

Question Paper

Exam Date & Time: 03-May-2024 (02:30 PM - 05:30 PM)



MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -
APRIL / MAY 2024
SUBJECT: ECE 2222/ECE_2222 - DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

- 1A) Compute the 6-point DFT of the sequence $x(n) = \{0, 1, 2, 3, 2, 1\}$ using matrix multiplication method. (5)
1B) State and prove the circular convolution property of DFT of two sequences $x_1(n)$ and $x_2(n)$. (3)
1C) Describe the Goertzel algorithm with expressions. What is it used for? (2)
2A) Compute the 8-point DFT of the sequence $x(n) = \{1, 0.5, 0, -0.5, -1, -0.5, 0, 0.5\}$ using decimation in frequency FFT algorithm. Illustrate that the computation is faster than the direct computation of DFT. (5)

- 2B) Analyze the FIR lattice structure whose lattice coefficients are: $K_1 = 0.65$, $K_2 = -0.34$ & $K_3 = 0.8$, and obtain its impulse response coefficients. (3)
2C) Realize the linear phase FIR filter of length $M = 7$, whose first four filter coefficients are: $1, 1/3, -1/8$ and $1/5$. (2)

- 3A) A LPF has the desired frequency response (5)

$$|H_d(e^{j\omega})| = \begin{cases} 1, & 0 \leq |\omega| \leq 0.5\pi \\ 0, & \text{elsewhere} \end{cases}$$

- Determine the filter coefficients $h(n)$ using frequency sampling technique. Assume filter length $M=9$.
3B) Determine the unit sample response $h(n)$ of a 4 length linear phase symmetric FIR filter having frequency response $H_r(0) = 1$ and $H_r\left(\frac{\pi}{2}\right) = 0.5$ (3)

- 3C) From Q3B determine the system function $H(z)$ and the phase $\emptyset(\omega)$ for $H_r(\omega) > 0$. (2)

- 4A) Certain IIR Butterworth LPF has the following specifications (5)

$$-1.5dB \leq 20\log_{10}(|H(e^{j\omega})|) \leq 0dB, \quad 0 \leq \omega \leq \pi/3$$

$$20\log_{10}(|H(e^{j\omega})|) \leq -10dB, \quad 0.5\pi \leq \omega \leq \pi$$

Assume $T=1$ second. Obtain the prewarped analog edge frequency specifications, order of filter, 3-dB cut-off frequency and poles of the filter.

- 4B) For the filter specification given in Question 4A, determine the analog transfer function $H(s)$. (3)

- 4C) For the filter specification given in Question 4A, determine the system function $H(z)$. Use bilinear transformation. (2)

- 5A) Given the system function $H(z) = \frac{1+z^{-1}+0.5z^{-2}}{1+0.2z^{-1}-0.15z^{-2}}$. Obtain the lattice ladder structure. (5)

- 5B) Convert the analog filter into its equivalent digital filter using impulse invariance method whose transfer function is given by $H(s) = \frac{s+1}{s^2+2s+17}$. Assume T=1 second. (3)
- 5C) Illustrate the concept of spectral leakage and spectral resolution problems occurring in spectral estimation from finite duration signals. (2)

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