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# Assignment-1

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#### PROBLEM 1.7

It is known that 10% of certain articles manufactured are defective. What is the probability that in a random sample of 12 such articles, 9 are defective?

### **SOLUTION 1.7**

The repeated selections of articles in a random sample space are Bernoulli trials. Let X denote the number of times of selecting defective articles in a random sample space of 12 articles.

Clearly X, has a binomial distribution with n=12 and p=10%= $\frac{1}{10}$ =0.1 and q=1-p=1- $\frac{1}{10}$ = $\frac{9}{10}$ 

$$\therefore X = B(n, p)$$

The probability mass function(p.m.f) for a general binomial distribution is given by

$$\Pr(X = k) = \binom{n}{k} \times p^k \times q^{n-k}$$

In this case n=12 , p= $\frac{1}{10}$  and q= $\frac{9}{10}$ , So

$$\Pr(k) = \binom{12}{k} \times (\frac{1}{10})^k \times (\frac{9}{10})^{12-k}$$

where Pr(k) is the probability of getting x number of defective articles and  $k \in \{0, 1, 2, \dots, 12\}$ 

In this case we want Pr(9)

$$Pr(9) = {12 \choose 9} \times (\frac{1}{10})^9 \times (\frac{9}{10})^3$$
$$= \frac{12!}{9!3!} \times \frac{1}{10^9} \times \frac{9^3}{10^3}$$
$$= \frac{12 \times 11 \times 10}{3 \times 2 \times 1} \times \frac{729}{10^{12}}$$
$$= \frac{16038}{10^{11}}$$

So, the probability of there being 9 defective articles in a random sample space of 12 articles is  $Pr(9) = 1.6038 \times 10^{-7}$ 

#### PYTHON CODE

Since the probability of producing 9 defective articles is very very low we need to run a large simulation. But a large simulation takes a large amount of time which is inefficient so we need to strike a balance between time and the precision to the original value. So a simulation of  $4\times10^8$  would likely yield a better results in a better time The codes can be downloaded from

Vasishtadepu/AI5002/tree/main/Assignment1/Codes