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T'S Stationarity- Code Explanation

```
Jupyter TimeSeries-Stationarity Last Checkpoint: a few seconds ago (autosaved)
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                                                                                                                                                       Python 3 (ipykernel) O
A + S
A ← A ← B
B ← A ← B
B ← B
C → Code
                                                                         $
                         # Augmented Dickey-Fuller (ADF) Test - To determine the stationarity of a TS
                         # Function to print out results in customised manner
                         # Importing adfuller function from the module named statsmodels.tsa.stattools
                      6 from statsmodels.tsa.stattools import adfuller
                      9 # Defining the function named adf_test with 3 parameters
                     10 def adf_test(timeseries,df,pollutant):
                     11
                              # Setting up Plotting Environment
                    14
15
                              plt.figure(figsize=(16,5))
                     16
                    17
18
                              from statsmodels.tsa.stattools import adfuller
                              print ('Results of Dickey-Fuller Test:')
                     19
                    20
21
                              # Performing ADF test on timeseries data with AIC (Akaike Information Criterion)
                     22
                               # used for automatic lag selection
                    23
24
25
26
27
28
                              dftest = adfuller(timeseries, autolag='AIC')
                              29
30
                              # For looping for extracting & displaying critical values from the ADF test
for key,value in dftest[4].items():
    dfoutput['Critical Value (%s)'%key] = value
                     31
                    32
                              print (dfoutput)
                    34
35
36
37
                              ans=dfoutput
                              print("Condition:")
print("p-value<=0.05-->Accept Alternate Hypothesis")
print("p-value>0.05-->Accept Null Hypothesis")
                    38
39
                              # Creating conditions to check for stationarity & non-stationarity & printing the o/p
if(ans['Test Statistic']<ans["Critical Value (1%)"] or ans['Test Statistic']<ans["Critical Value (5%)"] or a
print("Condition: statictic < any critical value and p-value <0.05 to reject null hypothesis")
print("Reject null hypothesis:Non Stationarity")
                     41
42
                     43
                                   print("Accept Alternate hypothesis:Staionarity ")
message="Stationarity based on ADH"
                     44
                     45
                                   print("Condition: statictic < any critical value and p-value <0.05 to reject null hypothsis")
print("Accept null hypothesis:Non Stationarity" )
print("Reject Alternate hypothesis:Staionarity ")</pre>
                     47
                     48
                     49
                     50
51
                                    message="Non-stationarity based on ADH"
                     53
54
55
                              # Plotting time series data using the matplotlib library customized with title legend
                              # & saving the plot as PNG file
                     56
57
                               plt.plot(df.index, df[pollutant], label = pollutant)
                              plt.legend(loc='best')
plt.title("{}_{}_2013 to 2021".format(message,pollutant))
plt.savefig("{}_ADH.png".format(pollutant))
                    59
60
                               plt.show()
                     61
                     62
                     63
                              # Returns the message whether the TS is stationarity or not based on ADF test
                              return message
                     65
```

Approximate Entropy (ApEn)

Approximate Entropy (ApEn) is a metric used to quantify the amount of regularity or predictability within a time series. It was introduced by Pincus in 1991 as a way to assess the complexity of physiological time series data. The ApEn algorithm is particularly useful in the analysis of data where the underlying dynamics may be complex and unpredictable.

Here's a more detailed explanation of how Approximate Entropy works:

1. Sequence Generation:

- Given a time series data set $U=\{u_1, u_2,...,u_N\}$, the first step is to create overlapping sequences of a specified length m.
- For each index i from 1 to N-m+1, a subsequence x_i is formed as $\{u_i, u_{i+1}, ..., u_{i+m-1}\}$.

2. Distance Calculation:

- Define a distance metric between two sequences x_i and x_j . In the code, the _maxdist function calculates the maximum absolute difference between corresponding elements of two sequences.
- The distance between x_i and x_j is considered significant if it is less than or equal to a specified threshold r.

3. Similarity Count:

- For each subsequence x_i , count the number of other subsequences x_j that are similar to x_i within the threshold r.
- The variable C is a list storing these counts.

4. Probability Calculation:

- Calculate the probability that two similar sequences x_i and x_j remain similar in the next incremental comparisons.
- This is done by dividing the count of similar sequences (C) by the total number of sequences (N-m+1).

5. Entropy Calculation:

- For each subsequence x_i, compute the natural logarithm of the probability and take the average over all subsequences.
- This is done in the _phi function.

6. Final ApEn Calculation:

- Compute the ApEn value as the absolute difference between the average logarithmic probabilities for subsequences of lengths m+1 and m.
- The larger the ApEn, the less predictable or more complex the time series is considered to be.

In summary, ApEn provides a measure of irregularity or complexity in a time series by examining the likelihood that similar patterns persist as the length of the patterns increases. A higher ApEn suggests greater complexity or unpredictability in the time series data. It has applications in various fields, including the analysis of physiological signals, financial time series, and other systems with dynamic and complex behaviour.

Apen - Approximate Entropy Code Explanation

Sample Entropy (SampEn)

Sample Entropy is another complexity measure used in time series analysis, similar to Approximate Entropy (ApEn). Sample Entropy is designed to overcome some limitations of ApEn, particularly its sensitivity to the length of the time series. Here's a step-by-step explanation of how Sample Entropy works:

1. Sequence Generation:

- Given a time series data set $U=\{u_1, u_2,...,u_N\}$, the first step is to create non overlapping sequences of a specified length m.
- For each index i from 1 to N-m+1, a subsequence x_i is formed as $\{u_i, u_{i+1}, \dots, u_{i+m-1}\}$.

2. Distance Calculation:

• Define a distance metric between two sequences x_i and x_j . In the context of Sample Entropy, the distance is the maximum absolute difference between corresponding elements of two sequences.

3. Pattern Matching:

- Count the number of similar sequences x_i to a reference sequence x_i within a specified threshold r.
- This is similar to the process in ApEn, but Sample Entropy considers nonoverlapping sequences.

4. Self-Matching Exclusion:

• Exclude the self-matching cases (when i=j) from the count.

5. Probability Calculation:

- Calculate the probability that two sequences are similar within the threshold r for a given length m.
- Divide the count of similar sequences by the total number of non-self-matching pairs.

6. Entropy Calculation:

- Compute the natural logarithm of the probability for each length m.
- Take the average of these logarithmic probabilities.

7. Final Sample Entropy Calculation:

• Sample Entropy (SampEn) is defined as the negative natural logarithm of the average probability: SampEn(U, m, r)=-ln(count(m)/count(m+1))

• This formula measures the likelihood that patterns of length m remain similar when the length is increased to m+1. A lower Sample Entropy value indicates a more regular or predictable time series.

In summary, Sample Entropy quantifies the regularity or predictability of a time series by comparing non-overlapping subsequences. It provides a complexity measure that is less sensitive to the length of the time series compared to ApEn. Lower Sample Entropy values suggest a more regular or ordered time series, while higher values indicate greater complexity or irregularity.

SampEN- Sample Entropy Code Explanation

```
spen - Sample Entropy Code Explanation
      Code: def SampEn(U, m, r):
"""Compute Sample entropy"""
  Explanation: The function SampEN takes 3 parameters namely U(TS data), m(length of comparable sequence) & r (threshold which defines how similar the 2 sequences must be to be considered as a match )
  1 Code: def _{maxdist(x_i, x_j)}:
                    return max([abs(ua - va) for ua, va in zip(x i, x i)])
  Explanation: \_maxdist is a helper function which is used to calculate the maximum absolute difference between the elements of 2 subsequences x\_i & x\_j.
      Code: def _phi(m):
                   X = [\underbrace{IU[j] \text{ for } j \text{ in } range(i, i + m - 1 + 1)}_{l} \text{ for } i \text{ in } range(N - m + 1)]
C = [\underbrace{len([1 \text{ for } j \text{ in } range(len(x)) \text{ } if \text{ } i \text{ } != \text{ } j \text{ } and \text{ } maxdist(x[i], x[j]) \text{ } <= \text{ } r]}_{l}) \text{ } for \text{ } i \text{ } i \text{ } range(len(x))]
                    return sum(C)
  6 Explanation: _phi is a helper function which is used to create a non-overlapping sub-sequence of length m for
      the given input series data (U). For each subsequence it counts the number similar sequence within the distance r, excluding self matching cases. The result calculates the sum of these counts.
  8
  1 Code: N = len(U)
             return -np.log(_phi(m+1) / _phi(m))
  Explanation: The main function calculates the Sample Entropy value by setting N as the length of the input series U & it is computed using the formula —log(_phi(m+1) / _phi(m)). This formula measures the likelihood that a pattern of length m to be in similar when the length is increased to m+1. The negative natural log is
       taken to obtain a positive value. Lower the Sample entropy value higher the regularity or forecastability of
       the TS data.
       Code Summary : The code calculates the SampEn value of the given time series data by measuring regularity or
       forecastability of the TS data. This is achieved by comparing the non- overlapping subsequences of specified length & counting the number of similar sequences within a given threshold distance & applying logrithamic transformation to measure the likelihood of pattern similarity accross different lengths.
```

TS- Model- VAR Function Code Execution

```
Assignment: Line by Line Code Execution of Below Function
         def cominbation(dataset, listt):
    print(data1)
    datasetTwo=dataset[listt]
    print(datasetTwo]
    test_obs = 28
    train =datasetTwo[-test_obs]
    print(train)
    test = datasetTwo[-test_obs:]
    print(frest)
test = data
print(test)
                   from statsmodels.tsa.api import VAR
for i in [1,2,3,4,5,6,7,8,9,10]:
    model = VAR(train)
    print(model)
    results = model.fit(i)
    print('order =', i)
    print('ATC: ', results.aic)
    print('ATC: ', results.bic)
    print('BTC: ', results.bic)
    print()
    x = model.select_order(maxlags=12)
    print(X)
    order=x.selectd_orders["aic"]
    print(order)
    result = model.fit(order)
    print(resul)
                     #result.summary()
lagged_Values = train.values[-order:]
print(lagged_Values)
pred = result.forecast(y=lagged_Values, steps=28)
                      pred = resu
print(pred)
                      preds=pd.DataFrame(pred,columns=listt)
                     print(preds)
preds.to_csv("varforecasted_{{}.csv".format(test_obs))
                    from sklearn.metrics import mean_squared_error
rmse= round(mean_squared_error(test,pred,squared=False))
print(rmse)
from sklearn.metrics import mean_absolute_percentage_error
mape=mean_absolute_percentage_error(test,pred)
print(mape)
                     performance["Model"].append(listt)
performance["RMSE"].append(rmse)
performance["MaPe"].append(mape)
performance["Lag"].append(order)
performance["Test"].append(test_obs)
                     perf=pd.DataFrame(performance)
In [14]: 1 print(data1)
2 print(listt)

        Open
0.51723
        High
0.52721
        Low
0.52221
        Close
0.52221

        0.59652
        0.491400
        0.530959
        0.519394

        0.494843
        0.472236
        0.532876
        0.517972

        0.506785
        0.472233
        0.532251
        0.520225

        0.507411
        0.479533
        0.527149
        0.513788

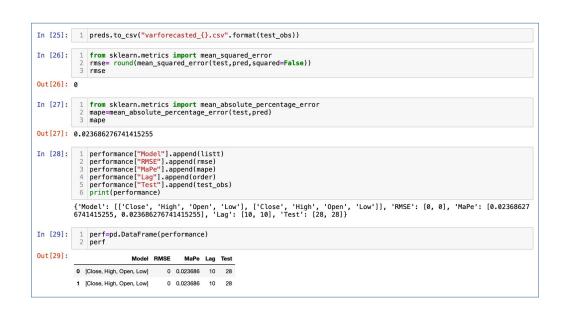
                     2139 0.877349 0.819410 0.900409 0.880633
2140 0.856733 0.887862 0.885130 0.87642
2141 0.848643 0.799017 0.873670 0.865612
2142 0.864301 0.810565 0.89224 0.873972
2143 0.864301 0.821130 0.894952 0.885998
                      [2144 rows x 4 columns]
['Close', 'High', 'Open', 'Low']
In [15]: 1 datasetTwo=data1[listt]
2 datasetTwo
                                                                        Open
                                       Close
                                                        High
                          0 0.522210 0.485749 0.517223 0.529877
                             1 0.519394 0.491400 0.500522 0.530969
                       2 0.517972 0.472236 0.498434 0.528786
                              3 0.520225 0.472236 0.506785 0.532251
                        4 0.513788 0.479533 0.507411 0.527149
                       2139 0.880633 0.819410 0.877349 0.900409
                        2140 0.870440 0.807862 0.856733 0.885130
                       2141 0.865612 0.799017 0.848643 0.873670
                       2142 0.873927 0.810565 0.864301 0.892224
                       2143 0.885998 0.821130 0.864301 0.894952
                      2144 rows × 4 columns
```

```
In [16]: 1 test_obs = 28
2 train =datasetTwo[:-test_obs]
            3 train
           Close High Open Low
Out[16]:
          0 0.522210 0.485749 0.517223 0.529877
             1 0.519394 0.491400 0.500522 0.530969
           2 0.517972 0.472236 0.498434 0.528786
              3 0.520225 0.472236 0.506785 0.532251
           4 0.513788 0.479533 0.507411 0.527149
             ... ... ... ... ...
           2111 0.906384 0.840786 0.786013 0.807640
           2112 0.874195 0.833170 0.888570 0.892497
           2113 0.868830 0.814742 0.853862 0.884038
           2114 0.853541 0.789189 0.845772 0.872578
           2115 0.878487 0.812285 0.832463 0.875307
           2116 rows × 4 columns
In [17]: 1 test = datasetTwo[-test_obs:]
2 test
Out[17]:
                  Close High Open Low
           2116 0.883315 0.815725 0.858820 0.896589
           2117 0.903433 0.834889 0.863779 0.897408
           2118 0.887607 0.824570 0.882568 0.907503
           2119 0.882779 0.808354 0.848382 0.889768
           2120 0.878755 0.814496 0.863779 0.897681
           2121 0.891899 0.819902 0.863779 0.905593
           2122 0.904238 0.839803 0.874739 0.915962
           2123 0.906652 0.844472 0.889353 0.925784
           2124 0.907994 0.835381 0.886482 0.923056
           2125 0.916577 0.849140 0.878914 0.917053
           2126 0.923015 0.858968 0.899791 0.931514
           2127 0.903970 0.851597 0.902923 0.921692
           2128 0.903970 0.826044 0.879958 0.906958
           2129 0.913627 0.852580 0.887787 0.929877
           2130 0.912822 0.852580 0.878392 0.920600
           2131 0.850858 0.830958 0.879958 0.857844
           2132 0.871781 0.800000 0.825157 0.829468
           2133 0.878487 0.808845 0.837944 0.873943
           2134 0.874463 0.858968 0.863518 0.884038
           2135 0.895118 0.825061 0.866388 0.906958
           2136 0.887875 0.823096 0.877610 0.897954
           2137 0.917918 0.839066 0.869259 0.915962
           2138 0.895386 0.835872 0.893006 0.912688
           2139 0.880633 0.819410 0.877349 0.900409
           2140 0.870440 0.807862 0.856733 0.885130
           2141 0.865612 0.799017 0.848643 0.873670
           2142 0.873927 0.810565 0.864301 0.892224
           2143 0.885998 0.821130 0.864301 0.894952
```

```
from statsmodels.tsa.api import VAR
for i in [1,2,3,4,5,6,7,8,9,10]:
    model = VAR(train)
    print(model)
    results = model.fit(1)
    print(results)
    print('Order =', 1)
    print('AIC: ', results.aic)
    print('BIC: ', results.bic)
    print()
In [18]:
                  8
9
10
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12ea9bb90>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f4352d0>
Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12e126750>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f436890>
                 0rder = 1
                 AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12ee94650>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f435e10>
Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12e126750>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f436dd0>
Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12f403a90>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f437f90>
                 Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12e126750>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f437fd0>
                 Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12f403a90>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f436250>

                 Order = 1
                 AIC: -39.01658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12e126750>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f436290>
Order = 1
AIC: -39.91658695115506
BIC: -38.96309465714579
                 <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12f403a90>
<statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f436690>
Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
                  <statsmodels.tsa.vector_ar.var_model.VAR object at 0x12f422610>
                  <statsmodels.tsa.vector_ar.var_model.VARResultsWrapper object at 0x12f44c150>
                 Order = 1
AIC: -39.01658695115506
BIC: -38.96309465714579
Out[19]: <statsmodels.tsa.vector_ar.var_model.LagOrderResults at 0x12f437690>
Out[20]: 10
                   1 result = model.fit(order)
2 result
In [21]:
Out[21]: <statsmodels.tsa.vector_ar.var_model.VARResultsWrapper at 0x12f435d90>
```

```
1 lagged_Values
2 lagged_Values
  In [22]:
                                        lagged_Values = train.values[-order:]
 Out[22]: array([[0.77870172, 0.73267815, 0.78601252, 0.77653481], [0.80606218, 0.75257989, 0.7651357, 0.80763984], [0.83476393, 0.77100741, 0.80114819, 0.83683496], [0.82376606, 0.76633912, 0.81732776, 0.84065486], [0.81330471, 0.75184274, 0.8063674, 0.82592091], [0.90638414, 0.84078626, 0.78601252, 0.88763984], [0.8741953, 0.83316954, 0.8885699, 0.89249661], [0.86883049, 0.81474202, 0.85386221, 0.8840382], [0.85354076, 0.78918921, 0.84577243, 0.87257841], [0.87848708, 0.81228502, 0.83246343, 0.87530692]])
                                pred = result.forecast(y=lagged_Values,steps=28)
pred
  In [23]:
Out[23]: array([[0.87807691, 0.82598206, 0.86232426, 0.8845791], [0.87568858, 0.81755924, 0.858365, 0.87981049], [0.87537281, 0.81755924, 0.858365, 0.87981049], [0.87537281, 0.81807134, 0.85883094, 0.88566697], [0.87632064, 0.8164118, 0.85774628, 0.87913361], [0.87623064, 0.8164118, 0.85774628, 0.87913361], [0.87594138, 0.81723438, 0.8564004, 0.879980614], [0.87594138, 0.81723438, 0.8564004, 0.87980614], [0.8759415, 0.8170654, 0.85506662, 0.88170201], [0.8759416, 0.8170654, 0.85509098, 0.83122196], [0.87435608, 0.81651541, 0.8559047, 0.8793504], [0.874379514, 0.81499682, 0.85919774, 0.87861856], [0.87443972, 0.81548939, 0.8542209, 0.87883689], [0.87517773, 0.8158027, 0.85468608, 0.88068921], [0.8744366, 0.81564719, 0.8559376, 0.87991274], [0.8744431, 0.81546427, 0.8559376, 0.87991274], [0.87449472, 0.81574177, 0.8559376, 0.87991274], [0.87441914, 0.81554834, 0.8549128, 0.8799274], [0.87451894, 0.81574177, 0.85499225, 0.879387], [0.87451894, 0.81574177, 0.8549822, 0.8799371], [0.87451894, 0.81574177, 0.8549822, 0.8799371], [0.87452643, 0.81546109, 0.85473186, 0.87995341], [0.87425044, 0.81546109, 0.85473186, 0.87995341], [0.87425044, 0.81546109, 0.85479125, 0.87993451], [0.8742643, 0.81546109, 0.85479125, 0.87993541], [0.8742504, 0.81546109, 0.85479526, 0.879917138], [0.8742504, 0.81546109, 0.85479526, 0.879917138], [0.8742504, 0.81546109, 0.85479526, 0.87993545], [0.87430662, 0.81546076, 0.85479526, 0.87993785], [0.8744096, 0.81546076, 0.8549071, 0.87910593], [0.8744096, 0.81546076, 0.8549071, 0.87910593], [0.87444778, 0.8155836, 0.8549071, 0.8792031], [0.87444778, 0.8155836, 0.8549071, 0.8792031], [0.87444778, 0.8155836, 0.8549071, 0.8792031], [0.87444778, 0.8155836, 0.8549071, 0.8792031], [0.87444778, 0.8155836, 0.8549071, 0.8792031], [0.87444777, 0.8155836, 0.8549071, 0.8792031], [0.87444777, 0.8155836, 0.8549039, 0.87920609]])
  Out[24]:
                                              Close
                                                                   High Open
                                                                                                                Low
                                0 0.878077 0.825982 0.862324 0.884579
                                 1 0.875689 0.817559 0.858365 0.879810
                              2 0.879318 0.817036 0.856617 0.882667
                                 3 0.875373 0.818071 0.858831 0.885699
                               4 0.870123 0.815102 0.854199 0.873987
                                   5 0.876231 0.816412 0.857746 0.879134
                                6 0.875941 0.817234 0.856400 0.879806
                                  7 0.877380 0.817867 0.855667 0.881702
                              8 0.875020 0.817707 0.857010 0.881222
                                 9 0.874356 0.816515 0.855905 0.879350
                               10 0.873795 0.814997 0.854916 0.878619
                               11 0.874440 0.815489 0.854221 0.878837
                               12 0.875178 0.815803 0.854868 0.880089
                                13 0.875061 0.816239 0.855250 0.879909
                                14 0.874441 0.815464 0.855504 0.879211
                                15 0.874464 0.815647 0.854913 0.878921
                               16 0.874495 0.815719 0.854969 0.879193
                                17 0.874519 0.815742 0.854992 0.879387
                               18 0.874344 0.815528 0.854889 0.879171
                                19 0.874312 0.815441 0.854814 0.879054
                               20 0.874226 0.815461 0.854786 0.878993
                               21 0.874258 0.815401 0.854732 0.879087
                               22 0.874307 0.815407 0.854704 0.879125
                                23 0.874410 0.815454 0.854759 0.879172
                               24 0.874424 0.815543 0.854871 0.879169
                               25 0.874438 0.815579 0.854906 0.879200
                              26 0.874448 0.815577 0.854905 0.879235
                               27 0.874467 0.815588 0.854904 0.879261
```



Note: IPyNb of this code execution can be found in my Github - Assignments/TSA/TS-Models/VAR.

Ipython Notebooks of other TS Models like VARMA,

Assignments/TSA/TS-Models

SES, HWES can also be found in Github -

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