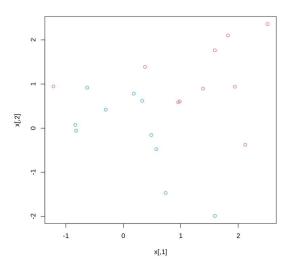
1

```
1 install.packages("e1071")
     Installing package into '/usr/local/lib/R/site-library'
     (as 'lib' is unspecified)
     also installing the dependency 'proxy'
 1 library(e1071)
 2 set.seed (1)
 3 # We now use the svm() function to fit the support vector classifier for a given value of the cost parameter.
 4 # Here we demonstrate the use of this function on a two-dimensional example so that we can plot the resulting
 5 # decision boundary.
 \ensuremath{\text{6}}\ \mbox{\#}\ \mbox{We} begin by generating the observations, which belong to two classes.
 7 x=matrix(rnorm(20*2), ncol=2)
 8 y=c(rep(-1,10), rep(1,10))
 9 \times [y==1,]=x[y==1,] + 1
10 x
11 y
12 \mbox{\tt \#} We begin by checking whether the classes are linearly separable.
13 plot(x, col=(3-y))
14 \# They are not. Next, we fit the support vector classifier.
15 # Note that in order for the svm() function to perform classification
16 \mbox{\ensuremath{\mbox{\#}}} we must encode the response as a factor variable.
17 \# We now create a data frame with the response coded as a factor.
18 dat <- data.frame(x = x,y = as.factor(y))
19 svmfit <- svm(y ~., data=dat, kernel="linear", cost=10,scale=FALSE)
20 # The argument scale=FALSE tells the svm() function not to scale each feature to
21 # have mean zero or standard deviation one;
22 \# depending on the application, one might prefer to use scale=TRUE.
23 \mbox{\tt\#} We can now plot the support vector classifier obtained:
24 plot(svmfit , dat)
25 \ \# Note that the two arguments to the plot.svm() function are the output of the call to svm(),
26 #as well as the data used in the call to svm().
27 # The region of feature space that will be assigned to the -1 class is shown in light blue,
28 \# and the region that will be assigned to the +1 class is shown in purple.
      0.5757814 -0.47815006
      -0.3053884 0.41794156
       2.5117812 2.35867955
       1.3898432 0.89721227
      0.3787594 1.38767161
      -1.2146999 0.94619496
      2.1249309 -0.37705956
      0.9550664 0.58500544
      0.9838097 0.60571005
       1.9438362 0.94068660
       1.8212212 2.10002537
      1.5939013 1.76317575
     -1 - -1 - -1 - -1 - -1 - -1 - -1 - -1 - -1 - -1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1
```



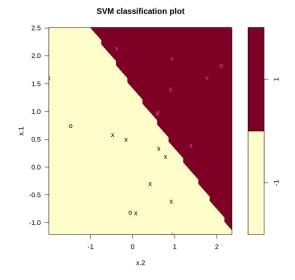


```
1 svmfit <- svm(y \sim., data=dat, kernel="linear", cost = 0.1, scale=FALSE)
```

## 2 plot(svmfit , dat)

3 svmfit\$index

## 1 · 2 · 3 · 4 · 5 · 7 · 9 · 10 · 12 · 13 · 14 · 15 · 16 · 17 · 18 · 20



```
1 set.seed (1)
  2 \; tune.out \; <- \; tune(svm, \; y \; \sim., data=dat, kernel="linear", \; ranges=list(cost=c(0.001, \; 0.01, \; 0.1, \; 1,5,10,100))) 
 3 # We can easily access the cross-validation errors for each of these models using the summary() command:
 4 summary(tune.out)
 5 # We see that cost=0.1 results in the lowest cross-validation error rate.
 6 \ \# The tune() function stores the best model obtained, which can be accessed as follows:
 7 bestmod=tune.out$best.model
 8 summary(bestmod)
9 # The predict() function can be used to predict the class label on a set of test observations,
10 # at any given value of the cost parameter. We begin by generating a test data set.
11 xtest=matrix(rnorm(20*2), ncol=2)
12 ytest=sample(c(-1,1), 20, rep=TRUE)
13 xtest[ytest==1,]=xtest[ytest==1,] + 1
14 testdat=data.frame(x=xtest, y=as.factor(ytest))
15 # Now we predict the class labels of these test observations.
16 \# Here we use the best model obtained through cross-validation in order to make predictions.
17 ypred <-predict(bestmod ,testdat)</pre>
18 table(predict=ypred, truth=testdat$y)
19 \#Thus, with this value of cost, 19 of the test observations are correctly classified.
20 # What if we had instead used cost= 0.01?
21 svmfit <- svm(y~., data=dat, kernel="linear", cost=.01, scale=FALSE)
22 ypred=predict(svmfit ,testdat)
23 table(predict=ypred, truth=testdat$y)
24 \mbox{\tt\#} In this case one additional observation is misclassified.
25 \ \text{\#} Now consider a situation in which the two classes are linearly separable.
```

 $27 \ \text{\#}$  We first further separate the two classes in our simulated data so that they are linearly separable:

26 # Then we can find a separating hyperplane using the svm() function.

28 x[y==1,]=x[y==1,]+0.5 29 plot(x, col=(y+5)/2, pch=19)

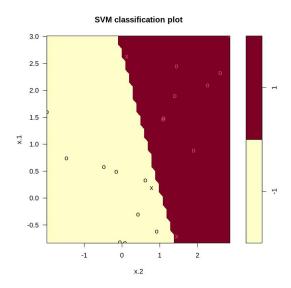
```
- sampling method: 10-fold cross validation
     - best parameters:
      cost
 1 #Now the observations are just barely linearly separable.
 2 \mbox{\tt\#} We fit the support vector classifier and plot the resulting hyperplane,
 3 \# using a very large value of cost so that no observations are misclassified.
 4 dat=data.frame(x=x,y=as.factor(y))
 5 svmfit <-svm(y~., data=dat, kernel="linear", cost=1e5)</pre>
 6 summary(svmfit)
 7 plot(svmfit,dat)
 \boldsymbol{8}\ \boldsymbol{\#}\ \text{No}\ \text{training} errors were made and only three support vectors were used.
 9 \# However, we can see from the figure that the margin is
10 \# very narrow (because the observations that are not support vectors, indicated as circles, are very
11 \# close to the decision boundary). It seems likely that this model will perform poorly on test data.
12 # We now try a smaller value of cost:
13 svmfit <- svm(y~., data=dat, kernel="linear", cost=1)
14 summary(svmfit)
15 plot(svmfit ,dat)
16 \; \# \; \text{Using cost=1, we misclassify a training observation, but we also obtain a much wider margin and make}
17 # use of seven support vectors.
18 # It seems likely that this model will perform better on test data than the model with cost=1e5.
     Call:
```

```
Call:
svm(formula = y ~ ., data = dat, kernel = "linear", cost = 1)

Parameters:
    SVM-Type: C-classification
SVM-Kernel: linear
    cost: 1

Number of Support Vectors: 7
    ( 4 3 )
Number of Classes: 2
```

Levels: -1 1



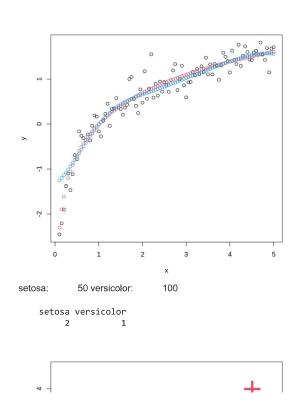


```
1 #We now examine the Khan data set, which consists of a number of tissue samples
 2 # corresponding to four distinct types of small round blue cell tumors
3 # For each tissue sample, gene expression measurements are available.
4 #The data set consists of training data, xtrain and ytrain, and testing data, xtest and ytest.
5 install.packages("ISLR")
 6 library(e1071)
 7 library(ISLR)
 8 names(Khan)
9 # Let's examine the dimension of the data:
10 # This data set consists of expression measurements for 2,308 genes.
11 # The training and test sets consist of 63 and 20 observations respectively
12 dim(Khan$xtrain )
13 dim(Khan$xtest )
14 length(Khan$ytrain )
15 length(Khan$ytest )
16 table(Khan$ytrain )
17 table(Khan$vtest )
18 \ \# We will use a support vector approach to predict cancer subtype using gene expression measurements.
19 \# In this data set, there are a very large number of features relative to the number of observations.
20 # This suggests that we should use a linear kernel, because the additional flexibility that will
21 # result from using a polynomial or radial kernel is unnecessary.
22 dat <- data.frame(x=Khan$xtrain , y = as.factor(Khan$ytrain ))
23 out <- svm(y ~., data=dat, kernel="linear",cost=10)
24 summary(out)
25 # We see that there are no training errors. In fact, this is not surprising, because the large number
26 # of variables relative to the number of observations implies that it is easy to find hyperplanes that
27 # fully separate the classes.
28 # We are most interested not in the support vector classifier's performance on the training observations,
29 # but rather its performance on the test observations.
30 dat.te=data.frame(x=Khan$xtest , y = as.factor(Khan$ytest ))
31 pred.te=predict(out, newdata=dat.te)
32 table(pred.te, dat.te$y)
33 # We see that using cost=10 yields two test set errors on this data
    Installing package into '/usr/local/lib/R/site-library'
(as 'lib' is unspecified)
    'xtrain' 'xtest' 'ytrain' 'ytest'
    63 · 2308
    20 · 2308
    63
    20
     1 2 3 4
     8 23 12 20
    1 2 3 4
    3 6 6 5
     svm(formula = y \sim ., data = dat, kernel = "linear", cost = 10)
    Parameters:
       SVM-Type: C-classification
      SVM-Kernel: linear
            cost: 10
    Number of Support Vectors: 58
     ( 20 20 11 7 )
    Number of Classes: 4
    Levels:
     1 2 3 4
    pred.te 1 2 3 4
          1 3 0 0 0
           20620
           3 0 0 4 0
           4 0 0 0 5
1 n <- 150 # number of data points
 2 p <- 2 # dimension
 3 sigma <- 1 # variance of the distribution
 4 meanpos <- 0 # centre of the distribution of positive examples
5 meanneg <- 3 # centre of the distribution of negative examples
 6 npos <- round(n/2) # number of positive examples
7 nneg <- n-npos # number of negative examples
 8 # Generate the positive and negative examples
9 xpos <- matrix(rnorm(npos*p,mean=meanpos,sd=sigma),npos,p)</pre>
10 xneg <- matrix(rnorm(nneg*p,mean=meanneg,sd=sigma),npos,p)</pre>
11 x <- rbind(xpos,xneg)</pre>
12 # Generate the labels
13 y <- matrix(c(rep(1,npos),rep(-1,nneg)))</pre>
14 # Visualize the data
15 plot(x,col=ifelse(y>0,1,2))
16 legend("topleft",c('Positive','Negative'),col=seq(2),pch=1,text.col=seq(2))
18 ntrain <- round(n*0.8) # number of training examples
             sample(n,ntrain) # indices of training samples
20 xtrain <- x[tindex,]
21 xtest <- x[-tindex,]</pre>
22 ytrain <- y[tindex]
23 ytest <- y[-tindex]
24 istrain=rep(0,n)
25 istrain[tindex]=1
26 # Visualize
27 plot(x,col=ifelse(y>0,1,2),pch=ifelse(istrain==1,1,2))
28 legend("topleft",c('Positive Train','Positive Trest','Negative Train','Negative Test'),col=c(1,1,2,2), pch=c(1,2,1,2), text.col=c(1,1,2,2))
30
```

```
    Positive Train
    △ Positive Test

 1 data(iris)
 2 attach(iris)
 4 ## classification mode
 5 # default with factor response:
 6 model <- svm(Species \sim ., data = iris)
 8 # alternatively the traditional interface:
 9 x <- subset(iris, select = -Species)
10 y <- Species
11 model <- svm(x, y)
12
13 print(model)
14 summary(model)
15
16 # test with train data
17 pred <- predict(model, x)
18 # (same as:)
19 pred <- fitted(model)
21 # Check accuracy:
22 table(pred, y)
23
24 # compute decision values and probabilities:
25 pred <- predict(model, x, decision.values = TRUE)</pre>
26 attr(pred, "decision.values")[1:4,]
28 # visualize (classes by color, SV by crosses):
29 plot(cmdscale(dist(iris[,-5])),
        col = as.integer(iris[,5]),
30
31
        pch = c("o","+")[1:150 \%in\% model\$index + 1])
33 ## try regression mode on two dimensions
34
35 # create data
36 \times - seq(0.1, 5, by = 0.05)
37 y <- \log(x) + rnorm(x, sd = 0.2)
39 # estimate model and predict input values
40 m \leftarrow svm(x, y)
41 new <- predict(m, x)
42
43 # visualize
44 plot(x, y)
45 points(x, log(x), col = 2)
46 points(x, new, col = 4)
47
48 ## density-estimation
50 # create 2-dim. normal with rho=0:
51 X <- data.frame(a = rnorm(1000), b = rnorm(1000))
52 attach(X)
53
54 # traditional way:
55 m <- svm(X, gamma = 0.1)
57 # formula interface:
58 m <- svm(~., data = X, gamma = 0.1)
59 # or:
60 m <- svm(\sim a + b, gamma = 0.1)
62 # test:
63 newdata <- data.frame(a = c(0, 4), b = c(0, 4))
64 predict (m, newdata)
66 # visualize:
67 plot(X, col = 1:1000 %in% m$index + 1, x \lim = c(-5,5), y \lim = c(-5,5))
68 points(newdata, pch = "+", col = 2, cex = 5)
70 # weights: (example not particularly sensible)
71 i2 <- iris
72 levels(i2$Species)[3] <- "versicolor"
73 summary(i2$Species)
74 wts <- 100 / table(i2$Species)
75 wts
76 m <- svm(Species \sim ., data = i2, class.weights = wts)
```

```
Call:
svm.default(x = x, y = y)
Parameters:
SVM-Type: C-classification
SVM-Kernel: radial
cost: 1
Number of Support Vectors: 51
Call:
svm.default(x = x, y = y)
Parameters:
 SVM-Type: C-classification
SVM-Kernel: radial
        cost: 1
Number of Support Vectors: 51
 ( 8 22 21 )
Number of Classes: 3
Levels:
 setosa versicolor virginica
               setosa versicolor virginica
pred
  setosa
                    50
   versicolor
                                 48
  virginica
                        A matrix: 4 × 3 of type dbl
     setosa/versicolor setosa/virginica versicolor/virginica
                                    1.091757
 1
               1.196152
                                                             0.6708810
                                     1.056185
                                                             0.8483518
 2
               1.064621
                                     1.074542
 3
                1.180842
                                                             0.6439798
                1.110699
                                     1.053012
                                                             0.6782041
cmdscale(dist(iris[, -5]))[,2]
    0.0
    -1.0
                         cmdscale(dist(iris[, -5]))[,1]
        TRUE 2:
                       FALSE
```



```
1 library(e1071)
 2 m1 <- matrix( c(
30, 0, 0,
                    1, 1,
                                        1, 2, 3, 2, 3, 3, 0, 1,2,3,
4 0, 1, 2, 3,
5 1, 2, 3,
                     2, 3,
                                        0, 0, 0, 1, 1, 2, 4, 4,4,4, 0,
                               3,
6 1, 2, 3,
7 1, 1, 1,
                    1, 1, 1, -1,-1, -1,-1,-1, 1,1,1,1, 1,
8 1,-1,-1
9 ), ncol = 3 )
10
11 Y = m1[,3]
12 X = m1[,1:2]
13
14 df = data.frame(X, Y)
15
16 par(mfcol=c(4,2))
17 for( cost in c( 1e-3 ,1e-2 ,1e-1, 1e0, 1e+1, 1e+2 ,1e+3)) {
18 #cost <- 1
19 model.svm <- svm( Y \sim . , data = df , type = "C-classification" , kernel =
20 "linear", cost = cost,
21
                            scale =FALSE )
22 #print(model.svm$SV)
23
24 plot(x=0,ylim=c(0,5), xlim=c(0,3),main= paste( "cost: ",cost, "\#SV: ",
25 nrow(model.svm$SV) ))
26 points(m1[m1[,3]>0,1], m1[m1[,3]>0,2], pch=3, col="green")
27 points(m1[m1[,3]<0,1], m1[m1[,3]<0,2], pch=4, col="blue")
28 points(model.svm$SV[,1],model.svm$SV[,2], pch=18, col = "red")
29 }
30
               cost: 0.01 #SV: 16
                                           cost: 100 #SV: 3
                                        0.5 1.0 1.5 2.0 2.5 3.0
            0.5 1.0 1.5 2.0 2.5 3.0
                cost: 1#SV: 8
1 # load the kernlab package
2 install.packages("kernlab")
 3 library(kernlab)
 4 # train the SVM
5 svp <- ksvm(xtrain,ytrain,type="C-svc",kernel='vanilladot',C=100,scaled=c())</pre>
 6 #Look and understand what svp contains
7 # General summary
8 svp
9 # Attributes that you can access
10 attributes(svp)
11 # For example, the support vectors
12 alpha(svp)
13 alphaindex(svp)
```

14 b(svp)

18

16 plot(svp,data=xtrain)

15 # Use the built-in function to pretty-plot the classifier

```
Installing package into '/usr/local/lib/R/site-library'
          (as 'lib' is unspecified)
            Setting default kernel parameters
          Support Vector Machine object of class "ksvm"
          SV type: C-svc (classification)
           parameter : cost C = 100
          Linear (vanilla) kernel function.
          Number of Support Vectors : 3
          Objective Function Value : -83.3392
          Training error : 0
          $param
          $param$C
          [1] 100
          $scaling
            `\001NULL\001`
          $coef
          $coef[[1]]
          [1] 78.294374 -83.301146 5.006772
          $alphaindex
          $alphaindex[[1]]
          [1] 32 81 87
          [1] -28.34212
          $obj
          [1] -83.33923
          $SVindex
          [1] 32 81 87
          $nSV
          [1] 3
          $prior
          $prior[[1]]
          $prior[[1]]$prior1
          $prior[[1]]$prior0
          [1] 58
          $prob.model
          $prob.model[[1]]
          NULL
          $alpha[[1]]
          [1] 78.294374 83.301146 5.006772
          $type
          [1] "C-svc"
          $kernelf
          Linear (vanilla) kernel function.
          $kpar
          list()
          $xmatrix
         $xmatrix[[1]]
X1
          32 1.511672 1.557370
          81 1.485503 1.755448
          87 -0.275778 2.658658
          $ymatrix
            $fitted
               [1] \quad 1 \, \cdot 1 \quad 1 \, \cdot 
             $lev
          [1] -1 1
          $nclass
          [1] 2
1 #### Use text with string kernels
2 data(reuters)
3 is(reuters)
4 tsv <- ksvm(reuters,rlabels,kernel="stringdot",
                                   kpar=list(length=5),cross=3,C=10)
6 tsv
          'list' 'vector' 'listOrNULL' 'input' 'listl' 'lpinput' 'output'
          Support Vector Machine object of class "ksvm"
          SV type: C-svc (classification)
            parameter : cost C = 10
          String kernel function. Type = spectrum
            Hyperparameters : sub-sequence/string length = 5
            Normalized
          Number of Support Vectors : 39
          Objective Function Value : -13.6834
          Training error : 0
          Cross validation error : 0.128205
                  1 32 81 87
```

5

8