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# Input Data and Distance Measures

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# Anatomy of unsupervised algorithms

## Internal choices / cost function:

- Usually, we cannot control these.
- Strongly affect the result, and define the range of possible outputs.

## Algorithm output:

- Density distribution.
- Clusters.
- Embedding in low-D space.
- Outliers.

The diagram illustrates the anatomy of unsupervised algorithms. At the center is the equation  $f(\vec{X}, \{a_1, a_2, \dots\}) = \vec{y}$ . Four arrows point from this equation to surrounding boxes: a teal arrow points from  $\vec{X}$  to the 'Input dataset' box; a red arrow points from  $\{a_1, a_2, \dots\}$  to the 'Internal choices / cost function' box; a green arrow points from  $f$  to the 'Hyperparameters' box; and a brown arrow points from  $\vec{y}$  to the 'Algorithm output' box.

$$f(\vec{X}, \{a_1, a_2, \dots\}) = \vec{y}$$

## Input dataset:

- Raw data (spectra, images, light-curves).
- Extracted features.
- Measured relations between different objects (distances, correlations).

## Hyperparameters:

- Tuning parameters of the algorithm.
- Can strongly affect the result.
- Traditionally, cannot be optimized for.

# Types of input data

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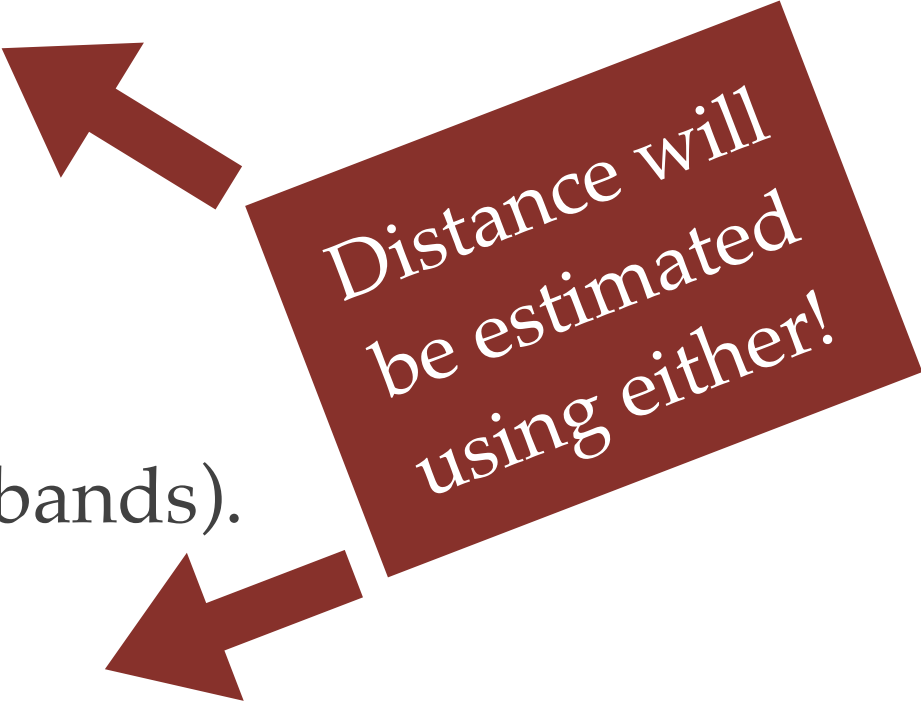
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Distance will be estimated using either!

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- ❖ **Simplicity:** the number of derived features will typically be lower than the number of dimensions in the original data. This means that we are trying to solve a simpler task and many algorithms do not scale well with the number of dimensions. It is always better to use knowledge we already have, rather than hoping it will come out naturally from the algorithm. While in some cases the algorithm will discover what we already know, it will often come at the expense of discovering something new.

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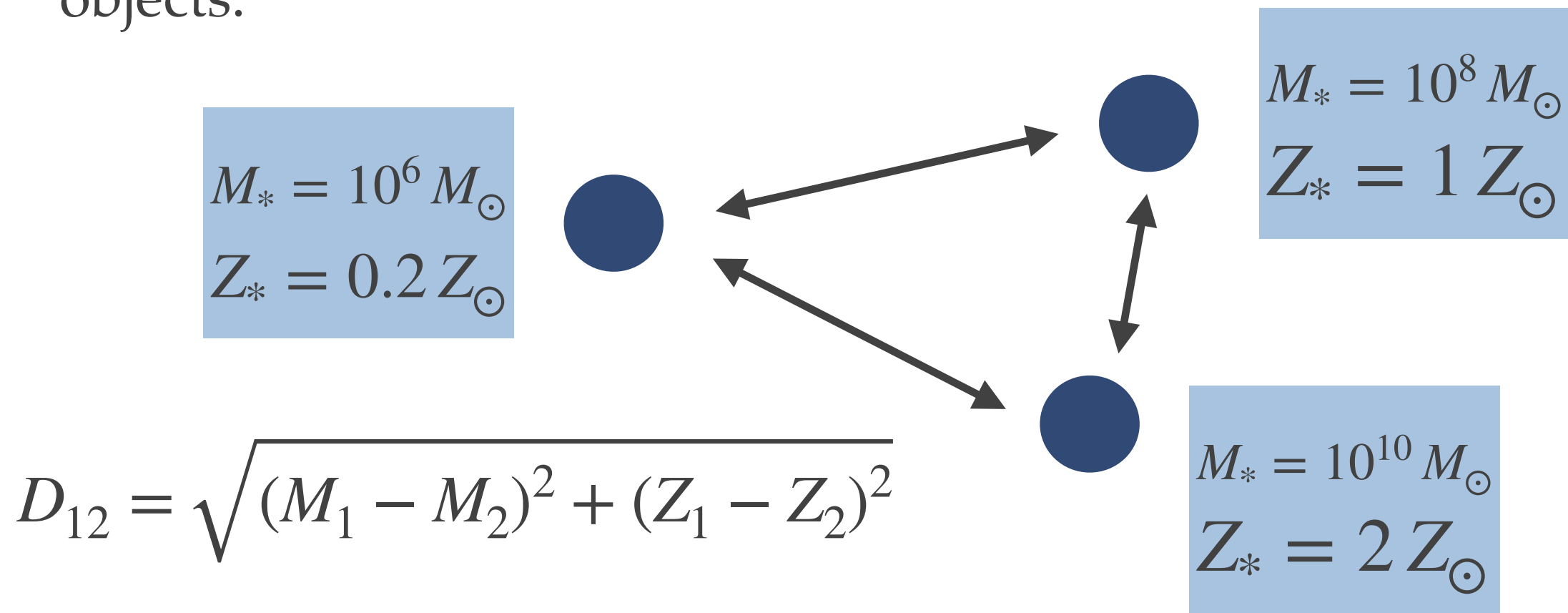
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- ❖ **Interpretability:** it is easier to understand what is the meaning of the algorithm's output using derived features.
- ❖ **Potential for new discoveries:** by using derived features we are limiting ourselves to a fewer number of parameters which we are already familiar with, which reduces the discovery potential. We only derive features for what we already know, what about the things we don't know?

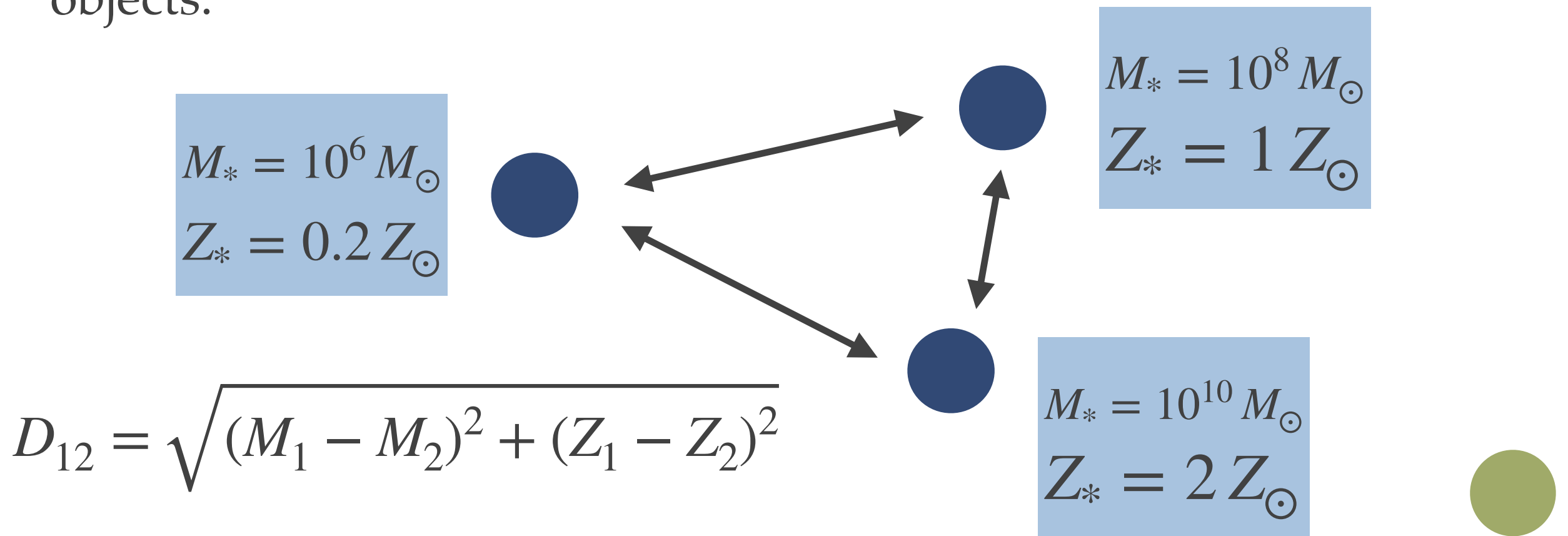
# Derived features: aspects to consider

- ❖ **Feature scaling and normalization:** features derived from astronomical observations have physical units, and might have different dynamical scales. Features with larger variance will dominate the summed Euclidean distance between individual objects.



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- ❖ **What to do?** Apply rescaling and normalization to all the features. Use the logarithm of the feature as the new feature, and/or normalize using the mean and standard deviation of the distribution:  $f_{norm} = (f - \mu_f) / \sigma_f$ .

# Derived features: aspects to consider


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- ❖ **Outliers:** some algorithms are based on the variance within each feature and are highly-sensitive to the presence of outliers in the data.
- ❖ **What to do?** Use histograms to inspect each feature separately and identify and / or remove outliers. A common practice is also to clip the feature values to be between the 0.5th and 99.5th percentiles of the distribution.



# Derived features: aspects to consider

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- ❖ **Correlated features:** a set of highly-correlated features in the dataset will result in a higher weight in the summed Euclidean distance, which may wash-out other structures in the dataset.
  - ❖ **What to do?**
    - ❖ Use PCA to obtain features in an orthogonal space. Might not be very interpretable.
    - ❖ Instead of using the correlated features, use the deviation of one feature from the correlation with another. Might not scale well for multiple features with multiple correlations.
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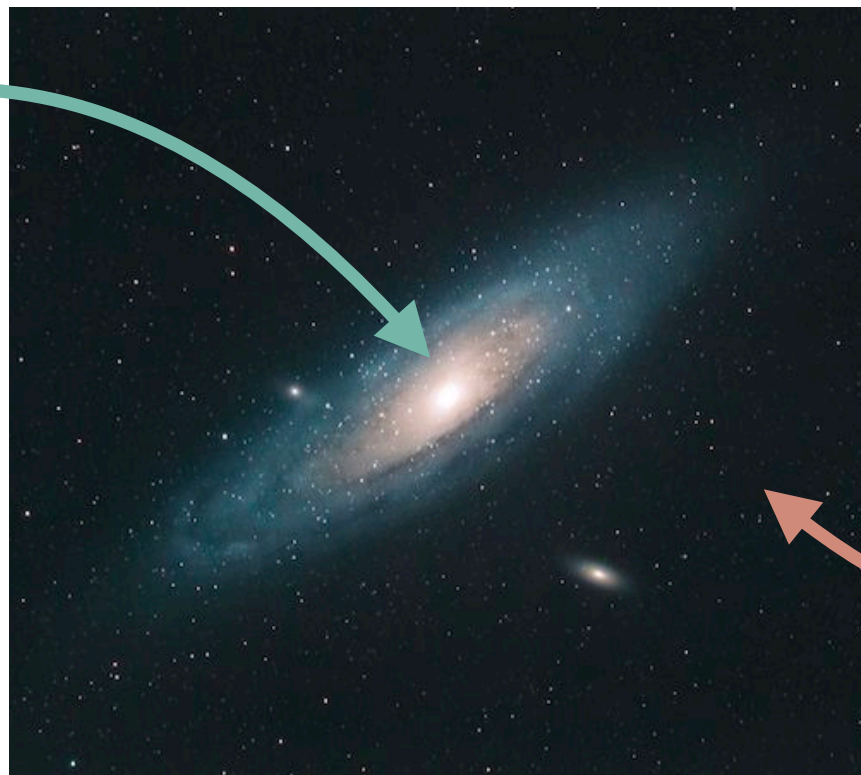
- ❖ Similarly to the derived features case, but depending on the data:
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- ❖ Not all features are equally-important.

More important  
pixels



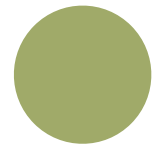
Less important  
pixels

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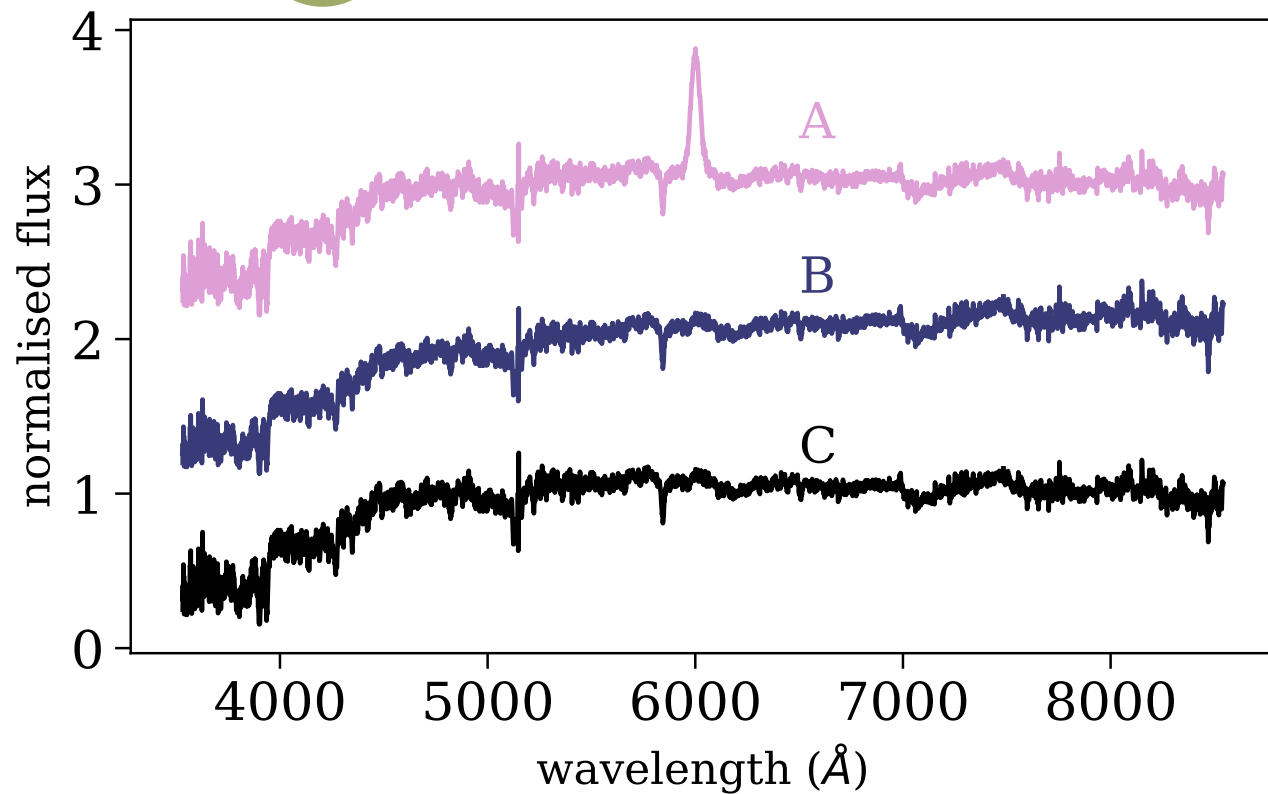
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  - ❖ Correlated features.
- ❖ Not all features are equally-important.
- ❖ May be beneficial to transform the data into a different space. For example:
  - ❖ Frequency domain for time series data.
  - ❖ Wavelet transform for imaging data.
  - ❖ Representation using “eigenvectors” of spectral information.

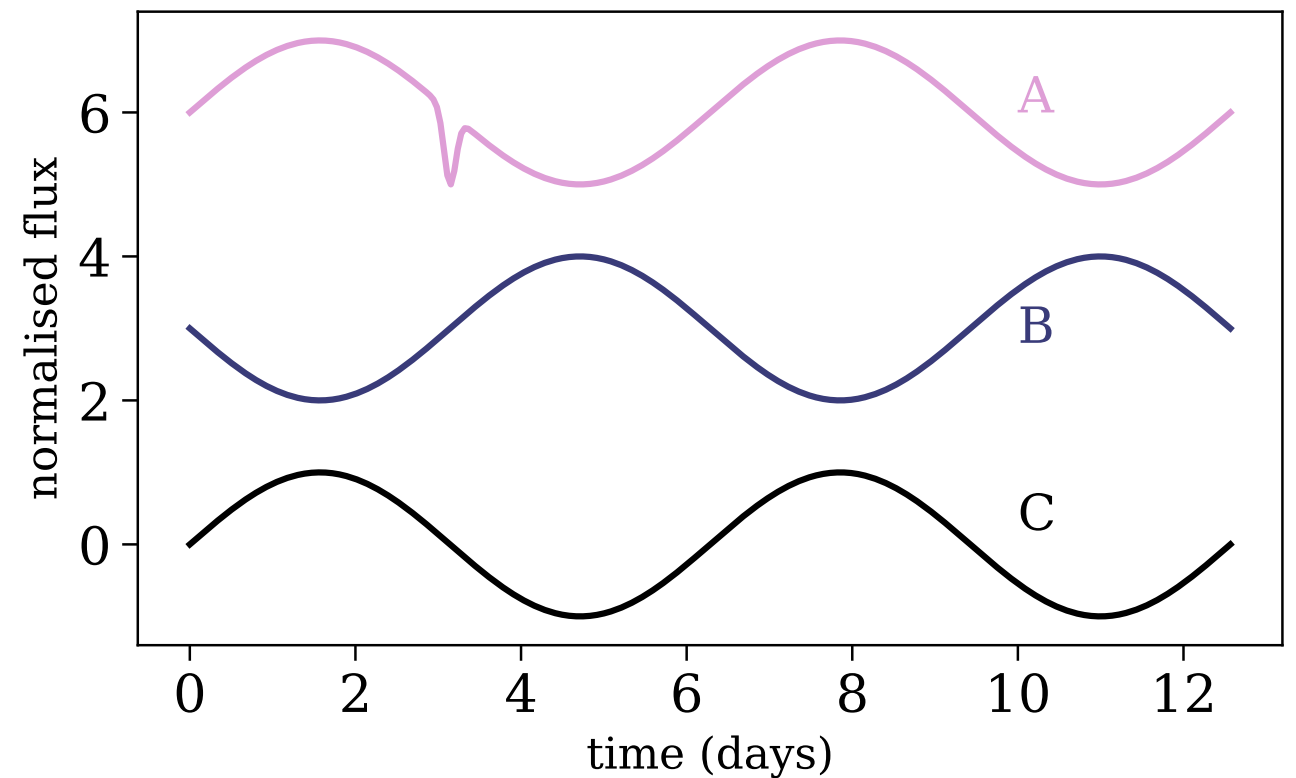
# Raw data: aspects to consider



Example of spectra:



Example of time-series:



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# Distance measures

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Regardless of whether we want to perform clustering, dimensionality reduction, or outlier detection, the large majority of algorithms start by estimating the pairwise distance between objects in the N-dimensional space.

# Distance measures

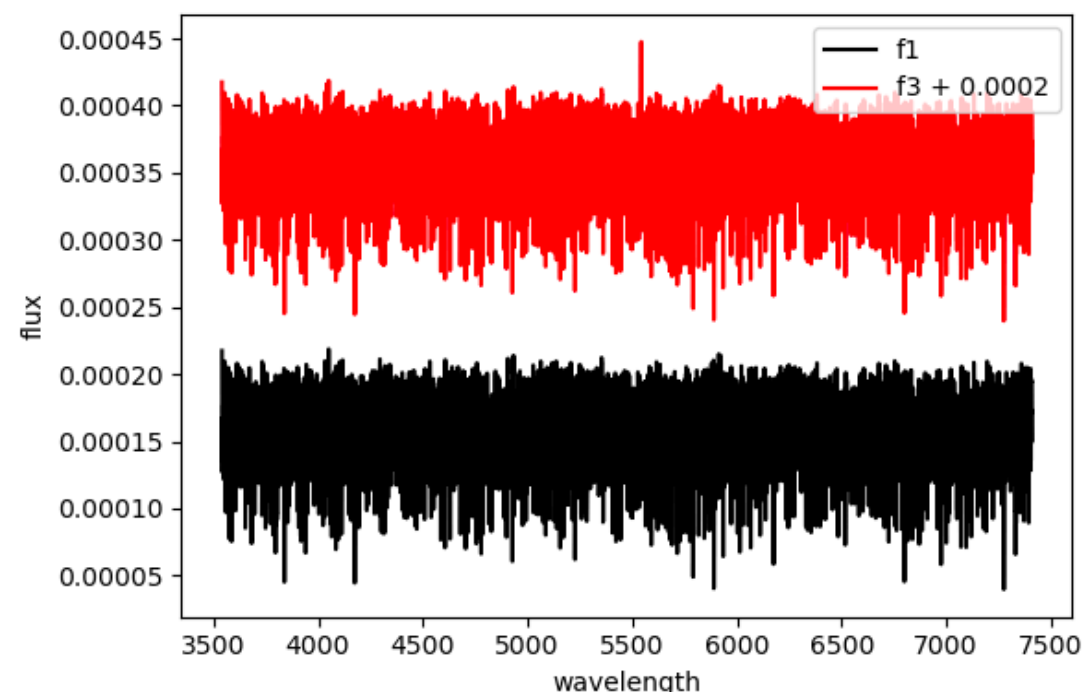
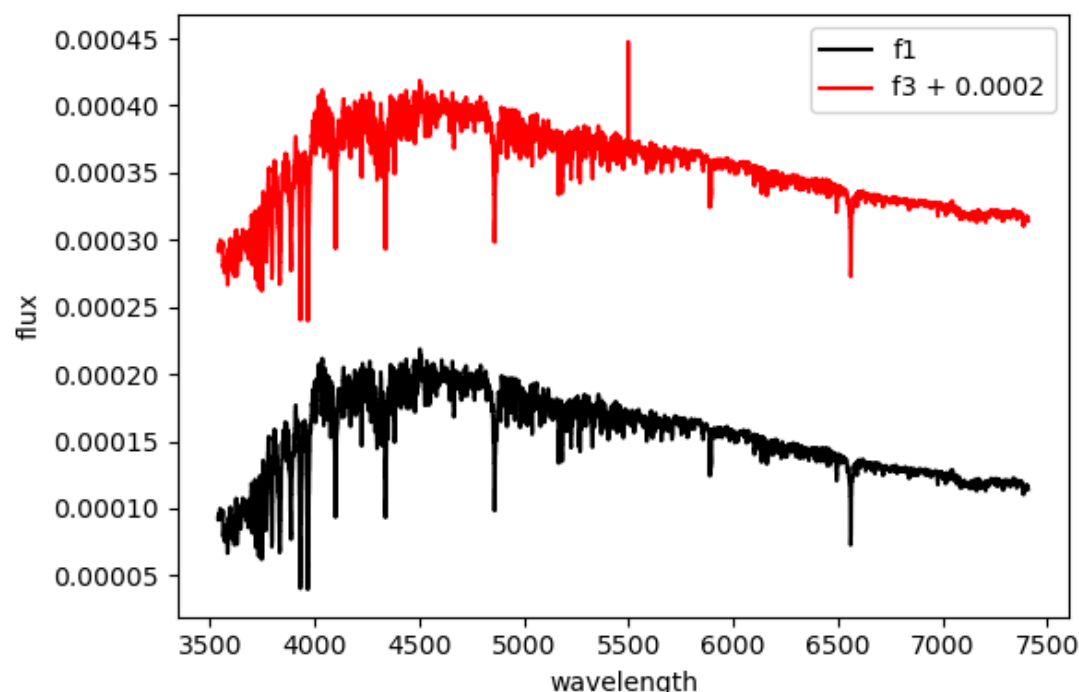
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## ❖ Euclidean Distance:

❖ The default distance metric assumed in most cases.

❖ All features are equally important:  $D_{ij}^2 = \sum_{f:\text{features}} (x_{if} - x_{jf})^2$

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- ❖ Other metrics:

- ❖ Pearson / Spearman correlation coefficient.

- ❖ KL-divergence.

- ❖ Earth mover's distance or energy distance: the relative order of the features matters!!.

- ❖ A list of popular metrics can be found here.