

# Question Paper

Exam Date & Time: 03-May-2024 (02:30 PM - 05:30 PM)



## MANIPAL ACADEMY OF HIGHER EDUCATION

FOURTH SEMESTER B.TECH. (ELECTRONICS AND COMMUNICATION ENGINEERING) DEGREE EXAMINATIONS -  
APRIL / MAY 2024  
SUBJECT: ECE 2222/ECE\_2222 - DIGITAL SIGNAL PROCESSING

Marks: 50

Duration: 180 mins.

Answer all the questions.

- 1A) Compute the 6-point DFT of the sequence  $x(n) = \{0, 1, 2, 3, 2, 1\}$  using matrix multiplication method. (5)
- 1B) State and prove the circular convolution property of DFT of two sequences  $x_1(n)$  and  $x_2(n)$ . (3)
- 1C) Describe the Goertzel algorithm with expressions. What is it used for? (2)
- 2A) Compute the 8-point DFT of the sequence  $x(n) = \{1, 0.5, 0, -0.5, -1, -0.5, 0, 0.5\}$  using decimation in frequency FFT algorithm. Illustrate that the computation is faster than the direct computation of DFT. (5)
- 2B) Analyze the FIR lattice structure whose lattice coefficients are:  $K_1 = 0.65$ ,  $K_2 = -0.34$  &  $K_3 = 0.8$ , and obtain its impulse response coefficients. (3)
- 2C) Realize the linear phase FIR filter of length  $M = 7$ , whose first four filter coefficients are: 1,  $1/3$ ,  $-1/8$  and  $1/5$ . (2)
- 3A) A LPF has the desired frequency response (5)
- $$|H_d(e^{j\omega})| = \begin{cases} 1, & 0 \leq |\omega| \leq 0.5\pi \\ 0, & \text{elsewhere} \end{cases}$$
- Determine the filter coefficients  $h(n)$  using frequency sampling technique. Assume filter length  $M=9$ .
- 3B) Determine the unit sample response  $h(n)$  of a 4 length linear phase symmetric FIR filter having frequency response  $H_r(0) = 1$  and  $H_r\left(\frac{\pi}{2}\right) = 0.5$  (3)
- 3C) From Q3B determine the system function  $H(z)$  and the phase  $\phi(\omega)$  for  $H_r(\omega) > 0$ . (2)
- 4A) Certain IIR Butterworth LPF has the following specifications (5)
- $$-1.5\text{dB} \leq 20\log_{10}(|H(e^{j\omega})|) \leq 0\text{dB}, \quad 0 \leq \omega \leq \pi/3$$
- $$20\log_{10}(|H(e^{j\omega})|) \leq -10\text{dB}, \quad 0.5\pi \leq \omega \leq \pi$$
- Assume  $T=1$  second. Obtain the prewarped analog edge frequency specifications, order of filter, 3-dB cut-off frequency and poles of the filter.
- 4B) For the filter specification given in Question 4A, determine the analog transfer function  $H(s)$ . (3)
- 4C) For the filter specification given in Question 4A, determine the system function  $H(z)$ . Use bilinear transformation. (2)
- 5A) Given the system function  $H(z) = \frac{1+z^{-1}+0.5z^{-2}}{1+0.2z^{-1}-0.15z^{-2}}$ . Obtain the lattice ladder structure. (5)

- 5B) Convert the analog filter into its equivalent digital filter using impulse invariance method whose transfer function is given by  $H(s) = \frac{s+1}{s^2+2s+17}$ . Assume T=1 second. (3)
- 5C) Illustrate the concept of spectral leakage and spectral resolution problems occurring in spectral estimation from finite duration signals. (2)

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