

**GUJARAT TECHNOLOGICAL UNIVERSITY****BE - SEMESTER-VI (NEW) EXAMINATION – SUMMER 2021****Subject Code:2160704****Date:05/08/2021****Subject Name:Theory of Computation****Time:02:30 PM TO 05:00 PM****Total Marks: 70****Instructions:**

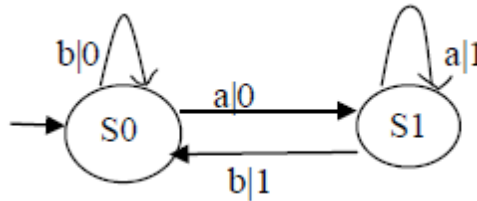
1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) Define DFA and NFA and NFA-  $\Lambda$  **03**
- (b) Write Regular Expressions corresponding to each of the following subsets of  $\{0,1\}^*$  **04**
- (i) The language of all strings containing both 101 and 010 as substrings.
- (ii) The language of all strings that do not end with 01.
- (c) Use the principle of mathematical induction to prove that  $1 + 3 + 5 + \dots + (2n-1) = n^2$  for all  $n > 0$  where  $r$  is an odd integer &  $n$  is the number of terms in the sum. **07**

- Q.2** (a) Define onto, one-to-one, and bijection functions. **03**
- (b) Using constructive approach determine NFA-  $\Lambda$  for the regular expression  $(0 + 1)^*1(0 + 1)$ . **04**
- (c) Convert the CFG,  $G (\{S,A,B\}, \{a,b\}, P, S)$  to CNF, where  $P$  is as follows **07**
- $S \rightarrow aAbB$
- $A \rightarrow Ab \mid b$
- $B \rightarrow Ba \mid a$

**OR**

- (c) Convert the Mealy machine shown in given figure into Moore machine. **07**



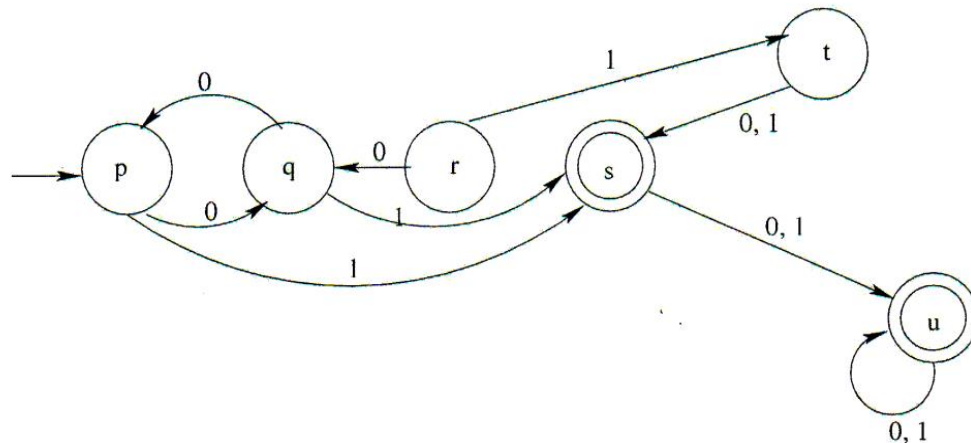
- Q.3** (a) Define CFG. When is a CFG called an 'ambiguous CFG'? **03**
- (b) Draw FA for accepting: The strings with odd no of 1's and odd no of 0's. **04**
- (c) Convert following NFA-  $\Lambda$  to NFA **07**

q	$\delta(q, \Lambda)$	$\delta(q, 0)$	$\delta(q, 1)$
A	{B}	{A}	$\varnothing$
B	{D}	{C}	$\varnothing$
C	$\varnothing$	$\varnothing$	{B}
D	$\varnothing$	{D}	$\varnothing$

**OR**

- Q.3** (a) Give recursive definitions of the extended transition functions,  $\delta^*$  for DFA and NFA. **03**
- (b) For the language  $L = \{ xcx^r \mid x \rightarrow \{a,b\}^* \}$  design a PDA(Push Down Automata). **04**
- (c) Write Kleene's Theorem part-I, Any regular language can be accepted by a finite automation. **07**

- Q.4** (a) State pumping lemma for regular languages. **03**  
 (b) Explain push down automata with example. **04**  
 (c) Minimize the DFA shown in Fig: **07**



**OR**

- Q.4** (a) What is Turing Machine? Write advantages of TM over FSM. **03**  
 (b) Write a short note on Universal Turing Machine. **04**  
 (c) Convert the following grammar to a PDA:  
 $I \rightarrow a \mid b \mid Ia \mid Ib \mid IO \mid II$   
 $E \rightarrow I \mid E * E \mid E + E \mid (E)$  **07**

- Q.5** (a) What are the applications of regular expressions and finite automata? **03**  
 (b) Consider following grammar:  
 $S \rightarrow ASB \mid \Lambda$   
 $A \rightarrow aAS \mid a$   
 $B \rightarrow SbS \mid A \mid bb$   
 i. Eliminate useless symbols, if any.  
 ii. Eliminate  $\Lambda$  productions. **04**  
 (c) Draw a Turing Machine(TM) to accept Palindromes over  $\{a,b\}$ . (Even as well as Odd Palindromes). **07**

**OR**

- Q.5** (a) Define grammar and chomsky hierarchy. **03**  
 (b) Write a short note on church-turing thesis. **04**  
 (c) Write a Turing Machine to copy strings. **07**

\*\*\*\*\*