

Uzhhorod National University

UzhNU Machata

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Contest (1)	
template.cpp	
// #pragma comment(linker, "/stack:200000000") // #pragma GCC optimize("Ofast") // #pragma GCC optimize("O3, unroll—loops") // #pragma GCC target("sse,sse2,sse3,ssse3,sse4") // #pragma GCC target("avx2,bmi,bmi2,popcnt,lzcnt")	101 lines
// #define _GLIBCXX_DEBUG // #define _GLIBCXX_DEBUG_PEDANTIC	
<pre>#include <cassert> #include <iomanip> #include <iostream> #include <vector> #include <algorithm> #include <map> #include <functional> #include <array> #include <array> #include <queue> #include <queue> #include <catority #include="" <array=""> #include <array> #</array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></array></catority></queue></queue></array></array></functional></map></algorithm></vector></iostream></iomanip></cassert></pre>	
<pre>const long double PI = 3.141592653589793; using ll = long long; const ll INF = le18; // #define int ll</pre>	
//> sashko123's defines:	
<pre>#define itn int</pre>	

```
int input()
   int x:
   cin>>x;
   return x;
template<typename T>
using graph = vector<vector<T>>;
template<typename T>
istream& operator>>(istream& in, vector<T>& a) {
   for (auto& i: a) {
      in >> i;
   }
   return in;
11 fast_pow(ll a, ll b, ll mod) {
   if (b == 0)
      return 1;
   if (b % 2) {
       return (111 * a * fast_pow(a, b - 1, mod)) % mod;
   11 k = fast_pow(a, b / 2, mod);
   return (111 * k * k) % mod;
11 fast pow(ll a, ll b) {
   if (b == 0)
       return 1:
   if (b % 2) {
       return (111 * a * fast_pow(a, b - 1));
   11 k = fast pow(a, b / 2);
   return (111 * k * k);
void solve() {
int32 t main(int32 t argc, const char * argv[]) {
   cin.tie(0);
   cout.tie(0);
   ios_base::sync_with_stdio(0);
   // insert code here...
   int tt= 1;
   // std::cin >> tt;
   while (tt--) {
       solve();
   return 0;
fast-input.h
double readNumber() {
   const int BSIZE = 4096;
```

static char buffer[BSIZE]; static char* bptr = buffer + BSIZE;

> if (bptr == buffer + BSIZE) { memset (buffer, 0, BSIZE);

> > cin.read(buffer, BSIZE);

auto getChar = []() {

```
35 lines
```

```
bptr = buffer;
   return *bptr++;
};
char c = getChar();
while (c && (c < '0' | | c > '9') && c != '-')
   c = getChar();
bool minus = false;
if (c == '-') minus = true, c = getChar();
double res = 0:
while (c >= '0' \&\& c <= '9') {
   res = res * 10 + c - '0';
   c = getChar();
 if (c == '.') {
   c = getChar();
   double cur = 0.1;
   while (c >= '0' \&\& c <= '9') {
       res = res + (c - '0') * cur;
       c = getChar();
       cur /= 10.0;
return minus ? -res : res;
```

.bashrc

3 lines alias c='q++ -Wall -Wconversion -Wfatal-errors -q -std=c++20 \ -fsanitize=undefined,address' xmodmap -e 'clear lock' -e 'keycode 66=less greater' #caps = \$

.vimrc

set cin aw ai is ts=4 sw=4 tm=50 nu noeb bg=dark ru cul sy on | im jk <esc> | im kj <esc> | no; : " Select region and then type : Hash to hash your selection. " Useful for verifying that there aren't mistypes. ca Hash w !cpp -dD -P -fpreprocessed \| tr -d '[:space:]' \ \| md5sum \| cut -c-6

6 lines

hash.sh

Hashes a file, ignoring all whitespace and comments. Use for # verifying that code was correctly typed. cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum |cut -c-6

Algebra (2)

xor-basis.h

Description: Xor basis, all elements in the main set can be constructed using xor operation and elements in the basis

Time: insert per element - $\mathcal{O}(log(A_max))$

```
hash46 lines
template<typename T = int, int max_bit = 31>
struct xor basis
 std::vector<T> basis; // basis[i] -> element with smallest
      set bit equal to i
 int sz; // Current size of the basis
 xor_basis() {
   basis.assign(max_bit);
 bool insert(T val) {
```

```
for (int i = 0; i < max bit; i++) {
     if (((val >> i)&1) == 0)
       continue;
      if (!basis[i]) {
       basis[i] = val;
       sz++;
       return true;
     val ^= basis[i];
    return false;
  bool contains (T val) {
    for (int i = 0; i < max_bit; i++) {</pre>
     if (((val >> i)&1) == 0)
       continue;
     if (!basis[i]) {
       return false;
     val ^= basis[i];
    return true;
 T max_element() { // not-sure
   T val = 0;
    for (int i = \max bit - 1; i >= 0; i--) {
     if (basis[i] && !((val>>i)&1)) {
       val ^= basis[i];
   }
    return val;
};
Description: FFT implementation
<vector>, <complex>
using cd = std::complex<double>;
```

Time: (n + m) * log(n + m)

```
hash56 lines
void fft(std::vector<cd> & a, bool invert) {
    int n = a.size();
    for (int i = 1, j = 0; i < n; i++) {
       int bit = n >> 1;
        for (; j & bit; bit >>= 1)
           j ^= bit;
        j ^= bit;
       if (i < j)
            swap(a[i], a[j]);
    for (int len = 2; len <= n; len <<= 1) {
       double ang = 2 * PI / len * (invert ? -1 : 1);
       cd wlen(cos(ang), sin(ang));
        for (int i = 0; i < n; i += len) {
           cd w(1);
            for (int j = 0; j < len / 2; j++) {
               cd u = a[i+j], v = a[i+j+len/2] * w;
                a[i+j] = u + v;
               a[i+j+len/2] = u - v;
                w \star = wlen;
```

```
if (invert) {
        for (cd & x : a)
           x /= n;
template<typename T>
std::vector<T> multiply(const std::vector<T>& a, const std::
    vector<T>& b) {
    std::vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end
    int n = 1;
    while (n < a.size() + b.size())</pre>
       n <<= 1;
    fa.resize(n);
    fb.resize(n);
    fft(fa, false);
    fft(fb, false);
    for (int i = 0; i < n; i++)
       fa[i] *= fb[i];
    fft(fa, true);
    std::vector<T> result(n);
    for (int i = 0; i < n; i++)
       result[i] = round(fa[i].real());
    result.resize(a.size() + b.size() - 1);
    return result;
```

hash68 lines

<vector>

Description: NNT implementation by modulo 998244353 Time: (n + m) * log(n + m)

```
const int root = 31; // primitive root of module
const int root_1 = fast_pow(root, MOD - 2, MOD); // (primitive
    root) ^ −1
const int root_pw = 1 << 23; // max power of 2 in MOD - 1</pre>
inline int inverse(int n, int mod) {
 return fast_pow(n, mod - 2, mod);
void nnt(std::vector<int> &a, bool invert, int mod) {
   int n = a.size();
    for (int i = 1, j = 0; i < n; i++) {
       int bit = n >> 1;
       for (; j & bit; bit >>= 1)
           j ^= bit;
       j ^= bit;
       if (i < j)
            std::swap(a[i], a[j]);
    for (int len = 2; len <= n; len <<= 1) {
       int wlen = invert ? root_1 : root;
       for (int i = len; i < root pw; i <<= 1)
           wlen = (int) (1LL * wlen * wlen % mod);
       for (int i = 0; i < n; i += len) {
           int w = 1:
            for (int j = 0; j < len / 2; j++) {
               int u = a[i+j], v = (int)(1LL * a[i+j+len/2] *
                     w % mod);
               a[i+j] = u + v < mod ? u + v : u + v - mod;
                a[i+j+len/2] = u - v >= 0 ? u - v : u - v + mod
```

```
w = (111 * w * wlen % mod);
       }
    if (invert) {
        int n_1 = inverse(n, mod);
        for (int& x : a)
            x = (111 * x * n_1 % mod);
std::vector<int> multiply(const std::vector<int>& a, const std
    ::vector<int>& b, int mod) {
 int n = a.size(), m = b.size();
 int k = n + m - 1;
 int 1 = 1;
 while (1 < k)
  1 <<= 1;
 std::vector<int> A(1), B(1);
 for (int i = 0; i < n; i++) {
   A[i] = a[i];
 for (int i = 0; i < m; i++) {
   B[i] = b[i];
 nnt(A, false, mod);
 nnt(B, false, mod);
  for (int i = 0; i < B.size(); i++) {
   A[i] = (111 * A[i] * B[i]) % mod;
  nnt(A, true, mod);
 A.resize(k);
 return A;
floor-sum.h
Description:
                             sum_{i=0}^{n-1}
floor((a * i + b) / m)
Time: log(n)
<utility>
                                                        hash24 lines
using ull = unsigned long long;
ull floor sum unsigned(ull n, ull m, ull a, ull b) {
    ull ans = 0;
    while (true) {
        if (a >= m) {
            ans += n * (n - 1) / 2 * (a / m);
            a %= m;
        if (b >= m) {
            ans += n * (b / m);
            b %= m;
        ull y_max = a * n + b;
        if (y_max < m) break;</pre>
        // y_{-}max < m * (n + 1)
```

 $// floor(y_max / m) \le n$

n = (ull) (v max / m);

 $b = (ull) (y_max % m);$

std::swap(m, a);

return ans:

```
berlekamp-massev.h
Description: For given n first elements of sequence a, return array c, a[i] =
sum(j = 1 ... -c-) a[i-j] * c[j]
Time: \mathcal{O}(n^2)
                                                         hash45 lines
template<typename T>
vector<T> berlekamp massey(const vector<T> &s) {
    vector<T> c:
    vector<T> oldC;
    int f = -1:
    for (int i=0; i<(int)s.size(); i++) {</pre>
       T delta = s[i];
        for (int j=1; j<=(int)c.size(); j++)
            delta -= c[j-1] * s[i-j];
        if (delta == 0)
            continue;
        if (f == -1) {
            c.resize(i + 1);
            mt19937 rng(chrono::steady_clock::now().
                 time_since_epoch().count());
            for (T &x : c)
                x = rnq();
            f = i:
        } else {
            vector<T> d = oldC;
            for (T &x : d)
                x = -x;
            d.insert(d.begin(), 1);
            T df1 = 0:
            for (int j=1; j<=(int)d.size(); j++)</pre>
                df1 += d[j-1] * s[f+1-j];
            assert (df1 != 0);
            T coef = delta / dfl;
            for (T &x : d)
                x *= coef;
            vector<T> zeros(i - f - 1);
            zeros.insert(zeros.end(), d.begin(), d.end());
            d = zeros:
            vector<T> temp = c;
            c.resize(max(c.size(), d.size()));
            for (int j=0; j<(int)d.size(); j++)</pre>
                c[j] += d[j];
            if (i - (int) temp.size() > f - (int) oldC.size())
                oldC = temp;
                f = i;
    return c;
Numeric (3)
primitive-root.h
Description: Primitive root of n
                                                         hash54 lines
constexpr long long safe_mod(long long x, long long m) {
   x %= m;
    if (x < 0) x += m;
    return x:
```

long long pow_mod(long long x, long long n, int m) {

unsigned int _m = (unsigned int)(m);

unsigned long long y = safe_mod(x, m);

if (m == 1) return 0;

unsigned long long r = 1;

```
while (n) {
        if (n \& 1) r = (r * y) % _m;
        y = (y * y) % _m;
        n >>= 1;
    return r;
int primitive_root(int m) {
    if (m == 2) return 1;
    if (m == 167772161) return 3:
    if (m == 469762049) return 3;
    if (m == 754974721) return 11;
    if (m == 998244353) return 3;
    int divs[20] = {};
    divs[0] = 2;
    int cnt = 1;
    int x = (m - 1) / 2;
    while (x \% 2 == 0) x /= 2;
    for (int i = 3; (long long)(i)*i <= x; i += 2) {
        if (x % i == 0) {
            divs[cnt++] = i;
            while (x \% i == 0) {
                x /= i;
    if (x > 1) {
        divs[cnt++] = x;
    for (int g = 2;; g++) {
        bool ok = true;
        for (int i = 0; i < cnt; i++) {
            if (pow_mod(g, (m - 1) / divs[i], m) == 1) {
                ok = false:
                break;
        if (ok) return q;
template <int m> constexpr int primitive_root = primitive_root(
pollard-rho.h
Description: Finds divider of N.
Time: \mathcal{O}\left(N^{(1/4)} * log(N)\right)
<numeric>
                                                        hash20 lines
long long mult (long long a, long long b, long long mod) {
    return (__int128)a * b % mod;
long long f(long long x, long long c, long long mod) {
    return (mult(x, x, mod) + c) % mod;
long long rho(long long n, long long x0=2, long long c=1) {
    long long x = x0;
    long long y = x0;
    long long q = 1;
    while (q == 1) {
       x = f(x, c, n);
       y = f(y, c, n);
        y = f(y, c, n);
        g = std::gcd(abs(x - y), n);
    return g;
```

```
miller-rabin.h
Description: checks whether given number (up to 1e18) is prime
Time: +-\mathcal{O}\left(\log^3(n)\right)
                                                          hash43 lines
using u128 = __uint128_t;
11 fast_pow(ll a, ll b, ll mod) {
    if (b == 0)
        return 1:
    if (b % 2) {
        return ((u128) a * fast_pow(a, b - 1, mod)) % mod;
    11 k = fast_pow(a, b / 2, mod);
    return ((u128) k * k) % mod;
bool check_composite(ll n, ll a, ll d, int s) {
    11 x = fast_pow(a, d, n);
    if (x == 1 | | x == n - 1)
        return false:
    for (int r = 1; r < s; r++) {
        x = (u128) x * x % n;
        if (x == n - 1)
            return false;
    return true;
};
bool miller rabin(ll n) {
    if (n < 2)
        return false;
    int r = 0;
    11 d = n - 1;
    while ((d \& 1) == 0) {
        d >>= 1;
        r++;
    for (int a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37})
        if (n == a)
            return true;
        if (check_composite(n, a, d, r))
            return false;
    return true:
euclidean-algorithm.h
Description: Find x and y, s.t. x^*a + y^*b = gcd(a, b) // extended Eu-
clidean algorithm
Time: \mathcal{O}(loamin(a,b))
<tuple>
                                                          hash12 lines
template<typename T>
std::pair<T, T> euclidean_algorithm(T a, T b) {
    T x = 1, y = 0;
    T \times 1 = 0, y1 = 1, a1 = a, b1 = b;
    while (b1) {
        T q = a1 / b1;
        std::tie(x, x1) = std::make\_tuple(x1, x - q * x1);
        std::tie(y, y1) = std::make\_tuple(y1, y - q * y1);
        std::tie(a1, b1) = std::make_tuple(b1, a1 - q * b1);
    return {x, y};
```

chinese-remainder-theorem.h

Description: Solves chinese remainder theorem.

Time: $\mathcal{O}(n)$, n - number of equations.

hash19 lines

```
struct Congruence {
   long long a, m;
long long chinese_remainder_theorem(vector<Congruence> const&
    congruences) {
    long long M = 1;
   for (auto const& congruence : congruences) {
       M *= congruence.m;
   long long solution = 0;
   for (auto const& congruence : congruences) {
       long long a_i = congruence.a;
       long long M i = M / congruence.m;
       long long N i = mod inv(M i, congruence.m);
       solution = (solution + a_i * M_i % M * N_i) % M;
   return solution;
```

Data structures (4)

fenwick-tree.h

Description: Fenwick Tree, update(+=) at element, sum at segment. R is excluded.

```
Time: update - \mathcal{O}(\log N), get - \mathcal{O}(\log N)
```

```
<cassert>, <vector>
                                                        hash32 lines
template <class T> struct fenwick_tree {
    fenwick_tree() : _n(0) {}
    fenwick_tree(int n) : _n(n), data(n) {}
    void add(int p, T x) {
       assert(0 <= p && p < _n);
        while (p \le _n) \{
            data[p - 1] += T(x);
            p += p & -p;
   T sum(int 1, int r) {
       assert(0 <= 1 && 1 <= r && r <= n);
        return sum(r) - sum(1);
  private:
    int _n;
    std::vector<T> data;
   T sum(int r) {
       T s = 0;
        while (r > 0) {
            s += data[r - 1];
            r -= r & -r;
        return s;
};
```

```
fenwick-tree-2d.h
```

Description: 2d fenwick tree, update(+=) at element, sum at 2d segment. R is excluded.

```
Time: update - \mathcal{O}(\log N * \log M), get - \mathcal{O}(\log N * \log M)
```

template <class T> struct fenwick_tree_2d{

unordered_map<int, T> data;

struct fenwick tree {

int n:

```
fenwick_tree(): n(0) {};
       fenwick_tree(int n): n(n) {};
       void add(int p, T x) {
            assert (0 <= p && p < n);
           p++;
            while (p \le n) {
                data[p - 1] += T(x);
               p += p & -p;
       T pref sum(int r){
           T s = 0;
            while (r > 0) {
               s += data[r - 1];
               r -= r & -r;
           return s;
   };
 std::vector<fenwick tree> data;
 fenwick_tree_2d(int n, int m): n(n), m(m), data(n,
      fenwick tree(m)) {};
 void add(int x, int y, T val) {
       assert(0 <= x && x < n);
   x++:
        while (x \le n) {
           data[x - 1].add(y, val);
           x += x & -x;
 T pref_sum(int xr, int yr){
       T s = 0:
       while (xr > 0) {
           s += data[xr - 1].pref_sum(yr);
            xr -= xr \& -xr;
        return s;
   T sum(int xl, int yl, int xr, int yr) {
       return pref_sum(xr, yr) - pref_sum(xr, yl) - pref_sum(
            xl, yr) + pref_sum(xl, yl);
};
```

segment-tree.h

Description: Segment tree, update(+=) at element, sum at segment. R is excluded.

```
Time: update - \mathcal{O}(\log N), get - \mathcal{O}(\log N)
```

```
template<typename T, int N = (1 << 18)> struct segment_tree {
 std::array<T, 2 * N> tree;
 segment tree() {
```

```
tree.fill(T());
void update(int pos, T val) {
 pos += N;
  tree[pos] += val;
  pos >>= 1;
  while (pos > 0) {
   tree[pos] = tree[pos << 1] + tree[(pos << 1) | 1];
    pos >>= 1;
T get sum(int 1, int r) {
 1 += N;
  r += N;
  T ans = T();
  while (1 < r) {
   if (1 & 1) {
     ans += tree[1++];
    if (r & 1) {
     ans += tree[--r];
   1 >>= 1;
    r >>= 1;
  return ans;
T get(int pos) {
  return tree[N + pos];
```

lazy-segment-tree.h

Description: Segment tree, update(+=) at segment, sum at segment. R is

```
Time: update - \mathcal{O}(\log N), get - \mathcal{O}(\log N)
<array>, <vector>
                                                          hash82 lines
template<typename T> struct lazy_segment_tree {
 struct node{
    T sum = 0;
    T promise = 0;
 };
 int n:
 std::vector<node> tree;
 lazy_segment_tree(int n_, const vector<T>& init): n(n_) {
    tree.assign(4 * n, node{});
    build(1, 0, n, init);
  void build(int v, int l, int r, const vector<T>& init) {
    if (1 + 1 == r) {
      tree[v].sum = init[l];
      return;
    if (1 >= r)
      return:
    int mid = (1 + r) / 2;
    build(2 * v, 1, mid, init);
    build(2 * v + 1, mid, r, init);
    tree[v].sum = (tree[2 * v].sum + tree[2 * v + 1].sum);
```

```
void update(int 1, int r, T value) {
   update(1, 0, n, 1, r, value);
  T get(int 1, int r) {
   return get(1, 0, n, 1, r);
 T get(int pos) {
   return get(1, 0, n, pos, pos + 1);
  void push(int v, int l, int r) {
   if (tree[v].promise == 0)
     return;
   tree[v].sum += tree[v].promise * (r - 1);
   if (1 + 1 < r) {
     tree[2 * v].promise += tree[v].promise;
     tree[2 * v + 1].promise += tree[v].promise;
   tree[v].promise = 0;
  void update(int v, int tl, int tr, int l, int r, T value) {
   push(v, tl, tr);
   if (1 >= tr || t1 >= r)
     return;
    if (1 <= t1 && tr <= r) {
     tree[v].promise += value;
     push(v, tl, tr);
     return;
    int mid = (tl + tr) / 2;
    update (2 * v, t1, mid, 1, r, value);
   update(2 * v + 1, mid, tr, 1, r, value);
    tree[v].sum = tree[2 * v].sum + tree[2 * v + 1].sum;
  T get(int v, int tl, int tr, int l, int r) {
   push(v, tl, tr);
    if (1 >= tr || t1 >= r)
     return 0;
   if (1 <= t1 && tr <= r) {
     return tree[v].sum;
   int mid = (tl + tr) / 2;
   auto left = get(2 * v, tl, mid, l, r);
   auto right = get(2 * v + 1, mid, tr, 1, r);
    return left + right;
};
persistent-segment-tree.h
Description: Persistent segment tree, update(+=) at segment, sum at seg-
ment. R is excluded.
Time: update - \mathcal{O}(\log N), get - \mathcal{O}(\log N)
                                                        hash83 lines
template<typename T> struct persistent_segment_tree {
  struct node {
   T sum:
   int left, right;
   node(T \ val = T()): sum(val), left(-1), right(-1) {}
   node(int left_, int right_): sum(T()), left(left_), right(
         right_) {}
```

```
std::vector<node> tree;
node create node(T val = 0) {
 return node(val);
node create_node(int left, int right) {
  auto v = node(left, right);
  v.sum = (left != -1 ? tree[left].sum : 0) + (right != -1 ?
      tree[right].sum : 0);
  return v:
int LAST = 0:
template<typename... params>
int new_node(params... args) {
  tree[++LAST] = create_node(args...);
  return LAST;
int n;
persistent_segment_tree(int n_, int sz_, const vector<T>& a,
     int& first_root): n(n_) {
  tree.resize(sz_);
  first root = build(0, n, a);
int build(int 1, int r, const vector<T>& a) {
  if (1 + 1 == r) {
   return new node(a[1]);
  int mid = (r + 1) / 2;
  int left = build(1, mid, a);
  int right = build(mid, r, a);
  return new_node(left, right);
int update(int root, int pos, T val) {
  return update(root, 0, n, pos, val);
T get(int root, int 1, int r) {
  return get (root, 0, n, 1, r);
T get(int root, int pos) {
  return get(root, 0, n, pos, pos + 1);
int update(int v, int l, int r, int pos, T val) {
  if (1 + 1 == r) {
    return new_node(val + tree[v].sum);
  int mid = (1 + r) / 2;
  if (pos < mid) {
    return new_node(
      update(tree[v].left, 1, mid, pos, val),
      tree[v].right
    );
  } else {
    return new node (
     tree[v].left,
      update(tree[v].right, mid, r, pos, val)
    );
T get(int v, int tl, int tr, int l, int r) {
  if (tr <= 1 || r <= t1)</pre>
    return 0;
```

```
if (1 <= t1 && tr <= r) {
      return tree[v].sum;
    int mid = (tl + tr) / 2;
    return get(tree[v].left, tl, mid, l, r) + get(tree[v].right
         , mid, tr, 1, r);
};
```

li-chao-tree.h

Description: Li-Chao tree, online convex hull for maximizing f(x) = k * x+ b, for minimization use (-k) * x + (-b)

hash74 lines

```
Time: add - \mathcal{O}(\log N), get - \mathcal{O}(\log N)
template<typename T> struct li_chao_tree {
 const T MX = 1e9 + 1;
 struct line {
    T k = 0;
    T b = -INF;
    T f(T x) const {
      return k * x + b;
 };
 struct node {
    line ln:
    node* left = nullptr;
    node* right = nullptr;
 node* new_node() {
    const int N = 100000;
    static node* block;
    static int count = N:
    if (count == N) {
      block= new node[N];
      count = 0;
    return (block + count++);
 node* root = new_node();
 T get(T x) {
    return get (root, -MX, MX, x);
    void add(line ln) {
        add(root, -MX, MX, ln);
 T get(node *& v, T l, T r, T x) {
    if (!v || 1 > r) {
      return -INF;
    T ans = v -> ln.f(x);
    if (r == 1) {
      return ans;
    T \text{ mid} = (r + 1) / 2;
    if (x <= mid) {</pre>
      return max(ans, get(v->left, 1, mid, x));
    } else {
            return max(ans, get(v->right, mid + 1, r, x));
    void add(node*& v, T l, T r, line ln) {
```

```
if (1 > r)
      return:
        if (!v) {
            v = new_node();
   T m = (r + 1) / 2;
        bool left = v->ln.f(1) < ln.f(1);</pre>
    bool md = v - > ln.f(m) < ln.f(m);
        if (md)
            swap (v->ln, ln);
        if (1 == r) {
            return;
        if (left != md) {
            add(v->left, l, m, ln);
        } else {
            add(v->right, m + 1, r, ln);
};
```

rope.h

Description: Rope data structure **Time:** all get queries $\mathcal{O}(\log N)$

ordered-set.h

Description: A red-black tree with the ability to get an element by index (find_by_order) and index of a specific element (order_of_key)

Time: get - $\mathcal{O}(\log N)$, segment tree is 2 times faster

sparse-table.h

Description: Min sparse table.

Time: build - $\mathcal{O}(N * \log N)$, get - $\mathcal{O}(1)$

xor-trie.h

Description: Binary t for integer numbers. Get finds maximum xor of two numbers

Time: add - $\mathcal{O}(\log A)$, get - $\mathcal{O}(\log A)$

```
<cassert>, <array>
                                                         hash35 lines
struct xor trie node {
 int cnt = 0;
 std::array<xor_trie_node*, 2> mp = {nullptr, nullptr};
 void add(int mask, int k = 30) {
   cnt++;
   if (k == -1)
     return:
    int bit = (mask>>k) &1;
   if (!mp[bit])
      mp[bit] = new xor trie node();
   mp[bit] \rightarrow add(mask, k - 1);
 void remove(int mask, int k = 30) {
   cnt--;
   if (k == -1)
     return:
    int bit = (mask>>k) &1;
    assert(mp[bit] && mp[bit]->cnt > 0);
   mp[bit]->remove(mask, k - 1);
 int get(int mask, int k = 30) {
   if(k == -1)
      return 0;
    int bit = (mask>>k)&1;
   int cur= bit;
   if (mp[!bit] && mp[!bit]->cnt)
      cur = !bit;
    return ((cur^bit) << k) | mp[cur]->get(mask, k - 1);
};
```

cartesian-tree.h

Description: Cartesian tree **Time:** all get queries $\mathcal{O}(\log N)$

```
struct Node {
   int val;
   int y;
   int 1, r;
   int cnt;

Node(int val = -1) {
```

```
this->val = val;
        y = rand();
        1 = -1;
        r = -1;
        cnt = 1;
};
array<Node, 2 * N> tree;
int getCnt(int v) {
    if (v == -1)
        return 0;
    return tree[v].cnt;
void upd(int v) {
    tree[v].cnt = getCnt(tree[v].1) + getCnt(tree[v].r) + 1;
pair<int, int> split(int v, int k) {
    if (v == -1)
        return {-1, -1};
    if (k == 0)
        return {-1, v};
    pair<int, int> res;
    if (getCnt(tree[v].1) >= k) {
        res = split(tree[v].1, k);
        tree[v].l = res.second;
        res.second = v;
    } else {
        res = split(tree[v].r, k - getCnt(tree[v].l) - 1);
        tree[v].r = res.first;
        res.first = v;
    upd(v);
    return res;
int merge(int u, int v) {
    if (u == -1)
        return v;
    if (v == -1)
        return u;
    int res = -1;
    if (tree[u].y > tree[v].y) {
        res = merge(tree[u].r, v);
        tree[u].r = res;
        res = u;
        res = merge(u, tree[v].1);
        tree[v].1 = res;
        res = v;
    upd(res);
    return res;
```

link-cut-tree.h

Description: Represents a forest of unrooted trees. You can add and remove edges (as long as the result is still a forest), and check whether two nodes are in the same tree.

Time: All operations take amortized O (log N).

hash90 lines

```
struct Node { // Splay tree. Root's pp contains tree's parent.
Node *p = 0, *pp = 0, *c[2];
bool flip = 0;
Node() { c[0] = c[1] = 0; fix(); }
void fix() {
   if (c[0]) c[0]->p = this;
```

```
if (c[1]) c[1] -> p = this;
    // (+ update sum of subtree elements etc. if wanted)
  void pushFlip() {
    if (!flip) return;
    flip = 0; swap(c[0], c[1]);
   if (c[0]) c[0]->flip ^= 1;
   if (c[1]) c[1]->flip ^= 1;
  int up() { return p ? p->c[1] == this : -1; }
  void rot(int i, int b) {
    int h = i ^ b;
   Node *x = c[i], *y = b == 2 ? x : x -> c[h], *z = b ? y : x;
    if ((y->p = p)) p->c[up()] = y;
    c[i] = z->c[i ^ 1];
    if (b < 2) {
     x->c[h] = y->c[h ^ 1];
     y - > c[h ^ 1] = x;
    z\rightarrow c[i ^1] = this;
    fix(); x->fix(); y->fix();
    if (p) p->fix();
    swap(pp, y->pp);
  void splay() {
    for (pushFlip(); p; ) {
     if (p->p) p->p->pushFlip();
     p->pushFlip(); pushFlip();
     int c1 = up(), c2 = p->up();
      if (c2 == -1) p -> rot(c1, 2);
      else p->p->rot(c2, c1 != c2);
  Node* first() {
    return c[0] ? c[0]->first() : (splay(), this);
};
struct LinkCut {
  vector<Node> node;
  LinkCut(int N) : node(N) {}
  void link(int u, int v) { // add an edge (u, v)
    assert(!connected(u, v));
    makeRoot(&node[u]);
   node[u].pp = &node[v];
  void cut(int u, int v) { // remove an edge (u, v)
   Node *x = &node[u], *top = &node[v];
    makeRoot(top); x->splay();
    assert(top == (x->pp ?: x->c[0]));
   if (x->pp) x->pp = 0;
    else {
     x->c[0] = top->p = 0;
     x->fix():
  bool connected (int u, int v) { // are u, v in the same tree?
   Node * nu = access(&node[u])->first();
    return nu == access(&node[v])->first();
  void makeRoot(Node* u) {
    access(u);
    u->splay();
    if(u->c[0]) {
     u - c[0] - p = 0;
     u - c[0] - flip ^= 1;
     u - c[0] - pp = u;
```

```
articulation-points bridges dsu
      u - > c[0] = 0;
      u \rightarrow fix();
 Node* access(Node* u) {
   u->splay();
    while (Node* pp = u->pp) {
      pp->splay(); u->pp = 0;
      if (pp->c[1]) {
        pp->c[1]->p = 0; pp->c[1]->pp = pp; }
      pp->c[1] = u; pp->fix(); u = pp;
    return u:
};
Graphs (5)
articulation-points.h
Description: Finds all articulation points.
Time: \mathcal{O}(N+M)
<set>, <vector>, <functional>
template<typename T>
using graph = std::vector<std::vector<T>>;
```

std::vector<int> used(n), tin(n), fup(n);

fup[v] = std::min(fup[v], tin[to]);

fup[v] = std::min(fup[v], fup[to]);

if (fup[to] >= tin[v] && p != -1) {

nodes.insert(v);

int T = 0:

std::set<int> nodes;

int cnt = 0;

used[v] = true;

tin[v] = fup[v] = T++;

for (auto to : g[v]) {

continue;

dfs(to, v);

if (used[to]) {

cnt++;

if (cnt > 1 && p == -1)

for (int i = 0; i < n; i++) {

if (!used[i]) dfs(i, -1);

return nodes;

bridges.h

Time: $\mathcal{O}(N+M)$

<vector>, <functional>

template<typename T>

nodes.insert(v);

Description: Finds all bridges in the undirected graph.

using graph = std::vector<std::vector<T>>;

if (to == p)

} else {

hash35 lines std::set<int> find_articulation_points(int n, graph<int> g) { dsu.hstd::function<void(int, int)> dfs = [&](int v, int p = -1) hash30 lines

```
std::vector<std::pair<int, int>> find_bridges(int n, graph<int>
    std::vector<int> used(n), tin(n), fup(n);
    int T = 0;
    std::vector<std::pair<int, int>> edges;
    std::function<void(int, int)> dfs = [\&](int v, int p = -1)
        used[v] = true;
        tin[v] = fup[v] = T++;
        for (auto to : q[v]) {
            if (to == p)
                continue;
            if (used[to]) {
                fup[v] = std::min(fup[v], tin[to]);
            } else {
                dfs(to, v);
                fup[v] = std::min(fup[v], fup[to]);
                if (fup[to] == tin[to]) {
                    edges.push_back({v, to});
        }
    };
    for (int i = 0; i < n; i++) {
        if (!used[i])
            dfs(i, -1);
    return edges;
Description: Disjoint Set Union
Time: \mathcal{O}(n) time (amortized) by sizes
<algorithm>, <cassert>, <vector>
                                                        hash59 lines
struct dsu {
 public:
    dsu() : _n(0) {}
    dsu(int n) : _n(n), parent_or_size(n, -1) {}
    int merge(int a, int b) {
        assert (0 <= a && a < _n);
        assert(0 <= b && b < _n);
        int x = leader(a), y = leader(b);
        if (x == y) return x;
        if (-parent_or_size[x] < -parent_or_size[y]) std::swap(</pre>
        parent_or_size[x] += parent_or_size[y];
        parent_or_size[y] = x;
        return x;
    bool same(int a, int b) {
        assert(0 <= a && a < _n);
        assert(0 <= b && b < _n);
        return leader(a) == leader(b);
    int leader(int a) {
        assert(0 <= a && a < n);
        if (parent_or_size[a] < 0) return a;</pre>
        return parent_or_size[a] = leader(parent_or_size[a]);
    int size(int a) {
        assert(0 <= a && a < _n);
        return -parent_or_size[leader(a)];
```

std::vector<std::vector<int>> groups() {

```
std::vector<int> leader_buf(_n), group_size(_n);
        for (int i = 0; i < _n; i++) {
            leader_buf[i] = leader(i);
            group_size[leader_buf[i]]++;
        std::vector<std::vector<int>> result(n);
        for (int i = 0; i < _n; i++) {
            result[i].reserve(group_size[i]);
        for (int i = 0; i < _n; i++) {
            result[leader_buf[i]].push_back(i);
        }
        result.erase(
            std::remove_if(result.begin(), result.end(),
                            [&] (const std::vector<int>& v) {
                                 return v.empty(); }),
            result.end());
        return result;
  private:
    // root node: -1 * component size
    // otherwise: parent
    std::vector<int> parent_or_size;
dynamic-connectivity-problem.h
Description: Disjoint Set Union with roolbacks
Time: \mathcal{O}(q * log(q) * log(n)), q - number of queries, n - number of vertices
<array>, <vector>
struct Query {
    int v, u;
    bool united;
    Query(int _v, int _u) : v(_v), u(_u) {}
};
struct DSU
  struct DSU_save
   int v, rang_v;
   int u, rang_u;
  };
  int n;
  std::vector<int> pred, rang;
  std::vector<DSU_save> saves;
  DSU(int n_): n(n_) {
   pred.resize(n);
    rang.resize(n);
    for (int i = 0; i < n; i++) {
     pred[i] = i;
      rang[i] = 0;
  int get(int v) {
    if (pred[v] == v) {
      return v;
    return get(pred[v]);
  bool merge(int u, int v) {
   u = get(u);
    v = get(v);
   if (u == v)
      return false;
    if (rang[u] < rang[v])</pre>
```

```
std::swap(u, v);
    saves.push_back({v, rang[v], u, rang[u]});
   pred[v] = u;
    if (rang[u] == rang[v]) {
     rang[u]++;
   return true;
 void rollback() {
   if (saves.empty())
     return;
    auto [v, rang_v, u, rang_u] = saves.back();
    rang[v] = rang_v;
    rang[u] = rang_u;
   pred[v] = v;
   pred[u] = u;
    saves.pop_back();
};
struct dynamic_connectivity_problem {
 std::vector<std::vector<Query>> tree;
 DSU dsu;
 dynamic_connectivity_problem(int q_, int n_): q(q_), n(n_),
      dsu(DSU(n_)) {
   tree.resize(4 * q);
 void add(Query a, int 1, int r) {
    add(1, 0, q, 1, r, a);
 void add(int v, int tl, int tr, int l, int r, const Query& a)
    if (1 <= t1 && tr <= r) {
     tree[v].push_back(a);
     return;
   if (1 >= tr || t1 >= r)
     return;
   int mid = (tr + t1) / 2;
   add(2 * v, t1, mid, 1, r, a);
   add(2 * v + 1, mid, tr, 1, r, a);
 void dfs(int v, int l, int r) {
   if (1 >= r)
     return;
    for (auto& q: tree[v]) {
     q.united = dsu.merge(q.u, q.v);
   if (1 + 1 == r) {
     int x = dsu.get(0);
      // do something
   } else {
     int mid = (r + 1) / 2;
     dfs(2 * v, 1, mid);
     dfs(2 * v + 1, mid, r);
    for (auto& q: tree[v]) {
     if (q.united)
        dsu.rollback();
```

```
q.united = false:
};
```

kuhn-matching.h

Description: Fast pair matching algorithm. To find the minimum vertex cover start dfs from each vertice in the left that is not in maximum matching, from the left side choce unvisited vertices and from right chose visited.

```
Time: \mathcal{O}(n*(n+m))
<vector>, <utility>
                                                        hash44 lines
using namespace std;
template<typename T>
using graph = vector<vector<T>>;
bool dfs(int v, graph<int>& g, vector<int>& mt, vector<int>&
    rev mt, vector<int>& used) {
    if (used[v] == 1)
        return false;
    used[v] = 1;
    for (auto to : q[v]) {
        if (mt[to] == -1) {
            rev_mt[v] = to;
            mt[to] = v;
            return true;
    for (auto to : g[v]) {
        if (dfs(mt[to], g, mt, rev_mt, used)) {
            rev_mt[v] = to;
            mt[to] = v;
            return true;
    return false;
pair<int, vector<int>> pair_matching(int n, int m, graph<int> q
    vector<int> mt (m, -1), used, rev_mt (n, -1);
    int cnt = 0:
    for (int it = 0; ; it++) {
        bool found = false;
        used.assign(n, 0);
        for (int i = 0; i < n; i++) {
            if (rev_mt[i] == -1 && dfs(i, q, mt, rev_mt, used))
                cnt++;
                found = true;
        if (!found) {
            break:
    return {cnt, mt};
```

max-flow.h

Description: Maximum flow problem

```
Time: \mathcal{O}\left(\min(n^{(2/3)}*m, m^{(3/2)})\right) - all capacities are 1, \mathcal{O}\left(n^2, m\right) - gen-
                                                                                                   hash104 lines
```

```
template<typename Cap>
struct mf_graph {
    struct mf_edge {
        int from, to;
```

```
Cap cap, flow;
     int back_id;
     int id;
 };
 int n;
 vector<vector<mf edge>> q;
bool need clear = false;
 mf_graph(int n): n(n) {
     g.assign(n, {});
 void add_edge(int from, int to, Cap cap, int id = -1) {
     int id1 = q[from].size();
     int id2 = g[to].size();
     g[from].push_back(mf_edge {
          .from = from,
          .to = to,
          .cap = cap,
          .flow = Cap(),
          .back_id = id2,
          .\_id = id
     });
     g[to].push_back(mf_edge {
          .from = to,
          .to = from,
          .cap = Cap(),
          .flow = Cap(),
          .back_id = id1,
          ._{id} = -1
     });
void clear() {
 for (int i = 0; i < n; i++) {
   for (mf_edge& e: g[i])
     e.flow = Cap();
 Cap flow(int s, int t, Cap limit) {
 if (need_clear)
   clear();
     vector<int> dist(n, n + 1);
     auto bfs = [\&] (int s, int t) {
          dist.assign(n, n + 1);
          dist[s] = 0;
          deque<int> q;
          q.push_back(s);
          while (!q.empty())
              int v = q.front();
             q.pop_front();
              for (mf_edge& e : g[v]) {
                  if (e.flow < e.cap \&\& dist[e.to] == n + 1)
                      dist[e.to] = dist[v] + 1;
                      q.push_back(e.to);
             }
          return dist[t] != n + 1;
     };
     vector<int> lst(n);
```

```
function<Cap(int, int, Cap)> dfs = [&](int v, int
            target, Cap F) {
            if (v == target)
               return F;
            Cap pushed = Cap();
            for (; lst[v] < g[v].size(); lst[v]++) {</pre>
                mf_edge& e = g[v][lst[v]];
                if (dist[e.to] == dist[v] + 1 && e.flow < e.cap
                    Cap x = dfs(e.to, target, min(F, e.cap - e.
                    if (x) {
                        e.flow += x;
                        g[e.to][e.back_id].flow -= x;
                        pushed += x;
                        F = x;
            return pushed;
       };
       Cap flow = 0;
       while (bfs(s, t)) {
           lst.assign(n, 0);
            while (Cap f = dfs(s, t, limit)) {
                flow += f;
    need_clear = true;
       return flow;
};
```

lca.h

Description: Finds lowest common ancestor of two vertices using sparce

Time: $\mathcal{O}(n * log(n))$ - build, $\mathcal{O}(1)$ - get

```
hash30 lines
struct LCA {
 vector<pair<int, int>> traversal;
 vector<int> pos;
 graph<int> g;
 int n:
 sparse_table<pair<int, int>> st;
 LCA(int n_, graph<int> g_, int root = 0): n(n_), g(g_) {
   pos.resize(n);
   dfs(root, -1, 0):
   st = sparse_table<pair<int, int>>(traversal.size(),
        traversal);
 void dfs(int v, int pred, int depth) {
   pos[v] = traversal.size();
   traversal.push_back({depth, v});
    for (auto to : q[v]) {
     if (to != pred) {
       dfs(to, v, depth + 1);
       traversal.push_back({depth, v});
 }
 int get(int a, int b) {
   if (a == b)
     return a;
```

```
return st.get(min(pos[a], pos[b]), max(pos[a], pos[b]) + 1)
};
two-sat.h
Description: 2-sat implementation
Time: \mathcal{O}(n)
<vector>
                                                        hash74 lines
template<typename T>
using graph = std::vector<std::vector<T>>;
struct two_sat {
    graph<int> g, rev;
    std::vector<int> used, order, comp, ans;
    two sat(int n): n(n) {
        g.assign(2 * n, {});
        rev.assign(2 * n, \{\});
    void add edge(int u, int v) {
        g[u].push_back(v);
        rev[v].push_back(u);
    void add clause or (int a, bool val a, int b, bool val b) {
        add edge(a + val a * n, b + !val b * n);
        add edge(b + val b * n, a + !val a * n);
    void add_clause_xor(int a, bool val_a, int b, bool val_b) {
        add_clause_or(a, val_a, b, val_b);
        add_clause_or(a, !val_a, b, !val_b);
    void add_clause_and(int a, bool val_a, int b, bool val_b) {
        add clause xor(a, !val a, b, val b);
    void top_sort(int v) {
        used[v] = 1;
        for (auto to : g[v]) {
            if (!used[to])
                top_sort(to);
        order.push_back(v);
    void compress(int v, int id) {
        comp[v] = id;
        for (auto to : rev[v]) {
            if (comp[to] == -1)
                compress(to, id);
    }
    bool satisfiable() {
        order.clear();
        used.assign(2 * n, 0);
        comp.assign(2 * n, -1);
        ans.assign(n, 0);
        for (int i = 0; i < 2 * n; i++) {
            if (!used[i])
                top_sort(i);
        reverse(order.begin(), order.end());
```

```
for (int i = 0; i < n; i++) {
            if (comp[i] == comp[i + n])
                 return false;
            ans[i] = (comp[i + n] < comp[i]);
        }
        return true;
};
eulerian-path.h
Description: Finds eulerian path and cycle for undirected graph
Time: \mathcal{O}\left(m*logm\right)
<vector>, <set>
                                                          hash101 lines
using namespace std;
struct eulerian_path
    vector<multiset<int>>graph;
    eulerian_path(vector<vector<int>>g)
        graph.resize(g.size());
        for(int i=0;i<q.size();i++)</pre>
             for(int j:g[i])
                graph[i].insert(j);
    void dfs(int u, vector<int>&cycle)
        auto p = graph[u];
        for(int j:p)
             if (graph[u].find(j) != graph[u].end())
                 graph[u].erase(graph[u].find(j));
                 graph[j].erase(graph[j].find(u));
                 dfs(j, cycle);
        cycle.push_back(u);
    vector<int> find_cycle(int v = 0)
        for(int i = 0;i < graph.size();i++)</pre>
            if(graph[i].size() % 2)
                return {};
        vector<int>cycle;
        dfs(v, cvcle);
        for(auto x:graph)
             if(x.size())
            return {};
        return cycle;
    vector<int> find_path()
```

int id = 0;

for (auto v : order) {

if (comp[v] == -1)

compress(v, id++);

```
int st = -1, fi = -1;
        int mx = 0:
         for(int i = 0; i < graph.size(); i++)
             if(graph[i].size() % 2)
                 if(st == -1)
                     st = i;
                 else
                 if(fi == -1)
                      fi = i;
                 else
                      return {};
             if (graph[mx].size() < graph[i].size()) mx = i;</pre>
        if(fi == -1)
        {
             auto cycle = find_cycle(mx);
             return cycle;
        graph[st].insert(fi);
        graph[fi].insert(st);
        auto cycle = find_cycle(st);
        if(!cycle.size())
        return {};
         cycle.pop_back();
        if(cycle[0]==st and cycle.back()==fi or cycle[0]==fi
              and cycle.back() == st)
             return cycle;
        vector<int>path;
        for(int i=0;;i++)
             if(cycle[i] == st and cycle[i+1] == fi or cycle[i]
                  == fi and cycle[i+1] == st)
                 for(int j = i + 1; j < cycle.size(); j++)
                      path.push_back(cycle[j]);
                  for (int j = 0; j \le i; j++)
                      path.push_back(cycle[j]);
                 break;
        return path;
};
max-flow.h
Description: Maximum flow problem
Time: \mathcal{O}\left(\min(n^{(2/3)}*m, m^{(3/2)})\right) - all capacities are 1, \mathcal{O}\left(n^2, m\right) - gen-
                                                           hash104 lines
template<typename Cap>
struct mf_graph {
    struct mf_edge {
        int from, to;
        Cap cap, flow;
        int back_id;
         int _id;
    };
    vector<vector<mf_edge>> g;
```

```
bool need clear = false;
  mf graph(int n): n(n) {
      g.assign(n, {});
  void add_edge(int from, int to, Cap cap, int id = -1) {
      int id1 = g[from].size();
      int id2 = g[to].size();
      g[from].push_back(mf_edge {
          .from = from,
          .to = to,
          .cap = cap,
          .flow = Cap(),
          .back_id = id2,
          .\_id = id
      });
      g[to].push_back(mf_edge {
          .from = to,
          .to = from,
          .cap = Cap(),
          .flow = Cap(),
          .back_id = id1,
          .\_id = -1
      });
void clear() {
  for (int i = 0; i < n; i++) {
    for (mf_edge& e: g[i])
      e.flow = Cap();
  Cap flow(int s, int t, Cap limit) {
  if (need_clear)
    clear();
      vector<int> dist(n, n + 1);
      auto bfs = [&](int s, int t) {
          dist.assign(n, n + 1);
          dist[s] = 0;
          deque<int> q;
          q.push_back(s);
          while (!q.empty())
              int v = q.front();
              q.pop_front();
              for (mf_edge& e : g[v]) {
                  if (e.flow < e.cap && dist[e.to] == n + 1)</pre>
                      dist[e.to] = dist[v] + 1;
                      q.push_back(e.to);
              }
          return dist[t] != n + 1;
      };
      vector<int> lst(n);
      function<Cap(int, int, Cap)> dfs = [&](int v, int
          target, Cap F) {
          if (v == target)
              return F;
          Cap pushed = Cap();
```

min-cut min-cost-flow ford-bellman spfa

```
for (; lst[v] < g[v].size(); lst[v]++) {</pre>
                mf_edge& e = g[v][lst[v]];
                if (dist[e.to] == dist[v] + 1 && e.flow < e.cap</pre>
                     Cap x = dfs(e.to, target, min(F, e.cap - e.
                     if (x) {
                        e.flow += x;
                        g[e.to][e.back_id].flow -= x;
                        pushed += x;
                        F -= x;
                }
            return pushed;
        };
        Cap flow = 0;
        while (bfs(s, t)) {
            lst.assign(n, 0);
            while (Cap f = dfs(s, t, limit)) {
                flow += f;
    need_clear = true;
        return flow;
};
```

min-cut.h

Description: Start dfs from source and using edges with capacity - flow > 0, mark visited vertices. Min cut is edges between marked and unmarked

Time: $\mathcal{O}(n+m)$

min-cost-flow.h

Description: Solves minimum-cost flow problem for specific flow value (or

Time: $\mathcal{O}(F*(n+m)*log(n+m))$, where F is the amount of the flow and m is the number of added edges.

```
hash106 lines
template<typename Cap, typename Cost>
struct mcf_graph
    struct mcf_edge {
       int from, to;
        Cap cap, flow;
       Cost cost;
       int back id:
        int _id;
    };
    int n;
    vector<vector<mcf_edge>> g;
    mcf_graph(int n): n(n) {
        q.assiqn(n, {});
    void add_edge(int from, int to, Cap cap, Cost cost, int _id
         = -1) {
        int id1 = g[from].size();
        int id2 = g[to].size();
        g[from].push back(mcf edge{
            .from = from,
            .to = to,
            .cap = cap,
            .flow = Cap(),
            .cost = cost,
```

```
.back_id = id2,
        .\_id = \_id
    g[to].push_back(mcf_edge{
        .from = to,
        .to = from,
        .cap = Cap(),
        .flow = Cap(),
        .cost = -cost,
        .back_id = id1,
        ._{id} = -1
    });
}
pair<Cap, Cost> flow(int s, int t, Cap target_flow) {
    Cap flow = Cap();
    vector<pair<int, int>> pred(n);
    vector<Cost> dist(n), dual(n, 0);
    auto shortests_path = [&](int s, int t) {
        pred.assign(n, \{-1, -1\});
        dist.assign(n, numeric_limits<Cost>::max());
        dist[s] = Cost();
        set<pair<int, int>> q;
        q.insert({dist[s], s});
        while (!q.empty()) {
            int v = q.begin()->second;
            q.erase(q.begin());
            for (int i = 0; i < g[v].size(); i++) {
                mcf_edge& e = g[v][i];
                if (e.flow >= e.cap)
                    continue;
                Cost cost = e.cost - dual[e.to] + dual[v];
                if (dist[e.to] > dist[v] + cost) {
                    q.erase({dist[e.to], e.to});
                    dist[e.to] = dist[v] + cost;
                    pred[e.to] = \{v, i\};
                    q.insert({dist[e.to], e.to});
        if (dist[t] == numeric_limits<Cost>::max())
            return false;
        for (int v = 0; v < n; v++) {
            if (dist[v] == numeric_limits<Cost>::max())
                continue;
            dual[v] -= dist[t] - dist[v];
        return true;
    };
    Cost total_cost = {};
    while (flow < target flow) {
        if (!shortests_path(s, t))
            break:
        Cap f = target_flow - flow;
        int cur = t;
        while (cur != s) {
            auto [p, id] = pred[cur];
            mcf_edge& e = g[p][id];
            f = min(f, e.cap - e.flow);
            cur = p;
        cur = t;
        while (cur != s) {
            auto [p, id] = pred[cur];
```

```
mcf_edge& e = g[p][id];
                e.flow += f;
                g[e.to][e.back id].flow -= f;
                cur = p;
            Cost d = -dual[s];
            flow += f;
            total_cost += f * d;
        return {flow, total_cost};
};
```

ford-bellman.h

Description: Single source shortest path with negative weight edges in dirceted graph

Time: $\mathcal{O}(n*m)$

```
hash16 lines
```

```
vector<int> d(n, INF);
d[v] = 0;
vector<int> p(n, -1);
for (;;) {
 bool any = false;
 for (Edge e : edges)
   if (d[e.a] < INF)</pre>
     if (d[e.b] > d[e.a] + e.cost) {
        d[e.b] = d[e.a] + e.cost;
        p[e.b] = e.a;
        any = true;
 if (!any)
    break;
```

spfa.h

Description: Single source shortest path with negative weight edges in directed graph

Time: $\mathcal{O}(n*m)$

hash36 lines

```
const int INF = 1000000000;
vector<vector<pair<int, int>>> adj;
bool spfa(int s, vector<int>& d) {
    int n = adj.size();
    d.assign(n, INF);
    vector<int> cnt(n, 0);
    vector<bool> inqueue(n, false);
    queue<int> q;
    d[s] = 0;
    q.push(s);
    inqueue[s] = true;
    while (!q.empty()) {
        int v = q.front();
        q.pop();
        inqueue[v] = false;
        for (auto edge : adj[v]) {
            int to = edge.first;
            int len = edge.second;
            if (d[v] + len < d[to]) {</pre>
                d[to] = d[v] + len;
                if (!inqueue[to]) {
                    q.push(to);
                    inqueue[to] = true;
                    cnt[to]++;
                    if (cnt[to] > n)
```

```
return false; // negative cycle
return true;
```

Strings (6)

z-function.h

Description: Z-functions, z[i] equal to the length of largest common prefix of string s and suffix of s starting at i.

Time: $\mathcal{O}(N)$, N - size of string s

hash18 lines

```
vector<int> z_function(const string& s) {
  int n = s.size();
  vector<int> z(n);
  int 1 = 0, r = 0;
  for (int i = 1; i < n; i++) {
   if(i < r) {
     z[i] = min(r - i, z[i - 1]);
   while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) {
     z[i]++;
   if(i + z[i] > r) {
    1 = i;
     r = i + z[i];
  return z:
```

prefix-function.h

Description: The prefix function for this string is defined as an array p of length n, where p[i] is the length of the longest valid prefix of the substring s[0...i], which is also a suffix of this substring.

Time: $\mathcal{O}(N)$, N - size of string s

hash13 lines

```
vector<int> prefix_function(string s) {
   int n = (int)s.length();
    vector<int> pi(n);
    for (int i = 1; i < n; i++) {
       int j = pi[i-1];
       while (j > 0 \&\& s[i] != s[j])
            j = pi[j-1];
       if (s[i] == s[j])
           j++;
       pi[i] = j;
    return pi;
```

Description: Suffix array will contain integers that represent the starting indexes of the all the suffixes of a given string, after the aforementioned suffixes are sorted.

Time: $\mathcal{O}(N * log(N))$, N - size of string s

hash65 lines

```
vector<int> suffix_arrays(string s) {
 s = s + "$";
  int n = s.size();
  std::vector<int> p(n);
  vector<vector<int>> c(20, vector<int>(n));
  int alphabet = 256;
```

```
auto set classes = [&](int k) {
      int classes = 0:
      c[k][p[0]] = classes++;
      for (int i = 1; i < n; i++) {
            auto cur = pair\{c[k - 1][p[i]], c[k - 1][(p[i] + (1 << (k - 1)[(p[i] + (k - 1)[(k - 1)
                         -1))) % n];
            auto prev = pair\{c[k-1][p[i-1]], c[k-1][(p[i-1]+
                             (1 << (k-1)) % n]};
            if (cur == prev) {
                c[k][p[i]] = c[k][p[i - 1]];
            } else {
                  c[k][p[i]] = classes++;
     }
};
vector<int> cnt(alphabet);
for (int i = 0; i < n; i++) {
      cnt[s[i]]++;
for (int i = 1; i < alphabet; i++) {
     cnt[i] += cnt[i - 1];
for (int i = n - 1; i >= 0; i--) {
     p[cnt[s[i]] - 1] = i;
      cnt[s[i]]--;
int classes = 0;
c[0][p[0]] = classes++;
for (int i = 1; i < n; i++) {
     if (s[p[i]] == s[p[i-1]]) {
           c[0][p[i]] = c[0][p[i - 1]];
     } else {
            c[0][p[i]] = classes++;
for (int k = 0; (1<<k) < n; k++) {
      vector<int> pn(n), cnt(n);
       for (int i = 0; i < n; i++) {
            pn[i] = (p[i] - (1 << k) + n) % n;
            cnt[c[k][pn[i]]]++;
      for (int i = 1; i < n; i++)
           cnt[i] += cnt[i - 1];
      for (int i = n - 1; i >= 0; i--) {
           p[cnt[c[k][pn[i]]] - 1] = pn[i];
            cnt[c[k][pn[i]]]--;
      set_classes(k + 1);
p.erase(p.begin());
return p;
```

lcp-array.h

Description: Largest common prefix of substrings. Given a string s of length n, it returns the LCP array of s. Here, the LCP array of s is the array of length n-1, such that the i-th element is the length of the LCP (Longest Common Prefix) of s[sa[i]..n) and s[sa[i+1]..n).

Time: $\mathcal{O}(N)$, N - size of string s

hash31 lines

r--; if (1 == 0)

```
template <class T>
std::vector<int> lcp_array(const std::vector<T>& s,
```

```
const std::vector<int>& sa) {
    int n = int(s.size());
    assert(n >= 1);
    std::vector<int> rnk(n);
    for (int i = 0; i < n; i++) {
        rnk[sa[i]] = i;
    std::vector<int> lcp(n - 1);
    int h = 0;
    for (int i = 0; i < n; i++) {
        if (h > 0) h--;
        if (rnk[i] == 0) continue;
        int j = sa[rnk[i] - 1];
        for (; j + h < n && i + h < n; h++) {
            if (s[j + h] != s[i + h]) break;
        lcp[rnk[i] - 1] = h;
    return lcp;
std::vector<int> lcp_array(const std::string& s, const std::
    vector<int>& sa) {
    int n = int(s.size());
    std::vector<int> s2(n);
    for (int i = 0; i < n; i++) {
        s2[i] = s[i];
    return lcp_array(s2, sa);
hash.h
Description: Polynomial hashes for strings
Time: \mathcal{O}(n * log(M)), n - size of string s, m - module
                                                        hash47 lines
template<int P, int MOD>
struct hash st {
    int n:
    vector<int> hash_, rev_, p, rev_p;
    hash_st(string s) {
        n = s.size();
        hash_.resize(n);
        rev_.resize(n);
        p.resize(n);
        rev_p.resize(n);
        p[0] = 1;
        rev p[0] = 1;
        for (int i = 1; i < n; i++) {
            p[i] = (p[i - 1] * P) % MOD;
            rev_p[i] = fast_pow(p[i], MOD - 2, MOD);
        int last = 0:
        for (int i = 0; i < n; i++) {
            hash_[i] = (last + p[i] * (s[i] - 'a' + 1)) % MOD;
            last = hash_[i];
        last = 0;
        for (int i = n - 1; i >= 0; i--) {
            rev_[i] = (last + p[n - 1 - i] * (s[i] - 'a' + 1))
                 % MOD;
            last = rev_[i];
    int get(int 1, int r) {
```

```
return hash_[r];
       int x = (MOD + hash_[r] - hash_[l - 1]) % MOD;
        return (x * rev p[1]) % MOD;
   int get_rev(int 1, int r) {
       r--;
       if (r == n - 1)
           return rev_[1];
       int x = (MOD + rev_[1] - rev_[r + 1]) % MOD;
       int st = n - 1 - r;
       return (x * rev_p[st]) % MOD;
};
```

trie.h

Description: Trie implementation

hash63 lines

```
Time: \mathcal{O}(n)
template<int N = (int) 1e6 + 1>
struct trie {
  struct node {
    int cnt = 0;
   array<int, 27> links;
   node() {
     links.fill(-1);
     cnt = 0;
  };
  array<node, N> tree;
  int sz = 0;
  int root = 0;
  trie() {
   root = sz++;
  void add(string s) {
   int cur = root;
   tree[cur].cnt++;
    for (int i = 0; i < s.size(); i++) {
     int nxt = tree[cur].links[s[i] - 'a'];
     if (nxt == -1) {
       nxt = sz++;
       tree[cur].links[s[i] - 'a'] = nxt;
     tree[nxt].cnt++;
     cur = nxt;
  void remove(string s) {
   int cur = root;
   tree[cur].cnt--;
    for (int i = 0; i < s.size(); i++) {
     int nxt = tree[cur].links[s[i] - 'a'];
     assert (nxt != -1);
     tree[nxt].cnt--;
     cur = nxt;
  int get_cnt_of_str(const string& s) {
   int cur = root;
    for (int i = 0; i < s.size(); i++) {
     int nxt = tree[cur].links[s[i] - 'a'];
     if (nxt == -1) {
```

```
return 0;
     cur = nxt;
   return tree[cur].cnt;
 void clear() {
   for (int i = 0; i < sz; i++)
     tree[i] = node();
};
aho-corasick.h
```

Description: creates suffix automaton

hash103 lines

```
Time: \mathcal{O}(|alphabet| * |sumoflengthofstrings|)
const int K = 26;
struct Vertex {
    int next[K];
    bool output = false;
    int p = -1;
    char pch;
    int link = -1;
    int ans link = -1;
   int go[K];
   Vertex(int p=-1, char ch='\$') : p(p), pch(ch) {
        fill(begin(next), end(next), -1);
        fill(begin(go), end(go), -1);
};
vector<Vertex> t(1);
void add string(string const& s) {
   int v = 0:
    for (char ch : s) {
       int c = ch - 'a';
       if (t[v].next[c] == -1) {
            t[v].next[c] = t.size();
            t.emplace_back(v, ch);
        v = t[v].next[c];
    t[v].output = true;
int go(int v, char ch);
int get_link(int v) {
    if (t[v].link == -1) {
        if (v == 0 | | t[v].p == 0)
            t[v].link = 0;
            t[v].link = go(get_link(t[v].p), t[v].pch);
    return t[v].link;
int go(int v, char ch) {
   int c = ch - 'a';
   if (t[v].go[c] == -1) {
        if (t[v].next[c] != -1)
            t[v].go[c] = t[v].next[c];
            t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
```

```
return t[v].go[c];
int get_ans_link(int v)
    if(v == 0)
    return 0;
    if(t[v].ans_link == -1)
        if (t [get_link(v)].output)
            t[v].ans_link = get_link(v);
        else
        t[v].ans_link = get_ans_link(get_link(v));
    return t[v].ans_link;
// returns all strings from dictionary that is suffix of given
vector<string> get_ans(int v)
    vector<string>ans;
    if(t[v].output)
        string cur = "";
        int v1 = v;
        while(v1)
            cur += t[v1].pch;
            v1 = t[v1].p;
        reverse(cur.begin(), cur.end());
        ans.push_back(cur);
    v = get_ans_link(v);
    while(v)
        string cur = "";
        int v1 = v;
        while(v1)
            cur += t[v1].pch;
            v1 = t[v1].p;
        reverse(cur.begin(), cur.end());
        ans.push_back(cur);
        v = get ans link(v);
    return ans;
```

13

Geometry (7)

point.h

Description: geometry formuls

```
<complex>, <iostream>
                                                       hash124 lines
class point : public std::complex<long double> {
 using ld = long double;
 static constexpr long double PI = 3.141592653589793;
public:
 point() : std::complex<long double>() {}
  point(ld x, ld y) : std::complex<long double>(x, y) {}
```

```
point(std::complex<long double> obj) : std::complex<long</pre>
     double>(obi) {}
ld x() {
 return this->real();
ld y() {
 return this->imag();
ld x() const {
 return this->real();
ld y() const {
 return this->imag();
// a_{-}x * b_{-}x + a_{-}y * b_{-}y
static ld dot_product(const point& a, const point& b) {
 return (conj(a) * b).real();
// a_{-}x * b_{-}y - a_{-}y * b_{-}x
static ld cross_product(const point& a, const point& b) {
  return (conj(a) * b).imag();
static ld squared_distance(const point& a, const point& b) {
 return norm(a - b);
static ld distance (const point& a, const point& b) {
  return abs(a - b);
// angle_of_elevation of line (a, b) to oX
static ld angle of elevation (const point & a, const point & b)
   {
  return arg(b - a);
// k \text{ from } y = k * x + b
static ld slope_of_line(const point& a, const point& b) {
  return tan(arg(b - a));
static point from polar(ld r, ld theta) {
 return std::polar(r, theta);
static point rotate above pivot (const point& a, const ld
     theta, const point& pivot = point(0, 0)) {
  return (a - pivot) * std::polar<ld>(1.0, theta) + pivot;
point& rotate(const ld theta, const point& pivot = point(0,
  *this = point::rotate above pivot(*this, theta, pivot);
  return *this;
// angle of ABC
static ld angle(const point& a, const point& b, const point&
  return abs(remainder(arg(a-b) - arg(c-b), 2.0 * PI));
```

```
static point project_on_vector(const point& p, const point& v
      ) {
   return v * dot product(p, v) / norm(v);
 static point project_on_line(const point& p, const point& a,
      const point & b) {
   return a + (b - a) * dot_product(p - a, b - a) / norm(b - a
        );
 static point reflect_accros(const point& p, const point& a,
      const point& b) {
   return a + conj((p - a) / (b - a)) * (b - a);
 // intersection of lines (a, b) and (p, q). if parallel
      returns {false, ...} else {true, intersection}.
 friend std::pair<bool, point> intersection_of_lines(const
      point& a, const point& b, const point& p, const point& q
   ld c1 = cross_product(p - a, b - a), c2 = cross_product(q -
         a, b - a);
   if (c1 == c2) {
     return {false, {}};
   return {true, (c1 * q - c2 * p) / (c1 - c2)}; // undefined
         if parallel
 // returns a, b, c from a * x + b * y + c = 0 by two points
 friend std::tuple<ld, ld, ld> get_line(const point& p, const
      point& q) {
   1d a = (p.y() - q.y());
   1d b = -(p.x() - q.x());
   1d c = p.y() * (p.x() - q.x()) - p.x() * (p.y() - q.y());
   return {a, b, c};
 friend ld distance_from_point_to_line(const point& p, const
      point& a, const point& b) {
   point q = project_on_line(p, a, b);
    return point::distance(p, q);
 friend ld distance from point to segment (const point & p,
      const point& a, const point& b) {
   point q = project_on_line(p, a, b);
   if (std::min(a.x(), b.x()) \le q.x() \&\& q.x() \le std::max(a.
        x(), b.x())
     return point::distance(p, q);
     return std::min(distance(p, a), distance(p, b));
 friend std::istream& operator>> (std::istream& in, point& p)
   ld x, y;
   in >> x >> v;
   p = point(x, y);
   return in;
};
```

faces-of-planar-graph.h

Description: Finds faces of planar graph. Rreturns a vector of vertices for each face, outer face goes first. Inner faces are returned in counter-clockwise orders and the outer face is returned in clockwise order.

```
Time: \mathcal{O}(nloq(n))
                                                         hash89 lines
<vector>
template<typename T>
using graph = vector<vector<T>>;
struct Point {
    int64_t x, y;
    Point(int64_t x_, int64_t y_): x(x_), y(y_) \{ \}
    Point operator - (const Point & p) const {
        return Point(x - p.x, y - p.y);
    int64_t cross (const Point & p) const {
        return x * p.y - y * p.x;
    int64_t cross (const Point & p, const Point & q) const {
        return (p - *this).cross(q - *this);
    int half () const {
        return int (y < 0 \mid | (y == 0 \&\& x < 0));
};
std::vector<std::vector<size_t>> find_faces(std::vector<Point>
     vertices, graph<int> adj) {
    size t n = vertices.size();
    std::vector<std::vector<char>> used(n);
    for (size t i = 0; i < n; i++) {
        used[i].resize(adj[i].size());
        used[i].assign(adj[i].size(), 0);
        auto compare = [&](size_t l, size_t r) {
            Point pl = vertices[1] - vertices[i];
            Point pr = vertices[r] - vertices[i];
            if (pl.half() != pr.half())
                return pl.half() < pr.half();</pre>
            return pl.cross(pr) > 0;
        std::sort(adj[i].begin(), adj[i].end(), compare);
    std::vector<std::vector<size t>> faces;
    for (size_t i = 0; i < n; i++) {</pre>
        for (size_t edge_id = 0; edge_id < adj[i].size();</pre>
             edge_id++) {
            if (used[i][edge id]) {
                continue;
            std::vector<size t> face;
            size t v = i;
            size_t e = edge_id;
            while (!used[v][e]) {
                used[v][e] = true;
                face.push_back(v);
                size t u = adj[v][e];
                size_t e1 = std::lower_bound(adj[u].begin(),
                     adj[u].end(), v, [&](size_t l, size_t r) {
                     Point pl = vertices[l] - vertices[u];
                     Point pr = vertices[r] - vertices[u];
                     if (pl.half() != pr.half())
                         return pl.half() < pr.half();</pre>
                     return pl.cross(pr) > 0;
                }) - adj[u].begin() + 1;
                if (e1 == adj[u].size()) {
                     e1 = 0;
```

v = u;

```
e = e1;
            std::reverse(face.begin(), face.end());
            int sign = 0;
            for (size_t j = 0; j < face.size(); j++) {</pre>
                size_t j1 = (j + 1) % face.size();
                size_t j2 = (j + 2) % face.size();
                int64_t val = vertices[face[j]].cross(vertices[
                     face[j1]], vertices[face[j2]]);
                if (val > 0) {
                    sign = 1;
                    break;
                } else if (val < 0) {
                    sign = -1;
                    break;
            if (sign <= 0) {
                faces.insert(faces.begin(), face);
                faces.emplace_back(face);
    return faces;
mec.h
Description: Minimum enclosing circle
Time: \mathcal{O}(n)
<algorithm>, <assert.h>, <iostream>, <math.h>, <vector>, <iomanip> hash89 lines
using namespace std;
const double INF = 1e18;
struct Point {
 double X, Y;
struct Circle {
 Point C:
 double R;
double dist(const Point& a, const Point& b)
  return sqrt(pow(a.X - b.X, 2)
        + pow(a.Y - b.Y, 2));
bool is_inside(const Circle& c, const Point& p)
  return dist(c.C, p) <= c.R;
Point get_circle_center(double bx, double by, double cx, double
     cy)
  double B = bx * bx + by * by;
  double C = cx * cx + cy * cy;
  double D = bx * cy - by * cx;
  return { (cy * B - by * C) / (2 * D),
      (bx * C - cx * B) / (2 * D) };
Circle circle_from(const Point& A, const Point& B, const Point&
 Point I = get_circle_center(B.X - A.X, B.Y - A.Y, C.X - A.X,
      C.Y - A.Y);
 I.X += A.X;
  I.Y += A.Y;
  return { I, dist(I, A) };
```

Circle circle_from(const Point& A, const Point& B)

```
Point C = \{ (A.X + B.X) / 2.0, (A.Y + B.Y) / 2.0 \};
 return { C, dist(A, B) / 2.0 };
bool is_valid_circle(const Circle& c, const vector<Point>& P)
 for (const Point& p : P)
   if (!is_inside(c, p))
     return false;
 return true;
Circle min_circle_trivial(vector<Point>& P)
 assert(P.size() <= 3);
 if (P.empty()) {
   return { { 0, 0 }, 0 };
 else if (P.size() == 1) {
   return { P[0], 0 };
 else if (P.size() == 2) {
   return circle_from(P[0], P[1]);
 for (int i = 0; i < 3; i++) {
   for (int j = i + 1; j < 3; j++) {
     Circle c = circle_from(P[i], P[j]);
     if (is_valid_circle(c, P))
       return c;
 return circle_from(P[0], P[1], P[2]);
Circle welzl_helper(vector<Point>& P, vector<Point> R, int n)
 if (n == 0 || R.size() == 3) {
   return min_circle_trivial(R);
 int idx = rand() % n;
 Point p = P[idx];
 swap(P[idx], P[n-1]);
 Circle d = welzl_helper(P, R, n - 1);
 if (is_inside(d, p)) {
   return d;
 R.push_back(p);
 return welzl_helper(P, R, n - 1);
Circle welzl(const vector<Point>& P)
 vector<Point> P_copy = P;
 random_shuffle(P_copy.begin(), P_copy.end());
 return welzl_helper(P_copy, {}, P_copy.size());
```

Misc. algorithms (8)

```
primes.txt

p = 962592769 is such that 221 | p - 1, which may be useful.
    For hashing use 970592641
(31-bit number), 31443539979727 (45-bit), 3006703054056749 (52-bit). There are 78498
primes less than 1 000 000.
```

```
sos-dp.h
```

Description: Sum over submasks

Time: $\mathcal{O}(n*2*n)$

hash7 lines

15

```
for (int i = 0; i < n; i++) {
  for (int mask = 0; mask < (1<<n); mask++) {
    if (mask&(1<<i)) {
      dp[mask] += dp[mask^(1<<i)];
    }
  }
}</pre>
```

Techniques (A)

techniques.txt

Bitonic cycle

161 lines

Recursion Divide and conquer Finding interesting points in N log N Algorithm analysis Master theorem Amortized time complexity Greedy algorithm Scheduling Max contiquous subvector sum Invariants Huffman encoding Graph theory Dynamic graphs (extra book-keeping) Breadth first search Depth first search * Normal trees / DFS trees Dijkstra's algorithm MST: Prim's algorithm Bellman-Ford Konig's theorem and vertex cover Min-cost max flow Lovasz toggle Matrix tree theorem Maximal matching, general graphs Hopcroft-Karp Hall's marriage theorem Graphical sequences Floyd-Warshall Euler cycles Flow networks * Augmenting paths * Edmonds-Karp Bipartite matching Min. path cover Topological sorting Strongly connected components Cut vertices, cut-edges and biconnected components Edge coloring * Trees Vertex coloring * Bipartite graphs (=> trees) * 3^n (special case of set cover) Diameter and centroid K'th shortest path Shortest cycle Dynamic programming Knapsack Coin change Longest common subsequence Longest increasing subsequence Number of paths in a dag Shortest path in a dag Dynprog over intervals Dynprog over subsets Dynprog over probabilities Dynprog over trees 3^n set cover Divide and conquer Knuth optimization Convex hull optimizations Slope trick Aliens trick RMQ (sparse table a.k.a 2^k-jumps)

Log partitioning (loop over most restricted) Combinatorics Computation of binomial coefficients Pigeon-hole principle Inclusion/exclusion Catalan number Pick's theorem Number theory Integer parts Divisibility Euclidean algorithm Modular arithmetic * Modular multiplication * Modular inverses * Modular exponentiation by squaring Chinese remainder theorem Fermat's little theorem Euler's theorem Phi function Frobenius number Quadratic reciprocity Pollard-Rho Miller-Rabin Hensel lifting Vieta root jumping Game theory Combinatorial games Game trees Mini-max Nim Games on graphs Games on graphs with loops Grundy numbers Bipartite games without repetition General games without repetition Alpha-beta pruning Probability theory Optimization Binary search Ternary search Unimodality and convex functions Binary search on derivative Numerical methods Numeric integration Newton's method Root-finding with binary/ternary search Golden section search Matrices Gaussian elimination Exponentiation by squaring Sorting Radix sort Geometry Coordinates and vectors * Cross product * Scalar product Convex hull Polygon cut Closest pair Coordinate-compression Quadtrees KD-trees All segment-segment intersection Discretization (convert to events and sweep) Angle sweeping Line sweeping Discrete second derivatives Strings

Longest common substring Palindrome subsequences Knuth-Morris-Pratt Tries Rolling polynomial hashes Suffix array Suffix tree Aho-Corasick Manacher's algorithm Letter position lists Combinatorial search Meet in the middle Brute-force with pruning Best-first (A*) Bidirectional search Iterative deepening DFS / A* Data structures LCA (2^k-jumps in trees in general) Pull/push-technique on trees Heavy-light decomposition Centroid decomposition Lazy propagation Self-balancing trees Convex hull trick (wcipeg.com/wiki/Convex_hull_trick) Monotone queues / monotone stacks / sliding queues Sliding queue using 2 stacks Persistent segment tree

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