

BM2043 - Algorithms and Data Structures

Exercise - 6

Dr Nagarajan Ganapathy

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Write the most efficient algorithm for the following problems in C++ and mention the Time and Space Complexity of your algorithms in the comments (at the end).

Backtracking

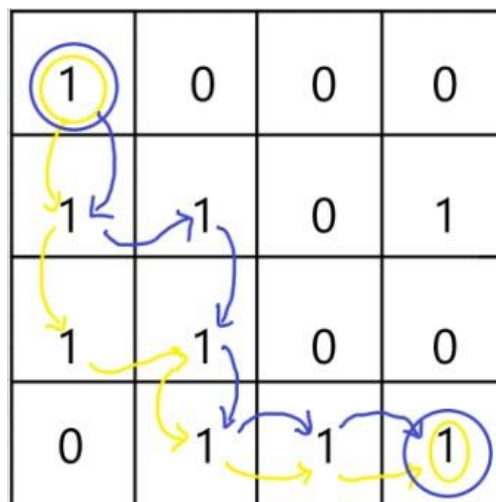
- Consider a rat placed at (0, 0) in a square matrix of size $m \times n$. It has to reach the destination at $(m-1, n-1)$. Find all possible paths that the rat can take to reach from source to destination. The directions in which the rat can move are 'U'(up), 'D'(down), 'L' (left), 'R' (right). Value 0 at a cell in the matrix represents that it is blocked and the rat cannot move to it while value 1 at a cell in the matrix represents that rat can travel through it.

Test Case:

Input: $m=4$, $n=4$, Matrix = $\{\{1, 0, 0, 0\}, \{1, 1, 0, 1\}, \{1, 1, 0, 0\}, \{0, 1, 1, 1\}\}$.

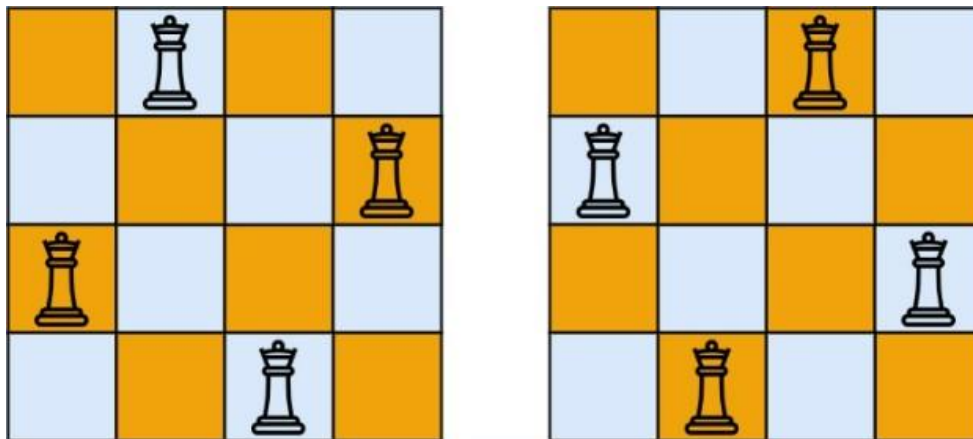
Output: "DDRDRR", "DRDDRR".

Explanation:



2. The n-queens puzzle is the problem of placing n queens on an $n \times n$ chessboard such that no two queens attack each other. Given an integer n , return all distinct solutions to the n - queens puzzle. You may return the answer in any order. Each solution contains a distinct board configuration of the n-queens' placement, where 'Q' and '.' both indicate a queen and an empty space, respectively.

Test Case:



Input: $n = 4$

Output: `[[".Q..", "...Q", "Q...", "..Q."],
["..Q.", "Q...", "...Q", ".Q.."]]`

Explanation: There exist two distinct solutions to the 4-queens puzzle as shown above

- 3. Given an integer array `nums` of unique elements, return all possible subsets (the power set). The solution set must not contain duplicate subsets. Return the solution in any order.**

Test Case:

Input: `Nums = [1,2,3]`

Output: `[[], [1], [2], [1,2], [3], [1,3], [2,3], [1,2,3]]`.

- 4. You have been given a string `s` and asked to partition `s` such that all the substrings are palindromes. Return all possible palindrome partitions of `s`.**

Test Case:

Input: `s = "aab"`

Output: `[["a","a","b"],["aa","b"]]`

