HW-2

vrohatgi

- Q-1: Four unique implementations of a function in R
- (a-c) Running all methods with varying input [3,3000] and testing with same seed value to check for same result
- (i) Using for loop & (ii) Using vectorized function sample()

```
library(dplyr)

Attaching package: 'dplyr'

The following objects are masked from 'package:stats':
    filter, lag

The following objects are masked from 'package:base':
    intersect, setdiff, setequal, union

library(ggplot2)
library(roxygen2)
library(tinytex)

## Random test for set.seed() function
set.seed(2)
sample(1:6, 6)
```

[1] 5 1 6 4 2 3

```
## function definition
dice_amount <- function(num_rolls,reps) {</pre>
  ## since it will cost $2 to play, define the starting amount
  ## case num_rolls = 0 or some other invalid input is ideally checked at input prompt
  ## creating record of multiple iterations of a set of throws (nxm)
  ## browser()
 trial_record = list()
 for (out_loop in 1:reps){
    start_amount <- -2
    current_amount <- 0</pre>
    won_amount <- 0</pre>
    for (in_loop in 1:num_rolls){
      dice_face <- sample(1:6,1,replace = TRUE)</pre>
      if (dice_face == 3) {
        current_amount <- current_amount + 6</pre>
        paste("At roll: ",in_loop)
        paste("current amount: ",sep = "",current_amount)
      else if (dice_face == 5){
        current_amount <- current_amount + 10</pre>
        paste("At roll: ",in_loop)
        paste("current amount: ",sep = "",current_amount)
      }
      else {
        paste("At roll: ",in_loop)
        paste("current amount: ",sep = "",current_amount)
        break
      }
      in_loop <- 0 ## reset value of inner loop</pre>
    won_amount <- current_amount + start_amount</pre>
    ## just setting new variable for won amount
```

```
trial_record[out_loop] <- won_amount</pre>
  }
  return (trial_record)
}
## num_rolls <- NA_integer_
## num_rolls <- as.integer(readline("Enter the number of dice-rolls: "))
(dice_amount(10,10))
[[1]]
[1] -2
[[2]]
[1] -2
[[3]]
[1] 4
[[4]]
[1] 4
[[5]]
[1] -2
[[6]]
[1] 4
[[7]]
[1] -2
[[8]]
[1] -2
[[9]]
[1] -2
[[10]]
[1] 4
```

• OBSERVATION: By default, when you create a numeric vector using the c() function it

will produce a vector of double precision numeric values. To create a vector of integers using c() you must specify explicitly by placing an L directly after each number.

(iii) Using single table to capture all dice throws

(iv) Using an "apply" class function

```
## Considering that "apply()" class functions
## simply help us avoid using for() loop explicitly

# Number of experiments
num_experiments <- 5

# Number of rolls per experiment
num_rolls <- 10

# Function to simulate rolling a die
roll_die <- function(n) {
    sample(1:6, n, replace = TRUE)
}

# Use apply to simulate the experiments
results <- t(apply(matrix(1:num_experiments, nrow = num_experiments), 1, function(x) roll_die
# Print the results
print(results)</pre>
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	1	6	5	6	6	3	1	5	5	6
[2,]	6	2	2	3	4	3	1	1	5	1
[3,]	2	4	5	6	5	4	2	5	6	5
[4,]	2	6	4	4	4	4	1	2	2	6
[5.]	6	3	5	3	6	5	5	1	5	6

Evaluating computational complexity using microbenchmark()

Evaluating fairness using Monte Carlo simulation

Q.2) Linear Regression on "Cars" Data set

```
cars_df <- data.frame(read.csv("cars.csv"))</pre>
```

(a) Rename the Data

1			
2			
3	Dimensions	Height	
4	Dimensions	Length	
5	Dimensions	Width	
6	Engine Information	Driveline	
7	Engine Information	Engine Type	
8	Engine Information	Hybrid	
9	Engine Information	Number of Forward Gears	
10	Engine Information	Transmission	
11	Engine Information	Engine Statistics	Horsepower
	Engine Information Engine Information	-	Horsepower Torque
12	_	-	
12 13	Engine Information	Engine Statistics	
12 13 14	Engine Information Fuel Information	Engine Statistics City mpg	
12 13 14 15	Engine Information Fuel Information Fuel Information	Engine Statistics City mpg Fuel Type	
12 13 14 15 16	Engine Information Fuel Information Fuel Information Fuel Information	Engine Statistics City mpg Fuel Type Highway mpg	
12 13 14 15 16 17	Engine Information Fuel Information Fuel Information Fuel Information Identification	Engine Statistics City mpg Fuel Type Highway mpg Classification	
12 13 14 15 16 17 18	Engine Information Fuel Information Fuel Information Fuel Information Identification Identification	Engine Statistics City mpg Fuel Type Highway mpg Classification ID	

Upon examining the csv file, we can determine the precise labels and devise a new, shorter name for each column.

colnames(cars_df)

- [1] "Dimensions.Height"
- [2] "Dimensions.Length"
- [3] "Dimensions.Width"
- [4] "Engine.Information.Driveline"
- [5] "Engine.Information.Engine.Type"
- [6] "Engine.Information.Hybrid"
- [7] "Engine.Information.Number.of.Forward.Gears"
- [8] "Engine.Information.Transmission"
- [9] "Fuel.Information.City.mpg"
- [10] "Fuel.Information.Fuel.Type"
- [11] "Fuel.Information.Highway.mpg"
- [12] "Identification.Classification"
- [13] "Identification.ID"
- [14] "Identification.Make"
- [15] "Identification.Model.Year"

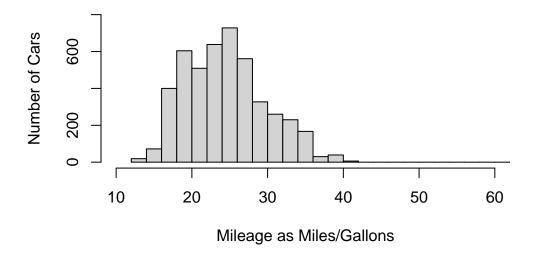
```
[16] "Identification. Year"
[17] "Engine.Information.Engine.Statistics.Horsepower"
[18] "Engine.Information.Engine.Statistics.Torque"
column_rename <- c("H","L","W","Eng_Dr_Line","Eng_Type","Eng_Hybrid","Eng_Forward_G","Eng_Translation
colnames(cars_df) <- column_rename</pre>
colnames(cars_df)
                        "L"
 [1] "H"
                                           "W"
                                                              "Eng_Dr_Line"
 [5] "Eng_Type"
                        "Eng_Hybrid"
                                           "Eng_Forward_G"
                                                              "Eng_Trans"
 [9] "City_MPG"
                        "Fuel_Type"
                                           "Highway_MPG"
                                                              "Car_Class"
[13] "Car_ID"
                        "Car_Make"
                                           "Car_Model_Year"
                                                              "Car_Year"
[17] "Eng_Horse_Power" "Eng_Torque"
## cars_df -- Used to check output
```

```
## extracting data for fuel type "gasoline"
gas_cars <- subset(cars_df,Fuel_Type == "Gasoline")</pre>
## gas_cars -- used to check output
```

```
## Distribution of highway mileage
```

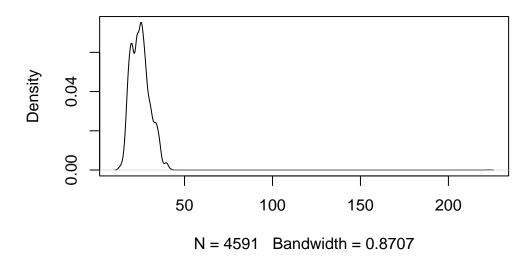
hist(gas_cars\$Highway_MPG, main = "Highway Mileage of Gasoline Cars", xlab = "Mileage as Mile

Highway Mileage of Gasoline Cars



temp_plot <- plot(density(gas_cars\$Highway_MPG))
polygon(temp_plot)</pre>

density(x = gas_cars\$Highway_MPG)



sd(gas_cars\$Highway_MPG)

[1] 6.033656

```
mean(gas_cars$Highway_MPG)
```

[1] 24.96689

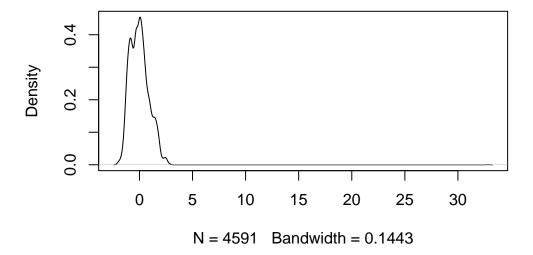
```
glimpse(gas_cars$Highway_MPG)
```

```
int [1:4591] 25 28 30 28 28 27 26 18 20 30 ...
```

Based on the above plots, highway mileage appears to have a normal distribution. The mean mileage is 24 while the standard deviation is roughly 6. We can attempt to Z-transform the scores to control for the deviation around the mean.

```
standardized_vals <- scale(gas_cars$Highway_MPG)
plot(density(standardized_vals))</pre>
```

density(x = standardized_vals)



sd(standardized_vals)

[1] 1

```
integer(mean(standardized_vals))
```

integer(0)

glimpse(standardized_vals)

```
num [1:4591, 1] 0.00549 0.5027 0.83417 0.5027 0.5027 ...
- attr(*, "scaled:center")= num 25
- attr(*, "scaled:scale")= num 6.03
```

It appears that, upon Z-transformation, the standard deviation reduces from 6 to 1 while the mean becomes zero. In order to check whether transformation of Highway Mileage variable is needed, we can later run the computations with both versions of the feature. But for the time being, if we use the standardized values, we might lose some of the detail captured in the relatively large variance in the original values.

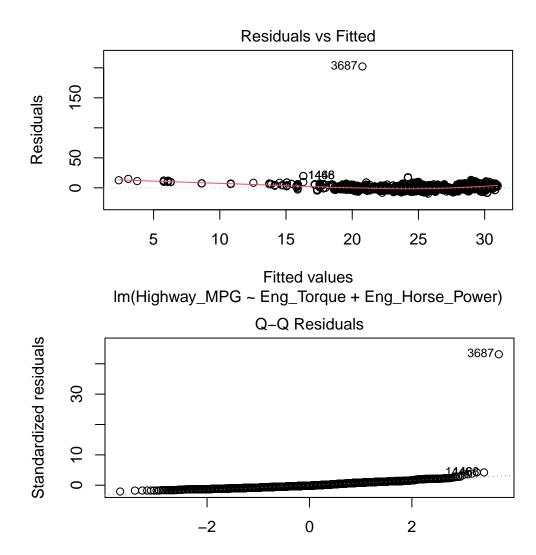
```
gas_cars<- na.omit(gas_cars) ## check to remove any rows with a missing value
```

Computing some general statistics:

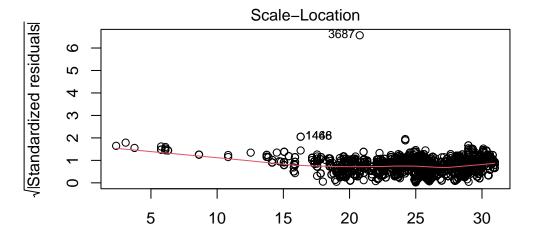
```
gas_cars_num <- gas_cars %>% select(where(is.numeric)) ## create a numeric columns only slic
## drop the non-comparable columns
gas_cars_2 <- data.frame(gas_cars$Eng_Forward_G,gas_cars$City_MPG,gas_cars$Highway_MPG,gas_car(gas_cars_2, method = c("pearson", "kendall", "spearman"))</pre>
```

```
gas_cars.Eng_Forward_G gas_cars.City_MPG
                                      1.00000000
gas_cars.Eng_Forward_G
                                                         -0.0695871
gas_cars.City_MPG
                                     -0.06958710
                                                          1.0000000
gas_cars.Highway_MPG
                                      0.03274557
                                                          0.8271942
gas_cars.Eng_Horse_Power
                                      0.33588453
                                                         -0.7409432
                                                         -0.7878203
gas_cars.Eng_Torque
                                      0.23254242
                          gas_cars.Highway_MPG gas_cars.Eng_Horse_Power
gas_cars.Eng_Forward_G
                                    0.03274557
                                                               0.3358845
gas_cars.City_MPG
                                                              -0.7409432
                                    0.82719420
gas cars. Highway MPG
                                    1.00000000
                                                              -0.5566069
gas_cars.Eng_Horse_Power
                                   -0.55660688
                                                               1.0000000
gas_cars.Eng_Torque
                                   -0.62114741
                                                               0.9474896
                          gas_cars.Eng_Torque
gas_cars.Eng_Forward_G
                                    0.2325424
gas_cars.City_MPG
                                   -0.7878203
gas_cars.Highway_MPG
                                   -0.6211474
gas_cars.Eng_Horse_Power
                                    0.9474896
gas_cars.Eng_Torque
                                    1.0000000
```

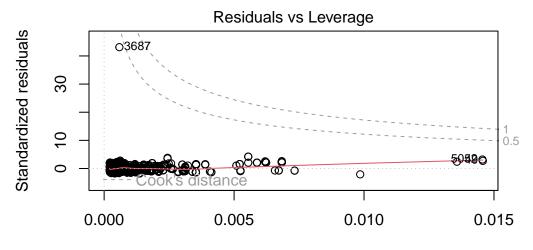
```
gas_cars_num <- data.matrix(gas_cars_2)</pre>
Linear_regress <- lm(Highway_MPG~Eng_Torque+Eng_Horse_Power, data=gas_cars)
summary(Linear_regress)
Call:
lm(formula = Highway_MPG ~ Eng_Torque + Eng_Horse_Power, data = gas_cars)
Residuals:
   Min
       1Q Median
                          3Q
                                Max
 -9.729 -2.632 -0.661 2.489 202.234
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)
             Eng_Torque -0.054600 0.002137 -25.551 <2e-16 ***
Eng_Horse_Power 0.019332 0.002222 8.699 <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4.691 on 4588 degrees of freedom
Multiple R-squared: 0.3958, Adjusted R-squared: 0.3955
F-statistic: 1503 on 2 and 4588 DF, p-value: < 2.2e-16
plot(Linear_regress)
```



Theoretical Quantiles
Im(Highway_MPG ~ Eng_Torque + Eng_Horse_Power)



Fitted values
Im(Highway_MPG ~ Eng_Torque + Eng_Horse_Power)



Leverage Im(Highway_MPG ~ Eng_Torque + Eng_Horse_Power)

ANOVA_COMP <- aov(Highway_MPG~Eng_Torque * Eng_Horse_Power, data=gas_cars) summary(ANOVA_COMP)

```
Df Sum Sq Mean Sq F value Pr(>F)
Eng_Torque
                                  64471
                                          64471 3323.96 <2e-16 ***
Eng_Horse_Power
                               1
                                   1665
                                           1665
                                                   85.86 <2e-16 ***
Eng_Torque:Eng_Horse_Power
                                  11995
                                          11995
                                                 618.41 <2e-16 ***
                               1
Residuals
                            4587
                                  88968
                                              19
Signif. codes:
                0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

To control for other variables in analyzing the relationship between Highway Mileage and Torque, we can start by making make separate data frames

