{\infty} 1/(2n-1)^2$$
 - Then computing on general term
 - $\pi^2/8 = 1/2 + \sum_{n=1}^{\infty} 2/((2n-1)^2(2n+1))$
- **Wallis Method**
 - This method provides an easy general nth term which can be computed parallelly.
 - General term is not in pipeline fashion.
 - It makes use of wallis integral $\int_0^{\pi/2} \sin(n)x \cos(m)x$ over $\pi/2$
 - It is equivalent to $(m-1)(n-1)(m-3)(n-3)\dots\dots\dots/(m+n-2)(m+n)(m+n-4)\dots\dots\dots * \pi/2;$

Graphs

Thread vs performance for fourier Series



No. of Threads	Time(s)
1	0.017880
2	0.014495
3	0.013436
4	0.009264
5	0.010605
6	0.009167
7	0.010015
8	0.009425
9	0.009071
10	0.009419
11	0.009410
12	0.009089
13	0.009322
14	0.008985
15	0.008945
16	0.009204
17	0.009573
18	0.009583
19	0.009215
20	0.009227

21	0.009288
22	0.009634
23	0.009243
24	0.009656
25	0.009204
26	0.009336
27	0.009205
28	0.009305
29	0.010403
30	0.009396
31	0.010123
32	0.009407
33	0.009316
34	0.009520
35	0.011737
36	0.010405
37	0.009706
38	0.010454
39	0.010646
40	0.009731
41	0.009791
42	0.009974
43	0.009943
44	0.009846
45	0.009654
46	0.009676
47	0.010436
48	0.010865
49	0.011504
50	0.009949
51	0.010172
52	0.009791
53	0.009809
54	0.009914
55	0.010049
56	0.010163
57	0.011396
58	0.010616
59	0.011789
60	0.010406
61	0.010388
62	0.011754
63	0.011729
64	0.010082
65	0.010300
66	0.010159

67	0.010214
68	0.010962
69	0.010025
70	0.010499
71	0.011726
72	0.011031
73	0.011097
74	0.010830
75	0.010479
76	0.010304
77	0.010294
78	0.010271
79	0.010894
80	0.011227
81	0.010175
82	0.010364
83	0.010443
84	0.010337
85	0.010380
86	0.013053
87	0.011722
88	0.010968
89	0.011344
90	0.010857
91	0.012532
92	0.011093
93	0.011400
94	0.010766
95	0.019348
96	0.012377
97	0.011388
98	0.010699
99	0.010697
100	0.011848
101	0.011074
102	0.011000
103	0.010969
104	0.010845
105	0.011030
106	0.011928
107	0.010779
108	0.011110
109	0.010940
110	0.010893
111	0.010900
112	0.011012

113	0.011125
114	0.011161
115	0.011099
116	0.011413
117	0.012008
118	0.011779
119	0.011819
120	0.011370
121	0.011170
122	0.011905
123	0.011498
124	0.011687
125	0.011216
126	0.011619
127	0.011780
128	0.011574
129	0.011616
130	0.011575
131	0.011403
132	0.011604
133	0.011654
134	0.012135
135	0.011464
136	0.011499
137	0.011428
138	0.011779
139	0.011451
140	0.011908
141	0.011659
142	0.012295
143	0.011641
144	0.011684
145	0.011551
146	0.012242
147	0.014375
148	0.012193
149	0.011791
150	0.011899
151	0.011711
152	0.012124
153	0.011889
154	0.011990
155	0.012332
156	0.012408
157	0.012862
158	0.012452

159	0.013097
160	0.013340
161	0.013470
162	0.012077
163	0.012651
164	0.012106
165	0.012106
166	0.012936
167	0.012633
168	0.012282
169	0.012236
170	0.012205
171	0.012664
172	0.012433
173	0.012563
174	0.012438
175	0.013224
176	0.012696
177	0.013496
178	0.012579
179	0.012646
180	0.012710
181	0.012944
182	0.012711
183	0.013237
184	0.012712
185	0.013035
186	0.012867
187	0.013191
188	0.012865
189	0.012817
190	0.013426
191	0.012869
192	0.013161
193	0.013035
194	0.019494
195	0.014613
196	0.014835
197	0.014270
198	0.013571
199	0.013209
200	0.013096
201	0.013886
202	0.013714
203	0.013209
204	0.013049

205	0.014204
206	0.015445
207	0.013193
208	0.013572
209	0.013881
210	0.013943
211	0.014422
212	0.013428
213	0.013275
214	0.013711
215	0.013674
216	0.013273
217	0.013668
218	0.013839
219	0.013756
220	0.013643
221	0.013966
222	0.013739
223	0.013991
224	0.013913
225	0.013592
226	0.014522
227	0.014341
228	0.013874
229	0.013779
230	0.014205
231	0.013546
232	0.014004
233	0.014366
234	0.014629
235	0.014413
236	0.013941
237	0.015842
238	0.014714
239	0.015371
240	0.014551
241	0.013970
242	0.013817
243	0.015381
244	0.014106
245	0.013983
246	0.014087
247	0.014592
248	0.014689
249	0.014302

Thread vs performance for wallis

