

# Adsorption[ solid liquid, gas-solid system]

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Solid –liquid Separation

# Dataset: Solid –gas system, calculation of specific surface area of an adsorbent

| P mm Hg<br>( $P_v=760$<br>mm Hg),<br>$T=77.4$ | 10   | 20    | 40    | 100   | 150  | 200  | 250  | 300  | 350  | 400  | 500  |
|---|------|-------|-------|-------|------|------|------|------|------|------|------|
| q (amount<br>adsorbed<br>per solid)           | 71.3 | 142.2 | 287.7 | 679.4 | 1025 | 1053 | 1175 | 1316 | 1996 | 3451 | 5283 |

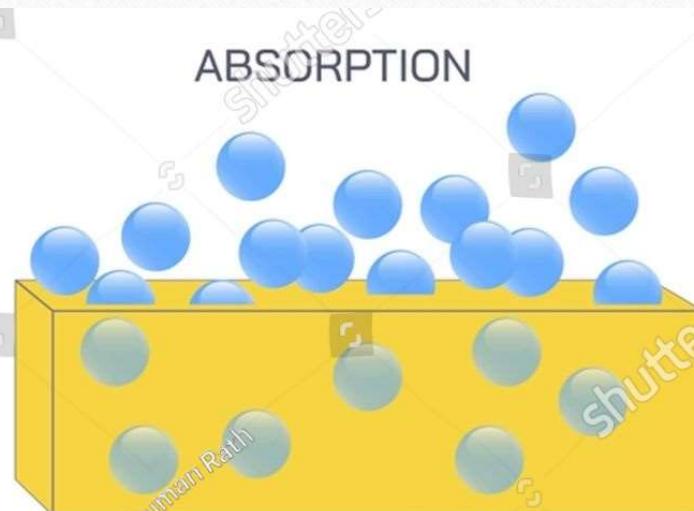
$P \rightarrow$  Pressure of  $N_2$  ( mm Hg)

$q \rightarrow$  Volume of  $N_2$  adsorbed / 100 gm solid ( $cm^3$ ) .

# Difference between Absorption and adsorption

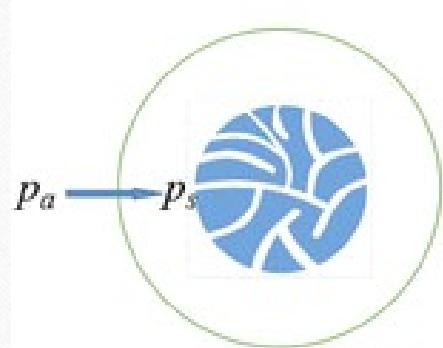


The adhesion of particles onto a surface of a substance.

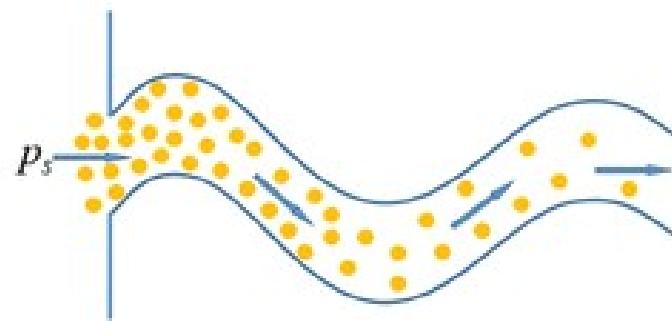


The particles of a substance enter into the volume/bulk of another.

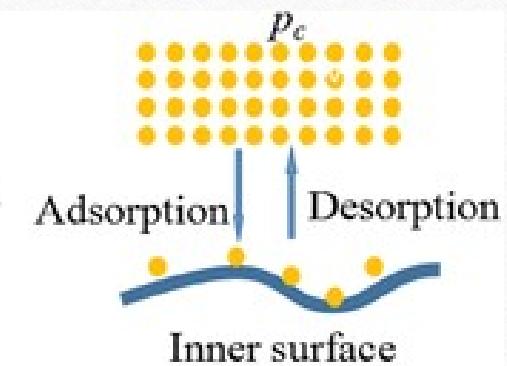
# Adsorption



Step 1 Interparticle diffusion



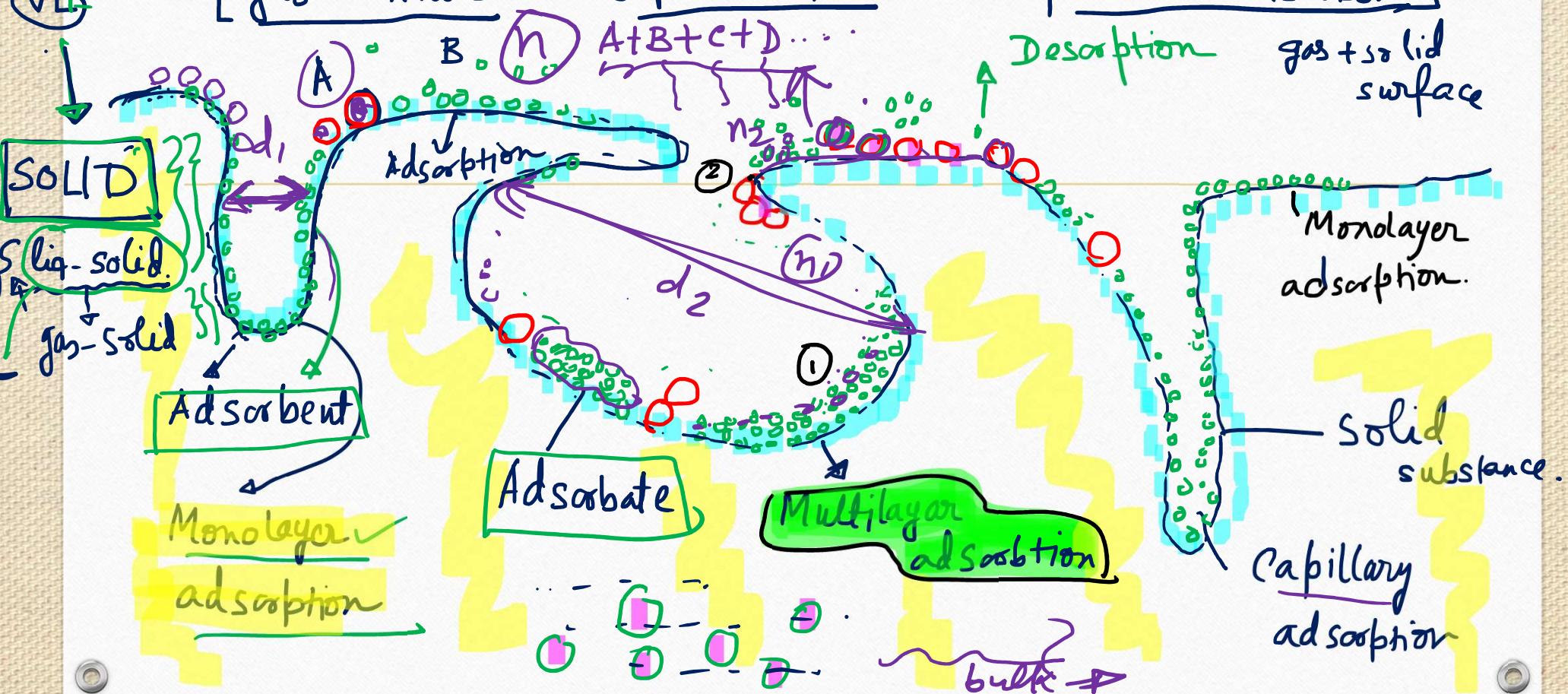
Step 2 Intraparticle diffusion



Step 3 Surface process

# Multilayer adsorption of a binary mixture

[gas-mixture or liquid mixture on porous adsorbent]



## ADSORPTION MECHANISM

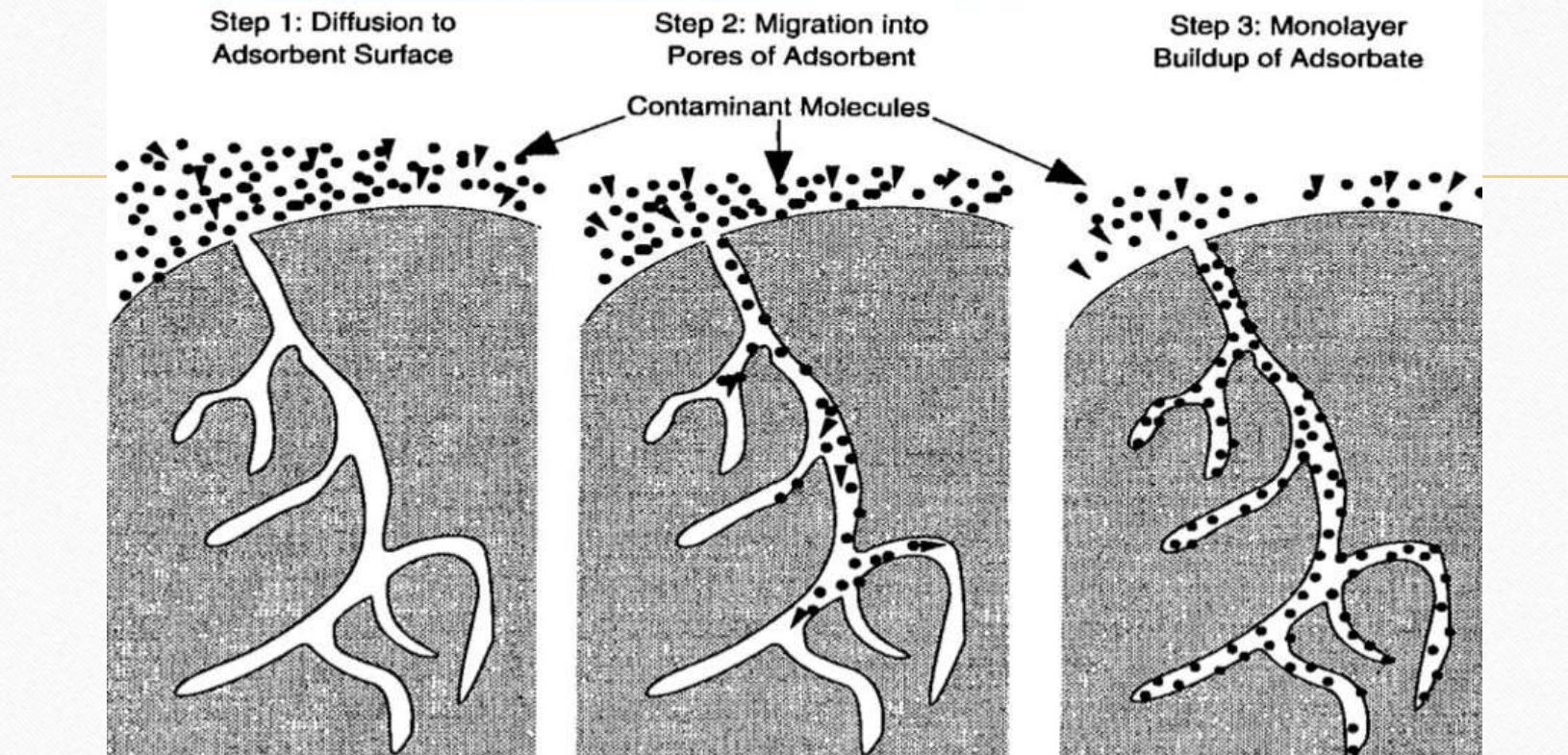
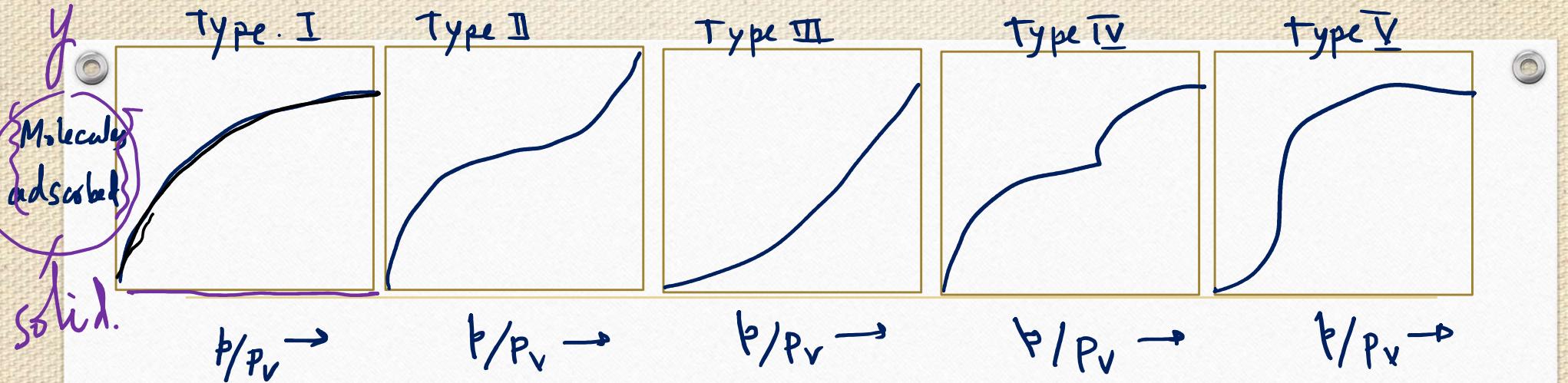


Figure 2.1 : Adsorption mechanism

# Adsorption video

[https://www.google.com/search?q=adsoption+process++youtube+video&sca\\_esv=594982741&sxsrf=AM9HkKmb8EpXx3QMIB2HGvhnpzePCAPyLA%3A1704160461988&ei=zWyTZb3-O9O6seMPspOziAw&ved=0ahUKEwj9mOi3zL2DAxVTXWwGHbLJDMEQ4dUDCBA&uact=5&oq=ads option+process++youtube+video&gs\\_lp=Egxnd3Mtd2l6LXNlcnAiIGFkc29wdGlvbiBwcm9jZXNzICB5b3V0dWJlIHZpZGVvMgoQIRigARjDBBgKMgoQIRigARjDBBgKSJAbUM8EWN8WcAB4AJABAJgBqgGgAesLqgEEMC4xMLgBA8gBAPgBACICBxAjGLACGCfiAwQYASBBiAYB&sclient=gws-wiz-serp#fpstate=ive&vld=cid:7b33acf0,vid:xGS-P7YRE5c,st:0](https://www.google.com/search?q=adsoption+process++youtube+video&sca_esv=594982741&sxsrf=AM9HkKmb8EpXx3QMIB2HGvhnpzePCAPyLA%3A1704160461988&ei=zWyTZb3-O9O6seMPspOziAw&ved=0ahUKEwj9mOi3zL2DAxVTXWwGHbLJDMEQ4dUDCBA&uact=5&oq=ads option+process++youtube+video&gs_lp=Egxnd3Mtd2l6LXNlcnAiIGFkc29wdGlvbiBwcm9jZXNzICB5b3V0dWJlIHZpZGVvMgoQIRigARjDBBgKMgoQIRigARjDBBgKSJAbUM8EWN8WcAB4AJABAJgBqgGgAesLqgEEMC4xMLgBA8gBAPgBACICBxAjGLACGCfiAwQYASBBiAYB&sclient=gws-wiz-serp#fpstate=ive&vld=cid:7b33acf0,vid:xGS-P7YRE5c,st:0)

[https://www.google.com/search?q=adsorption+youtube+video&sca\\_esv=594987936&sxsrf=AM9HkKl91vdPeb5W3LHc9ig1TGAb2Wg8Uw%3A1704161597486&source=hp&ei=PXGTZeG3G-3V4-EP5JCs6A0&iflsig=AO6bgOgAAAAAZZN\\_Tf2YfxzATNmboZIqValvA9fr8mmW&oq=&gs\\_lp=Egdnd3Mtd2l6IgAqAggAMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnSIYhUABYAHABeACQAQCyaQCgAQCqAQC4AQHI AQCoAgo&sclient=gws-wiz#fpstate=ive&ip=1&vld=cid:ed54b63b,vid:FcsE22UU18c,st:0](https://www.google.com/search?q=adsorption+youtube+video&sca_esv=594987936&sxsrf=AM9HkKl91vdPeb5W3LHc9ig1TGAb2Wg8Uw%3A1704161597486&source=hp&ei=PXGTZeG3G-3V4-EP5JCs6A0&iflsig=AO6bgOgAAAAAZZN_Tf2YfxzATNmboZIqValvA9fr8mmW&oq=&gs_lp=Egdnd3Mtd2l6IgAqAggAMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnMgcQIxjqAhgnSIYhUABYAHABeACQAQCyaQCgAQCqAQC4AQHI AQCoAgo&sclient=gws-wiz#fpstate=ive&ip=1&vld=cid:ed54b63b,vid:FcsE22UU18c,st:0)



Five basic types of adsorption isotherm -

$\rho$  = adsorbate pressure -

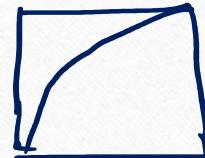
$P_v$  = saturation vapor pressure of the adsorbate.

$\rho y P_v - \frac{P_2}{P_v}$

$\frac{P_3}{P_v}$

Type I: Isotherm  $\rightarrow$  formation of mono molecule layer on adsorbate. [Solute in low concn].

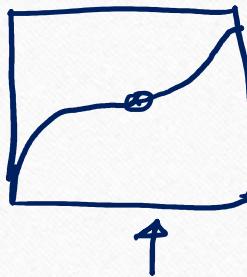
Mono layer



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Relatively higher concn  
of solute loading in solid.

(Ex)  $O_2$  in carbon black.



Type III  $\rightarrow$  formation of infinite multilayer - after having one monolayer.

(Ex)  $H_2O$  vap on carbon black.

Type III.: Amount of adsorption increases indefinitely.  
as its relative saturation  $p/p_v$  approaches  $\sim 1$ .

Unfavourable  $\rightarrow$

solute concn is low at a small concn in the fluid -

e.g.  $N_2$  adsorption-ice.

Type IV, g v.  $\rightarrow$  having the alternative convex and concave  
region  $\rightarrow$  possibly having capillary condensation in pores.



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LangMuir was awarded  
the Nobel Prize in  
Chemistry in 1932 for his  
work in surface chemistry.

# Langmuir isotherm: Irving Langmuir

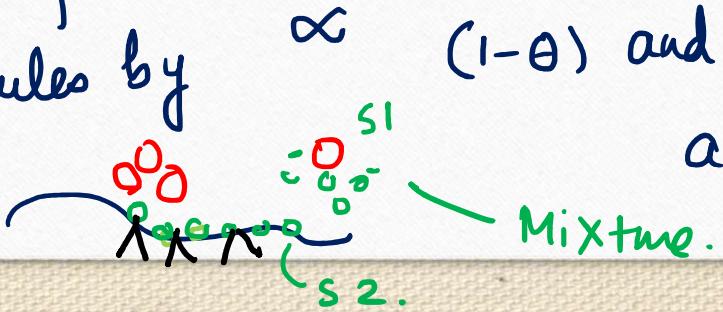
**Assumptions:** (1) Molecules are adsorbed at discrete active sites on the surface.

(2) Each active site adsorbs one molecule.

(3) The adsorbing surface is energetically uniform.

(4) There is no interaction among adsorbed molecules.

Rate of capture of  
adsorbate molecules by  
surface



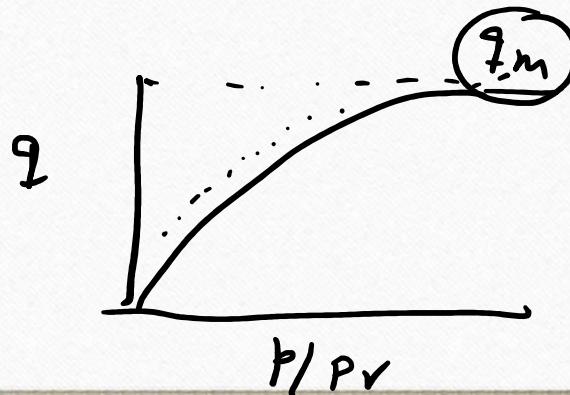
$\propto$  Fraction of uncovered area  
( $1-\theta$ ) and  $p \cdot \text{prt}$  concn of  
adsorbate.

## Notations

$q$  = amount of gas or liquid solute adsorbed.  
at equilibrium / gm of adsorbent at  $P$  or concn C.

$q_m$  = Maximum quantity of gas or liquid. solute.  
adsorbed/gm of adsorbent at saturation.

$$\theta = q/q_m.$$



## Theoretical Basis.

Rate of capture.

$$\text{or rate of adsorption} = k_1 p (1-\theta).$$

$$\text{Rate of desorption} = k_2 \theta.$$



$$k_1 p (1-\theta) = k_2 \theta.$$

$$\Rightarrow \theta = \frac{k_1 p}{k_2 + k_1 p} = \frac{K p}{1 + K p} \quad K = k_1/k_2.$$

$$\theta = q/q_m \Rightarrow$$

$$q = q_m \frac{K p}{1 + K p}$$

Langmuir  
isotherm.  
2 parameters  
 $K$  &  $q_m$ .

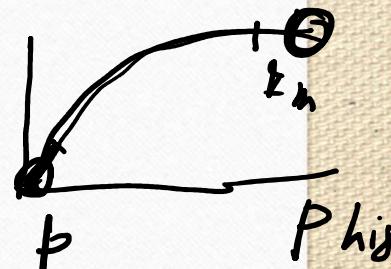
$$\text{Langmuir isotherm } q_i = \frac{q_m K_p}{1 + K_p} .$$

@ If p-pressure of the adsorbate is low  $K_p \ll 1$ .

$$q_i = q_m K_p = K_H p \rightarrow \begin{bmatrix} \text{linear isotherm} \\ \sim \text{Henry's law} \end{bmatrix}$$

If p-pressure is high  $K_p \gg 1$

$$\Rightarrow q_i = \frac{q_m K_p}{K_p} = q_m \cdot \underline{\text{saturation}} .$$



# Experimental data analysis

$$q = \frac{q_m K p}{1 + K p} \quad - \text{Langmuir isotherm}$$

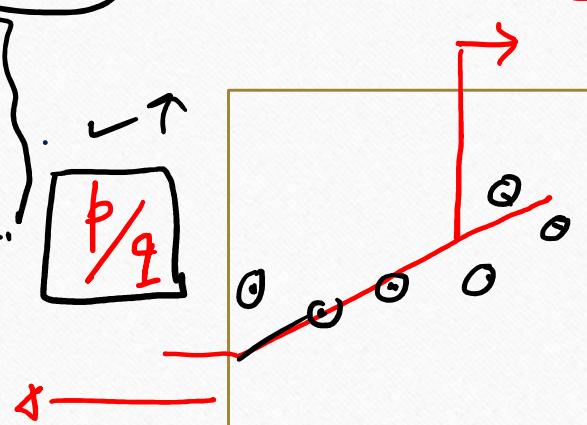
$$\rightarrow \frac{1}{q} = \frac{1 + K p}{q_m K p} = \frac{1}{q_m K} + \frac{1}{q_m} \quad \text{const.}$$

~~(X)~~

$$\Rightarrow \frac{p}{q} = \frac{1}{q_m K} + \frac{p}{q_m} \quad y = mx + c$$

$q_m$  &  $K$  can be estimated.

$$\text{Intercept} = \frac{1}{q_m K}$$



$p \rightarrow$

## What is isotherm?

The equilibrium relation between amount of gas/liquid.

(q) mass adsorbed per unit mass of the solid.

adsorbent or solute  $\rightarrow$  Adsorption Isotherm.

$$q = f(c) \text{ at constant } T$$

## What is isotere?

Plot of  $\ln(c)$  or  $\ln(P)$  of solute in fluid/gas vs  
inverse of absolute temperature  $Y_T$  for a constant  
loading of  $q$  of the adsorbant.,  $c = \gamma(Y_T)$ .  $P = \gamma'(Y_T)$  const $q$ .

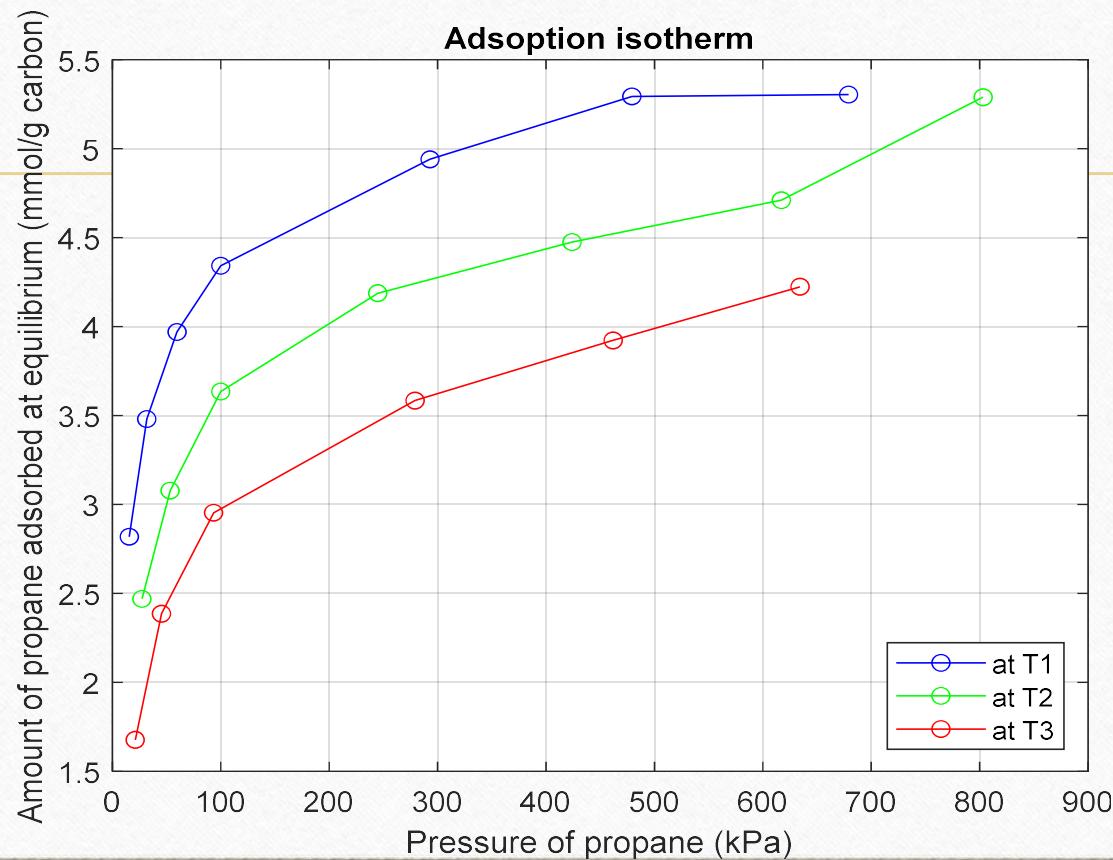
# Heat of adsorption

**12.4 (Fitting of Langmuir isotherm and determination of heat of adsorption)<sup>2</sup>** Ray and Box (*Ind. Eng. Chem.*, 42(1950) 1315) reported the following data on equilibrium adsorption of propane on activated carbon at three different temperatures.

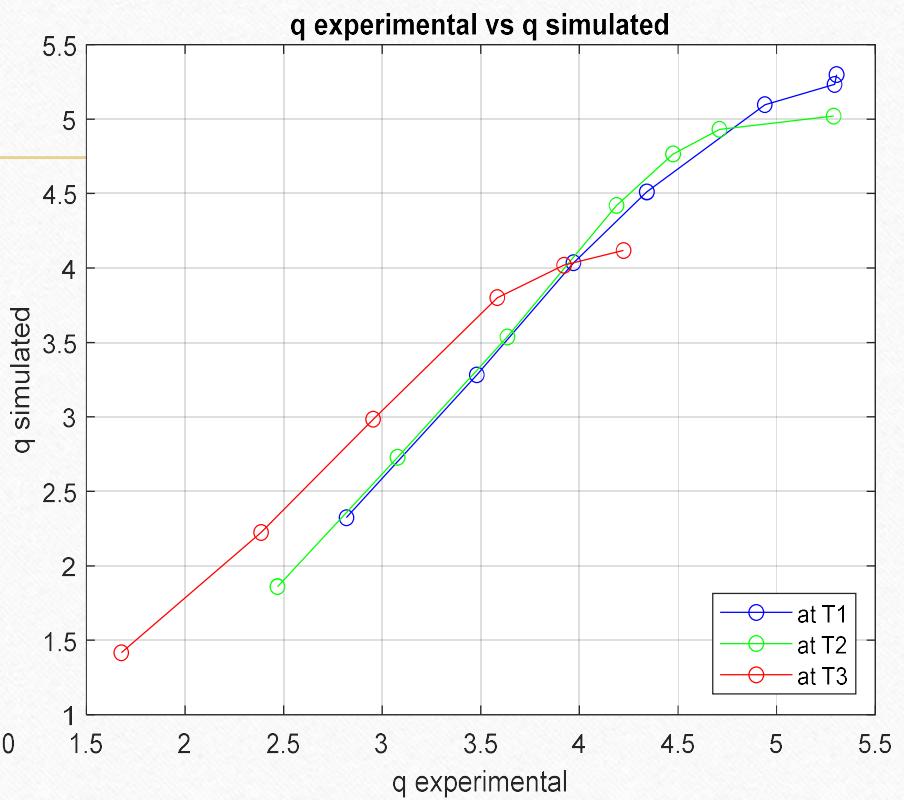
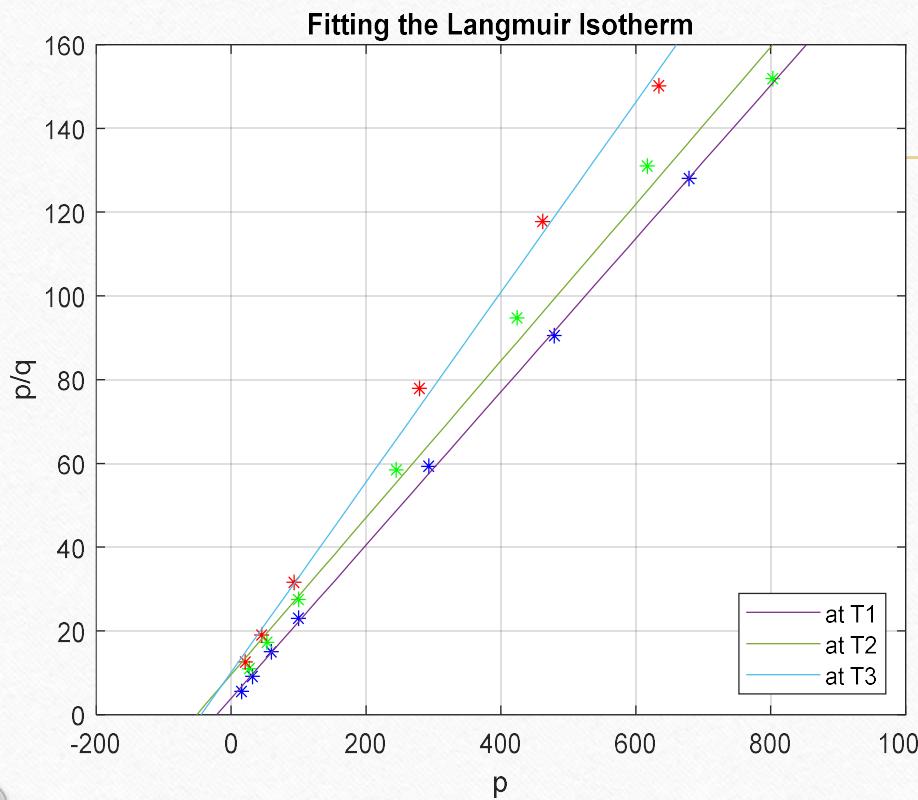
| $T = 310.9 \text{ K}$ |                      | $338.7 \text{ K}$ |                      | $366.5 \text{ K}$ |                      |
|-----------------------|----------------------|-------------------|----------------------|-------------------|----------------------|
| $p \text{ (kPa)}$     | $q \text{ (mmol/g)}$ | $p \text{ (kPa)}$ | $q \text{ (mmol/g)}$ | $p \text{ (kPa)}$ | $q \text{ (mmol/g)}$ |
| 15.6                  | 2.819                | 27.2              | 2.469                | 21.07             | 1.677                |
| 31.74                 | 3.48                 | 53.2              | 3.078                | 45.33             | 2.386                |
| 59.6                  | 3.97                 | 99.97             | 3.635                | 93.34             | 2.954                |
| 99.97                 | 4.342                | 244.8             | 4.188                | 279.2             | 3.584                |
| 293                   | 4.94                 | 424               | 4.475                | 461.9             | 3.922                |
| 479.2                 | 5.294                | 617.1             | 4.71                 | 634.3             | 4.244                |
| 679.1                 | 5.304                | 803.2             | 5.289                |                   |                      |

Fit the data using Langmuir isotherm and get the correlation coefficients. Determine the isosteric heat of adsorption.

# Adsorption of propane at different temperature



# Langmuir Isotherm fitting at different temperature



# Slope and intercept for Langmuir isotherm

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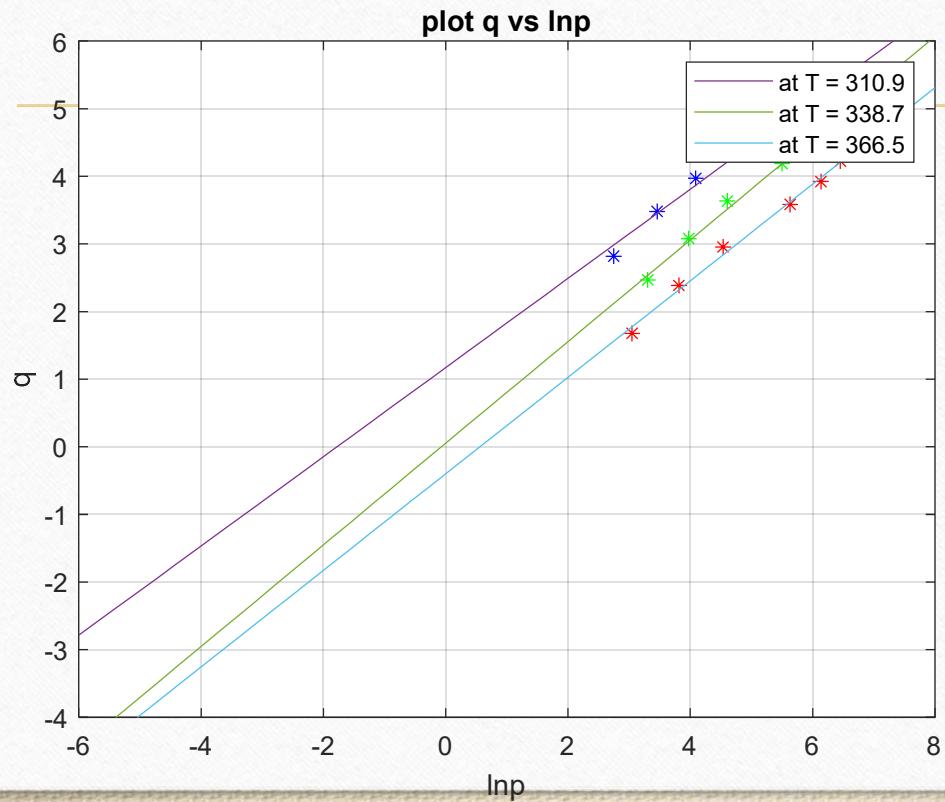
## Parameters

qm1 = 5.4631, k1 = 0.0474

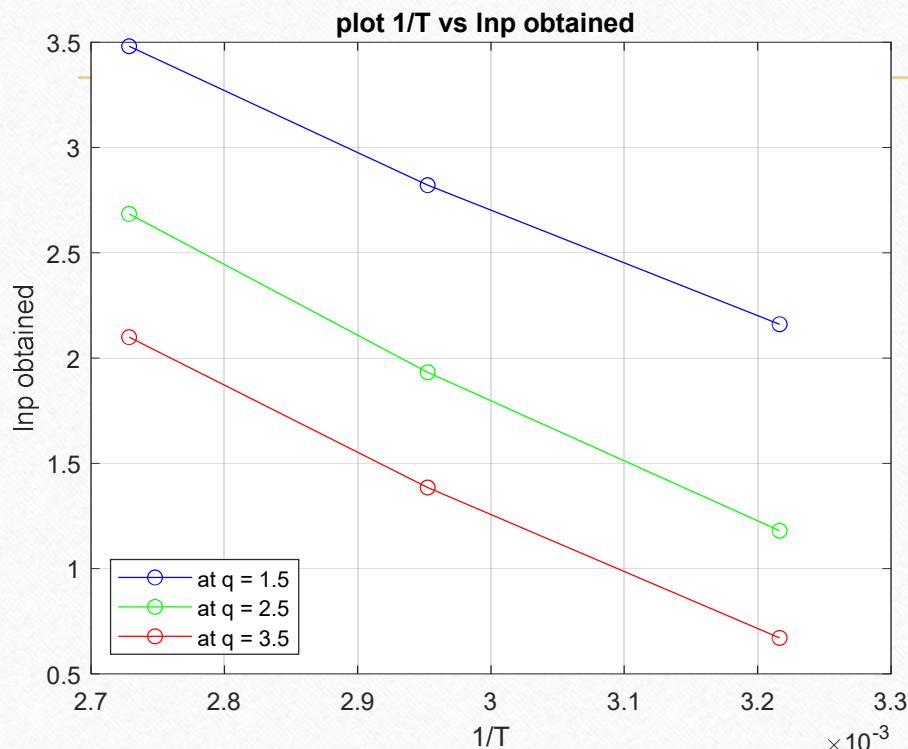
qm2 = 5.3379, k2 = 0.0197

qm3 = 4.4060, k3 = 0.0225

# Plot of q vs lnP



# Heat of adsorption



determination of heat of adsorption  
%from Clausius-Clayperon equation:

$$\Delta H_{iso} = -R \cdot (T^2) \cdot d(\ln P) / dT = R \cdot d(\ln P) / d(1/T)$$

$$\ln(P_2/P_1) = -(d\Delta H_{iso} / R) [(1/T_2 - 1/T_1)]$$

Freundlich isotherm? } SPE.

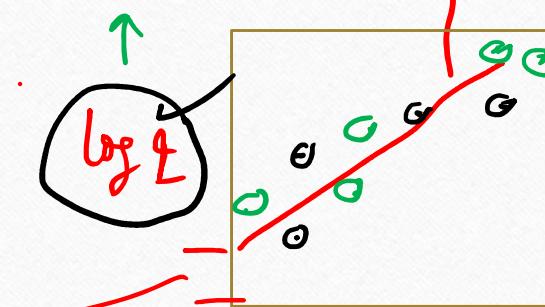
$$\rightarrow q = k' p^n \quad (\text{empirical}) \Rightarrow$$

$$q = k' C^{\frac{1}{n}} \quad \begin{matrix} \downarrow \\ \text{concentration} \end{matrix}$$

Amount of adsorbed @ eqbm has power law dependence on the partial pressure of gas solute [conc of liq solute]

$k'$ ,  $n$  → 2 adjustable parameters →

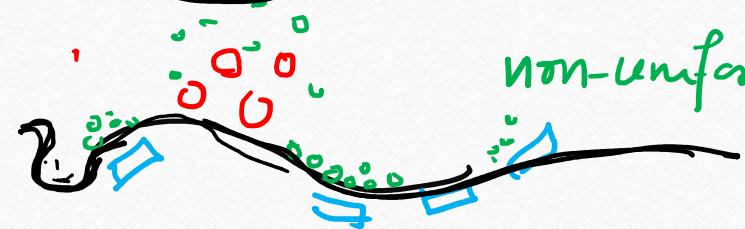
$$\log q = \frac{1}{n} \log p + \log k'$$



non-uniformity  
intercept

$$= \log k'$$

$\log p \rightarrow$



Non-uniform adsorbing surface // different sites are energetically not the same.

Toth isotherm?  $\xrightarrow{\quad}$  Mixture Model  $\rightarrow$ .

$$q = \frac{q_m b}{(b + b^n)^{y_n}}. \text{ (Empirical).}$$

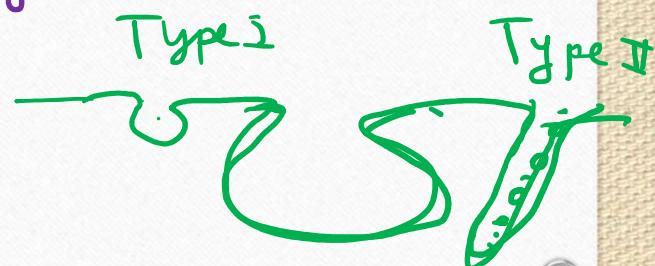
$\uparrow$  no of parameters.  $(b + b^n)^{y_n}$

$q_m, b, n$  three parameter isotherm.

[Applicable for heterogeneous adsorption surface]

at low  $p_r$ ,  $b^n \rightarrow 0$

$$\therefore q = \frac{q_m b}{b^{y_n}} = \kappa b \rightarrow \text{Henry's law.}$$



## Sips' isotherm?

3-parameter Model,

$$q = \frac{q_m \cdot ((K''P)^n)}{1 + (K''P)^n}$$

$q_m$  = max<sup>m</sup> adsorption capacity

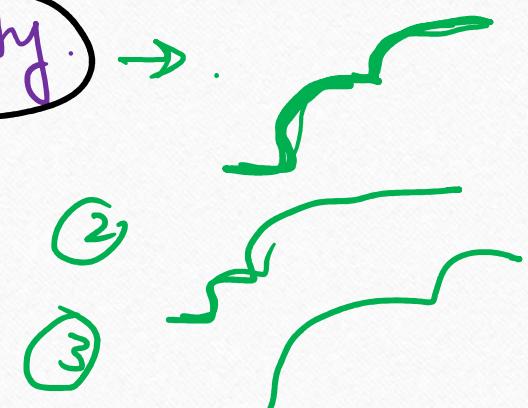
$K''$  = affinity co-efficient

$n$  = measure of system heterogeneity

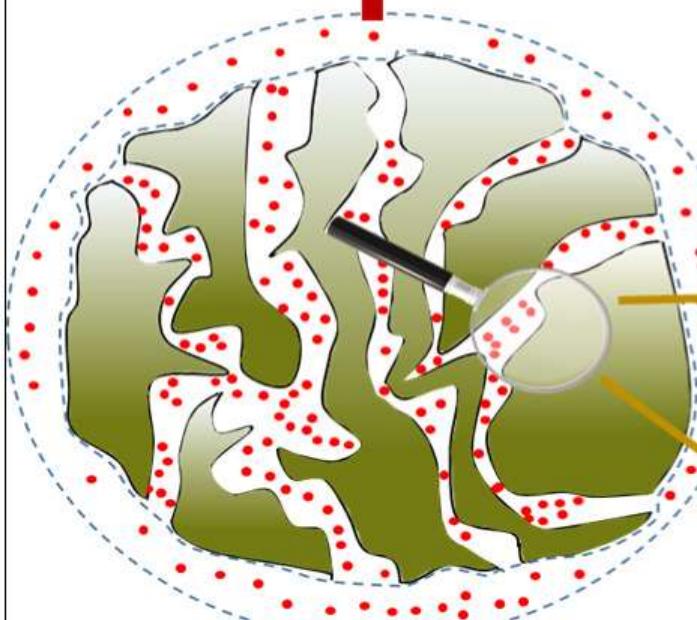
✓ statistical  
↔ Langmuir + Toth

(Langmuir +  
Toth)

①



### *Fluid film diffusion*



$$Bi = \frac{k_f \cdot r_p \cdot \bar{C}_0}{\mathfrak{D}_p \cdot \bar{C}_0 + \mathfrak{D}_s \cdot \rho_p \cdot \bar{q}_0}$$

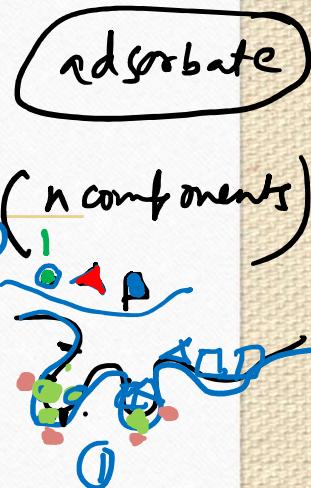
*Pore diffusion*

*Surface diffusion*

Approach. → Multicomponent adsorption isotherm

Use of Langmuir model. to describe adsorption equilibrium in a multicomponent system.

$$q_i^o = q_{im} \frac{b_i \beta_i}{1 + b_1 \beta_1 + b_2 \beta_2 + \dots + b_n \beta_n}$$
$$q_2 = q_3 = \dots$$
$$q_1 = \frac{q_{im} b_1 \beta_1}{1 + \sum b_i \beta_i}, \quad q_2 = \frac{q_{im} b_2 \beta_2}{1 + \sum b_i \beta_i}$$



Presence of another component competing for active sites.

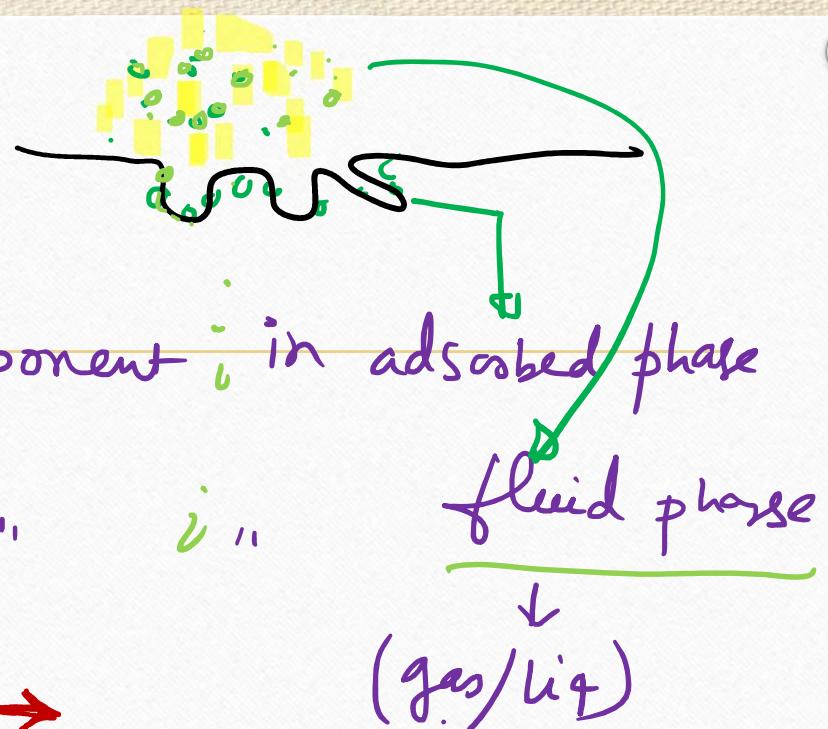
Separation factor:

$$\alpha_{12} = \frac{x_1/y_1}{x_2/y_2}$$

$x_i$  = mole fraction of component  $i$  in adsorbed phase

$y_i$  = " " "

$\alpha_{12} \Rightarrow$  Relative volatility  $\rightarrow$   
 $\downarrow$  Distillation-



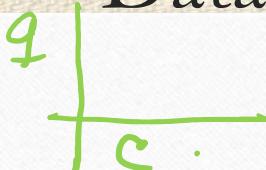
## Langmuir Freundlich model

$$\underline{q_i} = q_{im} \cdot \frac{b_i p_i^{n_i}}{1 + b_1 p_1^{n_1} + b_2 p_2^{n_2} + b_3 p_3^{n_3} + \dots + b_n p_n^{n_n}}$$

Multicomponent adsorption eq b.m. { [ Higher no of parameters ] }.

$$\frac{q_{im} b_i p_i^{n_i}}{1 + \sum b_i p_i^{n_i}}$$

# Dataset: Solid Liquid system



| Glycine                            |                        | Phenylalanine                      |                         |
|------------------------------------|------------------------|------------------------------------|-------------------------|
| fluid phase                        | Adsorbed phase         | fluid phase                        | adsorbed phase          |
| Concentration of the component [c] | Amount adsorbed [q]    | Concentration of the component [c] | Amount adsorbed [q]     |
| 0.0126                             | $0.794 \times 10^{-5}$ | 0.0112 ✓                           | $0.6 \times 10^{-4}$ ✓  |
| 0.0251                             | $1.41 \times 10^{-5}$  | 0.0224 ✓                           | $1.2 \times 10^{-4}$ ✓  |
| 0.10                               | $5.62 \times 10^{-5}$  | 0.0302 ✓                           | $1.58 \times 10^{-4}$ ✓ |
| 0.1995                             | $11.2 \times 10^{-5}$  | 0.0355 ✓                           | $1.78 \times 10^{-4}$ ✓ |

$c, P, T$

$f(c, P, T) \rightarrow .$

$$q = q_m \cdot \frac{P}{K + P} [L.I]$$

$$q = q_m b \cdot x_n [F.I]$$

## Calculation of specific area of an adsorbent

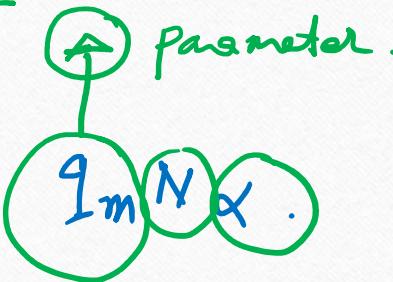
$$\alpha = \text{Projected area of an adsorbed molecule} = 1.09 \left( \frac{M}{N\bar{P}} \right)^{2/3}$$

$M$  = Molecular weight,  $\rho$  = density of the adsorbate,

$N$  = Avogadro number,

Specific surface area of the adsorbent =  $q_m N A$ .

$q_m$  = gm mole adsorbed component / gm of adsorbent.



# BET's isotherm, Braunauer-Emmet-Teller Equation

BET eqn represent multilayer adsorption eqn for many system.

$$q = q_m \frac{c'x}{(1-x)[1+(c'-1)x]}$$

$\uparrow T$

[ 3-parameter model,  $q_m, c, c'$  ]

$x = p/p_v$ ,  $q = \underline{\text{quantity of component (liquid/gas) adsorbed. in gm/gm of adsorbant.}}$

$q_m = \begin{cases} \text{Quantity of component adsorbed to form monolayer} \\ \text{on the surface, [gm adsorbed/gm adsorbent]} \end{cases}$

$c'$  = a temperature dependent constant for a particular gas-solid,

$p_v$  = vapour pr of the adsorbate at at a given temp.

BET equation:

$$q = \frac{q_m c' p / P_v}{(1 - p / P_v) [1 + (c' - 1)p / P_v]} \quad \text{- Non-linear.}$$

$$\Rightarrow \left( \frac{P_v - p}{P_v} \right) \left( 1 + \frac{(c' - 1)p}{P_v} \right) = \frac{q_m c' p}{P_v q}.$$

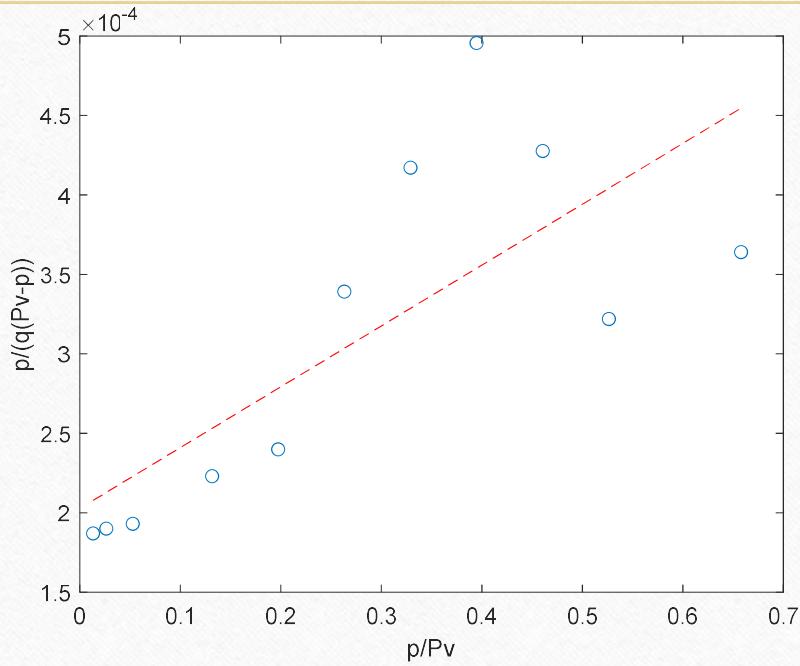
$$\Rightarrow \frac{(P_v - p)}{P_v} + \frac{(P_v - p)(c' - 1)p}{P_v} = \frac{q_m c' p}{P_v q}. \quad [\text{divide both sides by } (P_v - p)]$$

$$\Rightarrow \frac{1}{c' q_m} + \frac{(c' - 1) \frac{p}{P_v}}{c' q_m P_v} \cdot p = \left[ \frac{p}{q(P_v - p)} \right] y \quad (P_v - p) q_m c'$$

$$\Rightarrow \boxed{\frac{p}{q(P_v - p)}} = \frac{1}{c' q_m} + \frac{c' - 1}{c' q_m P_v} \cdot p \quad \text{— (Can be used in parameter estimation)}$$

In order to fit the BET equation,

plot  $\frac{P}{q(P_v - P)}$  vs  $P/P_v$  — Should be a st. line for an adsorbate-adsorbent pair.



Linear Regression:

Polyfit function

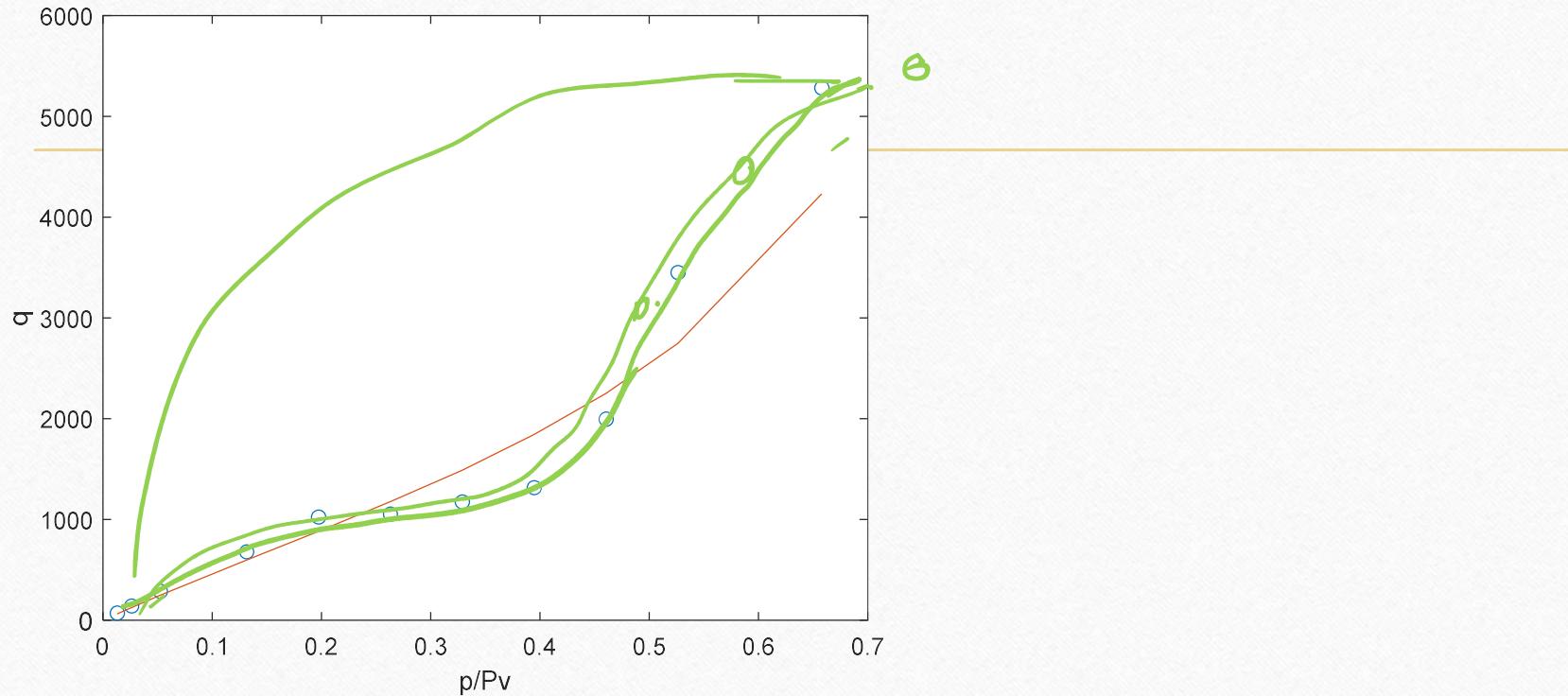
# Dataset: Solid –gas system, calculation of specific surface area of an adsorbent

| P mm Hg<br>( $P_v=760$<br>mm Hg),<br>$T=77.4$ | 10   | 20    | 40    | 100   | 150  | 200  | 250  | 300  | 350  | 400  | 500  |
|---|------|-------|-------|-------|------|------|------|------|------|------|------|
| q (amount adsorbed per solid)                 | 71.3 | 142.2 | 287.7 | 679.4 | 1025 | 1053 | 1175 | 1316 | 1996 | 3451 | 5283 |

P → Pressure of  $N_2$  ( mm Hg)

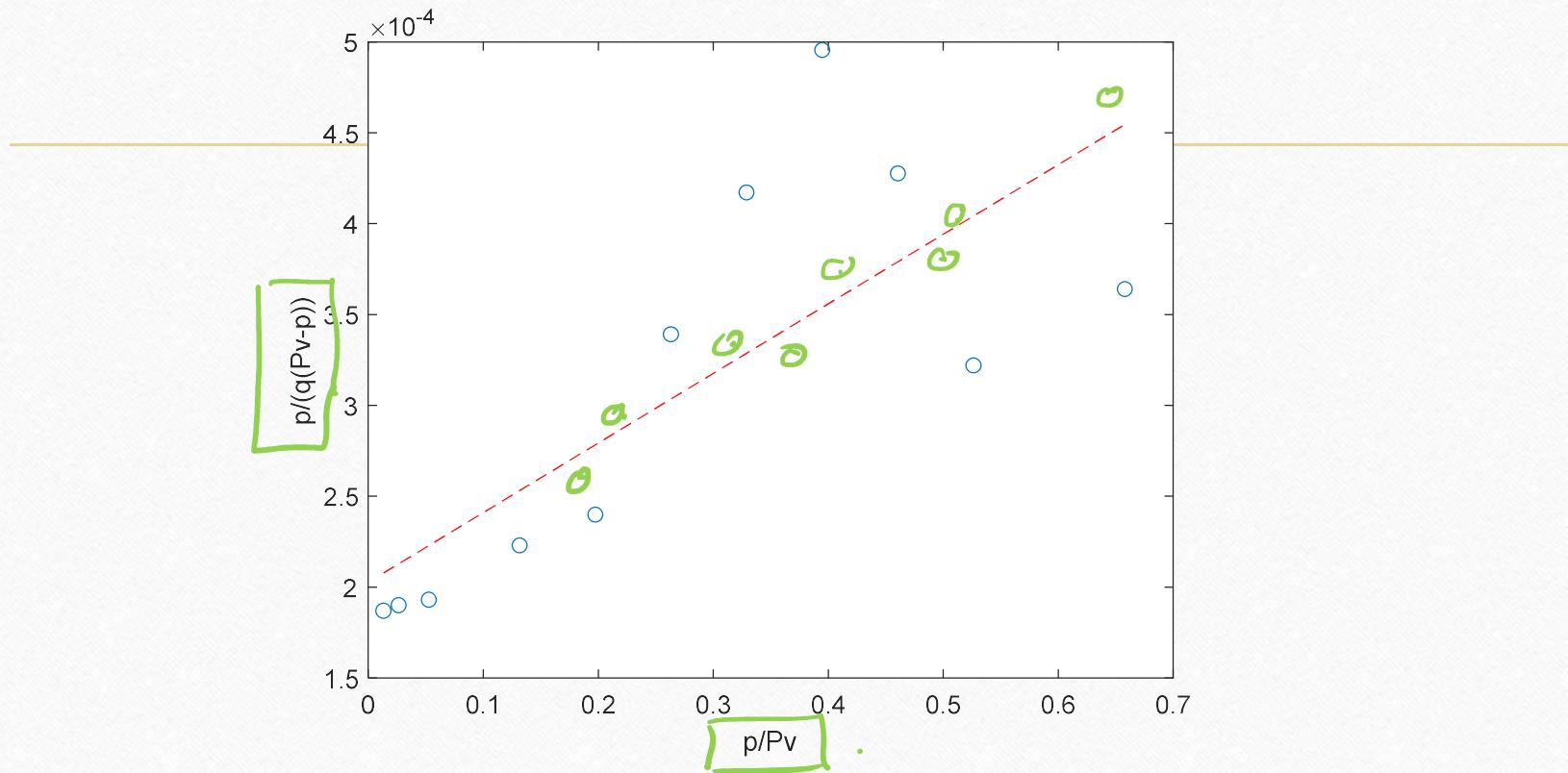
q → Volume of  $N_2$  adsorbed / 100 gm solid ( $cm^3$ ) .

# BET's isotherm, Braunauer-Emmet –Teller Equation



# Model fitting to adsorption process

Plotting for straight line form



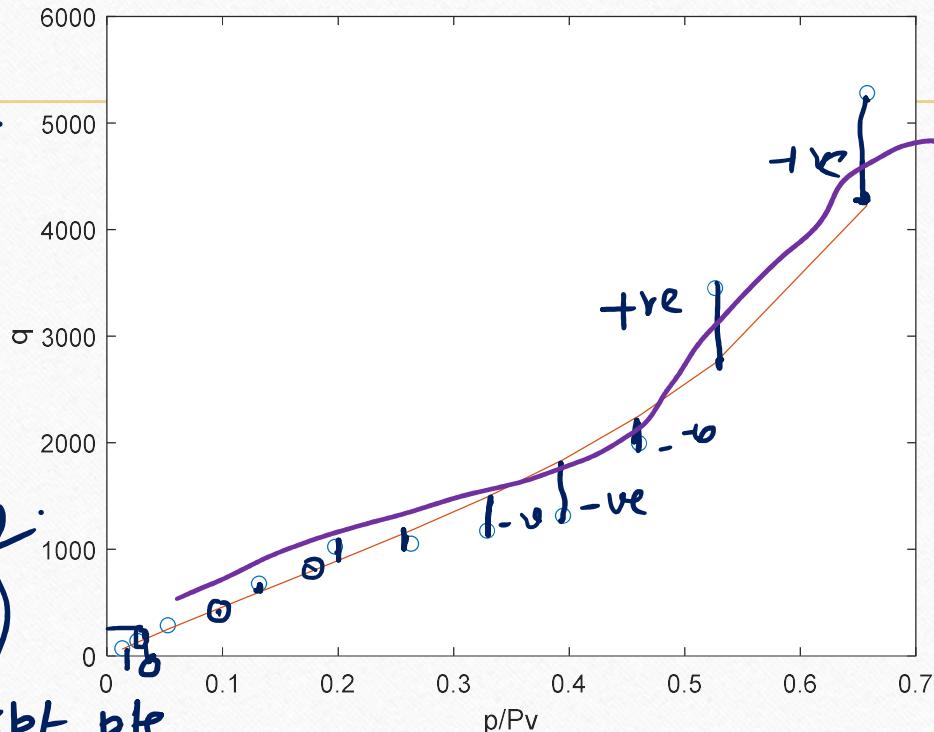
# Amount adsorbed experimental vs. amount adsorbed theoretical

*goodness of fit /*

12 pts n=12.

*quantify .*

$$\frac{x_{1,\text{exp}}(y_{1,\text{exp}})}{x_{1,\text{exp}}(y_{1,\text{sim}})} \\ \sum_{i=1}^n (y_{\text{exp},i} - y_{\text{sim},i})^2 \\ n = \text{no of expt pts.}$$



RMSE

Root mean square  
error.

$$= \sqrt{\frac{1}{n} \sum_{i=1}^n (y_{\text{exp},i} - y_{\text{sim},i})^2}$$

*RMSE | Model 1.*

*RMSE | Model 2.*

## Plotting of amount absorbed vs p. pressure

