

# Question Paper

Exam Date & Time: 03-May-2024 (02:30 PM - 05:30 PM)



## MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -  
APRIL / MAY 2024  
SUBJECT: ECE 2222/ECE\_2222 - DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

- 1A) Compute the 6-point DFT of the sequence  $x(n) = \{0, 1, 2, 3, 2, 1\}$  using matrix multiplication method. (5)
- 1B) State and prove the circular convolution property of DFT of two sequences  $x_1(n)$  and  $x_2(n)$ . (3)
- 1C) Describe the Goertzel algorithm with expressions. What is it used for? (2)
- 2A) Compute the 8-point DFT of the sequence  $x(n) = \{1, 0.5, 0, -0.5, -1, -0.5, 0, 0.5\}$  using decimation in frequency FFT algorithm. Illustrate that the computation is faster than the direct computation of DFT. (5)
- 2B) Analyze the FIR lattice structure whose lattice coefficients are:  $K_1 = 0.65$ ,  $K_2 = -0.34$  &  $K_3 = 0.8$ , and obtain its impulse response coefficients. (3)
- 2C) Realize the linear phase FIR filter of length  $M = 7$ , whose first four filter coefficients are: 1,  $1/3$ ,  $-1/8$  and  $1/5$ . (2)
- 3A) A LPF has the desired frequency response (5)
- $$|H_d(e^{j\omega})| = \begin{cases} 1, & 0 \leq |\omega| \leq 0.5\pi \\ 0, & \text{elsewhere} \end{cases}$$
- Determine the filter coefficients  $h(n)$  using frequency sampling technique. Assume filter length  $M=9$ .
- 3B) Determine the unit sample response  $h(n)$  of a 4 length linear phase symmetric FIR filter having frequency response (3)
- $$H_r(0) = 1 \text{ and } H_r\left(\frac{\pi}{2}\right) = 0.5$$
- 3C) From Q3B determine the system function  $H(z)$  and the phase  $\phi(\omega)$  for  $H_r(\omega) > 0$ . (2)
- 4A) Certain IIR Butterworth LPF has the following specifications (5)
- $$-1.5\text{dB} \leq 20\log_{10}(|H(e^{j\omega})|) \leq 0\text{dB}, \quad 0 \leq \omega \leq \pi/3$$
- $$20\log_{10}(|H(e^{j\omega})|) \leq -10\text{dB}, \quad 0.5\pi \leq \omega \leq \pi$$
- Assume  $T=1$  second. Obtain the prewarped analog edge frequency specifications, order of filter, 3-dB cut-off frequency and poles of the filter.
- 4B) For the filter specification given in Question 4A, determine the analog transfer function  $H(s)$ . (3)
- 4C) For the filter specification given in Question 4A, determine the system function  $H(z)$ . Use bilinear transformation. (2)
- 5A) Given the system function (5)
- $$H(z) = \frac{1+z^{-1}+0.5z^{-2}}{1+0.2z^{-1}-0.15z^{-2}} \quad \text{Obtain the lattice ladder structure.}$$

- 5B) Convert the analog filter into its equivalent digital filter using impulse invariance method whose transfer function is given by  $H(s) = \frac{s+1}{s^2+2s+17}$ . Assume T=1 second. (3)
- 5C) Illustrate the concept of spectral leakage and spectral resolution problems occurring in spectral estimation from finite duration signals. (2)

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# Question Paper

Exam Date & Time: 26-May-2023 (02:30 PM - 05:30 PM)



## MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -  
MAY/JUNE 2023  
SUBJECT: ECE 2255/ECE\_2255 DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

Missing data may be suitably assumed.

- 1A) Sketch the frequency sampling realization of  $M=16$  and  $\alpha=0$ , linear phase FIR filter (5)  
which has frequency samples  $H\left(\frac{2\pi k}{16}\right) = \begin{cases} 1, & k = 0, 1, 2 \\ 0.5, & k = 3 \\ 0, & k = 4, 5, \dots, 7 \end{cases}$
- 1B) Consider an FIR filter with lattice coefficients  $K_1 = 0.45$ ,  $K_2 = -0.61$ ,  $K_3 = 0.7$ . Obtain the impulse response of the filter and sketch its direct form structure. (3)
- 1C) Determine the system function of a causal LTI system, with zeros at  $z = 0.5$  and  $z = 0.8$ , and a complex pair of poles at  $z = 1.5 e^{j\frac{\pi}{4}}$ . State whether the system is stable and justify your answer, with the help of a pole-zero plot. (2)
- 2A) Develop radix-2 DIF FFT algorithm. Illustrate with signal flow diagram for  $N=8$ . Highlight the computational advantage of this algorithm. (5)
- 2B) Illustrate with mathematical relations, use of DFT/IDFT in determining the circular convolution between two finite duration sequences. Explain how this is used in determining the response of LTI system to the given input. (3)
- 2C) Consider the finite duration signal  $x[n] = n$ ,  $0 \leq n \leq 7$  and 0 elsewhere with 8-point DFT  $X[k]$ . Using suitable properties of DFT, determine sequence  $y[n]$  whose 8-point DFT is  $Y[k] = \text{Real part of } |X[k]|$  (2)
- 3A) The specifications of the desired low-pass filter are (5)  
• Passband edge: 4kHz, Stopband edge: 8 kHz  
• Passband ripple: 1 dB, Stopband Attenuation: 40 dB  
• Sampling frequency: 24 kHz  
Determine the order and poles of Butterworth filter required to meet the above filter specification. Use bilinear transformation.
- 3B) For the filter specification given in Question 3A, determine analog system function  $H_a(s)$  and use bilinear transformation to obtain  $H(z)$  of Butterworth digital filter. (3)
- 3C) Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution. (2)
- 4A) Determine the filter coefficients for a linear phase FIR LPF of length  $M=7$ . The approximate desired frequency specifications for the filter is (5)

$$H_d(e^{j\omega}) = \begin{cases} e^{-j\omega\alpha}, & 0 \leq |\omega| \leq 0.3\pi \\ 0, & \text{elsewhere} \end{cases}$$

Use suitable window with a minimum stop band attenuation of 50dB.

- 4B) Convert the analog filter to its equivalent digital filter whose system function is given (3)  
by  $H(s) = \frac{s+0.4}{s^2+0.8s+25.16}$  using impulse invariance technique. Assume sampling frequency of 10Hz.

- 4C) Obtain the direct-form II realization for the system  $H(z) = \frac{(1-z^{-1}+2z^{-2})}{(1+0.2z^{-1})(1-0.5z^{-1}+0.7z^{-2})}$  (2)

- 5A) Describe with mathematical expressions the Blackman-Tukey method of power spectrum estimation. (5)  
Describe the spectral leakage and spectral resolution problems occurring in estimation of spectra from finite duration observation of signals.

- 5B) Realize an efficient direct form structure of the linear phase FIR filter whose system function is (3)  
 $H(z) = 0.015 - 0.145z^{-1} + 0.268z^{-2} - 0.268z^{-4} + 0.145z^{-5} - 0.015z^{-6}$   
Determine the corresponding input-output equation.

- 5C) For the filter given in Question 5B, write the equations for the magnitude response and phase response. Is this filter suitable for the design of a lowpass filter? Justify your answer. (2)

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## FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION

JUNE 2022

SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255)

TIME: 3 HOURS

MAX. MARKS: 50

### Instructions to candidates

- Answer **ALL** questions.
- Missing data may be suitably assumed.

Q. No.	Questions	M*	C*	A*	B*
1A.	Determine the location of poles and all possible impulse response associated with the system function $H(z) = \frac{5z^{-1}}{3-7z^{-1}+2z^{-2}}$ . Indicate ROC of H(z) in each case	5	1	1,2	3
1B.	Using DFT-IDFT method determine the response of LTI system with impulse response $h(n) = [1, 2]$ to the input $x(n) = [1, 2, 1]$ .	3	2	1,2	3
1C.	Mention the procedure of overlap add method for filtering of long data sequences.	2	2	1,2	2
2A.	Develop DITFFT algorithm for N=8. Compute 8-point DFT of a sequence $x(n) = \{0.5, 0.5, 0.5, 0.5\}$ using DITFFT algorithm.	5	2	1,2	3
2B.	Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution.	3	2	1,2	2
2C.	Obtain the parallel structure for the following system $y(n) = \frac{3}{4}y(n-1) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1)$ .	2	3	1,2	3
3A.	A second order low-pass Butterworth filter is required to meet the following specifications: $\omega_p = 0.3\pi$ , $\omega_s = 0.7\pi$ , -2dB ripple in the passband and a stopband attenuation of -20dB. Determine the pre-warped analog edge frequencies $\Omega_p$ and $\Omega_s$ , 3-dB cut off frequency $\Omega_c$ and transfer function H(s) of the filter, using bilinear transformation at 6Hz sampling.	5	3	1,2	3
3B.	For the above question given in Q3A, Obtain the digital filter system function H(z) using bilinear transformation at 6Hz sampling.	3	3	1,2	3

3C.	Derive the equation for phase response of an even symmetric linear phase FIR filter.	2	4	1,2	2
4A.	<p>A low pass linear phase FIR filter is to be designed with the following desired frequency response:</p> $H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega}, & \text{for } -\frac{\pi}{2} \leq \omega \leq \frac{\pi}{2} \\ 0, & \text{for } \frac{\pi}{2} \leq \omega \leq \pi \end{cases}$ <p>Determine the filter coefficients for M=7 using Hamming window.</p>	5	4	1,2	3
4B.	For the above question given in Q4A, determine the transfer function H(z) and the frequency response H(e <sup>jw</sup> ) of the designed filter.	3	4	1,2	3
4C.	Explain the limitation of rectangular window function for the design of FIR filters.	2	4	1,2	2
5A.	Obtain the lattice ladder structure for $H(z) = \frac{1+2z^{-1}+3z^{-2}+2z^{-3}}{1+0.9z^{-1}-0.8z^{-2}+0.5z^{-3}}$	5	3	1,2	4
5B.	Describe Bartlett method of Power spectrum estimation. Highlight the computation requirement of this method.	3	5	1,2 ,18	2
5C.	List the advantages of Non parametric methods.	2	5	1,2 ,18	2

**M\*--Marks, C\*--CLO, A\*--AHEP LO, B\* Blooms Taxonomy Level**



## FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION

**JULY 2022**

**SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255 )**

**TIME: 3 HOURS**

**MAX. MARKS: 50**

**Instructions to candidates**

- Answer **ALL** questions.
- Missing data may be suitably assumed.

Q. No.	Questions	M*	C*	A*	B*
1A.	Use unilateral z transform to find the response $y(n) \geq 0$ , for the system described by the difference equation $y(n) = x(n-1) + 0.5y(n-1)$ with $x(n) = 0.25^n u(n)$ and $y(-1) = 1$ .	5	1	1,2	3
1B.	Given two 8 point sequence $x_1(n) = [A, C, A, D, E, M, I, C]$ and $x_2(n) = [E, M, I, C, A, C, A, D]$ with 8 point DFT's $X_1(K)$ and $X_2(K)$ . Express $X_2(K)$ in terms of $X_1(K)$ in a simplified form.	3	2	1,2	3
1C.	Mention the procedure of overlap save method for filtering of long data sequences.	2	2	1,2	2
2A.	Develop DIFFFT algorithm for $N=8$ . Compute 8-point DFT of a sequence $x(n) = \{3, 2, 1, 0, 1, 2\}$ using DIFFFT algorithm.	5	2	1,2	3
2B.	Explain how the Goertzel algorithm exploits the periodicity of the complex phase factor and obtain realization of the system to compute the DFT as a linear convolution.	3	2	1,2	2
2C.	Obtain the direct form-II structure for the following system $y(n) = \frac{3}{4}y(n-1) - \frac{1}{8}y(n-2) + x(n) + \frac{1}{3}x(n-1)$ .	2	3	1,2	3
3A.	Determine the system function of a second order analog Chebyshev type-1 low pass filter with pass band cut-off frequency 200 Hz at sampling frequency of 1000Hz. The allowable ripple in the pass band is 2dB.	5	3	1,2	3
3B.	Determine the order of a lowpass Butterworth filter that has a -3dB bandwidth of 500Hz and a stopband attenuation of -40dB at 1000Hz.	3	3	1,2	3

3C.	Derive the equation for phase response of an odd antisymmetric linear phase FIR filter.	2	4	1,2	2
4A.	<p>A low pass filter is to be designed with the following desired frequency response:</p> $H_d(e^{j\omega}) = \begin{cases} e^{-j3\omega}, & \text{for } -\frac{\pi}{2} \leq \omega \leq \frac{\pi}{2} \\ 0, & \text{for } \frac{\pi}{2} \leq \omega \leq \pi \end{cases}$ <p>Determine the filter coefficients for M=7 using Hanning window.</p>	5	4	1,2	3
4B.	For the above question given in Q4A, determine the transfer function H(z) and the frequency response H(e <sup>jw</sup> ) of the designed filter.	3	4	1,2	3
4C.	Explain the zero-location symmetry property of linear-phase FIR filter.	2	4	1,2	2
5A.	Obtain the lattice ladder structure for $y(n) = -0.1y(n-1) + 0.72y(n-2) + x(n) - 0.8x(n-1) + 0.15x(n-2)$	5	3	1,2	4
5B.	Describe Welch method of PSD estimation. Highlight the computation requirement of this method.	3	5	1,2,18	2
5C.	List the AR model estimation methods.	2	5	1,2,18	2

**M\*--Marks, C\*--CLO, A\*--AHEP LO, B\* Blooms Taxonomy Level**





## FOURTH SEMESTER BTECH. (E & C) DEGREE END SEMESTER EXAMINATION AUGUST 2021

**SUBJECT: DIGITAL SIGNAL PROCESSING (ECE - 2255)**

**TIME: 2 HOURS**

**MAX. MARKS: 40**

### Instructions to candidates

- Answer **any four full** questions.
- Missing data may be suitably assumed.

- 1A. It is required to design a causal discrete LTI system such that it produces an output  $y[n] = \left(\frac{1}{3}\right)^n u[n]$  when the input  $x[n] = \left(\frac{1}{2}\right)^n \left\{u[n] - \frac{1}{2}u[n-1]\right\}$
- i. Determine impulse response  $h(n)$  and system function  $H(z)$
  - ii. Determine difference equation.
  - iii. Is the system stable? If so, identify and sketch the ROC of  $H(z)$
- 1B. With example explain the concept of circular shift of a sequence. Determine 8-point circular convolution between the signals  $x_1[n] = [1 \ 2 \ 3 \ 1]$  and  $x_2[n] = [4 \ 3 \ 2 \ 1]$  using DFT/IDFT calculations.
- (5+5)
- 2A. Using radix-2 DIF algorithm, determine 8-point inverse DFT of  $X[k] = [0 \ 4 \ 0 \ 0 \ 0 \ 0 \ 0 \ 4]$ . Clearly indicate the values at every node of the flow diagram.
- 2B. Derive Goertzel algorithm for the computation of N-point DFT of a signal. Determine the system function  $H(z)$  and difference equation for the system that uses Goertzel algorithm to compute DFT value  $X(-k)_N$  for the real valued signal  $x(n)$ .
- (5+5)
- 3A. Obtain and sketch the direct form I, direct form II and cascade structures for the IIR system  $H(z) = \frac{2(z-1)(z^2+\sqrt{2}z+1)}{(z+0.5)(z^2-0.9z+0.81)}$
- Second order sections are allowed in cascade structure.
- 3B. Consider an FIR system having impulse response  $h(n) = \delta(n) + \delta(n-1) + 0.5\delta(n-2) + \delta(n-3) + \delta(n-4)$ . Realize the system using frequency sampling structure.
- (5+5)
- 4A. With relevant mathematical analysis explain the design of IIR filters by the bilinear transformation. Describe why pre-warping is necessary when using bilinear transformation.
- 4B. Determine the poles and transfer function  $H(s)$  for the third order analog Butterworth prototype (cut-off frequency=1 rad/sec) filter. Digitize this using impulse invariance transformation with  $T=0.1$ sec and obtain the system function  $H(z)$ .
- (5+5)
- 5A. Illustrate with diagram the frequency response of Chebyshev type-I LPF. Compute the minimum order and analog transfer function  $H(s)$  of such filter, where the maximum allowable ripple is 1dB

in the pass-band extending from 0 to  $0.1\pi$  radians/sec. The minimum attenuation should be 40dB at the stop-band edge frequency of  $0.3\pi$  radians/sec.

- 5B. Design digital IIR notch filter to suppress 50 Hz interference. The filter should work at a sampling frequency of 500 Hz. The notch bandwidth should be 5Hz. Assume  $b_0=1$ . Write down the corresponding frequency response.

(5+5)

- 6A. Describe the time domain and frequency domain characteristics of linear phase FIR filters. Obtain an expression for system function  $H(z)$  of even length symmetric linear phase FIR filter in terms of  $(M-1)/2$  coefficients where  $M$  is the length of the filter. Sketch the tapped delay line realization for the same.
- 6B. Determine coefficients of 9 length symmetric digital FIR high pass filter using causal hamming window. The filter has desirable pass band extending from 400 Hz to 1000 Hz at a sampling frequency of 2000 Hz. The filter should have precisely linear phase response in the pass band. Obtain the frequency response of this filter.

(5+5)