

Question Paper

Exam Date & Time: 03-May-2024 (02:30 PM - 05:30 PM)



MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -
APRIL / MAY 2024
SUBJECT: ECE 2222/ECE_2222 - DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

- 1A) Compute the 6-point DFT of the sequence $x(n) = \{0, 1, 2, 3, 2, 1\}$ using matrix multiplication method. (5)
1B) State and prove the circular convolution property of DFT of two sequences $x_1(n)$ and $x_2(n)$. (3)
1C) Describe the Goertzel algorithm with expressions. What is it used for? (2)
2A) Compute the 8-point DFT of the sequence $x(n) = \{1, 0.5, 0, -0.5, -1, -0.5, 0, 0.5\}$ using decimation in frequency FFT algorithm. Illustrate that the computation is faster than the direct computation of DFT. (5)

- 2B) Analyze the FIR lattice structure whose lattice coefficients are: $K_1 = 0.65$, $K_2 = -0.34$ & $K_3 = 0.8$, and obtain its impulse response coefficients. (3)
2C) Realize the linear phase FIR filter of length $M = 7$, whose first four filter coefficients are: $1, 1/3, -1/8$ and $1/5$. (2)

- 3A) A LPF has the desired frequency response (5)

$$|H_d(e^{j\omega})| = \begin{cases} 1, & 0 \leq |\omega| \leq 0.5\pi \\ 0, & \text{elsewhere} \end{cases}$$

- Determine the filter coefficients $h(n)$ using frequency sampling technique. Assume filter length $M=9$.
3B) Determine the unit sample response $h(n)$ of a 4 length linear phase symmetric FIR filter having frequency response $H_r(0) = 1$ and $H_r\left(\frac{\pi}{2}\right) = 0.5$ (3)

- 3C) From Q3B determine the system function $H(z)$ and the phase $\emptyset(\omega)$ for $H_r(\omega) > 0$. (2)

- 4A) Certain IIR Butterworth LPF has the following specifications (5)

$$-1.5dB \leq 20\log_{10}(|H(e^{j\omega})|) \leq 0dB, \quad 0 \leq \omega \leq \pi/3$$

$$20\log_{10}(|H(e^{j\omega})|) \leq -10dB, \quad 0.5\pi \leq \omega \leq \pi$$

Assume $T=1$ second. Obtain the prewarped analog edge frequency specifications, order of filter, 3-dB cut-off frequency and poles of the filter.

- 4B) For the filter specification given in Question 4A, determine the analog transfer function $H(s)$. (3)

- 4C) For the filter specification given in Question 4A, determine the system function $H(z)$. Use bilinear transformation. (2)

- 5A) Given the system function $H(z) = \frac{1+z^{-1}+0.5z^{-2}}{1+0.2z^{-1}-0.15z^{-2}}$. Obtain the lattice ladder structure. (5)

- 5B) Convert the analog filter into its equivalent digital filter using impulse invariance method whose transfer function is given by $H(s) = \frac{s+1}{s^2+2s+17}$. Assume T=1 second. (3)
- 5C) Illustrate the concept of spectral leakage and spectral resolution problems occurring in spectral estimation from finite duration signals. (2)

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Question Paper

Exam Date & Time: 26-May-2023 (02:30 PM - 05:30 PM)



MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -
MAY/JUNE 2023
SUBJECT: ECE 2255/ECE_2255 DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

Missing data may be suitably assumed.

- 1A) Sketch the frequency sampling realization of $M=16$ and $\alpha=0$, linear phase FIR filter (5)
which has frequency samples $H\left(\frac{2\pi k}{16}\right) = \begin{cases} 1, & k = 0, 1, 2 \\ 0.5, & k = 3 \\ 0, & k = 4, 5, \dots, 7 \end{cases}$
- 1B) Consider an FIR filter with lattice coefficients $K_1 = 0.45$, $K_2 = -0.61$, $K_3 = 0.7$. Obtain the impulse response of the filter and sketch its direct form structure. (3)
- 1C) Determine the system function of a causal LTI system, with zeros at $z = 0.5$ and $z = 0.8$, and a complex pair of poles at $z = 1.5 e^{j\frac{\pi}{4}}$. State whether the system is stable and justify your answer, with the help of a pole-zero plot. (2)
- 2A) Develop radix-2 DIF FFT algorithm. Illustrate with signal flow diagram for $N=8$. Highlight the computational advantage of this algorithm. (5)
- 2B) Illustrate with mathematical relations, use of DFT/IDFT in determining the circular convolution between two finite duration sequences. Explain how this is used in determining the response of LTI system to the given input. (3)
- 2C) Consider the finite duration signal $x[n] = n$, $0 \leq n \leq 7$ and 0 elsewhere with 8-point DFT $X[k]$. Using suitable properties of DFT, determine sequence $y[n]$ whose 8-point DFT is $Y[k] = \text{Real part of } |X[k]|$ (2)
- 3A) The specifications of the desired low-pass filter are (5)
 - Passband edge: 4kHz, Stopband edge: 8 kHz
 - Passband ripple: 1 dB, Stopband Attenuation: 40 dB
 - Sampling frequency: 24 kHzDetermine the order and poles of Butterworth filter required to meet the above filter specification. Use bilinear transformation.
- 3B) For the filter specification given in Question 3A, determine analog system function $H_a(s)$ (3) and use bilinear transformation to obtain $H(z)$ of Butterworth digital filter.
- 3C) Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution. (2)
- 4A) Determine the filter coefficients for a linear phase FIR LPF of length $M=7$. The approximate desired frequency specifications for the filter is (5)

$$H_d(e^{j\omega}) = \begin{cases} e^{-j\omega\alpha}, & 0 \leq |\omega| \leq 0.3\pi \\ 0, & elsewhere \end{cases}$$

Use suitable window with a minimum stop band attenuation of 50dB.

- 4B) Convert the analog filter to its equivalent digital filter whose system function is given (3)
by $H(s) = \frac{s+0.4}{s^2+0.8s+25.16}$ using impulse invariance technique. Assume sampling frequency of 10Hz.
- 4C) Obtain the direct-form II realization for the system $H(z) = \frac{(1-z^{-1}+2z^{-2})}{(1+0.2z^{-1})(1-0.5z^{-1}+0.7z^{-2})}$ (2)
- 5A) Describe with mathematical expressions the Blackman-Tukey method of power spectrum estimation. (5)
Describe the spectral leakage and spectral resolution problems occurring in estimation of spectra from finite duration observation of signals.
- 5B) Realize an efficient direct form structure of the linear phase FIR filter whose system function is (3)
 $H(z) = 0.015 - 0.145z^{-1} + 0.268z^{-2} - 0.268z^{-4} + 0.145z^{-5} - 0.015z^{-6}$
Determine the corresponding input-output equation.
- 5C) For the filter given in Question 5B, write the equations for the magnitude response and phase response. Is this filter suitable for the design of a lowpass filter? Justify your answer. (2)

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**FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION
JUNE 2022**

SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255)

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.

Q. No.	Questions	M*	C*	A*	B*
1A.	Determine the location of poles and all possible impulse response associated with the system function $H(z) = \frac{5z^{-1}}{3-7z^{-1}+2z^{-2}}$. Indicate ROC of H(z) in each case	5	1	1,2	3
1B.	Using DFT-IDFT method determine the response of LTI system with impulse response $h(n) = [1,2]$ to the input $x(n) = [1,2,1]$.	3	2	1,2	3
1C.	Mention the procedure of overlap add method for filtering of long data sequences.	2	2	1,2	2
2A.	Develop DITFFT algorithm for N=8. Compute 8-point DFT of a sequence $x(n) = \{0.5, 0.5, 0.5, 0.5\}$ using DITFFT algorithm.	5	2	1,2	3
2B.	Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution.	3	2	1,2	2
2C.	Obtain the parallel structure for the following system $y(n) = \frac{3}{4}y(n-1) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1)$.	2	3	1,2	3
3A.	A second order low-pass Butterworth filter is required to meet the following specifications: $\omega_p = 0.3\pi$, $\omega_s = 0.7\pi$, -2dB ripple in the passband and a stopband attenuation of -20dB. Determine the pre-warped analog edge frequencies Ω_p and Ω_s , 3-dB cut off frequency Ω_c and transfer function H(s) of the filter, using bilinear transformation at 6Hz sampling.	5	3	1,2	3
3B.	For the above question given in Q3A, Obtain the digital filter system function H(z) using bilinear transformation at 6Hz sampling.	3	3	1,2	3

3C.	Derive the equation for phase response of an even symmetric linear phase FIR filter.	2	4	1,2	2
4A.	A low pass linear phase FIR filter is to be designed with the following desired frequency response: $H_d(e^{jw}) = \begin{cases} e^{-j3w}, & \text{for } -\frac{\pi}{2} \leq \omega \leq \frac{\pi}{2} \\ 0, & \text{for } \frac{\pi}{2} \leq \omega \leq \pi \end{cases}$ Determine the filter coefficients for M=7 using Hamming window.	5	4	1,2	3
4B.	For the above question given in Q4A, determine the transfer function H(z) and the frequency response H(e ^{jw}) of the designed filter.	3	4	1,2	3
4C.	Explain the limitation of rectangular window function for the design of FIR filters.	2	4	1,2	2
5A.	Obtain the lattice ladder structure for $H(z) = \frac{1+2z^{-1}+3z^{-2}+2z^{-3}}{1+0.9z^{-1}-0.8z^{-2}+0.5z^{-3}}$	5	3	1,2	4
5B.	Describe Bartlett method of Power spectrum estimation. Highlight the computation requirement of this method.	3	5	1,2 ,18	2
5C.	List the advantages of Non parametric methods.	2	5	1,2 ,18	2

M*--Marks, C*--CLO, A*--AHEP LO, B* Blooms Taxonomy Level

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**FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION
JULY 2022**

SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255)

TIME: 3 HOURS

MAX. MARKS: 50

Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.

Q. No.	Questions	M*	C*	A*	B*
1A.	Use unilateral z transform to find the response $y(n) \geq 0$, for the system described by the difference equation $y(n)=x(n-1)+0.5y(n-1)$ with $x(n) = 0.25^n u(n)$ and $y(-1) = 1$.	5	1	1,2	3
1B.	Given two 8 point sequence $x_1(n)=[A,C,A,D,E,M,I,C]$ and $x_2(n)=[E,M,I,C,A,C,A,D]$ with 8 point DFT's $X_1(K)$ and $X_2(K)$. Express $X_2(K)$ in terms of $X_1(K)$ in a simplified form.	3	2	1.2	3
1C.	Mention the procedure of overlap save method for filtering of long data sequences.	2	2	1,2	2
2A.	Develop DIFFFT algorithm for $N=8$. Compute 8-point DFT of a sequence $x(n) = \{3, 2, 1, 0, 1, 2\}$ using DIFFFT algorithm.	5	2	1,2	3
2B.	Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution.	3	2	1,2	2
2C.	Obtain the direct form-II structure for the following system $y(n) = \frac{3}{4}y(n-1) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1)$.	2	3	1,2	3
3A.	Determine the system function of a second order analog Chebyshev type-1 low pass filter with pass band cut-off frequency 200 Hz at sampling frequency of 1000Hz. The allowable ripple in the pass band is 2dB.	5	3	1,2	3
3B.	Determine the order of a lowpass Butterworth filter that has a -3dB bandwidth of 500Hz and a stopband attenuation of -40dB at 1000Hz.	3	3	1,2	3

3C.	Derive the equation for phase response of an odd antisymmetric linear phase FIR filter.	2	4	1,2	2
4A.	A low pass filter is to be designed with the following desired frequency response: $H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega}, & \text{for } -\frac{\pi}{2} \leq \omega \leq \frac{\pi}{2} \\ 0, & \text{for } \frac{\pi}{2} \leq \omega \leq \pi \end{cases}$ Determine the filter coefficients for M=7 using Hanning window.	5	4	1,2	3
4B.	For the above question given in Q4A, determine the transfer function H(z) and the frequency response H(e ^{jω}) of the designed filter.	3	4	1,2	3
4C.	Explain the zero-location symmetry property of linear-phase FIR filter.	2	4	1,2	2
5A.	Obtain the lattice ladder structure for $y(n) = -0.1y(n-1) + 0.72y(n-2) + x(n) - 0.8x(n-1) + 0.15x(n-2)$	5	3	1,2	4
5B.	Describe Welch method of PSD estimation. Highlight the computation requirement of this method.	3	5	1,2 ,18	2
5C.	List the AR model estimation methods.	2	5	1,2 ,18	2

M*--Marks, C*--CLO, A*--AHEP LO, B* Blooms Taxonomy Level

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FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION

AUGUST 2021

SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255)

TIME: 2 HOURS

MAX. MARKS: 40

Instructions to candidates

- Answer **any four full** questions.
- Missing data may be suitably assumed.

1A. It is required to design a causal discrete LTI system such that it produces an output $y[n] = \left(\frac{1}{3}\right)^n u[n]$ when the input $x[n] = \left(\frac{1}{2}\right)^n \left\{u[n] - \frac{1}{2}u[n-1]\right\}$

- i. Determine impulse response $h(n)$ and system function $H(z)$
- ii. Determine difference equation.

iii. Is the system stable? If so, identify and sketch the ROC of $H(z)$

1B. With example explain the concept of circular shift of a sequence. Determine 8-point circular convolution between the signals $x_1[n] = [1 2 3 1]$ and $x_2[n] = [4 3 2 1]$ using DFT/IDFT calculations.

(5+5)

2A. Using radix-2 DIF algorithm, determine 8-point inverse DFT of $X[k] = [0 4 0 0 0 0 0 4]$. Clearly indicate the values at every node of the flow diagram.

2B. Derive Goertzel algorithm for the computation of N-point DFT of a signal. Determine the system function $H(z)$ and difference equation for the system that uses Goertzel algorithm to compute DFT value $X(-k)_N$ for the real valued signal $x(n)$.

(5+5)

3A. Obtain and sketch the direct form I, direct form II and cascade structures for the IIR system $H(z) = \frac{2(z-1)(z^2+\sqrt{2}z+1)}{(z+0.5)(z^2-0.9z+0.81)}$

Second order sections are allowed in cascade structure.

3B. Consider an FIR system having impulse response $h(n) = \delta(n) + \delta(n-1) + 0.5\delta(n-2) + \delta(n-3) + \delta(n-4)$. Realize the system using frequency sampling structure.

(5+5)

4A. With relevant mathematical analysis explain the design of IIR filters by the bilinear transformation. Describe why pre-warping is necessary when using bilinear transformation.

4B. Determine the poles and transfer function $H(s)$ for the third order analog Butterworth prototype (cut-off frequency=1 rad/sec) filter. Digitize this using impulse invariance transformation with $T=0.1$ sec and obtain the system function $H(z)$.

(5+5)

5A. Illustrate with diagram the frequency response of Chebyshev type-I LPF. Compute the minimum order and analog transfer function $H(s)$ of such filter, where the maximum allowable ripple is 1dB

in the pass-band extending from 0 to 0.1π radians/sec. The minimum attenuation should be 40dB at the stop-band edge frequency of 0.3π radians/sec.

- 5B. Design digital IIR notch filter to suppress 50 Hz interference. The filter should work at a sampling frequency of 500 Hz. The notch bandwidth should be 5Hz. Assume $b_0=1$. Write down the corresponding frequency response.

(5+5)

- 6A. Describe the time domain and frequency domain characteristics of linear phase FIR filters. Obtain an expression for system function $H(z)$ of even length symmetric linear phase FIR filter in terms of $(M-1)/2$ coefficients where M is the length of the filter. Sketch the tapped delay line realization for the same.

- 6B. Determine coefficients of 9 length symmetric digital FIR high pass filter using causal hamming window. The filter has desirable pass band extending from 400 Hz to 1000 Hz at a sampling frequency of 2000 Hz. The filter should have precisely linear phase response in the pass band. Obtain the frequency response of this filter.

(5+5)