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1 Contest

2 Data structures

Contest (1)

template.cpp 88 lines

```
// #pragma comment(linker, "/stack:200000000")
// #pragma GCC optimize("Ofast")
// #pragma GCC optimize("O3,unroll-loops")
// #pragma GCC target("sse,sse2,sse3,ssse3,sse4,avx2")

// #define _GLIBCXX_DEBUG
// #define _GLIBCXX_DEBUG_PEDANTIC

#include <iostream>
#include <vector>
#include <algorithm>
#include <map>
#include <set>
#include <queue>
#include <deque>
#include <cmath>
#include <climits>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

using namespace __gnu_pbds;
using namespace std;

const int MOD = 998244353;
using ll = long long;
const ll INF = 1e18;

// #define int ll

template<typename T>
using ordered_set = tree<T,null_type,less<T>,rb_tree_tag,
    tree_order_statistics_node_update>;

template<typename T>
using graph = vector<vector<T>>;

template<typename T>
istream& operator>>(istream& in, vector<T>& a) {
    for (auto& i: a) {
        in >> i;
    }
    return in;
}

template<typename T>
ostream& operator<<(ostream& out, vector<T>& a) {
    for (auto& i: a) {
        out << i << " ";
    }
    return out;
}

int fast_pow(int a, int b, int mod) {
    if (b == 0)
        return 1;
    if (b % 2) {
        return (a * fast_pow(a, b - 1, mod)) % mod;
    }
    int k = fast_pow(a, b / 2, mod);
    return (k * k) % mod;
}
```

```
1 }

1 int fast_pow(int a, int b) {
    if (b == 0)
        return 1;
    if (b % 2) {
        return (a * fast_pow(a, b - 1));
    }
    int k = fast_pow(a, b / 2);
    return (k * k);
}

void solve() {

}

int32_t main(int32_t argc, const char * argv[]) {
    cin.tie(0);
    cout.tie(0);
    ios_base::sync_with_stdio(0);
    // insert code here...
    int tt= 1;
    // std::cin >> tt;
    while (tt--) {
        solve();
    }
    return 0;
}
```

.bashrc 3 lines

```
alias c='g++ -Wall -Wconversion -Wfatal-errors -g -std=c++20 \
    -fsanitize=undefined,address'
xmodmap -e 'clear lock' -e 'keycode 66=less greater' #caps =<
```

.vimrc 6 lines

```
set cin aw ai is ts=4 sw=4 tm=50 nu noeb bg=dark ru cul
sy on | im jk <esc> | im kj <esc> | no ; :
" Select region and then type :Hash to hash your selection.
" Useful for verifying that there aren't mistypes.
ca Hash w !cpp -dD -P -fpreprocessed \ | tr -d '[:space:]' \
    \ | md5sum \ | cut -c-6
```

hash.sh 3 lines

```
# Hashes a file, ignoring all whitespace and comments. Use for
# verifying that code was correctly typed.
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum | cut -c-6
```

Data structures (2)

SegmentTreeNode.h

Description: Customizable segment tree node.

Time: update - $\mathcal{O}(\log N)$, get - $\mathcal{O}(\log N)$

ed0532, 116 lines

```
template<class T, T default_value, T (*merge_value)(const T&,
    const T&), void (*update_value)(T&, const T&)>
class Node {
protected:
    using NodeT = Node<T, default_value, merge_value,
        update_value>;
    using ll = long long;

    Node* left = nullptr;
    Node* right = nullptr;

    T value;
```

```
Node* my_copy() {
    Node* result = new NodeT();
    result->left = this->left;
    result->right = this->right;
    result->value = this->value;
    return result;
}

Node* get_left_node() {
    if(left == nullptr)
        left = new NodeT();
    return left;
}

Node* get_right_node() {
    if(right == nullptr)
        right = new NodeT();
    return right;
}

const T& get_left_val() const {
    if(left == nullptr)
        return default_value;
    return left->value;
}

const T& get_right_val() {
    if(right == nullptr)
        return default_value;
    return right->value;
}

void recalculate() {
    if(!left && !right) {
        this->value = default_value;
        return;
    }
    if(!left) {
        this->value = merge_value(default_value,
            get_right_node()->value);
        return;
    }
    if(!right) {
        this->value = merge_value(get_left_node()->value,
            default_value);
        return;
    }
    this->value = merge_value(get_left_node()->value,
        get_right_node()->value);
}

void upd_acreate_shadow(ll l, ll r, ll pos, T new_value) {
    if (l == r) {
        update_value(this->value, move(new_value));
        return;
    }
    ll m = (l + r) / 2;
    if(pos <= m) {
        if(this->left) {
            this->left = this->left->upd_acreate(l, m, pos,
                move(new_value));
        } else {
            this->left = new NodeT();
            this->left->upd(l, m, pos, move(new_value));
        }
    } else {
        if(this->right) {
```

```

        this->right = this->right->upd_acreate(m + 1, r
        , pos, move(new_value));
    } else {
        this->right = new NodeT();
        this->right->upd(m + 1, r, pos, move(new_value)
        );
    }
}
recalculate();
}

public:
explicit Node(): value(default_value) {}

void upd(ll l, ll r, ll pos, T new_value) {
    if(l == r) {
        update_value(this->value, move(new_value));
        return;
    }
    ll m = (l + r) / 2;
    (pos <= m ? get_left_node()->upd(l, m, pos, move(
        new_value)) : get_right_node()->upd(m + 1, r, pos,
        move(new_value)));
    recalculate();
}

Node* upd_acreate(ll l, ll r, ll pos, T new_value) {
    Node* result = my_copy();
    result->upd_acreate_shadow(l, r, pos, new_value);
    return result;
}

T get(ll l, ll r, ll L, ll R) {
    if(r < L || R < l)
        return default_value;
    if(L <= l && r <= R)
        return this->value;
    ll m = (l + r) / 2;

    if(!left && !right) return this->value;
    if(!left) return right->get(m + 1, r, L, R);
    if(!right) return left->get(l, m, L, R);

    return merge_value(get_left_node()->get(l, m, L, R),
        get_right_node()->get(m + 1, r, L, R));
}
};

```

SegmentTree.h

Description: Customizable segment tree

Time: update - $\mathcal{O}(\log N)$, get - $\mathcal{O}(\log N)$

<SegmentTreeNode.h> 412028, 19 lines

```

template<class T, T default_value, T (*merge_value)(const T&,
    const T&), void (*update_value)(T&, const T&)>
class Tree {
private:
    ll l, r;
    Node<T, default_value, merge_value, update_value>* root =
        nullptr;
public:
    Tree(ll l, ll r): l(l), r(r), root(new Node<T,
        default_value, merge_value, update_value>()) {}

    void upd(ll pos, T value) {
        root->upd(l, r, pos, move(value));
    }

    T get(ll L, ll R) {
        return root->get(l, r, L, R);
    }
}

```

```

    }
};

template<class T, T default_value>
using SumTree = Tree<T, default_value, sum<T>, add_value<T>>;

PersistentSegmentTree.h
Description: Persistent segment tree
Time: update -  $\mathcal{O}(\log N)$ , get -  $\mathcal{O}(\log N)$ 
<SegmentTreeNode.h> 04748a, 22 lines

template<class T, T default_value, T (*merge_value)(const T&,
    const T&), void (*update_value)(T&, const T&)>
class PersistentTree {
private:
    ll l, r;
    vec<Node<T, default_value, merge_value, update_value>*>
        roots;
public:
    PersistentTree(ll l, ll r): l(l), r(r) {
        roots.push_back(new Node<T, default_value, merge_value,
            update_value>());
    }

    size_t update(ll pos, T value) {
        roots.push_back(roots[roots.size() - 1]->upd_acreate(l,
            r, pos, move(value)));
        return roots.size() - 1;
    }

    T get(ll tree_id, ll L, ll R) {
        return roots[tree_id]->get(l, r, L, R);
    }
};

template<class T, T default_value>
using PersistentSumTree = PersistentTree<T, default_value, max<
    T>, set_value<T>>;

```

Strings (3)

ZFunction.h

Description: Z-functions, $z[i]$ equal to the length of largest common prefix of string s and suffix of s starting at i .

Time: $\mathcal{O}(N)$, N - size of string s

0c3dd4, 16 lines

```

vector<int> z_function(const string& s) {
    int n = s.size();
    vector<int> z(n);
    int l = 0, r = 0;
    for (int i = 1; i < n; i++) {
        if (i <= r)
            z[i] = max(r - i + 1, z[i - l]);
        while (z[i] + i < n && s[z[i] + i] == s[z[i]])
            z[i]++;
        if (z[i] + i - 1 > r) {
            r = z[i] + i - 1;
            l = i;
        }
    }
    return z;
}

```

SuffixArray.h

Description: Suffix array will contain integers that represent the starting indexes of the all the suffixes of a given string, after the aforementioned suffixes are sorted.

Time: $\mathcal{O}(N * \log_2(N))$, N - size of string s

```

vector<int> suffix_arrays(string s) {
    s = s + "$";
    int n = s.size();

    vector<int> p(n);
    vector<vector<int>> c(20, vector<int>(n));
    int alphabet = 256;

    auto set_classes = [&](int k) {
        int classes = 0;
        c[k][p[0]] = classes++;
        for (int i = 1; i < n; i++) {
            auto cur = pair{c[k - 1][p[i]], c[k - 1][(p[i] + (1<<(k
                - 1))) % n]};
            auto prev = pair{c[k - 1][p[i - 1]], c[k - 1][(p[i - 1] +
                (1<<(k - 1))) % n]};
            if (cur == prev) {
                c[k][p[i]] = c[k][p[i - 1]];
            } else {
                c[k][p[i]] = classes++;
            }
        }
    };

    auto init_base = [&]() {
        vector<int> cnt(alphabet);
        for (int i = 0; i < n; i++) {
            cnt[s[i]]++;
        }
        for (int i = 1; i < alphabet; i++) {
            cnt[i] += cnt[i - 1];
        }
        for (int i = n - 1; i >= 0; i--) {
            p[cnt[s[i]] - 1] = i;
            cnt[s[i]]--;
        }

        int classes = 0;
        c[0][p[0]] = classes++;
        for (int i = 1; i < n; i++) {
            if (s[p[i]] == s[p[i - 1]]) {
                c[0][p[i]] = c[0][p[i - 1]];
            } else {
                c[0][p[i]] = classes++;
            }
        }
    };

    init_base();

    for (int k = 0; (1<<k) < n; k++) {
        vector<int> pn(n), cnt(n);
        for (int i = 0; i < n; i++) {
            pn[i] = (p[i] - (1<<k) + n) % n;
            cnt[c[k][pn[i]]]++;
        }

        for (int i = 0; i < alphabet; i++)
            cnt[i] += cnt[i - 1];

        for (int i = n - 1; i >= 0; i--) {
            p[cnt[c[k][pn[i]] - 1] = pn[i];
            cnt[c[k][pn[i]]]--;
        }

        set_classes(k + 1);
    }
}

```

```
    p.erase(p.begin());  
    return p;  
}
```

Techniques (A)

techniques.txt	159 lines
Recursion	
Divide and conquer	
Finding interesting points in N log N	
Algorithm analysis	
Master theorem	
Amortized time complexity	
Greedy algorithm	
Scheduling	
Max contiguous subvector sum	
Invariants	
Huffman encoding	
Graph theory	
Dynamic graphs (extra book-keeping)	
Breadth first search	
Depth first search	
* Normal trees / DFS trees	
Dijkstra's algorithm	
MST: Prim's algorithm	
Bellman-Ford	
Konig's theorem and vertex cover	
Min-cost max flow	
Lovasz toggle	
Matrix tree theorem	
Maximal matching, general graphs	
Hopcroft-Karp	
Hall's marriage theorem	
Graphical sequences	
Floyd-Warshall	
Euler cycles	
Flow networks	
* Augmenting paths	
* Edmonds-Karp	
Bipartite matching	
Min. path cover	
Topological sorting	
Strongly connected components	
2-SAT	
Cut vertices, cut-edges and biconnected components	
Edge coloring	
* Trees	
Vertex coloring	
* Bipartite graphs (=> trees)	
* 3^n (special case of set cover)	
Diameter and centroid	
K'th shortest path	
Shortest cycle	
Dynamic programming	
Knapsack	
Coin change	
Longest common subsequence	
Longest increasing subsequence	
Number of paths in a dag	
Shortest path in a dag	
Dynprog over intervals	
Dynprog over subsets	
Dynprog over probabilities	
Dynprog over trees	
3^n set cover	
Divide and conquer	
Knuth optimization	
Convex hull optimizations	
RMQ (sparse table a.k.a 2^k-jumps)	
Bitonic cycle	
Log partitioning (loop over most restricted)	
Combinatorics	

Computation of binomial coefficients
Pigeon-hole principle
Inclusion/exclusion
Catalan number
Pick's theorem
Number theory
Integer parts
Divisibility
Euclidean algorithm
Modular arithmetic
* Modular multiplication
* Modular inverses
* Modular exponentiation by squaring
Chinese remainder theorem
Fermat's little theorem
Euler's theorem
Phi function
Frobenius number
Quadratic reciprocity
Pollard-Rho
Miller-Rabin
Hensel lifting
Vieta root jumping
Game theory
Combinatorial games
Game trees
Mini-max
Nim
Games on graphs
Games on graphs with loops
Grundy numbers
Bipartite games without repetition
General games without repetition
Alpha-beta pruning
Probability theory
Optimization
Binary search
Ternary search
Unimodality and convex functions
Binary search on derivative
Numerical methods
Numeric integration
Newton's method
Root-finding with binary/ternary search
Golden section search
Matrices
Gaussian elimination
Exponentiation by squaring
Sorting
Radix sort
Geometry
Coordinates and vectors
* Cross product
* Scalar product
Convex hull
Polygon cut
Closest pair
Coordinate-compression
Quadtrees
KD-trees
All segment-segment intersection
Sweeping
Discretization (convert to events and sweep)
Angle sweeping
Line sweeping
Discrete second derivatives
Strings
Longest common substring
Palindrome subsequences

Knuth-Morris-Pratt
Tries
Rolling polynomial hashes
Suffix array
Suffix tree
Aho-Corasick
Manacher's algorithm
Letter position lists
Combinatorial search
Meet in the middle
Brute-force with pruning
Best-first (A*)
Bidirectional search
Iterative deepening DFS / A*
Data structures
LCA (2^k-jumps in trees in general)
Pull/push-technique on trees
Heavy-light decomposition
Centroid decomposition
Lazy propagation
Self-balancing trees
Convex hull trick (wcipeg.com/wiki/Convex_hull_trick)
Monotone queues / monotone stacks / sliding queues
Sliding queue using 2 stacks
Persistent segment tree