Reinforcement Learning Report

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Contents

1	Cor	mplete Python Code for Task 1	2	
2	Task 1			
	2.1	Value Iteration	4	
		2.1.1 Algorithm	4	
	2.2	Policy Iteration	5	
		2.2.1 Algorithm		
	2.3	Linear Programming	6	
		2.3.1 Linear Programming Formulation	6	
3	Complete Python Code for Task 2			
	3.1	Graphs of Task 2 and Observations	16	

1 Complete Python Code for Task 1

```
Listing 1: Complete Python Code for Task 1
\#python\ code\ for\ task1
import numpy as np
import argparse
import pulp
def Value_Policy (T, R, gamma, S, Policy):
           Vpi = np.zeros(S)
           Vpi_1 = np.zeros(S)
           eps = 1e-12
           while True:
                     Vpi_{-1} = Vpi.copy()
                     for i in range(S):
                                Vpi[i] = np.sum(T[i, int(Policy[i])] * (R[i, int(Policy[i])] + gamma > int(Policy[i])
                      if abs(np.max(Vpi - Vpi_1)) < eps and <math>abs(np.max(Vpi_1-Vpi)) < eps:
          Qpi = np.sum(np.multiply(T, (R + gamma * Vpi)), axis=2)
          return Vpi, Qpi
def PolicyIteration (T, R, S, gamma):
           Policy = np.zeros(S)
           Pre_Policy = np.zeros(S)
          V, Q = Value_Policy (T, R, gamma, S, Policy)
           while True:
                      Pre_Policy = Policy.copy()
                     IA = []
                     for i in range(S):
                                indices = np.where(Q[i] > V[i])
                                indices = list(indices[0])
                               IA.append(indices)
                     for i in range(S):
                                if len(IA[i]) > 0:
                                           Policy[i] = np.argmax(Q[i])
                     V, Q = Value_Policy (T, R, gamma, S, Policy)
                     if np.array_equal(Pre_Policy, Policy):
                          break
          return Policy
def LinearProgramming (T,R,gamma,S,A):
           problem = pulp.LpProblem("LP", pulp.LpMinimize)
           num_vars = S
          V = [pulp.LpVariable(f"V{i}") for i in range(num_vars)]
           problem += pulp.lpSum(V[s] for s in range(S))
           for s in range(S):
                     for a in range (A):
                                problem += V[s] >= pulp.lpSum(T[s][a][s\_prime] * (R[s][a][s\_prime] + g[s\_prime] +
           problem . solve (pulp . PULP_CBC_CMD (msg=False))
           optimal_Vs = [V[s].varValue for s in range(S)]
          Vs = np.array(optimal_Vs)
          As = np.argmax(np.sum(T*(R+gamma*Vs), axis=2), axis = 1)
          return Vs, As
```

```
def ValueIteration (T, R, gamma, S, A, endstate):
    Vt = np.zeros(S)
    At = np.zeros(S)
    Vt_1 = np.zeros(S)
    eps = 1e-10
    \mathbf{sum} = 0
    while (True):
         Vt_-1 = Vt.copy()
         for i in range(S):
              if i not in endstate:
                  Vt[i] = np.max(np.sum(T[i]*(R[i]+gamma*Vt_1), axis=1))
                  At[i] = np.argmax(np.sum(T[i]*(R[i]+gamma*Vt_1), axis=1))
              else:
                  Vt[i] = 0
                  At[i] = -1
         if(abs(np.max(Vt-Vt_1)) < eps and abs(np.max(Vt_1-Vt)) < eps):
             break
    return Vt, At
def ReadFile (mdppath):
    States = 0
    Actions = 0
    T = None
    R = None
    gamma = 0
    mtype = "not-specified"
    endstate = -1
    with open(mdppath, 'r') as file:
         lines = file.readlines()
         for line in lines:
             parts = line.strip().split(',')
              parts = [i for i in parts if i != '']
              if parts[0] == 'numStates':
                  States = int(parts[1])
              elif parts[0] == 'numActions':
                  Actions = int(parts[1])
                  T = \text{np.zeros}((\text{States}, \text{Actions}, \text{States}))
R = \text{np.zeros}(\text{shape} = (\text{States}, \text{Actions}, \text{States}), \text{dtype} = \text{np.float32}
              elif parts[0] = 'transition':
                  s1, ac, s2 = map(int, parts[1:4])
                  p = float(parts[5])
                  r = float(parts[4])
                  T[s1, ac, s2] = p
                  R[s1, ac, s2] = r
              elif parts[0] == 'mdptype':
                  mtype = parts[1]
              elif parts[0] == 'discount':
                  gamma = float (parts [1])
              elif parts [0] = 'end':
                  endstate = parts[1:]
    return States, Actions, T, R, gamma, mtype, endstate
def ReadPolicy (policypath, States):
    P = np. zeros (States)
    N = []
```

```
with open(policypath, 'r') as file:
        lines = file.readlines()
        for line in lines:
            parts = line.strip().split('-')
            parts = [i for i in parts if i != '']
            N. append (int (parts [0]))
   P = np.array(N)
    return P
if __name__ == "__main__":
    parse = argparse.ArgumentParser()
    parse.add_argument("—mdp", type=str, help="MDP-file-path-to-be-entered")
    parse.add_argument("-algorithm", type=str, help="Algorithm-to-be-executed",
    parse.add\_argument("--policy", \ \mathbf{type} = \mathbf{str}, \ \mathbf{help} = "Policy" for `Value `Function")
    argument = parse.parse_args()
    mdppath = argument.mdp
    algorithm = argument.algorithm
    policypath = argument.policy
    States, Actions, T, R, gamma, mtype, endstate = ReadFile(mdppath)
    if policypath != None:
        Policy = ReadPolicy (policypath, States)
        Vpi, Qpi = Value_Policy (T,R,gamma, States, Policy)
        for i in range (States):
            print(Vpi[i], "-", Policy[i])
    elif algorithm == 'vi':
        Vt, At = ValueIteration (T,R,gamma, States, Actions, endstate)
        for i in range (States):
            print(Vt[i], "-", int(At[i]))
    elif algorithm == 'hpi':
        Policy = PolicyIteration (T,R, States, gamma)
        Vt, Qt = Value_Policy (T, R, gamma, States, Policy)
        for i in range(States):
            print(Vt[i], "-", int(Policy[i]))
    elif algorithm == 'lp':
        Vt, At = LinearProgramming(T, R, gamma, States, Actions)
        for i in range(States):
            print (Vt[i],"-",At[i])
```

2 Task 1

The code for planner.py is shown above and piecewise explanation of the code for each algorithm is done below. The MDP file given is read and 2 3-D Matrices are formed T and R respectively and the rest information is stored inside variables with there respective names.

2.1 Value Iteration

For this I made a function and inside it I have used 2 1-D arrays to store the current and previous values of the states and another 1-D array for storing Action (Optimal). Initially filled with 0(arbitrary value). Variable eps is used to store precision. Inside the loop firstly the value of current states is copied to arrays storing previous value states. After that for every state the value is calculated using the bellman optimality operator. Since np.argmax() is used for finding optimal action the tie break is taken care by taking the first value which is the maximum.

2.1.1 Algorithm

```
def ValueIteration (T, R, gamma, S, A, endstate):
    Vt = np.zeros(S)
    At = np.zeros(S)
    Vt_1 = np.zeros(S)
    eps = 1e-10
    sum = 0
    while (True):
        Vt_1 = Vt.copy()
        for i in range(S):
             if i not in endstate:
                 Vt[i] = np.max(np.sum(T[i]*(R[i]+gamma*Vt_1), axis=1))
                 At[i] = np.argmax(np.sum(T[i]*(R[i]+gamma*Vt_1), axis)
                    =1))
             else:
                 Vt[i] = 0
                 At[i] = -1
        if(abs(np.max(Vt-Vt_1)) < eps and abs(np.max(Vt_1-Vt)) < eps):
             break
    return Vt, At
```

2.2 Policy Iteration

The code for policy iteration is given below. Here I have used 2 function one for policy iteration and another for finding the value of the policy which is value-policy function. Initially a policy which takes action 0 for every state is assigned and then policy iteration is done where value and action-value for each state is calculated and then new policy is made by taking those actions for which the action-value is maximized for that state.

2.2.1 Algorithm

```
Listing 3: Complete Python Code for Task 1 (Policy Iteration)
    def Value_Policy (T, R, gamma, S, Policy):
     Vpi = np.zeros(S)
     Vpi_1 = np.zeros(S)
     eps = 1e-12
     while True:
          Vpi_1 = Vpi.copy()
          for i in range(S):
              Vpi\left[\:i\:\right] \: = \: np.sum(T\left[\:i\:,\:\:int\left(\:Policy\left[\:i\:\right]\right)\:\right] \: * \: (R\left[\:i\:,\:\:int\left(\:Policy\left[\:i\:\right]\right]\right])
                   if abs(np.max(Vpi - Vpi_1)) < eps and abs(np.max(Vpi_1-Vpi))
              < eps:
              break
    Qpi = np.sum(np.multiply(T, (R + gamma * Vpi)), axis=2)
    return Vpi, Qpi
def PolicyIteration (T, R, S, gamma):
     Policy = np.zeros(S)
     Pre_Policy = np.zeros(S)
    V, Q = Value_Policy(T, R, gamma, S, Policy)
     while True:
          Pre_Policy = Policy.copy()
         IA = []
          for i in range(S):
```

```
indices = np.where(Q[i] > V[i])
indices = list(indices[0])
IA.append(indices)
for i in range(S):
    if len(IA[i]) > 0:
        Policy[i] = np.argmax(Q[i])
V, Q = Value_Policy(T, R, gamma, S, Policy)
if np.array_equal(Pre_Policy, Policy):
    break
return Policy
```

2.3 Linear Programming

Here as stated I have used pulp library for the calculation of optimal value for each state and for calculating the optimal action I have used the action-value function.

2.3.1 Linear Programming Formulation

3 Complete Python Code for Task 2

The code for encoder is shown. Here I have printed all the transitions with non-zero probabillities and for that the code is given below which shown The comments given describe the code completely.

In brief what I have done is to find possible positions of opponent with non-zero probabilities since those are the only valid states for which the probability will be non-zeros than I have independently coded each action starting from 0 till 9 where in for actions 0 - 7 I have first checked the conditions for the which the player goes out of bound or not than I have checked status of ball (i.e. which player has the ball) than after that I have checked for the case tackling if the player with the ball moves otherwise simply put probabilities. For action 8 and 9 similar to above found the next positions of the opponent and than for 8 checked if next position of R comes in line of both the players or not than put the probabilities accordinly For action 9 I checked the position of R in the next positions where it was standing infront of the goal and put the probabilities if it was not standing in front of the goals than I didn't halved the probabilities

Listing 5: Complete Python Code for Task 2

import numpy as np

import argparse

```
def read_probabilities_file(file_path):
    #This function is for reading the opponents file and getting all
        this inside a numpy array.
    # Initialize an empty list to store the data.
    data = []
    # Open the file for reading
    with open(file_path, 'r') as file:
         lines = file.readlines()
        \# Iterate over lines, starting from the second line
         for line in lines [1:]:
             # Split the line into fields using space as the delimiter
             fields = line.strip().split(',')
             #this is the reading part for the probabilities
             state = fields[0]
             p_{-l} = float (fields [1])
             p_r = float (fields [2])
             p_u = float (fields [3])
             p_d = float (fields [4])
             data.append((state, p_l, p_r, p_u, p_d))
    # Convert the list of tuples to a NumPy array
    \texttt{data\_array} \; = \; \texttt{np.array} \, (\, \texttt{data} \, , \; \; \texttt{dtype} \! = \! [(\, \, \text{`State'} \, , \, \, \, \text{`U7'}) \, , \; \, (\, \, \text{`P(L)'} \, , \, \, \, ) \, ] \, .
        float), ('P(R)', float), ('P(U)', float), ('P(D)', float)])
    return data_array
def get_R_probabilities (data_array, state_name):
    #This function is for finding the probabilities of R for a given
    filtered_data = data_array[data_array['State'] == state_name]
    # Check if the state was found
    if len(filtered_data) > 0:
         answer = np.array([filtered_data[0][1], filtered_data[0][2],
             filtered_data [0][3], filtered_data [0][4]])
         return answer # Return the first matching row as a NumPy
             array
    else:
         print ("found - None")
         return None
def findxy(num):
    #This function is used to find the coordinates of the position of
    ####Note!!!!!!!! I have used coordinates starting from top left
         corner as (1,1) and bottom right corner as (4,4)
    \#\#Positive x-axis is towards the right and positive y-axis is
        downwards
    x = num\%4
    y = 0
    if(x = 0):
      x = 4
```

```
if num in [1,2,3,4]:
      y = 1
    elif num in [5,6,7,8]:
      y = 2
    elif num in [9,10,11,12]:
      y = 3
    else:
      y = 4
    return x,y
def give_Positions (State):
    #This function is used to the positions of all the player and the
         state of ball for a given state.
    Positions = np. array ([int(State[0:2]),int(State[2:4]),int(State
        [4:6]), int (State [6])])
    return Positions
def MapState():
    \#This\ Dictionary\ is\ a\ mapping\ from\ state\ to\ integers\ from\ 0-8193
        in which 0-8191 are the states and 8192 is the lose state
    #8193 is the win state
    mydict = \{\}
    s = 0
    P = ['01', '02', '03', '04', '05', '06', '07', '08', '09', '10', '11', '12',
        '13', '14', '15', '16']
    B = [', 1', ', 2']
    for i in P:
      for j in P:
         for k in P:
           for e in B:
             mydict[i+j+k+e] = s
             s += 1
    mydict['lose'] = 8192
    mydict [ 'win '] = 8193
    return mydict
\mathbf{def} \ \text{check\_line} (x1, y1, x2, y2, x3, y3):
    #This code for checking that whether R is in the line of B1 and
        B2 while passing
    #For this I have checked along the line x+y=c and x-y=c and
        horizontal and vertical line
    #this returns a bool stating whether R is present between them
        while\ passing\ or\ not
    if x1+y1 = x2+y2 = x3+y3 and ((x3)=x1 and x3<=x2) or (x3<=x1)
        and x3>=x2):
        return True
    elif x1-y1 == x2-y2 == x3-y3 and ((x3>=x1 \text{ and } x3<=x2) \text{ or } (x3<=x1)
        and x3>=x2):
         return True
    elif x1 == x2 == x3 and ((y3 >= y1 \text{ and } y3 <= y2) \text{ or } (y3 <= y1 \text{ and } y3 <= y2)
         y3 >= y2):
         return True
    elif y1 == y2 == y3 and ((x3>=x1 \text{ and } x3<=x2) \text{ or } (x3<=x1 \text{ and } x3>=x1)
        x2)):
        return True
    else:
         return False
```

```
def give_T_and_R(op_policy, p, q):
    #This is the main function for building the MDP
    \# T = np.zeros((8194,10,8194))
    Statemap = MapState()
    #Here I am considering the case of game end when player goes out
        of bounds so in this case these are block positions after
    \#taking the action and if a player B1 was in 5 and took action 0
        then it will move to 4 in code but in grid it will
    #fall out of it hence these values taken taking care of that.
    LB = np. array([0,4,8,12])
                                     #This is used for checking
        whether after moving in left a player goes out of bounds or
        not
    RB = np. array([5, 9, 13, 17])
                                      #Same as above for right
    UB = np. array([-3, -2, -1, 0])
                                      #For Up
    DB = np. array([17, 18, 19, 20])
                                      #For Down
    #From here I am starting to calculate Transition probabilities
    for states in op_policy['State']:
        positions = give_Positions(states) #find positions given the
            state
        R_p = get_R_probabilities(op_policy, states) #get
            probabilities of R given the state
        R_{-next} = [positions[2] - 1, positions[2] + 1, positions[2] -
            4, positions [2] + 4] #Position of in possible next state
        non_zero_indices = np.nonzero(R_p)[0] #removing all the zero
            probabilities states of R
        R_next = [R_next[i] for i in non_zero_indices] #Finding non-
            zero next positions of R
        R_prob = [R_p[i] for i in non_zero_indices] #Finding their
            respective probabilities
        R_{\text{-}next} = [\mathbf{str}(x) \cdot z \text{ fill } (2) \ \mathbf{for} \ x \ \mathbf{in} \ R_{\text{-}next} \ \mathbf{if} \ 0 < x < 17] \ \#
            Check for the out-bounds case for R
        prob1 = 0
        losing = 0
#For Action 0 this is the calculation of probabilities
        B1-next = str(positions[0]-1).zfill(2) #finding next position
             of B1 for action 0
        if not int(B1_next) in LB: #checking is B1 goes out of bounds
             if positions [3] \Longrightarrow 2: \#Since\ this\ is\ movement\ case
                checking for ball status if 2 then probabilities are
                set accordingly
                 for v, i in enumerate (R_next): #For all possible next
                     state of R
                     nextS = B1_next + str(positions[1]).zfill(2) + i
                         + '2'
                     prob1 = (1-p)*R_prob[v]
                     losing += p*(R_prob[v])
                     if prob1!=0:
                           print("transition", Statemap[states],0,
                              Statemap [nextS], 0, prob1)
             else:
                 for v, i in enumerate (R_next):
                     nextS = B1_next + str(positions[1]).zfill(2) + i
                     #Below condition is for tackling case here I have
                          just checked the final position of R and
                         B1\_next
```

```
#Whether they are same of interchanged these 2
                 conditions are considered as tackling
              if B1_next = i or (B1_next = str(positions[2]).
                 z fill(2) and i = str(positions[0]).zfill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
              else: #condition if no tackling is present
                  prob1 = (1-2*p)*R_prob[v]
                  losing += 2*p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],0,
                      Statemap [nextS], 0, prob1)
 else:
     losing = 1
 print ("transition", Statemap [states], 0, Statemap ['lose'], 0,
    losing)
 prob1 = 0
 losing = 0
#For Action 1
 B1\_next = positions[0]+1 #same as above finding the next
    position of player
 B2\_next = states[2:4] #next position of second player which
     will be same as before for Action 1
 if not B1_next in RB:
     if positions [3] == 2: #check of ball status
         for v, i in enumerate (R_next): #Probabilities if
             player doesn't has ball
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
              \operatorname{prob} 1 = (1-p) * R_{-}\operatorname{prob} [v]
              losing += p*(R_prob[v])
              if prob1!=0:
                  print("transition", Statemap[states],1,
                      Statemap [nextS], 0, prob1)
     else: #Probability if the player has the ball
         for v, i in enumerate(R_next):
              nextS = str(B1\_next).zfill(2) + str(B2\_next).
                  z fill(2) + i + '1'
             #here tackling is checked
              if str(B1\_next). zfill(2) == i or (str(B1\_next).
                 z fill(2) = str(positions[2]) . z fill(2) and i
                 = str(positions [0]).zfill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
              else: #if no tackling than
                  prob1 = (1-2*p)*R_prob[v]
                  losing += 2*p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],1,
                      Statemap [nextS], 0, prob1)
 else:
     losing = 1
 print ("transition", Statemap [states], 1, Statemap ['lose'], 0,
    losing)
\#The\ same\ process\ is\ repeated\ is\ for\ action\ from\ 0-7\ as\ the
   comments mention above for the respective player.
#for Action 2
```

```
prob1 = 0
losing = 0
B1_next = str(positions[0]-4)
if len(B1\_next) == 1:
    B1_next = '0' + B1_next
B2_next = states[2:4]
ball_next = states [6]
if not int(B1_next) in UB:
     if positions [3] = 2:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
              \operatorname{prob} 1 = (1-p) * R_{\operatorname{prob}} [v]
              losing += p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],2,
                      Statemap [nextS], 0, prob1)
     else:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '1'
              if B1\_next = i or (B1\_next = str(positions[2]).
                  z fill(2) and i = str(positions[0]).z fill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
                  prob1 = (1-2*p)*R_prob[v]
                  losing += 2*p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],2,
                      Statemap [nextS], 0, prob1)
else:
    losing = 1
print("transition", Statemap[states],2,Statemap['lose'],0,
    losing)
#for Action 3
prob1 = 0
losing = 0
B1-next = str(positions[0]+4). zfill(2)
B2_next = states [2:4]
if not int(B1_next) in DB:
    if positions [3] = 2:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
              \operatorname{prob} 1 = (1-p) * R_{\operatorname{prob}} [v]
              losing \; +\!\!= \; p\!*\!\,R_{\text{-}}prob\,[\,v\,]
              if prob1!=0:
                  print("transition", Statemap[states],3,
                      Statemap [nextS], 0, prob1)
    else:
         for v, i in enumerate (R_next):
              nextS = B1_next + B2_next + i + '1'
              if B1_next = i or (B1_next = str(positions[2]).
                  z fill(2) and i = str(positions[0]).z fill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
              else:
                  \operatorname{prob1} = (1-2*p)*R_{-}\operatorname{prob}[v]
                  losing += 2*p*R_prob[v]
```

```
if prob1!=0:
                  print("transition", Statemap[states],3,
                      Statemap [nextS], 0, prob1)
else:
    losing = 1
print("transition", Statemap[states],3,Statemap['lose'],0,
    losing)
#for Action 4
prob1 = 0
losing = 0
B2_next = str(positions[1]-1)
if len(B2\_next) == 1:
    B2\_next = '0' + B2\_next
B1_{\text{next}} = \text{states} [0:2]
ball_next = states[6]
if not int(B2_next) in LB:
    if positions [3] == 1:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '1'
              \operatorname{prob} 1 = (1-p) * R_{-} \operatorname{prob} [v]
              losing += p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],4,
                      Statemap [nextS], 0, prob1)
    else:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
              if B2_next == i or (B2_next == str(positions[2]).
                  z fill(2) and i = str(positions[1]).z fill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
              else:
                  \operatorname{prob} 1 = (1-2*p)*R_{\operatorname{prob}}[v]
                  losing += 2*p*R_prob[v]
              if prob1!=0:
                  print("transition", Statemap[states],4,
                      Statemap [nextS], 0, prob1)
else:
    losing = 1
print ("transition", Statemap [states], 4, Statemap ['lose'], 0,
    losing)
#for Action 5
losing = 0
prob1 = 0
B2-next = str(positions[1]+1)
if len(B2\_next) == 1:
    B2\_next = '0' + B2\_next
B1_next = states[0:2]
ball_next = states[6]
if not int(B2_next) in RB:
     if positions [3] = 1:
         for v, i in enumerate (R_next):
              nextS = str(B1\_next).zfill(2) + B2\_next + i + '1'
              \operatorname{prob} 1 = (1-p) * R_{-}\operatorname{prob} [v]
              losing += p*R_prob[v]
              if prob1!=0:
```

```
print("transition", Statemap[states],5,
                      Statemap [nextS], 0, prob1)
    else:
         for v, i in enumerate(R_next):
             nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
             if B2_next = i or (B2_next = str(positions[2]).
                  z fill(2) and i = str(positions[1]).z fill(2)):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
             else:
                  \operatorname{prob1} = (1-2*p)*R_{\operatorname{prob}}[v]
                  losing += 2*p*R_prob[v]
             if prob1!=0:
                  print("transition", Statemap[states],5,
                      Statemap [nextS], 0, prob1)
else:
    losing = 1
print ("transition", Statemap [states], 5, Statemap ['lose'], 0,
    losing)
#for Action 6
prob1 = 0
losing = 0
B2_next = str(positions[1]-4)
if len(B2\_next) == 1:
    B2_next = '0' + B2_next
B1_next = states[0:2]
ball_next = states [6]
if not int(B2_next) in UB:
    if positions [3] = 1:
         for v, i in enumerate (R_next):
             nextS = str(B1\_next).zfill(2) + B2\_next + i + '1'
             \operatorname{prob1} = (1-p) * R_{\operatorname{prob}} [v]
             losing += p*R_prob[v]
             if prob1!=0:
                  print("transition", Statemap[states],6,
                      Statemap [nextS], 0, prob1)
    else:
         for v, i in enumerate (R_next):
             nextS = str(B1\_next).zfill(2) + B2\_next + i + '2'
             if B2_next = i or (B2_next = str(positions[2]).
                 z fill(2) and i = str(positions[1]) . <math>z fill(2):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
             else:
                  \operatorname{prob1} = (1-2*p)*R_{-}\operatorname{prob}[v]
                  losing += 2*p*R_prob[v]
             if prob1!=0:
                  print("transition", Statemap[states],6,
                      Statemap [nextS], 0, prob1)
else:
    losing = 1
print("transition", Statemap[states],6,Statemap['lose'],0,
    losing)
#for Action 7
prob1 = 0
losing = 0
```

```
B2_next = str(positions[1]+4).zfill(2)
B1_{-next} = states[0:2]
if not int(B2_next) in DB:
    if positions [3] == 1:
         for v, i in enumerate (R_next):
             nextS = str(B1\_next).zfill(2) + B2\_next + i + '1'
             \operatorname{prob} 1 = (1-p) * R_{\operatorname{prob}} [v]
             losing += p*R_prob[v]
             if prob1!=0:
                  print("transition", Statemap[states],7,
                     Statemap [nextS], 0, prob1)
    else:
         for v, i in enumerate (R_next):
             nextS = str(B1_next).zfill(2) + B2_next + i + '2'
             if B2_{\text{next}} = i or (B2_{\text{next}} = str(positions[2]).
                 z fill(2) and i = str(positions[1]) . <math>z fill(2):
                  prob1 = (1-2*p)*R_prob[v]/2
                  losing += (1-(1-2*p)/2)*R_prob[v]
             else:
                  \operatorname{prob1} = (1-2*p)*R_{-}\operatorname{prob}[v]
                  losing += 2*p*R_prob[v]
             if prob1!=0:
                  print("transition", Statemap[states],7,
                     Statemap[nextS], 0, prob1)
else:
    losing = 1
print("transition", Statemap[states],7,Statemap['lose'],0,
    losing)
#For action 8 since we require the coordinates hence they are
     calculted using the function shown above
B1x, B1y = findxy(positions[0])
B2x, B2y = findxy(positions[1])
prob1 = 0
losing = 0
#for Action 8
B1_{next} = str(positions[0]).zfill(2) #next positions of the
    players
B2_next = str(positions[1]).zfill(2)
for v, i in enumerate (R_next):
    B1x, By = findxy(positions[0])
    B2x, B2y = findxy(positions[1])
    Rx, Ry = findxy(int(i))
    if str(positions[3]) = '1':
         nextS = B1_next + B2_next + i + '2'
    if str(positions[3]) = '2':
         nextS = B1\_next + B2\_next + i + '1'
    if check_line(B1x,B1y,B2x,B2y,Rx,Ry): #Here if R's next
        position is between B1 and B2 then probabilities are
        halved
         \operatorname{prob1} = (q-0.1*\max(abs(B1x-B2x),abs(B1y-B2y)))*R_{\operatorname{prob}}
         losing += (1 - (q-0.1*max(abs(B1x-B2x),abs(B1y-B2y)))
             /2)*R_prob[v]
    else:#If R's next position is not between B1 and B2 then
        probabilities as shown
         prob1 = (q-0.1*max(abs(B1x-B2x),abs(B1y-B2y)))*R_prob
```

```
[v]
                 losing += (1 - (q-0.1*max(abs(B1x-B2x),abs(B1y-B2y)))
                    ) * R_prob [v]
             if prob1!=0:
                 print("transition", Statemap[states],8,Statemap[nextS
                     ], 0, \text{prob1})
        print ("transition", Statemap [states], 8, Statemap ['lose'], 0,
            losing)
        #for Action 9
        B1_{-next} = str(positions[0]).zfill(2) #next positions of the
        B2_{\text{next}} = \mathbf{str}(\text{positions}[1]) \cdot z \text{ fill } (2)
        prob1 = 0
        losing = 0
        \# if Statemap[states] == 63:
        for v, i in enumerate (R_next):
            Rx, Ry = findxy(int(i)) #next positions of the opponent
             if Rx = 4 and (Ry = 2 or Ry = 3): \#condition if R is
                present infront of goal post
                 if positions [3] == 1: #status of the ball while
                     shooting if B1 or B2
                     prob1 += (q - 0.2*(4-B1x))*R_prob[v]/2
                     losing += (1 - (q - 0.2*(4-B1x))/2)*R_prob[v]
                 else: #shooting done by B2
                      prob1 += (q - 0.2*(4-B2x))*R_prob[v]/2
                      losing += (1 - (q - 0.2*(4-B2x))/2)*R_prob[v]
             else: #If R is not infront of the goal post than the
                 probabilities of transition are shown below
                 if positions [3] == 1: #if Shooting done by B1
                      prob1 += (q - 0.2*(4-B1x))*R_prob[v]
                      losing += (1 - (q - 0.2*(4-B1x)))*R_prob[v]
                 else: #shooting done by B2
                      prob1 += (q - 0.2*(4-B2x))*R_prob[v]
                      losing += (1 - (q - 0.2*(4-B2x)))*R_prob[v]
        print("transition", Statemap[states],9,Statemap['lose'],0,
            losing)
        print("transition", Statemap[states],9,Statemap['win'],1,
            prob1)
    \# return T
if -name_{-} = "-main_{-}":
    #Code for the command line arguments
    parse = argparse.ArgumentParser()
    parse.add_argument("—opponent", type=str, help="Opponent Policy -
        File path")
    parse.add_argument("—p", type=float, help="Value-for-p")
parse.add_argument("—q", type=float, help="Policy-for-Value-
        Function")
    argument = parse.parse_args()
    OPpath =argument.opponent
    p = argument.p
```

```
q = argument.q
op_policy = read_probabilities_file(OPpath) # code to get
    opponent policy
#printing the MDP
print("numStates * 8194")
print("numActions * 10")
print("end * 8192 * 8193")
give_T_and_R(op_policy,p,q)
print("mdptype * episodic")
print("discount * 1")
```

3.1 Graphs of Task 2 and Observations

The graphs are shown below:

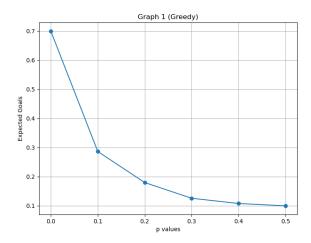


Figure 1: Graph with P varying

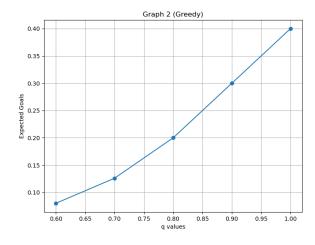


Figure 2: Graph with Q varying

The observation's made are that while keeping q constant and increasing p the expected goals decrease. While keeping p constant and increasing q the expected goals increases as the probability of shooting increases with q. While the expected number of goals are decreasing for keeping q constant and increasing p because increasing p is reducing the movement probability and for p=0.5 the movement probability is becoming 0 which states that the players whoever

has the ball is either passing it or directly of shooting which is decreasing the probability of wining and hence the expected number of goals.