Assignment

11.9.1 - 9

EE23BTECH11220 - R.V.S.S Varun

QUESTION

Find a_9 in the sequence $a_n = (-1)^{n-1} n^3$

SOLUTION

	Symbol	Value	Description
	x(0)	1	First term of the sequence
	x(n)	$(-1)^n (n+1)^3 u(n)$	$(n+1)^{th}$ term of the sequence
TABLE 0			

TABLE OF PARAMETERS

To obtain 9^{th} term of the sequence put n=8 in x(n)

$$x(8) = 729\tag{1}$$

From up-scaling property,

$$x(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} X(z)$$
 (2)

$$x(kn) \stackrel{\mathcal{Z}}{\longleftrightarrow} X(z^k)$$
 (3)

$$x(2n) = (2n+1)^3 u(2n)$$
 (4)

Using Z transform,

$$x(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} X(z)$$
 (5)

$$x(2n) \stackrel{\mathcal{Z}}{\longleftrightarrow} G(z)$$
 (6)

$$=X\left(z^{2}\right) \tag{7}$$

$$u(2n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{1}{(1-z^{-2})}, |z| > 1 \tag{8}$$

$$2n \ u(2n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-2}}{(1-z^{-2})^2}, |z| > 1$$
 (9)

$$(2n)^{2} u(2n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-2} \left(z^{-2} + 1\right)}{\left(1 - z^{-2}\right)^{3}}, |z| > 1$$
 (10)

$$(2n)^3 u(2n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-2} \left(1 + 4z^{-2} + z^{-4}\right)}{\left(1 - z^{-2}\right)^4}, |z| > 1$$
 (11)

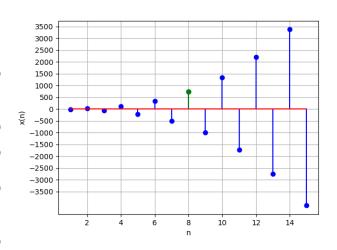
$$G(z) = \sum_{2n=-\infty}^{2n=\infty} (2n+1)^3 u(2n) z^{-2n}$$
 (12)

$$G(z) = \sum_{2n=-\infty}^{2n=\infty} \left((2n)^3 + 3(2n)^2 + 3(2n) + 1 \right) u(2n) z^{-2n} \quad \{z : |z| > 1\}$$
(13)

 $G(z) = \frac{4z^6 + z^4 - 3z^2}{(z^2 - 1)^4}, |z| > 1$ (14)

Replace z^2 by z in (14)

$$X(z) = \frac{4z^3 + z^2 - 3z}{(z - 1)^4}, |z| > 1$$
 (15)



Graph of x(n)