# Pràctica 2: Implementació del Simplex Primal

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# 1 Informació

[Arxiu adjunt: Simplex.m]

Els conjunts de dades assignats per aquesta pràctica són el 10 i el 55.

# 2 Observacions

#### 2.1 Fase I

Hem escollit integrar la fase I al codi. Aquesta utilitza la matriu A i els vector b i c per identificar una primera solució bàsica factible amb la qual començar la Fase II.

Aquesta última, a cada iteració, donades les mateixes dades que a la Fase I i, a més, una base factible del problema amb la seva solució bàsica factible associada, detecta si la solució en qüestió és òptima, comprova si el problema és il·limitat i, si no, calcula una nova base factible amb una solució bàsica factible que millori la funció objectiu.

#### 2.2 Taxació

Implementem tant la regla de Bland com la regla dels costos reduïts més negatius al mateix script, per optar a una o l'altra cal canviar el valor "Bland".

### 2.3 Tractament de degeneració

Com tenim la opció de fer la regla de Bland, tractem la degeneració activant la regla de Bland i deixant iterar l'algorisme.

### 2.4 Inversa de la Matriu Bàsica

Per al càlcul de la matriu inversa de B hem optat per fer servir la matriu E (vist a classe) per a actualitzar  $B^{-1}$  en cada iteració (a excepció de la primera iteració de cada fase, on això no és possible), agilitzant el cost computacional de l'algorisme.

#### 2.5 Problemes Infactibles

Si el problema a resoldre és infactible, l'algorisme ho detectarà al acabar la Fase I, ja que si la funció objectiu és positiva (o, com veurem més endevant, no molt propera a zero) vol dir que cal donar valors positius a alguna de les variables artificials per poder resoldre el sistema. És a dir, que s'ha necessitat una columna artificial per completar el rang de la matriu.

#### 2.6 Errors de càlcul

Al fer moltes iteracions per resoldre el problema, els errors de càlcul que comet l'ordinador es van acumulant, podent fer que el resultat no sigui correcte. És per això que, al acabar la fase I, enlloc de comprovar si z=0 el que comprovem és si z és menor a una certa tolerància.

# 3 Resultats

### 3.1 Conjunt de Dades 10, Problema 1

```
Fase I
  Iteracio \ 1 \ : \ iout = 0 \, , \ q = 1 \, , \ B(p) \, = \, 27 \, , \ theta* = \, 0.27 \, , \ z \, = \, 1956.157
   Iteracio 2: iout = 0, q = 2, B(p) = 30, theta* = 0.19, z = 1835.686
   Iteracio 3: iout = 0, q = 3, B(p) = 29, theta* = 0.12, z = 1810.967
   Iteracio\ 4\ :\ iout\ =\ 0\,,\ q\ =\ 4\,,\ B(p)\ =\ 26\,,\ theta*\ =\ 0.10\,,\ z\ =\ 1730.924
   Iteracio 5 : iout = 0, q = 5, B(p) = 4, theta* = 0.47, z = 1629.776
   Iteracio 6: iout = 0, q = 27, B(p) = 28, theta* = 94.14, z = 1469.797
   Iteracio 7: iout = 0, q = 30, B(p) = 27, theta* = 36.35, z = 1421.589
   Iteracio 8: iout = 0, q = 6, B(p) = 1, theta* = 0.82, z = 1421.013
   Iteracio 9 : iout = 0, q = 7, B(p) = 21, theta* = 1.09, z = 1327.536
   Iteracio 10 : iout = 0, q = 1, B(p) = 6, theta* = 0.48, z = 1234.097
   Iteracio 11 : iout = 0, q = 8, B(p) = 25, theta* = 0.51, z = 1199.014
   Iteracio 12 : iout = 0, q = 29, B(p) = 22, theta* = 507.23, z = 1160.254
13
   Iteracio 13 : iout = 0, q = 9, B(p) = 3, theta* = 2.01, z = 958.135
   Iteracio 14 : iout = 0, q = 22, B(p) = 29, theta* = 272.72, z = 20
   Iteracio 15 : iout = 0, q = 10, B(p) = 23, theta* = 0.97, z = 386.621
16
   Iteracio 16 : iout = 0, q = 4, B(p) = 24, theta* = 0.23, z = 274.006
17
   Iteracio 17 : iout = 0, q = 3, B(p) = 4, theta* = 0.70, z = 266.082
18
   Iteracio 18 : iout = 0, q = 6, B(p) = 9, theta* = 1.06, z = 260.245
   Iteracio 19 : iout = 0, q = 11, B(p) = 6, theta* = 0.37, z = 200.001
20
   Iteracio 20 : iout = 0, q = 4, B(p) = 22, theta* = 1.40, z = 1.40
21
   Iteracio 21 : iout = 0, q = 13, B(p) = 30, theta* = 1.69, z = 1.69
  SBF trobada
  Fase II
24
   Iteracio 22 : iout = 0, q = 9, B(p) = 10, theta* = 1.49, z = 248.032
25
   Iteracio 23 : iout = 0, q = 14, B(p) = 3, theta* = 0.19, z = 177.110
   Iteracio 24 : iout = 0, q = 10, B(p) = 13, theta* = 1.98, z = 122.027
   Iteracio 25 : iout = 0, q = 12, B(p) = 7, theta* = 2.63, z = -132.616
28
   Iteracio 26 : iout = 0, q = 13, B(p) = 5, theta* = 0.08, z = -134.977
29
   Iteracio 27 : iout = 0, q = 15, B(p) = 14, theta* = 365.40, z = -167.494
   Iteracio 28 : iout = 0, q = 16, B(p) = 1, theta* = 396.31, z = -309.178
   Iteracio 29 : iout = 0, q = 17, B(p) = 2, theta* = 1.18, z = -310.213
32
   Iteracio 30 : iout = 0, q = 5, B(p) = 8, theta* = 0.46, z = -334.007
33
   Iteracio 31 : iout = 0, q = 14, B(p) = 13, theta* = 1.07, z = -430.831
   Iteracio 32 : iout = 0, q = 8, B(p) = 15, theta* = 0.40, z = -467.904
35
   Iteracio 33 : iout = 0, q = 19, B(p) = 8, theta* = 57.41, z = -486.367
36
   Iteracio 34 : iout = 0, q = 20, B(p) = 14, theta* = 224.47, z = -520.223
37
   Solucio optima trobada, iteracio 34, z = -520.223
  Fi del simplex primal
39
   Solucio optima:
40
   base =
41
       12
                    9
                          19
                                 5
                                       20
                                             16
                                                   10
                                                          11
                                                                17
42
  xb =
43
                                    150.1295
                                                 0.8764
       2.7334
                 2.8801
                            5.1418
                                                          224.4677
                                                                    579.3937
                                                                                 2.2320
44
               0.6360
                        97.1503
  z =
45
    -520.2228
46
  r =
47
     122.6035
                 0.4621
                         118.3616
                                   137.9023
                                                33.6201
                                                                    159.0863
                                                                                 0.1386
                                                           47.3763
                      20.6711
           43.0010
```

# 3.2 Conjunt de Dades 10, Problema 2

```
<sub>1</sub> Fase I
  Iteracio 1: iout = 0, q = 1, B(p) = 30, theta* = 2.18, z = 2327.411
  Iteracio 2: iout = 0, q = 2, B(p) = 21, theta* = 1.05, z = 2077.613
   Iteracio 3: iout = 0, q = 3, B(p) = 23, theta* = 0.13, z = 2040.542
   Iteracio 4: iout = 0, q = 4, B(p) = 3, theta* = 0.41, z = 1975.756
   Iteracio 5 : iout = 0, q = 21, B(p) = 2, theta* = 40.10, z = 1883.317
   Iteracio \ 6 \ : \ iout \ = \ 0 \, , \ q \ = \ 6 \, , \ B(p) \ = \ 22 \, , \ theta* \ = \ 0.74 \, , \ z \ = \ 1723.487
   Iteracio 7 : iout = 0, q = 7, B(p) = 28, theta* = 0.35, z = 1641.901
   Iteracio 8: iout = 0, q = 8, B(p) = 26, theta* = 0.52, z = 1415.332
   Iteracio 9 : iout = 0, q = 2, B(p) = 21, theta* = 0.14, z = 1381.637
   Iteracio 10 : iout = 0, q = 30, B(p) = 1, theta* = 52.31, z = 1338.142
11
   Iteracio 11 : iout = 0, q = 5, B(p) = 24, theta* = 0.55, z = 1322.644
   Iteracio 12 : iout = 0, q = 22, B(p) = 5, theta* = 76.53, z = 1221.983
   Iteracio 13 : iout = 0, q = 1, B(p) = 6, theta* = 1.74, z = 1080.719
14
   Iteracio 14 : iout = 0, q = 10, B(p) = 27, theta* = 0.59, z = 933.473
15
   Iteracio\ 15\ :\ iout\ =\ 0\,,\ q\ =\ 6\,,\ B(p)\ =\ 29\,,\ theta*\ =\ 0.45\,,\ z\ =\ 905.514
   Iteracio 16 : iout = 0, q = 5, B(p) = 2, theta* = 0.45, z = 876.496
   Iteracio 17 : iout = 0, q = 9, B(p) = 4, theta* = 0.02, z = 871.283
18
   Iteracio 18 : iout = 0, q = 11, B(p) = 30, theta* = 0.04, z = 840.336
19
   Iteracio 19 : iout = 0, q = 3, B(p) = 10, theta* = 2.67, z = 435.127
   Iteracio 20 : iout = 0, q = 2, B(p) = 1, theta* = 1.44, z = 270.034
   Iteracio 21 : iout = 0, q = 12, B(p) = 7, theta* = 0.33, z =
22
   Iteracio 22 : iout = 0, q = 1, B(p) = 25, theta* = 0.09, z = 1
   Iteracio 23 : iout = 0, q = 13, B(p) = 1, theta* = 0.28, z =
   Iteracio 24 : iout = 0, q = 29, B(p) = 22, theta* = 16.43, z =
                                                                         16.431
   Iteracio 25 : iout = 0, q = 23, B(p) = 29, theta* = 6.09, z = 0
                                                                         6.090
26
   Iteracio 26 : iout = 0, q = 4, B(p) = 23, theta* = 0.06, z = 0.06
27
  SBF trobada
  Fase II
   Iteracio 27 : iout = 0, q = 18, B(p) = 8, theta* = 315.79, z = -644.542
30
   Iteracio 28 : iout = 0, q = 19, B(p) = 5, theta* = 333.11, z = -709.018
   Solucio optima trobada, iteracio 28, z = -709.018
   Fi del simplex primal
   Solucio optima:
34
   base =
35
       19
                                                    12
                                 13
                                       18
                                               3
                                                            6
                                                                 11
36
  xb =
37
     333.1076
                 2.3381
                            1.9319
                                       1.1814
                                                  0.1318
                                                           108.0757
                                                                        1.4591
                                                                                  1.8980
38
             0.8771
                       3.2170
  z =
    -709.0183
40
  r =
41
      48.8310 \quad 151.3618
                           59.7230
                                      40.2335
                                                  0.5348
                                                             0.1167
                                                                        0.5252
                                                                                 36.8256
42
             49.8478
                        0.0189
```

# 3.3 Conjunt de Dades 10, Problema 3

```
<sub>1</sub> Fase I
  Iteracio 1: iout = 0, q = 1, B(p) = 24, theta* = 0.40, z = 1118.597
  Iteracio 2: iout = 0, q = 2, B(p) = 30, theta* = 0.29, z = 1027.017
  Iteracio 3: iout = 0, q = 6, B(p) = 1, theta* = 0.28, z = 1015.200
   Iteracio 4: iout = 0, q = 9, B(p) = 22, theta* = 0.67, z = 783.861
  Iteracio 5 : iout = 0, q = 24, B(p) = 29, theta* = 4.12, z = 4.12
                                                                  747.064
   Iteracio 6: iout = 0, q = 30, B(p) = 2, theta* = 12.32, z = 721.041
  Iteracio 7 : iout = 0, q = 3, B(p) = 30, theta* = 0.14, z = 717.276
  Iteracio 8 : iout = 0, q = 1, B(p) = 24, theta* = 0.02, z = 0.02
  Iteracio 9 : iout = 0, q = 30, B(p) = 3, theta* = 6.54, z =
  Iteracio 10 : iout = 0, q = 8, B(p) = 1, theta* = 0.07, z =
  Iteracio 11 : iout = 0, q = 11, B(p) = 28, theta* = 0.06, z = 681.653
12
   Iteracio 12 : iout = 0, q = 15, B(p) = 25, theta* = 39.50, z = 10.50
                                                                    642.154
   Iteracio 13 : iout = 0, q = 3, B(p) = 30, theta* = 0.02, z = 0.02
                                                                   641.542
14
   Iteracio 14 : iout = 0, q = 14, B(p) = 3, theta* = 0.07, z = 10
15
  Iteracio 15 : iout = 0, q = 24, B(p) = 11, theta* = 2.41, z = 2.41
                                                                    637.550
  Iteracio 16 : iout = 0, q = 30, B(p) = 8, theta* = 1.77, z = 1.79
                                                                   637.509
   Iteracio 17 : iout = 0, q = 3, B(p) = 30, theta* = 0.03, z =
                                                                   636.334
18
  Iteracio 18 : iout = 0, q = 17, B(p) = 27, theta* = 65.38, z =
                                                                    570.952
19
  Iteracio 19 : iout = 0, q = 29, B(p) = 3, theta* = 3.41, z =
                                                                   569.563
   Iteracio 20 : iout = 0, q = 7, B(p) = 29, theta* = 0.04, z = 1
                                                                   569.233
  Iteracio 21 : iout = 0, q = 12, B(p) = 7, theta* = 0.02, z = 566.504
  Iteracio 22 : iout = 0, q = 19, B(p) = 12, theta* = 3.41, z = 566.150
  Problema Infactible
```

# 3.4 Conjunt de Dades 10, Problema 4

```
<sub>1</sub> Fase I
  Iteracio 1: iout = 0, q = 1, B(p) = 25, theta* = 6.60, z = 3862.409
   Iteracio 2: iout = 0, q = 2, B(p) = 29, theta* = 3.89, z = 2939.685
   Iteracio \ 3 \ : \ iout \ = \ 0 \, , \ q \ = \ 3 \, , \ B(p) \ = \ 32 \, , \ theta* \ = \ 1.38 \, , \ z \ = \ 2334.725
   Iteracio 4: iout = 0, q = 4, B(p) = 34, theta* = 3.54, z = 1766.504
   Iteracio 5 : iout = 0, q = 29, B(p) = 30, theta* = 217.18, z = 1687.086
   Iteracio 6: iout = 0, q = 5, B(p) = 2, theta* = 1.13, z = 1591.856
   Iteracio 7: iout = 0, q = 30, B(p) = 28, theta* = 372.22, z = 1315.186
   Iteracio 8 : iout = 0, q = 6, B(p) = 1, theta* = 2.53, z = 961.683
   Iteracio 9: iout = 0, q = 34, B(p) = 33, theta* = 62.64, z = 787.294
10
   Iteracio 10 : iout = 0, q = 8, B(p) = 29, theta* = 0.34, z = 695.842
11
   Iteracio 11 : iout = 0, q = 33, B(p) = 30, theta* = <math>91.30, z = 368.609
12
   Iteracio 12 : iout = 0, q = 2, B(p) = 26, theta* = 0.46, z =
                                                                   270.184
   Iteracio 13 : iout = 0, q = 7, B(p) = 27, theta* = 0.03, z =
                                                                   266.862
14
   Iteracio 14 : iout = 0, q = 26, B(p) = 31, theta* = 104.79, z = 217.073
15
   Iteracio 15 : iout = 0, q = 1, B(p) = 26, theta* = 0.73, z = 209.071
   Iteracio 16 : iout = 0, q = 10, B(p) = 33, theta* = 0.70, z = 195.912
   Iteracio 17 : iout = 0, q = 11, B(p) = 34, theta* = 1.95, z = 1.95
18
  SBF trobada
19
  Fase II
20
   Iteracio 18 : iout = 0, q = 13, B(p) = 3, theta* = 3.12, z = -914.900
21
   Iteracio 19 : iout = 0, q = 14, B(p) = 6, theta* = 0.11, z = -926.543
22
   Iteracio 20 : iout = 0, q = 3, B(p) = 11, theta* = 0.01, z = -927.080
23
   Iteracio 21 : iout = 0, q = 15, B(p) = 3, theta* = 0.50, z = -927.393
   Iteracio 22 : iout = 0, q = 6, B(p) = 14, theta* = 0.37, z = -942.839
25
   Iteracio 23 : iout = 0, q = 12, B(p) = 10, theta* = 0.61, z = -952.563
26
   Iteracio 24 : iout = 0, q = 3, B(p) = 12, theta* = 0.15, z = -966.492
27
   Iteracio 25 : iout = 0, q = 16, B(p) = 3, theta* = 13.76, z = -972.083
   Iteracio 26 : iout = 0, q = 14, B(p) = 6, theta* = 0.95, z = -973.099
29
   Iteracio 27 : iout = 0, q = 17, B(p) = 14, theta* = 92.04, z = -1004.973
30
   Iteracio 28 : iout = 0, q = 3, B(p) = 16, theta* = 0.41, z = -1005.841
31
   Iteracio 29 : iout = 0, q = 18, B(p) = 13, theta* = 81.05, z = -1051.551
   Iteracio 30 : iout = 0, q = 6, B(p) = 1, theta* = 0.58, z = -1052.621
   Iteracio 31 : iout = 0, q = 16, B(p) = 6, theta* = 107.21, z = -1137.769
34
   Iteracio 32 : iout = 0, q = 9, B(p) = 3, theta* = 0.55, z = -1157.876
35
   Iteracio 33 : iout = 0, q = 11, B(p) = 9, theta* = 0.17, z = -1199.424
   Iteracio 34 : iout = 0, q = 20, B(p) = 11, theta* = 57.35, z = -1219.737
37
   Iteracio 35 : iout = 0, q = 6, B(p) = 2, theta* = 0.36, z = -1223.348
38
   Iteracio 36 : iout = 0, q = 21, B(p) = 6, theta* = 25.95, z = -1270.318
   Iteracio 37 : iout = 0, q = 3, B(p) = 5, theta* = 0.64, z = -1321.966
   Iteracio 38 : iout = 0, q = 13, B(p) = 15, theta* = 3.45, z = -1331.711
41
   Iteracio 39 : iout = 0, q = 19, B(p) = 3, theta* = 36.67, z = -1400.692
42
   Iteracio 40 : iout = 0, q = 14, B(p) = 7, theta* = 2.69, z = -1431.162
43
   Iteracio 41 : iout = 0, q = 15, B(p) = 13, theta* = 385.52, z = -1499.816
   Iteracio 42 : iout = 0, q = 11, B(p) = 15, theta* = 4.78, z = -1884.048
45
   Iteracio 43 : iout = 0, q = 22, B(p) = 14, theta* = 30.45, z = -1986.052
46
   Iteracio 44 : iout = 0, q = 10, B(p) = 11, theta* = 3.03, z = -2095.509
47
   Iteracio 45 : iout = 0, q = 9, B(p) = 10, theta* = 2.15, z = -2318.861
   Iteracio 46: iout = 0, q = 3, B(p) = 9, theta* = 2.21, z = -2426.874
49
   Iteracio 47 : iout = 0, q = 15, B(p) = 3, theta* = 228.43, z = -2483.484
   Iteracio 48 : iout = 0, q = 23, B(p) = 15, theta* = 1288.14, z = -5849.825
   Iteracio 49 : iout = 0, q = 1, B(p) = 4, theta* = 2.16, z = -8300.591
   Iteracio 50 : iout = 0, q = 24, B(p) = 1, theta* = 333.20, z = -12280.000
  Problema il limitat
  Fi del simplex primal
```

# 3.5 Conjunt de Dades 55, Problema 1

```
<sub>1</sub> Fase I
  Iteracio 1: iout = 0, q = 1, B(p) = 27, theta* = 0.01, z = 2409.100
  Iteracio 2: iout = 0, q = 2, B(p) = 1, theta* = 0.01, z = 2409.043
   Iteracio 3: iout = 0, q = 3, B(p) = 21, theta* = 0.59, z = 2123.705
   Iteracio 4 : iout = 0, q = 27, B(p) = 2, theta* = 28.63, z = 2113.579
   Iteracio 5 : iout = 0, q = 1, B(p) = 27, theta* = 0.26, z = 2098.569
   Iteracio \ 6 \ : \ iout = 0 \, , \ q = 4 \, , \ B(p) \, = \, 23 \, , \ theta* = \, 0.50 \, , \ z \, = \, 1817.551
   Iteracio 7: iout = 0, q = 2, B(p) = 28, theta* = 0.75, z = 1660.427
   Iteracio 8 : iout = 0, q = 21, B(p) = 3, theta* = 48.81, z = 1605.401
  Iteracio 9: iout = 0, q = 5, B(p) = 26, theta* = 0.08, z = 1557.199
   Iteracio 10 : iout = 0, q = 27, B(p) = 30, theta* = 51.82, z = 1463.435
11
   Iteracio 11 : iout = 0, q = 3, B(p) = 21, theta* = 0.86, z = 1336.936
12
   Iteracio 12 : iout = 0, q = 23, B(p) = 27, theta* = 0.85, z = 1335.791
   Iteracio 13 : iout = 0, q = 21, B(p) = 29, theta* = 67.67, z = 1324.836
14
   Iteracio 14 : iout = 0, q = 6, B(p) = 21, theta* = 0.80, z = 1066.636
15
   Iteracio 15 : iout = 0, q = 28, B(p) = 3, theta* = 77.50, z = 1044.937
   Iteracio 16 : iout = 0, q = 27, B(p) = 28, theta* = 55.17, z = 961.853
   Iteracio 17: iout = 0, q = 8, B(p) = 1, theta* = 0.36, z = 883.790
18
   Iteracio 18 : iout = 0, q = 29, B(p) = 24, theta* = 62.79, z = 842.338
19
   Iteracio 19 : iout = 0, q = 28, B(p) = 29, theta* = 17.83, z = 804.780
   Iteracio 20 : iout = 0, q = 7, B(p) = 28, theta* = 0.26, z = 1
                                                                   780.978
   Iteracio 21 : iout = 0, q = 1, B(p) = 23, theta* = 0.14, z = 779.182
22
   Iteracio 22 : iout = 0, q = 10, B(p) = 7, theta* = 0.95, z = 538.379
23
  Iteracio 23 : iout = 0, q = 26, B(p) = 27, theta* = 89.65, z = 404.642
  Iteracio 24 : iout = 0, q = 3, B(p) = 2, theta* = 1.26, z = 355.871
   Iteracio 25 : iout = 0, q = 9, B(p) = 25, theta* = 0.25, z = 316.855
26
   Iteracio\ 26\ :\ iout\ =\ 0\,,\ q\ =\ 2\,,\ B(p)\ =\ 3\,,\ theta*\ =\ 0.34\,,\ z\ =\ 249.441
27
   Iteracio 27 : iout = 0, q = 24, B(p) = 8, theta* = 51.34, z = 246.415
   Iteracio 28 : iout = 0, q = 28, B(p) = 26, theta* = 11.60, z = 244.819
29
   Iteracio 29 : iout = 0, q = 11, B(p) = 28, theta* = 0.20, z = 196.924
30
   Iteracio 30 : iout = 0, q = 8, B(p) = 24, theta* = 0.09, z = 120.565
31
   Iteracio 31 : iout = 0, q = 3, B(p) = 6, theta* = 3.00, z =
                                                                    30.690
32
   Iteracio 32 : iout = 0, q = 29, B(p) = 22, theta* = 29.73, z =
   Iteracio 33 : iout = 0, q = 7, B(p) = 29, theta* = 0.17, z =
34
  SBF trobada
35
  Fase II
   Iteracio 34 : iout = 0, q = 17, B(p) = 4, theta* = 207.07, z = -706.532
37
   Iteracio 35 : iout = 0, q = 6, B(p) = 8, theta* = 0.44, z = -734.419
38
   Iteracio 36 : iout = 0, q = 12, B(p) = 7, theta* = 0.05, z = -786.620
   Iteracio 37 : iout = 0, q = 13, B(p) = 6, theta* = 0.08, z = -801.905
   Iteracio 38 : iout = 0, q = 18, B(p) = 13, theta* = 79.55, z = -860.028
41
   Iteracio 39 : iout = 0, q = 7, B(p) = 2, theta* = 0.07, z = -938.105
42
   Iteracio 40 : iout = 0, q = 14, B(p) = 5, theta* = 0.42, z = -948.471
43
   Solucio optima trobada, iteracio 40, z = -948.471
   Fi del simplex primal
45
   Solucio optima:
46
   base =
47
       11
             12
                   17
                          10
                                      14
                                             18
                                                    7
48
49
       1.4594
                 0.8636
                          664.3604
                                      5.3055
                                                 1.2950
                                                           0.4248
                                                                    272.7265
                                                                                 0.1501
50
               0.6442
                         4.2500
51
  z =
    -948.4705
52
  r =
53
     186.2178
                91.7305
                          202.0726
                                     39.5675
                                                 1.0149
                                                           0.9102
                                                                     37.7126
                                                                              158.6999
            0.7030
                       0.8416
```

# 3.6 Conjunt de Dades 55, Problema 2

```
<sub>1</sub> Fase I
  Iteracio 1: iout = 0, q = 1, B(p) = 26, theta* = 1.05, z = 2574.073
  Iteracio 2: iout = 0, q = 2, B(p) = 27, theta* = 0.63, z = 2415.526
   Iteracio 3: iout = 0, q = 3, B(p) = 24, theta* = 1.17, z = 2131.182
   Iteracio 4: iout = 0, q = 26, B(p) = 2, theta* = 5.10, z = 2114.472
   Iteracio 5 : iout = 0, q = 5, B(p) = 26, theta* = 0.05, z = 2088.310
   Iteracio 6 : iout = 0, q = 6, B(p) = 3, theta* = 1.39, z = 2014.752
   Iteracio 7: iout = 0, q = 8, B(p) = 29, theta* = 0.94, z = 1730.709
   Iteracio 8: iout = 0, q = 4, B(p) = 1, theta* = 0.56, z = 1679.654
   Iteracio 9: iout = 0, q = 9, B(p) = 30, theta* = 0.35, z = 1494.690
   Iteracio 10 : iout = 0, q = 24, B(p) = 22, theta* = 92.69, z = 1423.607
11
   Iteracio 11 : iout = 0, q = 2, B(p) = 6, theta* = 0.29, z = 1417.196
   Iteracio 12 : iout = 0, q = 1, B(p) = 4, theta* = 2.48, z = 1187.821
   Iteracio 13 : iout = 0, q = 22, B(p) = 24, theta* = 17.59, z = 1186.351
14
   Iteracio 14 : iout = 0, q = 26, B(p) = 22, theta* = 24.21, z = 1163.647
15
   Iteracio 15 : iout = 0, q = 3, B(p) = 26, theta* = 0.06, z = 1147.999
   Iteracio 16 : iout = 0, q = 4, B(p) = 1, theta* = 2.43, z = 1042.071
   Iteracio 17 : iout = 0, q = 10, B(p) = 25, theta* = 0.69, z = 771.889
18
   Iteracio 18 : iout = 0, q = 6, B(p) = 21, theta* = 2.76, z = 450.366
19
   Iteracio 19 : iout = 0, q = 7, B(p) = 3, theta* = 0.89, z = 410.067
   Iteracio 20 : iout = 0, q = 30, B(p) = 6, theta* = 184.85, z = 379.424
   Iteracio 21 : iout = 0, q = 12, B(p) = 9, theta* = 0.29, z =
22
   Iteracio 22 : iout = 0, q = 6, B(p) = 30, theta* = 1.83, z =
                                                                   357.670
23
  Iteracio 23 : iout = 0, q = 11, B(p) = 2, theta* = 1.46, z =
                                                                   355.303
  Iteracio 24 : iout = 0, q = 1, B(p) = 5, theta* = 1.12, z = 354.819
   Iteracio 25 : iout = 0, q = 13, B(p) = 28, theta* = 1.49, z =
26
   Iteracio 26 : iout = 0, q = 21, B(p) = 4, theta* = 53.99, z = 100
                                                                     91.011
27
   Iteracio 27 : iout = 0, q = 5, B(p) = 23, theta* = 0.33, z = 0.33
                                                                    80.428
   Iteracio 28 : iout = 0, q = 29, B(p) = 5, theta* = 48.72, z =
                                                                     65.034
29
   Iteracio 29 : iout = 0, q = 4, B(p) = 21, theta* = 0.06, z =
                                                                    63.020
30
   Iteracio 30 : iout = 0, q = 2, B(p) = 4, theta* = 0.04, z = 0
                                                                   58.119
31
   Iteracio 31 : iout = 0, q = 5, B(p) = 29, theta* = 1.62, z =
                                                                    -0.000
  SBF trobada
  Fase II
34
   Iteracio 32 : iout = 0, q = 9, B(p) = 12, theta* = 0.22, z = -239.451
35
   Iteracio 33 : iout = 0, q = 14, B(p) = 7, theta* = 0.35, z = -387.711
   Iteracio 34 : iout = 0, q = 16, B(p) = 5, theta* = 251.47, z = -467.494
37
   Iteracio 35 : iout = 0, q = 17, B(p) = 11, theta* = 12.57, z = -470.727
38
   Iteracio 36 : iout = 0, q = 18, B(p) = 17, theta* = 20.85, z = -470.910
   Iteracio 37 : iout = 0, q = 20, B(p) = 2, theta* = 126.52, z = -566.223
   Iteracio 38 : iout = 0, q = 3, B(p) = 14, theta* = 1.80, z = -603.666
41
   Iteracio 39 : iout = 0, q = 11, B(p) = 3, theta* = 1.12, z = -607.769
42
   Iteracio 40 : iout = 0, q = 17, B(p) = 11, theta* = 169.92, z = -714.766
43
   Iteracio 41 : iout = 0, q = 19, B(p) = 1, theta* = 86.13, z = -722.621
   Iteracio 42 : iout = 0, q = 2, B(p) = 13, theta* = 0.14, z = -723.939
45
   Solucio optima trobada, iteracio 42, z = -723.939
   Fi del simplex primal
47
   Solucio optima:
48
   base =
49
       6
             17
                   16
                         18
                                10
                                      20
                                            19
50
  xb =
51
       2.4038
              261.1016
                         668.3034
                                    363.2464
                                                3.4425
                                                        434.6705
                                                                   124.5015
                                                                               0.1403
52
              4.8161
                         2.9391
  z =
53
    -723.9394
55
     160.2853
                62.3552
                         133.3848
                                    113.6042
                                                0.5313
                                                        132.1589
                                                                              68.6913
                                                                    46.1953
56
                      3.1909
           22.5421
```

# 3.7 Conjunt de Dades 55, Problema 3

```
<sub>1</sub> Fase I
  Iteracio 1 : iout = 0, q = 1, B(p) = 24, theta* = 0.04, z = 1661.266
  Iteracio 2 : iout = 0, q = 2, B(p) = 28, theta* = 0.50, z = 1332.404
  Iteracio 3: iout = 0, q = 4, B(p) = 2, theta* = 0.71, z = 1298.859
  Iteracio 4: iout = 0, q = 6, B(p) = 30, theta* = 0.75, z = 1271.574
  Iteracio 5 : iout = 0, q = 2, B(p) = 4, theta* = 0.03, z = 1269.297 Iteracio 6 : iout = 0, q = 8, B(p) = 2, theta* = 0.04, z = 1266.636
  Iteracio 7 : iout = 0, q = 10, B(p) = 8, theta* = 0.18, z = 1218.917
  Iteracio 8 : iout = 0, q = 24, B(p) = 6, theta* = 15.30, z = 1045.202
  Iteracio 9 : iout = 0, q = 11, B(p) = 24, theta* = 0.25, z = 1031.280
  Iteracio 10 : iout = 0, q = 14, B(p) = 10, theta* = 0.55, z = 994.290
  Iteracio 11 : iout = 0, q = 24, B(p) = 29, theta* = 7.93, z = 992.138
  Iteracio 12 : iout = 0, q = 17, B(p) = 27, theta* = 266.14, z = 725.995
  Iteracio 13 : iout = 0, q = 19, B(p) = 24, theta* = 6.24, z = 722.782
  Iteracio 14 : iout = 0, q = 10, B(p) = 14, theta* = 0.64, z = 718.586
  Iteracio 15 : iout = 0, q = 20, B(p) = 11, theta* = 10.43, z = 716.784
  Problema Infactible
```

# 3.8 Conjunt de Dades 55, Problema 4

```
<sub>1</sub> Fase I
   Iteracio 1: iout = 0, q = 1, B(p) = 32, theta* = 7.60, z = 2876.534
   Iteracio 2: iout = 0, q = 2, B(p) = 25, theta* = 2.02, z = 2126.702
   Iteracio 3: iout = 0, q = 32, B(p) = 34, theta* = 61.43, z = 2021.746
   Iteracio 4: iout = 0, q = 3, B(p) = 31, theta* = 2.26, z = 1306.742
   Iteracio\ 5\ :\ iout\ =\ 0\,,\ q\ =\ 25\,,\ B(p)\ =\ 30\,,\ theta*\ =\ 82.09\,,\ z\ =\ 1099.575
   Iteracio \ 6 \ : \ iout = 0 \, , \ q = 4 \, , \ B(p) \, = \, 25 \, , \ theta* = \, 0.72 \, , \ z \, = \, \, 978.465
   Iteracio \ 7 \ : \ iout \ = \ 0 \, , \ q \ = \ 5 \, , \ B(p) \ = \ 27 \, , \ theta* \ = \ 0.49 \, , \ z \ = \ 950.904
   Iteracio 8: iout = 0, q = 6, B(p) = 5, theta* = 0.88, z = 907.089
   Iteracio 9: iout = 0, q = 7, B(p) = 32, theta* = 0.83, z = 785.779
   Iteracio 10 : iout = 0, q = 25, B(p) = 3, theta* = 1.93, z =
11
   Iteracio 11 : iout = 0, q = 8, B(p) = 33, theta* = 0.17, z =
                                                                     742.821
12
   Iteracio 12 : iout = 0, q = 3, B(p) = 29, theta* = 2.99, z =
                                                                      324.492
   Iteracio 13 : iout = 0, q = 30, B(p) = 28, theta* = 8.11, z = 6
14
   Iteracio 14 : iout = 0, q = 5, B(p) = 30, theta* = 0.10, z = 0
15
   Iteracio 15 : iout = 0, q = 9, B(p) = 25, theta* = 0.64, z = 0.64
                                                                      280.046
   Iteracio 16 : iout = 0, q = 29, B(p) = 2, theta* = 13.77, z = 264.299
   Iteracio 17 : iout = 0, q = 10, B(p) = 7, theta* = 2.69, z = 10
18
   Iteracio 18 : iout = 0, q = 11, B(p) = 6, theta* = 0.58, z =
19
   Iteracio 19 : iout = 0, q = 34, B(p) = 3, theta* = 8.66, z =
                                                                      203.713
   Iteracio 20 : iout = 0, q = 2, B(p) = 26, theta* = 2.15, z =
                                                                      146.309
   Iteracio 21 : iout = 0, q = 3, B(p) = 29, theta* = 0.35, z = 0
22
   Iteracio 22 : iout = 0, q = 7, B(p) = 1, theta* = 0.24, z = 137.863
23
   Iteracio\ 23\ :\ iout\ =\ 0\,,\ q\ =\ 29\,,\ B(\,p\,)\ =\ 3\,,\ theta\,*\ =\ 10.09\,,\ z\ =\ 129.900
   Iteracio 24 : iout = 0, q = 26, B(p) = 34, theta* = 81.75, z = 111.638
   Iteracio 25 : iout = 0, q = 12, B(p) = 26, theta* = 1.16, z = 102.492
26
                                                                        72.927
   Iteracio 26 : iout = 0, q = 13, B(p) = 10, theta* = 0.37, z = 10
27
   Iteracio 27 : iout = 0, q = 1, B(p) = 4, theta* = 1.50, z = 1.50
                                                                      56.002
   Iteracio 28 : iout = 0, q = 14, B(p) = 29, theta* = 0.33, z =
29
  SBF trobada
30
   Fase II
31
   Iteracio 29 : iout = 0, q = 4, B(p) = 1, theta* = 0.99, z = -860.810
   Iteracio 30 : iout = 0, q = 6, B(p) = 8, theta* = 1.07, z = -909.091
   Iteracio 31 : iout = 0, q = 10, B(p) = 2, theta* = 0.68, z = -947.619
   Iteracio 32: iout = 0, q = 8, B(p) = 13, theta* = 2.23, z = -1012.738
35
   Iteracio\ 33\ :\ iout\ =\ 0\,,\ q\ =\ 16\,,\ B(p)\ =\ 5\,,\ theta*\ =\ 10.24\,,\ z\ =\ -1016.715
   Iteracio 34 : iout = 0, q = 17, B(p) = 11, theta* = 91.63, z = -1130.057
37
   Iteracio 35 : iout = 0, q = 2, B(p) = 7, theta* = 0.01, z = -1130.552
38
   Iteracio 36 : iout = 0, q = 5, B(p) = 10, theta* = 5.69, z = -1226.938
   Iteracio 37 : iout = 0, q = 18, B(p) = 12, theta* = 76.13, z = -1308.886
   Iteracio 38 : iout = 0, q = 13, B(p) = 4, theta* = 0.75, z = -1386.325
41
   Iteracio 39 : iout = 0, q = 3, B(p) = 2, theta* = 1.19, z = -1397.078
42
   Iteracio 40 : iout = 0, q = 15, B(p) = 3, theta* = 66.45, z = -1420.619
43
   Iteracio 41 : iout = 0, q = 20, B(p) = 8, theta* = 217.25, z = -1580.025
   Iteracio\ 42\ :\ iout\ =\ 0\,,\ q\ =\ 3\,,\ B(p)\ =\ 14\,,\ theta*\ =\ 1.10\,,\ z\ =\ -1632.906
45
   Iteracio 43 : iout = 0, q = 2, B(p) = 9, theta* = 0.54, z = -1647.407
46
   Iteracio 44 : iout = 0, q = 10, B(p) = 2, theta* = 1.95, z = -1758.327
47
   Iteracio 45 : iout = 0, q = 4, B(p) = 13, theta* = 0.10, z = -1770.525
   Iteracio 46 : iout = 0, q = 14, B(p) = 15, theta* = 0.01, z = -1771.060
49
   Iteracio 47 : iout = 0, q = 11, B(p) = 14, theta* = 0.02, z = -1771.308
   Iteracio 48 : iout = 0, q = 9, B(p) = 3, theta* = 0.11, z = -1772.254
   Iteracio 49 : iout = 0, q = 21, B(p) = 4, theta* = 1.33, z = -1772.814
   Iteracio 50 : iout = 0, q = 3, B(p) = 9, theta* = 0.68, z = -1777.831
53
   Iteracio 51 : iout = 0, q = 15, B(p) = 11, theta* = 5.80, z = -1779.692
   Iteracio 52 : iout = 0, q = 22, B(p) = 10, theta* = 13.72, z = -1794.277
   Iteracio 53 : iout = 0, q = 11, B(p) = 3, theta* = 2.17, z = -1968.131
   Iteracio\ 54\ :\ iout\ =\ 0\,,\ q\ =\ 23\,,\ B(p)\ =\ 11\,,\ theta*\ =\ 63.18\,,\ z\ =\ -2023.092
   Iteracio 55 : iout = 0, q = 19, B(p) = 22, theta* = 974.96, z = -2193.896
```

```
Iteracio 56 : iout = 0, q = 8, B(p) = 15, theta* = 1.50, z = -2254.441 Iteracio 57 : iout = 0, q = 4, B(p) = 5, theta* = 1.62, z = -2463.949 Iteracio 58 : iout = 0, q = 24, B(p) = 4, theta* = 212.78, z = -3193.214 Iteracio 59 : iout = 0, q = 14, B(p) = 8, theta* = 3.53, z = -3195.737 Iteracio 60 : iout = 0, q = 22, B(p) = 23, theta* = 8899.62, z = -8348.149 Iteracio 61 : iout = 0, q = 8, B(p) = 6, theta* = 9.95, z = -8522.101 Iteracio 62 : iout = 0, q = 15, B(p) = 8, theta* = 4019.00, z = -64042.000 Problema illimitat
```